

EEN 1043/EE452

Wireless and Mobile Communication

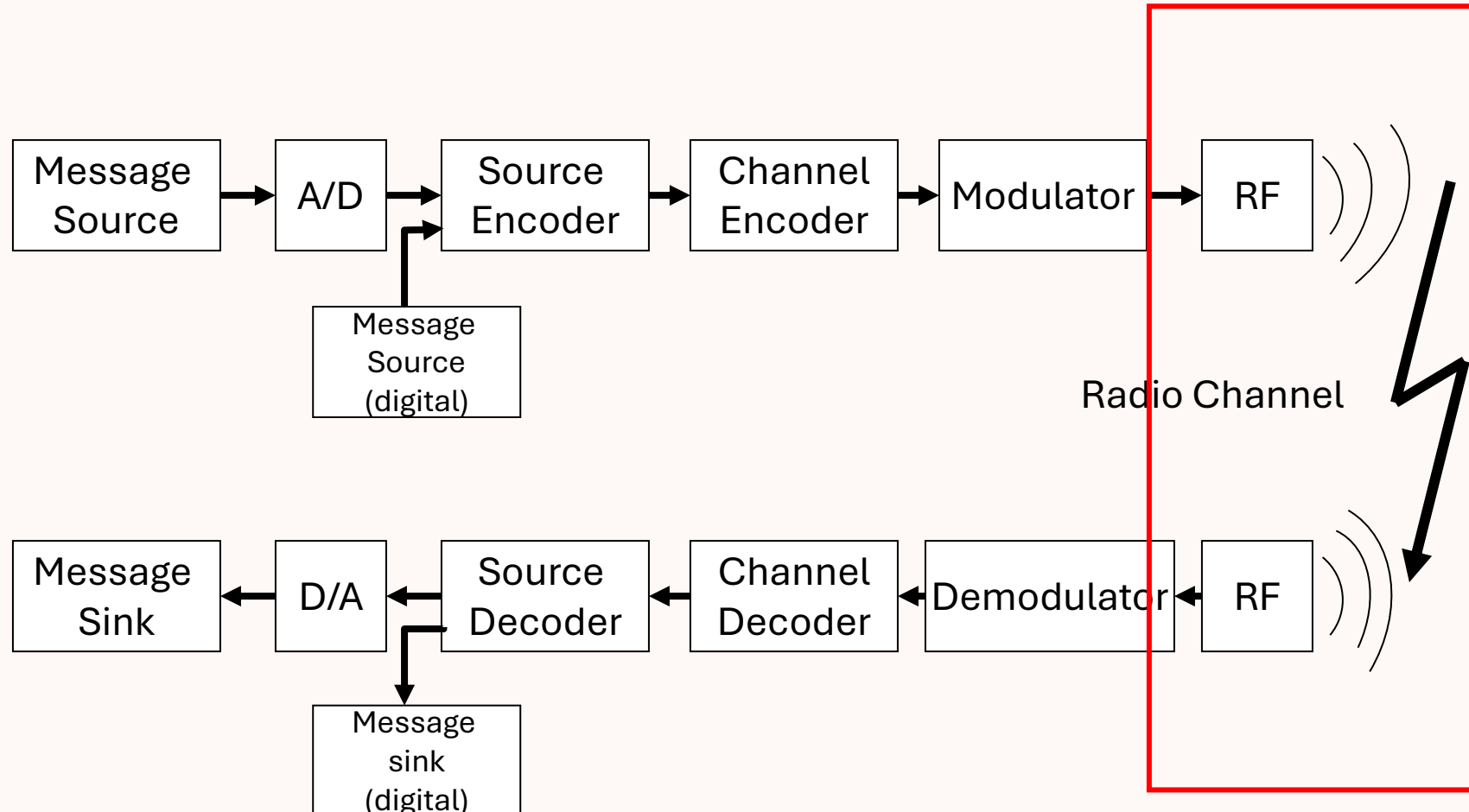
Channel Characterization III

Sobia Jangsher

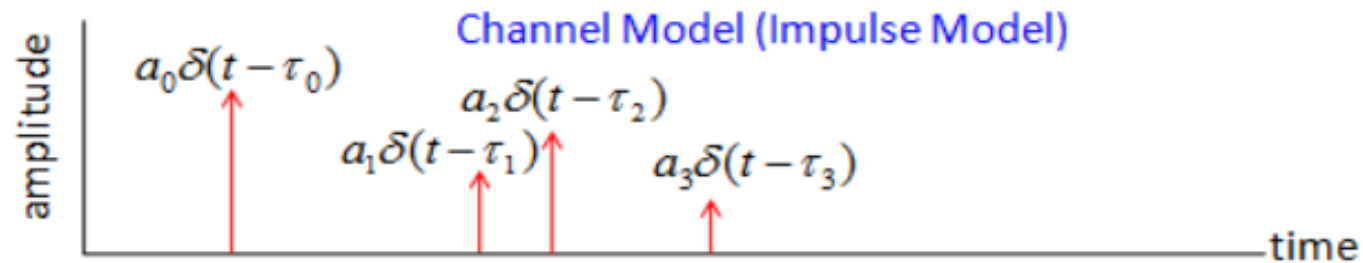
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Radio Link



Channel Impulse Response



$$h(t) = a_0\delta(t-\tau_0) + a_1\delta(t-\tau_1) + a_2\delta(t-\tau_2) + a_3\delta(t-\tau_3)$$

$$= \sum_{i=0}^3 a_i\delta(t-\tau_i)$$

Function representing
the channel impulse

Channel

- Channel adds noise (Additive White Gaussian Noise)

$$y(t) = x(t) + n(t)$$

- Channel delays the signal

$$y(t) = x(t - \tau) + n(t)$$

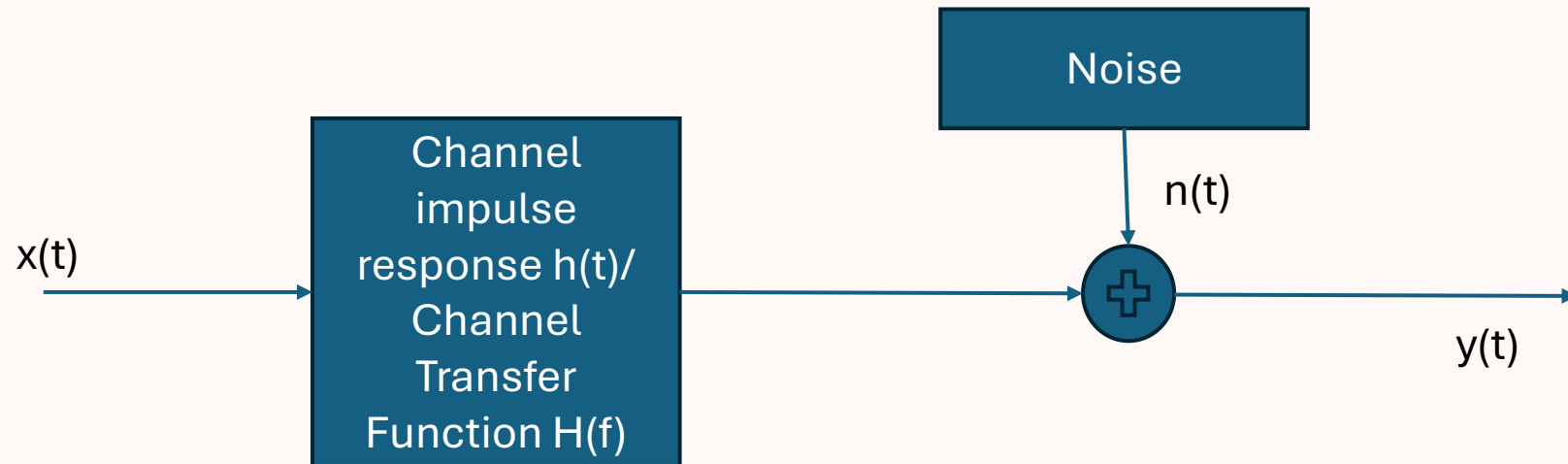
- Channel attenuates the signal

$$y(t) = hx(t - \tau) + n(t), \quad h \propto \frac{\lambda}{d}$$

- Channel rotates the signal (add phase)

$$y(t) = hx(t - \tau) + n(t), \quad h \propto \frac{\lambda}{d} e^{j\phi}$$

Channel



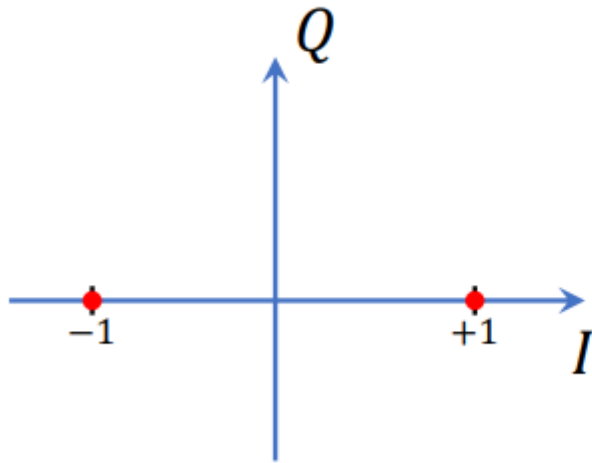
$$y(t) = \textcolor{red}{h}x(t - \tau) + n(t),$$

Channel

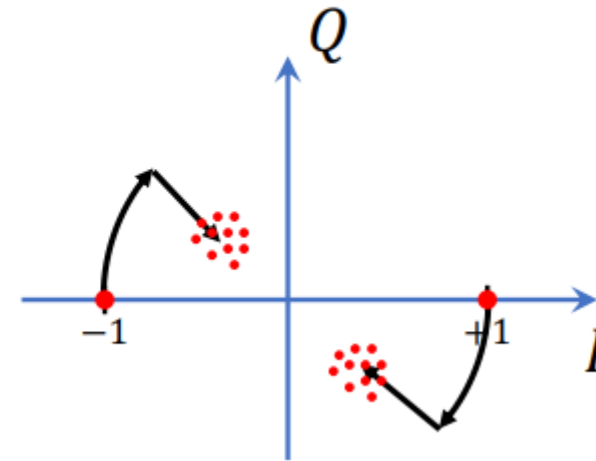
Consider BPSK modulation

0 \rightarrow -1

1 \rightarrow +1



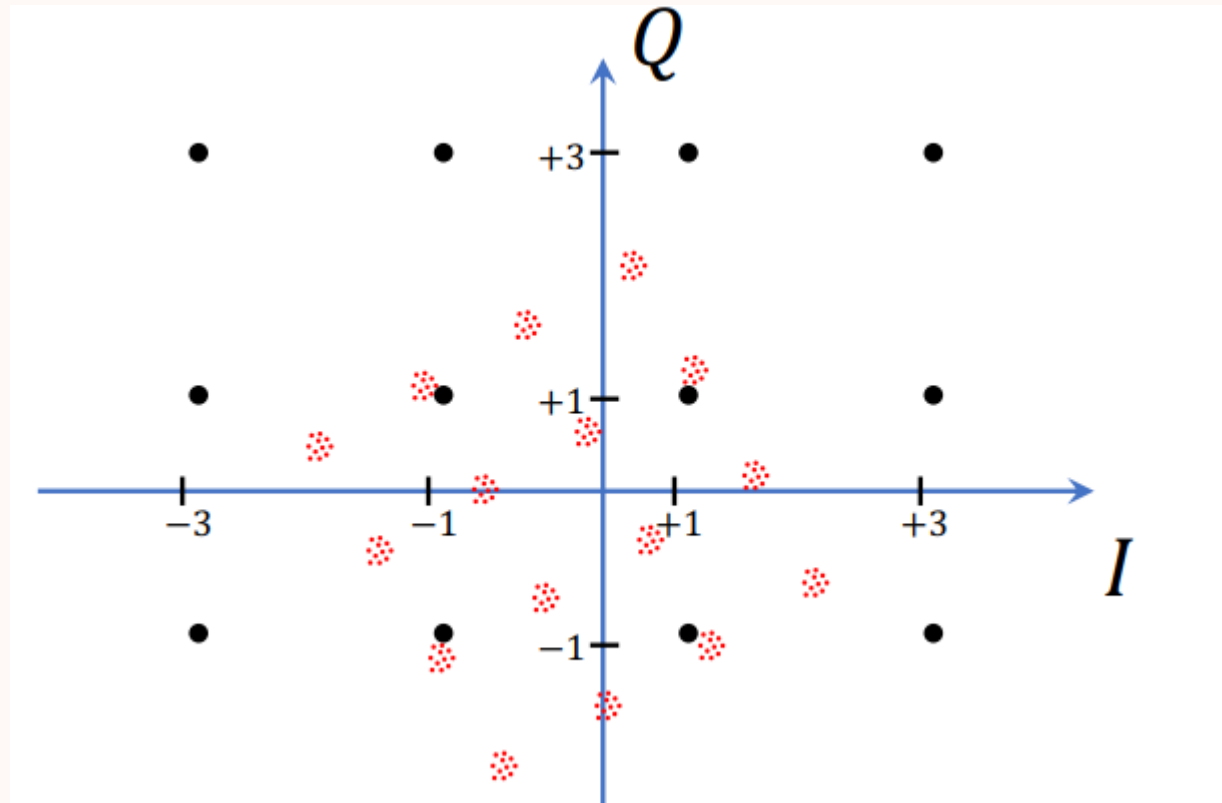
$x(t)$



$y(t) = h * x(t) + n(t)$

Channel

Consider 16-QAM



$$y(t) = h * x(t) + n(t)$$

Multiple Path Channel

- The signal arrives at destination with multiple delays and attenuation

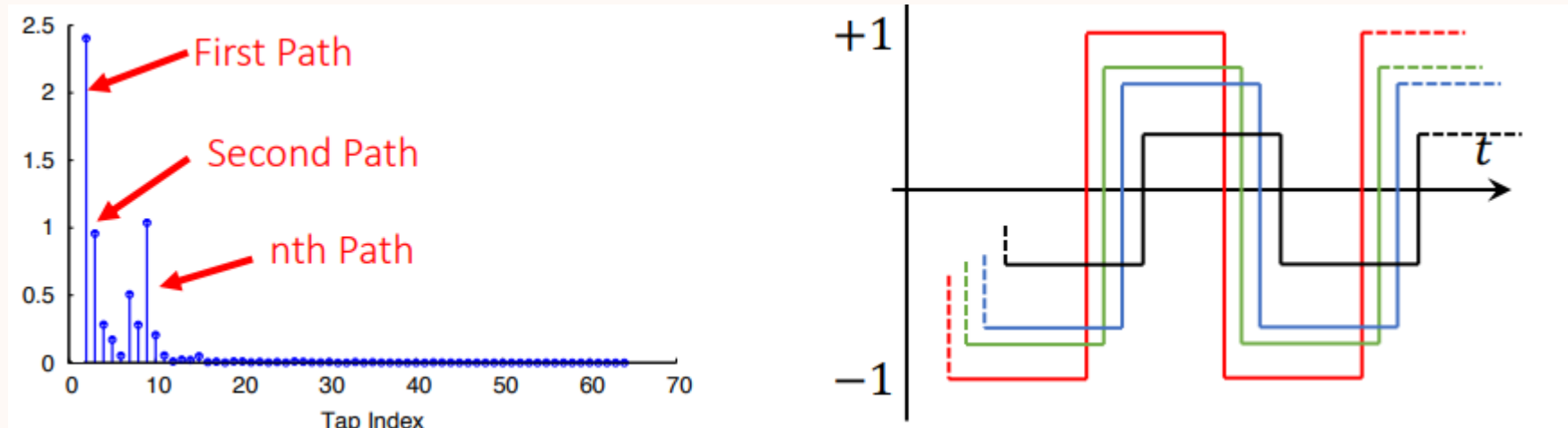
$$y(t) = \alpha_0 e^{\phi_0} x(t - \tau_0) + \alpha_1 e^{\phi_1} x(t - \tau_1) + \dots + \alpha_{L-1} e^{\phi_{L-1}} x(t - \tau_{L-1})$$

$$y(t) = \sum_k \alpha_k e^{\phi_k} x(t - \tau_k)$$

$$y(t) = \sum_k h(\tau_k) x(t - \tau_k)$$

$$y(t) = h(t) * x(t)$$

Multiple Path Channel: Inter Symbol Interference

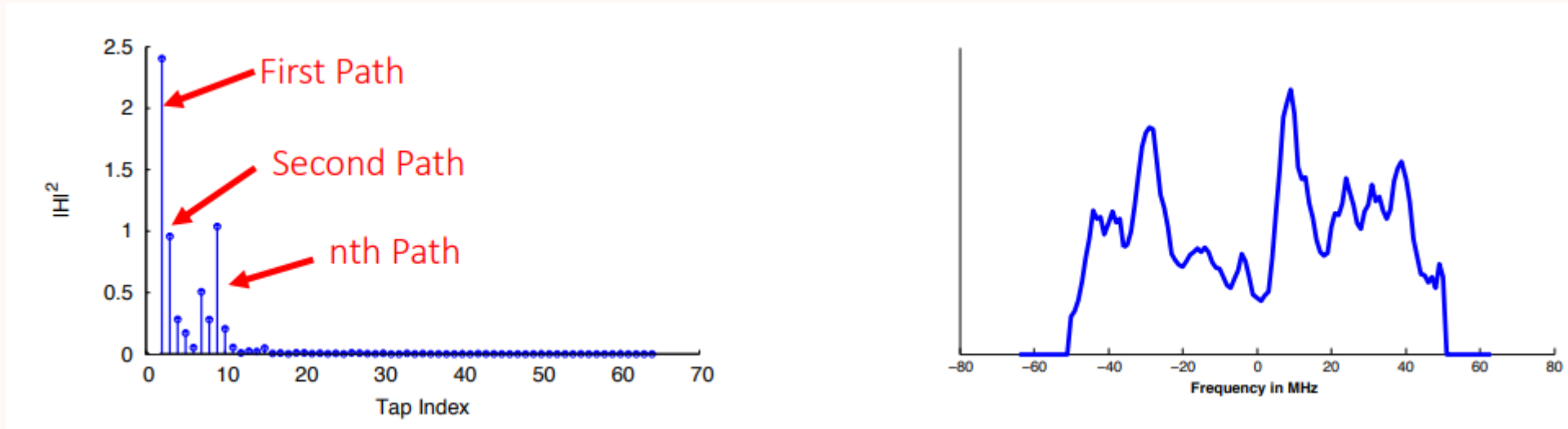


Multi Tap Channel => Inter Symbol Interference (ISI)
Symbols arriving along late paths
interfere with following symbols.

Multiple Path Channel

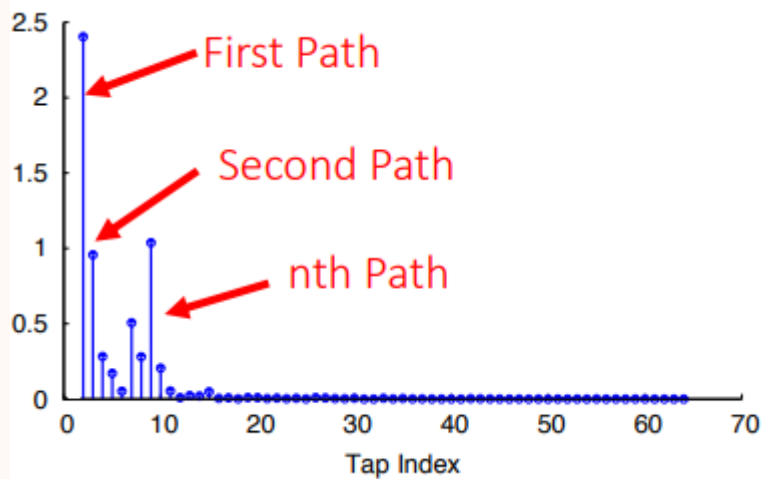
$$y(t) = h(t) * x(t)$$

$$Y(f) = H(f)X(f)$$

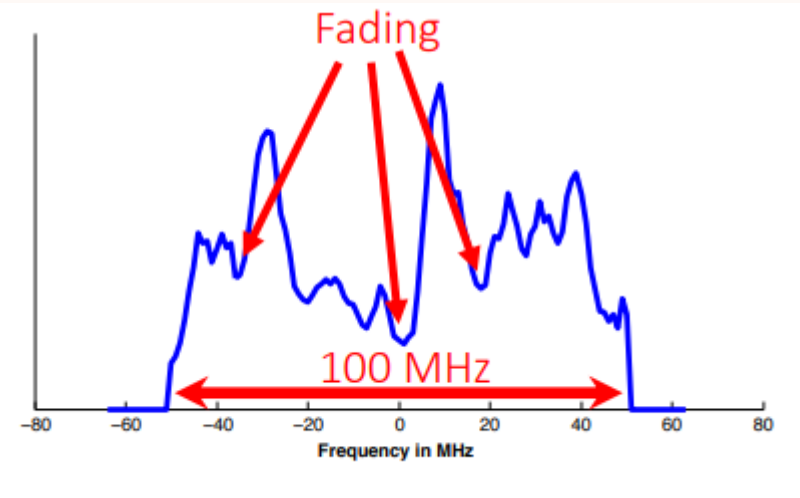


Multiple Path Channel

$$y(t) = h(t) * x(t)$$

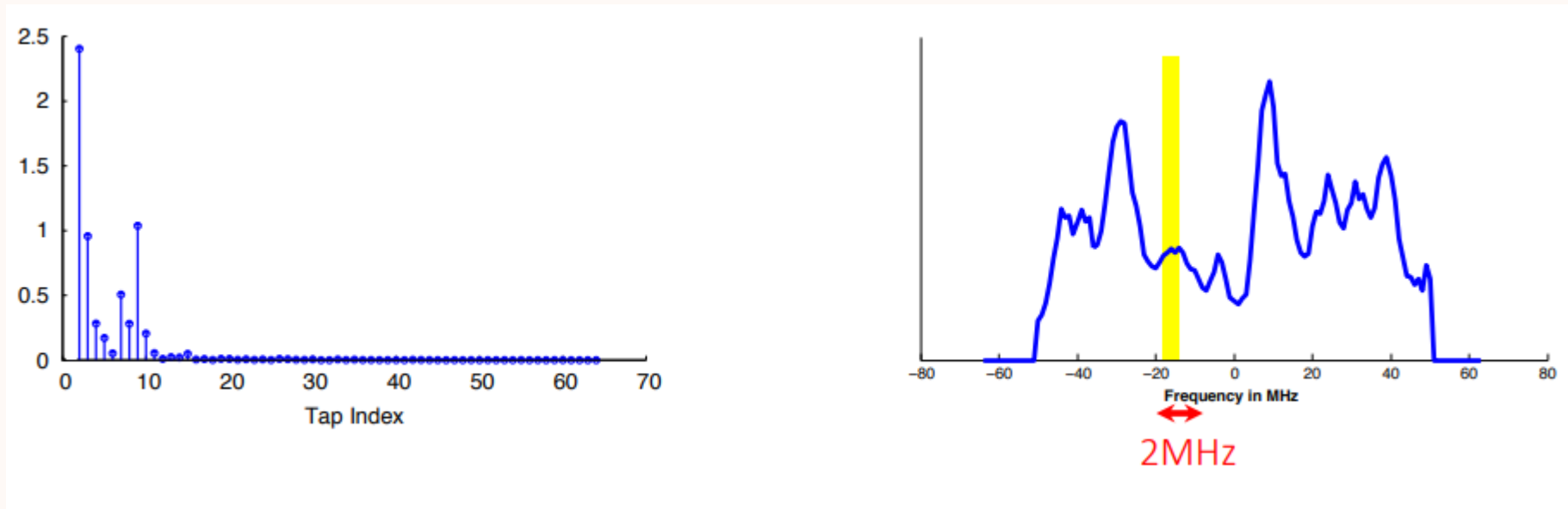


$$Y(f) = H(f)X(f)$$

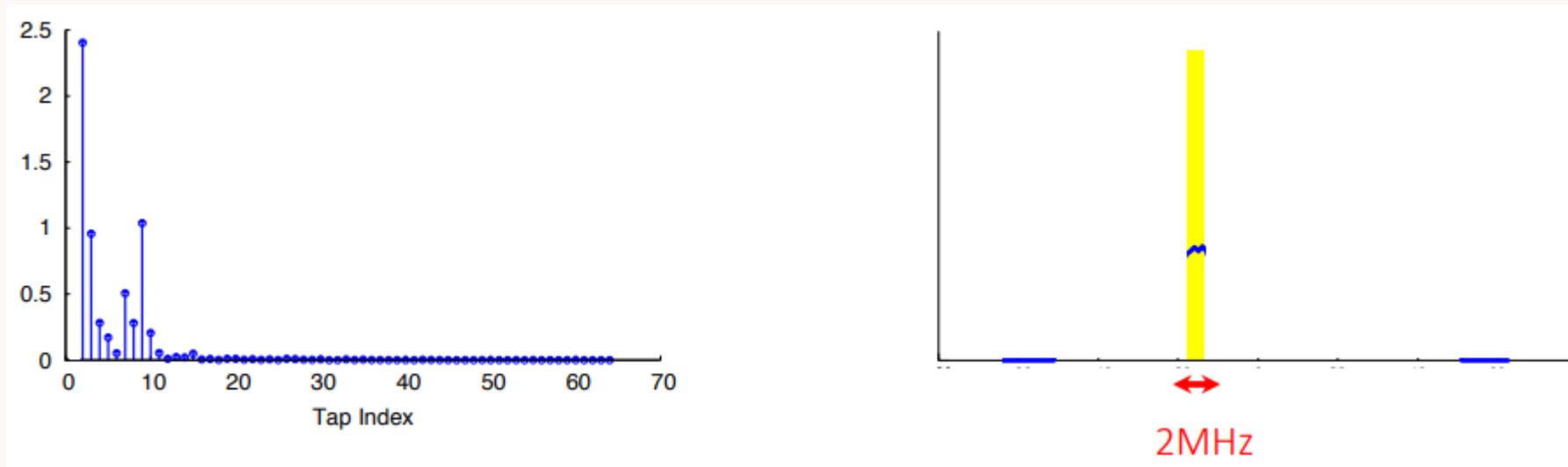


Frequency Selective Fading
Symbols arriving along different paths sum up destructively

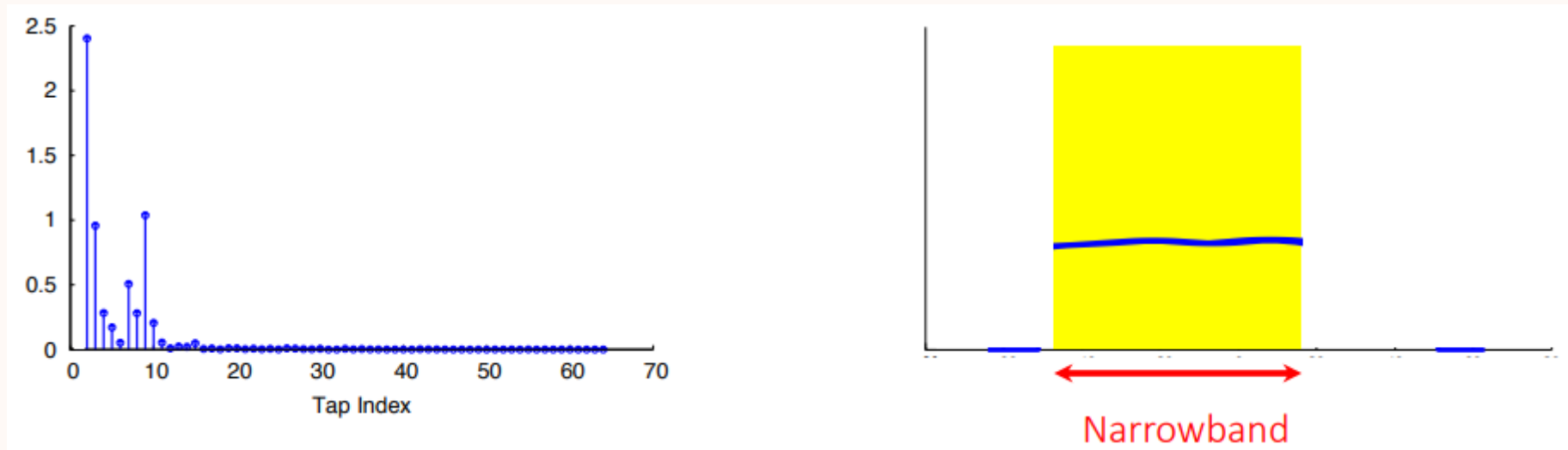
Multiple Path Channel: Narrowband Channel



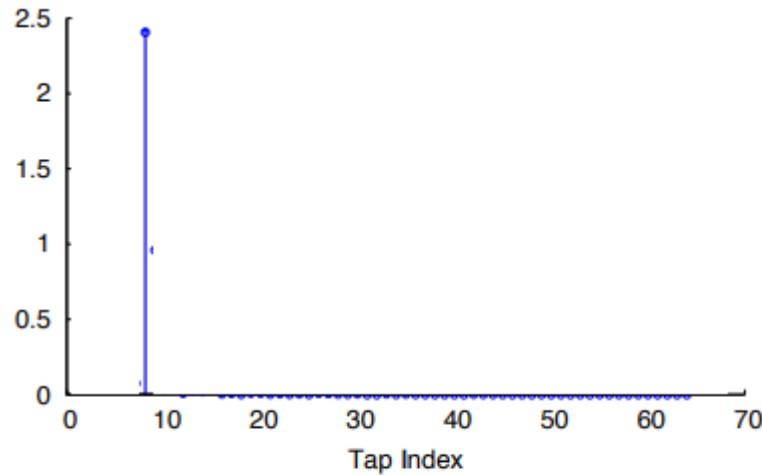
Multiple Path Channel: Narrowband Channel



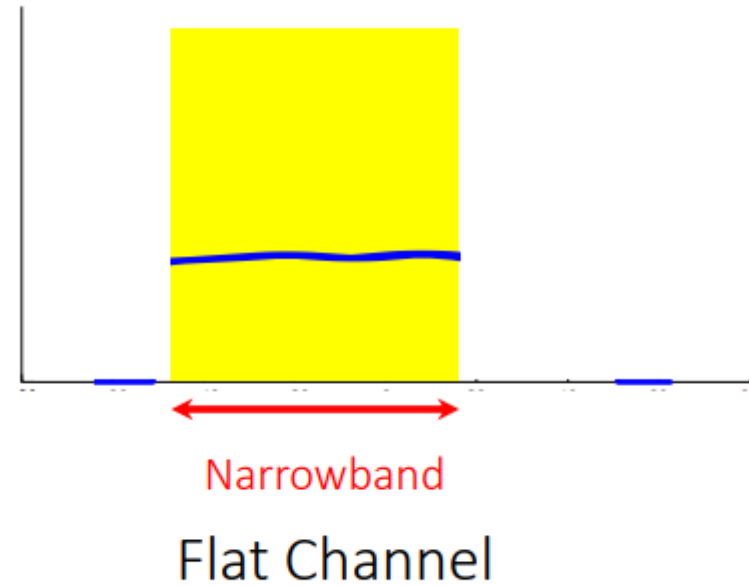
Multiple Path Channel: Narrowband Channel



Multiple Path Channel: Narrowband Channel

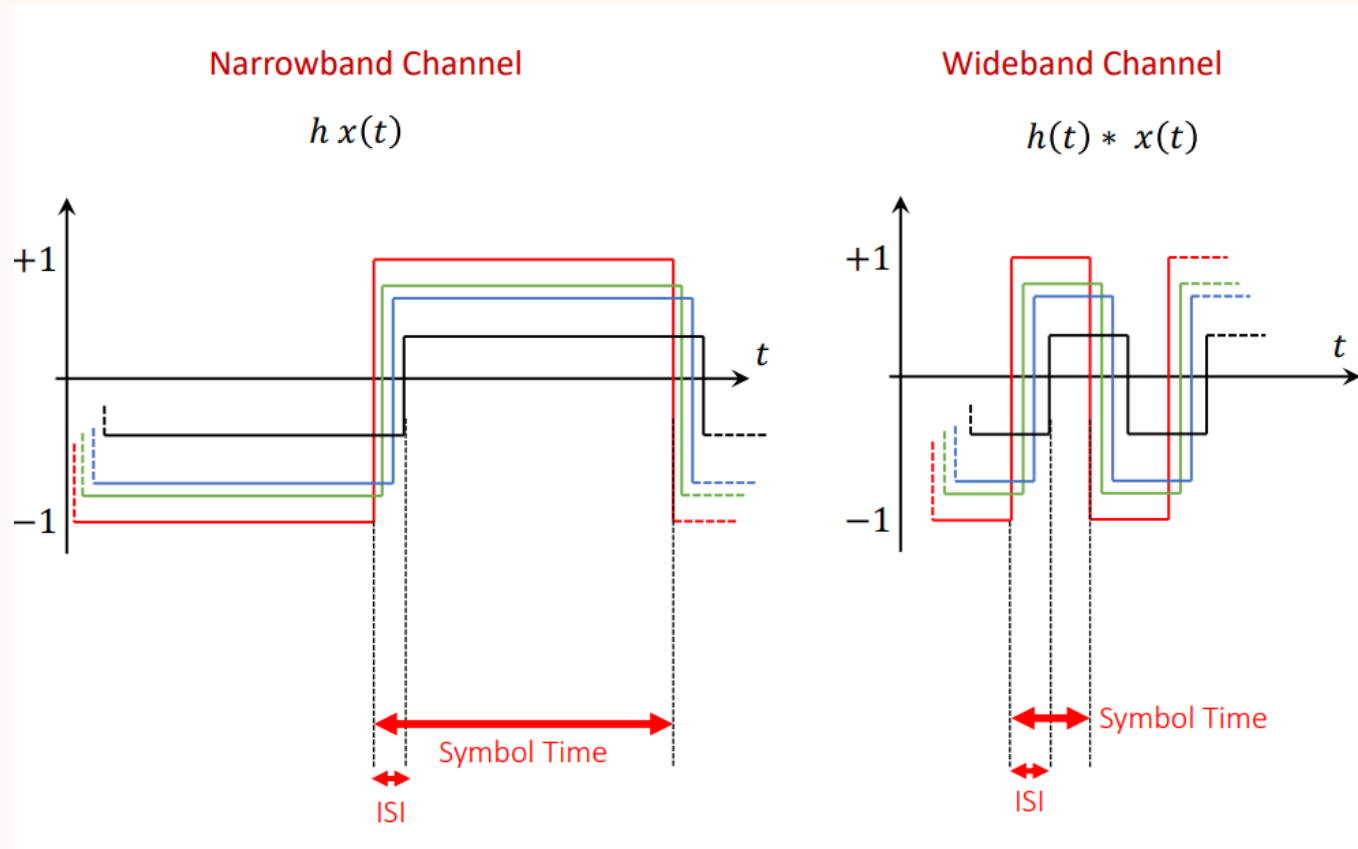


$$\text{Symbol time: } T \propto \frac{1}{\text{Bandwidth}} \gg \tau_k$$



Narrowband Channel is Approximated by a Single Tap Channel

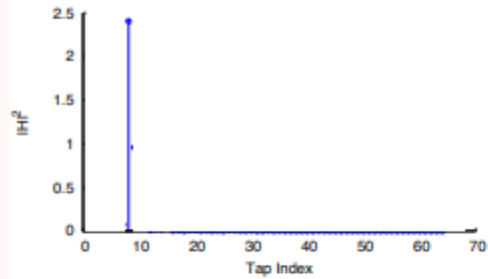
Multiple Path Channel: Narrowband Channel



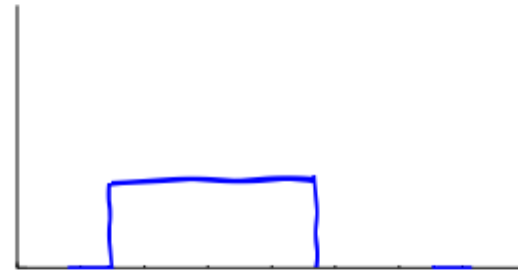
Wireless Channel

Narrowband Channel

$$h x(t) \Leftrightarrow h X(f)$$



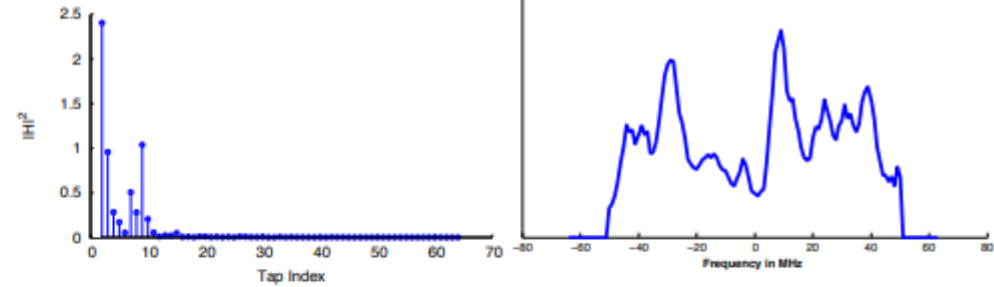
\approx Single Tap



\approx Flat Channel

Wideband Channel

$$h(t) * x(t) \Leftrightarrow H(f) X(f)$$



Multi-tap
Channel
(ISI)

Frequency
Selective Channel

Channel Equalization

- Channel equalization is the process of reducing amplitude, frequency and phase distortion in a radio channel with the intent of improving transmission performance.
- *Channel estimation* provides information about distortion of the transmission signal when it propagates through the channel.
- This information is then used by equalizers so that the fading effect and/or co-channel interference can be removed and the original transmitted signal can be restored.
- Channel Equalization is required to deal with ISI

Channel Equalization

- Estimating $h(t)$
- Correcting for $h(t)$

$$y(t) = h(t) * x(t)$$
$$\tilde{x}(t) = f(t) * y(t) = f(t) * h(t) * x(t)$$

Ideally $f(t) = h^{-1}(t)$

$$\tilde{x}(t) = f(t) * y(t) = h^{-1}(t) * h(t) * x(t) = x(t)$$

Channel Estimation and Correction

- Send training sequence (known bits)
- $x(0) = 1 \Rightarrow y(0) = 1 + n(0)$
- $x(1) = 1 \Rightarrow y(1) = 1 + n(1)$
- $x(2) = -1 \Rightarrow y(2) = -1 + n(2)$

Estimate Channel

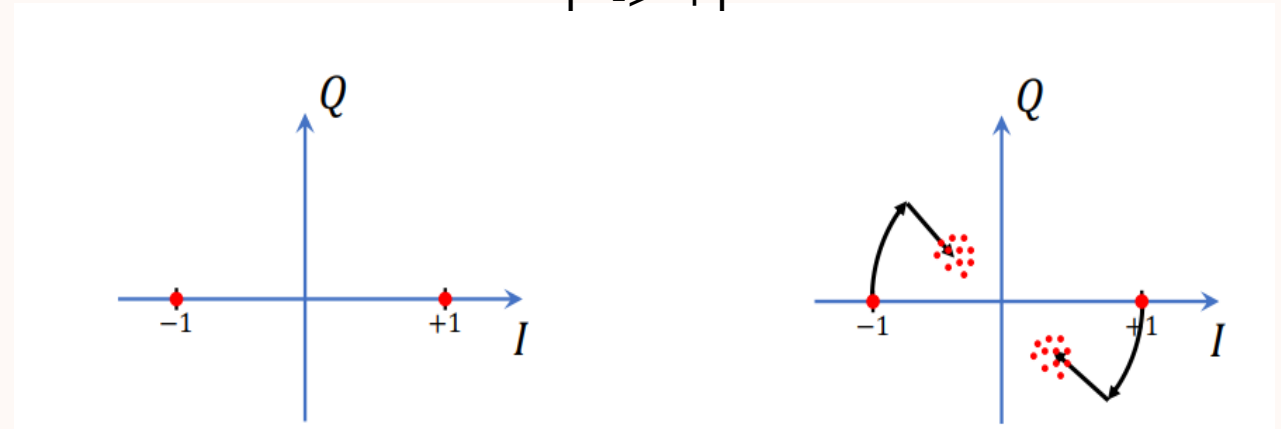
$$\tilde{h} = \sum_k \frac{y(k)}{x(k)}$$

Channel Correction

$$\tilde{x}(t) = \frac{y(t)}{\tilde{h}}$$

Consider BPSK modulation

0 \rightarrow -1
1 \rightarrow +1



$$y(t) = h * x(t) + n(t)$$

Channel Correction Mechanisms

- Forward Error Correction: The receiver only uses the information contained in the incoming digital transmission and corrects bit errors in the data
- Adaptive Equalization: Adjust equalization techniques based on the channel
- Adaptive Modulation and Coding: Choose modulation and coding based on the channel

Channel Correction Mechanisms

- Orthogonal Frequency Division Multiplexing: split signal into multiple lower bit rate streams that are transmitted over precisely spaced frequencies
- Spread Spectrum: Transmitted signal is spread over a wide frequency band

Summary

- The signal arrives at destination with multiple delays and attenuation
$$y(t) = \alpha_0 e^{\phi_0} x(t - \tau_0) + \alpha_1 e^{\phi_1} x(t - \tau_1) + \dots + \alpha_{L-1} e^{\phi_{L-1}} x(t - \tau_{L-1})$$
- Multipath effect will give rise to Inter Symbol Interference (ISI)
- Channel Equalization is required to deal with ISI