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## 3rd Exercise in HPC

## Exercise 1

Make yourself acquainted with firstprivate and lastprivate, i.e., write a little OpenMP program containing parallel sections making use of firstprivate and lastprivate and print the effect.

## Exercise 2

The Jacobi method is an iterative methods to solve a linear system

$$Ax = b$$
.

The iterates are defined as

$$u_{n+1} = -D^{-1}(L+U)u_n + D^{-1}b,$$

where A = L + D + U and D = diag(A) is the diagonal of A, L a lower triangular matrix and U an upper triangular matrix. Use  $u_0 = 0$  as a start vector. Remark: If  $||D^{-1}(L + U)||_{\infty} < 1$  then this iteration converges.

Define the  $n \times n$ -Matrix

$$A = \begin{pmatrix} +2^{0} & -2^{-2} & -2^{-4} & -2^{-8} & \dots & -2^{-2^{n-1}} \\ -2^{-2} & +2^{0} & -2^{-2} & -2^{-4} & \dots & -2^{-2^{n-2}} \\ -2^{-4} & -2^{-2} & +2^{0} & -2^{-2} & \dots & -2^{-2^{n-3}} \\ -2^{-8} & -2^{-4} & -2^{-2} & +2^{0} & \dots & -2^{-2^{n-4}} \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ -2^{-2^{n-1}} & -2^{-2^{n-2}} & -2^{-2^{n-3}} & -2^{-2^{n-4}} & +2^{0} \end{pmatrix}$$

and the right hand side  $b = (1, ..., 1)^T$ .

Implement a parallel Jacobi iteration using OpenMP. The iterations is stopped when the norm of the residual r = b - Au is below  $\varepsilon$ . What speedups do you achieve if you change the number of threads? Choose, e.g., n = 20000 and  $\varepsilon = 1e - 3$ .