

Assignment 5

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Question 1

$$H(Y) = - \sum_{i=1}^K P(Y=y_i) \log_2 P(Y=y_i)$$

$$P(Y=\text{Meh}) = 5/10 = 1/2$$

$$P(Y=\text{Yummy}) = 5/10 = 1/2$$

$$H(Y) = -1/2 \log_2 1/2 - 1/2 \log_2 1/2 = 1/2 + 1/2 = 1$$

Question 2

$$IG(X) = H(Y) - H(Y|X)$$

$$IG(X=\text{Visual Defects}) = H(Y) - H(Y|X=\text{Visual Defects})$$

$$H(Y) = 1$$

$$H(Y|X) = - \sum_{j=1}^K P(X=x_j) \sum_{i=1}^K P(Y=y_i | X=x_j) \log_2 P(Y=y_i | X=x_j)$$

$$P(\text{Visual Defects} = \text{some}) = 3/10$$

$$P(\text{Visual Defects} = \text{none}) = 4/10$$

$$P(\text{Visual Defects} = \text{Many}) = 3/10$$

	X		
	some	None	Many
Y=Meh	3	2	0
Y=Yummy	0	2	3

$$= -3/10 (1 \log_2 1 + 0 \log_2 0) - 4/10 (1/2 \log_2 1/2 + 1/2 \log_2 1/2) - 3/10 (0 \log_2 0 + 1 \log_2 1)$$

$$= -4/10 = -0.4$$

$$IG(X) = 1 - 0.4 = 0.6$$

Question 3

$$H(\text{Taste} | \text{Visual Defect} = \text{some})$$

$$= -P(X=\text{some}) (P(Y=\text{Meh} | X=\text{some}) \log_2 P(Y=\text{Meh} | X=\text{some}) + P(Y=\text{Yummy} | X=\text{some}) \log_2 P(Y=\text{Yummy} | X=\text{some}))$$

$$= -3/10 (1 \log_2 1 + 0 \log_2 0) = 0$$

$$H(\text{Taste} | \text{Visual Defect} = \text{none})$$

$$= -P(X=\text{none}) (P(Y=\text{Meh} | X=\text{none}) \log_2 P(Y=\text{Meh} | X=\text{none}) + P(Y=\text{Yummy} | X=\text{none}) \log_2 P(Y=\text{Yummy} | X=\text{none}))$$

$$= -4/10 (1/2 \log_2 1/2 + 1/2 \log_2 1/2) = -4/10 (-0.5 - 0.5) = -4/10 (-1)$$

$$= 4/10 = 0.4$$