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Principles of Programming Languages Homework 1 Section 02

## 1

**1.1** 
$$f(x) = x + 1, x > 0$$

#### Rules

- $1. \$ \rightarrow |$
- 2.  $|\# \to |$

#### Sequence

- 1.  $||\#| \rightarrow |||\#| \pmod{1}$
- 2.  $||||\# \rightarrow ||||$  (Rule 2)

**1.2** 
$$f(x) = 2x, x > 0$$

#### Rules

- 1.  $|\rightarrow||$
- $2. \$| \rightarrow |$
- 3.  $|\# \to |$

#### Sequence

- 1.  $||\# \rightarrow |||$  (Rule 1)
- 2.  $|||||# \rightarrow |||||# (Rule 2)$
- 3.  $|||||\# \rightarrow |||||$  (Rule 3)

# **1.3** f(x,y) = x + y, x, y > 0

#### Rules

- 1. &  $\rightarrow NULL$
- 2.  $| | \rightarrow |$
- 3.  $|\# \to |$

#### Sequence

- 1.  $||\&|| \# \rightarrow |||| (\text{Rule 1})$
- 2.  $||||# \rightarrow ||||#(Rule 2)$
- 3.  $||||# \rightarrow ||||| \text{ (Rule 3)}$

### 2

#### 2.1 Rules

- 1.  $(0+0) \to 0$
- 2.  $(0+1) \to 1$
- 3.  $(1+0) \to 1$
- 4.  $(0+2) \to 2$
- 5.  $(2+0) \rightarrow 2$
- 6.  $(1+1) \rightarrow 2$
- 7.  $(1+2) \to 0$
- 8.  $(2+1) \to 0$
- 9.  $(2+2) \to 1$

## 2.2 Sequence Example

**Sequence 1:** (0 + (1 + 2))

- 1.  $((1+2)+0) \rightarrow (0+0)$  (Rule 7)
- 2.  $(0+0) \to 0$  (Rule 1)

**Sequence 2:** (1 + (2 + 2))

- 1.  $(1 + (2 + 2)) \rightarrow (1 + 1)$  (Rule 9)
- 2.  $(1+1) \to 2$  (Rule 6)

#### 2.3

No, in ((1+1)+(2+2)) 2 rules can be applied

### 3

#### 3.1

Yes:  $r^+ = r \& r^*$ 

### 3.2

No: At least one of those operators is necessary to express an infinite quantity

#### 4

$$R = (-|\epsilon)(digit)^{+}.(digit)^{+}(E(-|\epsilon)(digit)^{+}|\epsilon)$$

## **5**

#### 5.1

All strings/combinations over the alphabet a, b including the empty string

## 5.2

All strings over the alphabet 0,1 which begin with 1 and end in 001 or 011

# 6

## 6.1

 $R = (b^*c|a|c|d)^*b^*$ 

### 6.2

```
\begin{split} R &= a^*(b|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*\\ &|a^*(c|\epsilon)a^*(b|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*\\ &|a^*(c|\epsilon)a^*(c|\epsilon)a^*(b|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*\\ &|a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(b|\epsilon)a^*(c|\epsilon)a^*\\ &|a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(b|\epsilon)a^*(c|\epsilon)a^*\\ &|a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(c|\epsilon)a^*(b|\epsilon)a^*\\ \end{split}
```