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### Python for Data Analytics

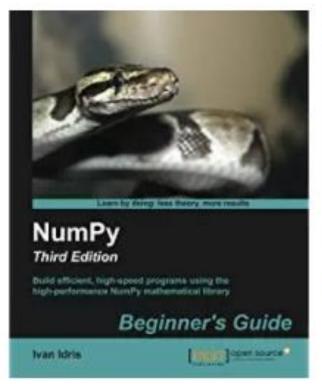
# NumPy I

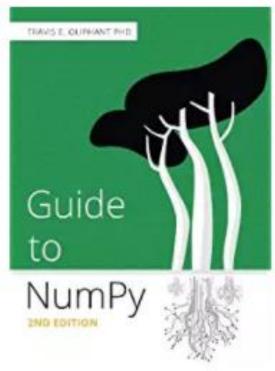


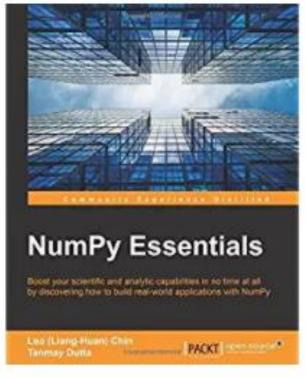
### Outline

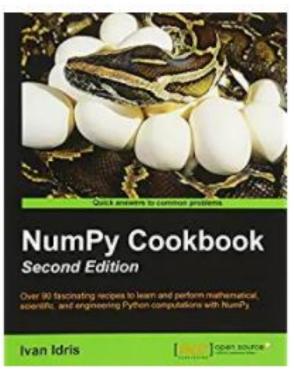
- What is NumPy?
- Creating Arrays
- Manipulating Arrays
- Statistical Operations
- Matrix Operations

## Many NumPy Books









## What is "NumPy" Module?

- The "NumPy" (Numeric Python) package provides basic routines for manipulating large arrays and matrices of numeric data
- The "SciPy" (Scientific Python) package extends the functionality of NumPy with a substantial collection of useful algorithms
  - Minimization, Fourier transformation, regression, and other applied math techniques
- Numpy and SciPy are open source add-on modules (not Python Standard Library)
- More than functionalities of commercial packages like MatLab
- To catch up functionalities of R
- >>> import numpy as np

## NumPy History

- Numeric (ancestor of Numpy)
  - Released in 1995 by Jim Hugunin by generalizing Jim Fulton's matrix package
- Numarray
  - A more flexible replacement for Numeric
  - Faster for large arrays, slower than Numeric on small arrays
- SciPy module
  - Created by Travis Oliphant et al. in 2001
  - Provides scientific and technical operations
  - NumPy I.0 released (as part of SciPy) in 2006 by porting Numarray's features to Numeric
- NumPy module separated from SciPy as a stand-alone package

## numpy.ndarray: The N-dimensional Array

- A multidimensional container of items of the same type and size
  - shape: a tuple of N non-negative integers that specify the sizes of each dimension
  - data-type object (dtype): the type of items in the array
- ID numpy.ndarray object
  - Example: array([3,6]) array([3.5,6.4,7.2])
- 2D numpy.ndarray object
  - Example: array([[1,0,2], [3,5,2]])
- 3D numpy.ndarray object
  - Example: array([[[0,0,1],[1,2,3]], [[1,0,2],[2,3,4]], [[3,5,2],[1,1,1]]])

## Array Example

```
>>> import numpy as np
>>> x = np.array([[1, 2, 3], [4, 5, 6]], int)
>>> print(x)
[[1 2 3]
 [4 5 6]]
>>> type(x)
<class 'numpy.ndarray'>
>>> x.shape
(2, 3)
                       # (number of rows, number of columns)
>>> x.dtype
dtype('int64')
```

## List vs. Array.array vs. Numpy.ndarray

#### Lists

- Simple
- Can't constrain the type of elements stored in a list

### Array.array

- All elements of the array must be of the same numeric type
- May be used to interface with C code

### Numpy.ndarray

 Supports various computations on arrays and matrices

```
>>> a = [[0]*3 for i in range(3)]
>>> a
[[0, 0, 0], [0, 0, 0], [0, 0, 0]]
>>> b = [1, 3.5, 'hello']
```

```
>>> import array
>>> a = array.array('i', [1, 2, 3])
>>> a
array('i', [1, 2, 3])
```

```
>>> import numpy
>>> a = numpy.array([1, 2, 3], float)
>>> a
array([1., 2., 3.])
```

# Creating Arrays

# array()

- np.array (object, dtype=None, ...)
  - object: usually a list
  - dtype: the desired data type
    - If omitted, the type will be determined as the minimum type required to hold the objects

```
>>> l = [1, 2, 3, 4, 5]
>>> np.array(l)
>>> np.array(l, int)
>>> np.array(l, dtype='i')
>>> np.array(l, dtype=np.uint8)
>>> np.array(l, dtype='f')
>>> np.array(l, float)
```

Data types		Type code
Boolean	bool	?
Integers	<pre>int8 int16 int32 int64 (int)</pre>	i1, b i2, h i4, i i8, l, q
Unsigned integers	uint8 uint16 uint32 uint64	u1, B u2, H u4, I u8, L, Q,
Floating points	float16 float32 float64 (float) float128	f2 f4, f f8, d f16, g
Complex	<pre>complex64 complex128 (complex) complex256</pre>	c8, F c16, D c32, G
Unicode string	unicode	U

## np.inf and np.nan

- np.inf (infinity)
  - Too large to be represented
  - e.g., n / 0, np.inf \* np.inf, np.inf + np.inf,...
- np.nan (not-a-number)
  - A value that is undefined or unrepresentable
  - e.g., 0 / 0, np.inf / np.inf, np.inf \* 0, np.inf - np.inf, ...

```
>>> np.inf
inf

>>> a = array([3, 2, 5])
>>> a / 0
array([inf, inf, inf])
```

```
>>> np.nan
nan
>>> np.log(-1)
nan
>>> np.log([-1, 1, 2])
array([ nan, 0. , 0.69314718])
```

## full() and empty()

- np.full(shape, value[, dtype][, order])
  - Return a new array of given shape and type, filled with value
- np.full\_like(a, value, ...)

- np.empty (shape[, dtype][, order])
  - Return a new array of given shape and type, without initializing entries
  - Faster than others
- np.empty\_like(a, ...)

## zeros() and ones()

- np.zeros (shape[, dtype][, order])
  - Return a new array of given shape and type, filled with zeros
  - order: 'C' = row-major (C-style),
     'F' = column-major (Fortran-style)
- np.ones (shape, [, dtype][, order])
  - Return a new array of given shape and type, filled with ones

## zeros\_like() and ones\_like()

- np.zeros\_like(a[, dtype], ...)
  - Return an array of zeros with the same shape and type as a given array

- np.ones\_like(a[, dtype], ...)
  - Return an array of ones with the same shape and type as a given array

## identity() and eye()

- np.identity(n[, dtype])
  - Return the identity array (a square array with ones on the main diagonal)
  - n: number of rows (and columns)

- np.eye(N[, M][, k][, dtype][, order])
  - Return a 2D array with ones on the diagonal and zeros elsewhere
  - M: number of columns (default N)
  - k: index of the diagonal (default 0)

## arange()

- np.arange([start, ]stop[, step][, dtype])
  - Return an array with evenly spaced values within a given interval: [start, stop)
  - When using a non-integer step, it may produce unexpected results
    - → Use np.linspace() instead

```
>>> np.arange(10, 30, 5)
array([10 15 20 25])
>>> np.arange(0, 2, 0.3)
array([0.  0.3 0.6 0.9 1.2 1.5 1.8])
>>> np.arange(0, -1, -0.1)
array([ 0. , -0.1, -0.2, -0.3, -0.4, -0.5, -0.6, -0.7, -0.8, -0.9])
>>> np.arange(8.0, 8.4, 0.05)
array([8. , 8.05, 8.1 , 8.15, 8.2 , 8.25, 8.3 , 8.35, 8.4])
```

## linspace()

- np.linspace(start, stop[, num][, endpoint]...)
  - Return an array with evenly spaced numbers over a specified interval: [start, stop]
  - num: the number of evenly spaced samples (default 50)
  - endpoint: if True, the endpoint of the interval is excluded (default False)

## logspace()

- np.logspace(start, stop[, num][, endpoint][, base], ...)
  - Return *num* numbers spaced evenly on a log scale
  - In linear space, the sequence starts at basestart and ends with basestop
  - base: the base of the log space (default: 10.0)

```
>>> np.logspace(0, 1, 11)
array([ 1. , 1.25892541, 1.58489319, 1.99526231, 2.51188643,
       3.16227766, 3.98107171, 5.01187234,
                                            6.30957344, 7.94328235,
      10.
>>> import math
>>> math.log10(3.16227766)
0.499999999768755
```

## geomspace()

- np.geomspace(start, stop[, num][, endpoint], ...)
  - Return *num* numbers spaced evenly on a log scale (a geometric progression)
  - Each output sample is a constant multiple of the previous

```
>>> import math
>>> [ math.exp(i) for i in np.linspace(math.log(1), math.log(1000), 4) ]
>>> np.geomspace(1, 1000, 4)
      1., 10., 100., 1000.])
>>> np.geomspace(-1000, -1, num=4)
array([-1000., -100., -10., -1.])
>>> np.geomspace(1, 256, 9)
       1., 2., 4., 8., 16., 32., 64., 128., 256.])
```

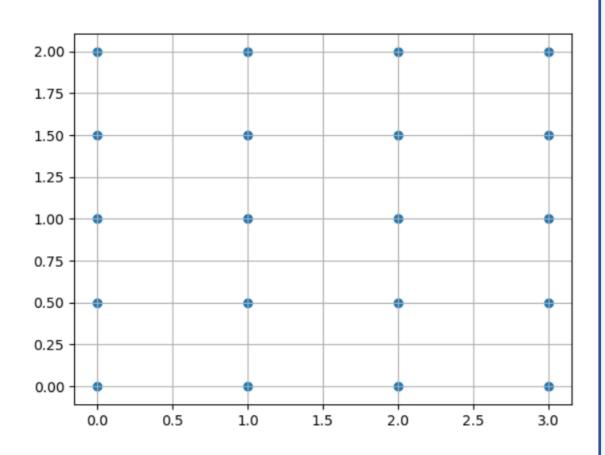
## meshgrid()

- np.meshgrid(x1, x2, ..., xn, ...)
  - Return coordinate matrices from coordinate vectors

```
\Rightarrow x = np.linspace(0, 2, 3)
>>> X
array([0., 1., 2.])
>>> y = np.linspace(0, 1, 3)
>>> V
array([0., 0.5, 1.])
>>> xv, yv = np.meshgrid(x, y)
```

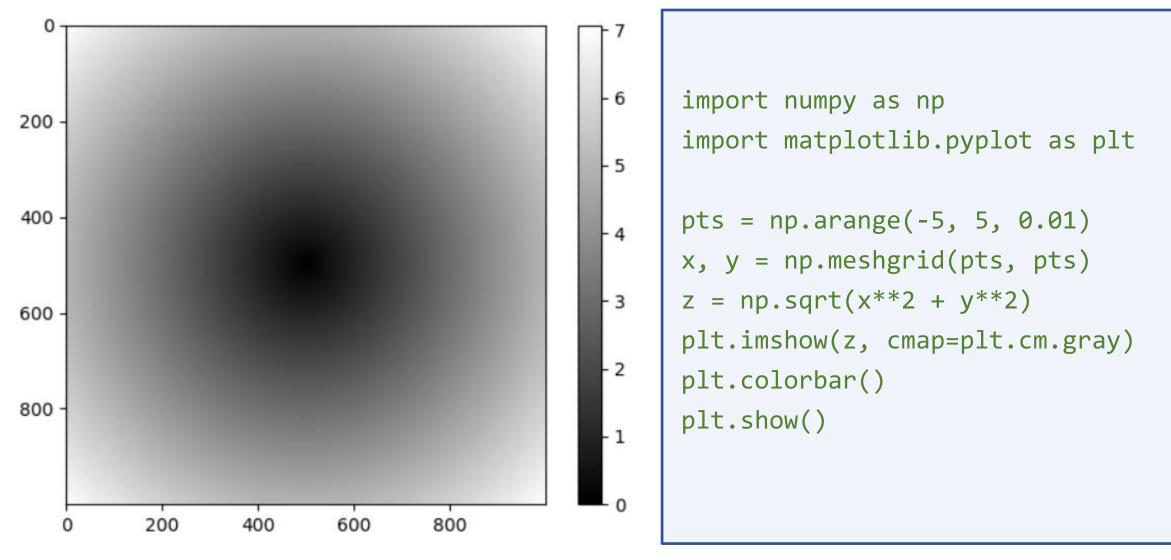
```
>>> XV
array([[0., 1., 2.],
       [0., 1., 2.],
      [0., 1., 2.]
>>> yv
array([[0., 0., 0.],
      [0.5, 0.5, 0.5],
       [1., 1., 1.]
```

## meshgrid()



```
>>> import matplotlib.pyplot as plt
>>> plt.scatter(xv, yv)
>>> plt.grid(True)
>>> plt.show()
>>> mg = [list(zip(x,y)) for x, y \]
         in zip(xv, yv)]
>>> mg
[[(0.0, 0.0), (1.0, 0.0), (2.0, 0.0)],
[(0.0, 0.5), (1.0, 0.5), (2.0, 0.5)],
[(0.0, 1.0), (1.0, 1.0), (2.0, 1.0)]
```

## meshgrid() Example



## random.random() and random.randint()

- numpy.random submodule provides various random number generators
- np.random.random(size)
  - Return random floats in the interval [0.0, 1.0)
  - size: integer or tuple of integers for output array shape
- np.random.randint(low[, high]
  [, size],...)
  - Return random integers in the interval [low, high)
  - If high is omitted, results are from [0, low)

```
>>> np.random.randint(100)
91
>>> np.random.randint(10, size=5)
array([6, 5, 9, 5, 1])
```

## random.rand() and random.randn()

- np.random.rand(d0, d1, ..., dn)
  - Return random floats in the interval [0.0, 1.0)
  - d0, d1, ..., dn: the dimensions of the output array (not tuple)

- np.random.randn(d0, d1, ..., dn)
  - Return samples from the "standard normal" distribution N(0, 1)
  - For random samples from  $N(\mu, \sigma^2)$ , use  $\sigma^*$  np.random.randn() +  $\mu$

## random.uniform()

- np.random.uniform([low=0.0], [high=1.0], [size])
  - Draw samples from a uniform distribution
  - Samples are uniformly distributed over the interval [low, high)

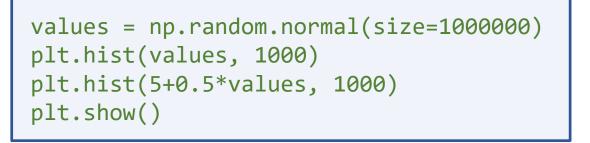
```
>>> np.random.uniform(1.0, 2.0)
1,6937903416817646
>>> np.random.uniform(1.0, 2.0, 5)
array([1.1922301 , 1.72618062, 1.82763685, 1.32765954, 1.45356649])
>>> import math
>>> np.random.uniform(0, math.pi, (3,4))
array([[0.53309063, 1.56158409, 2.34588318, 2.40615273],
       [0.28675017, 0.37922173, 1.24792002, 0.05974539],
       [2.02903176, 0.98991193, 0.61068395, 2.40537881]])
```

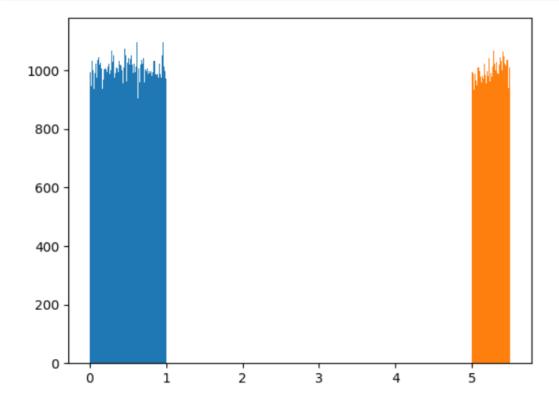
## random.normal()

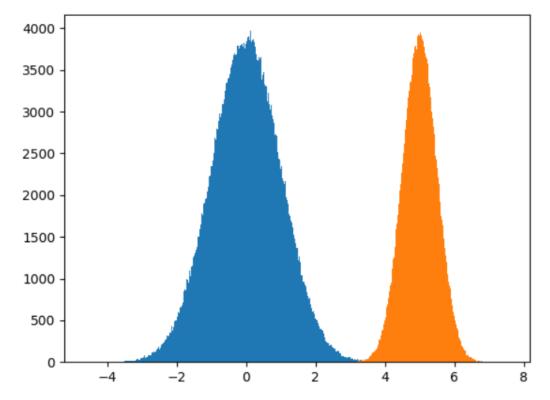
- np.random.normal([loc=0.0], [scale=1.0], [size])
  - Draw samples from a normal (Gaussian) distribution
  - loc: mean of the distribution, scale: standard deviation of the distribution
  - random.normal(loc, scale) == loc + scale\*random.normal()

### Uniform vs. Normal

```
values = np.random.uniform(size=1000000)
plt.hist(values, 1000)
plt.hist(5+0.5*values, 1000)
plt.show()
```





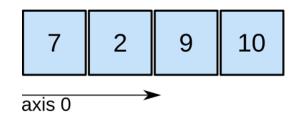


# Manipulating Arrays

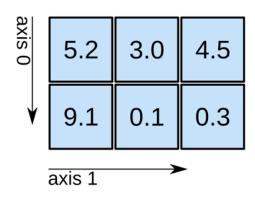
# **Array Shape**

### 2D array

### 1D array

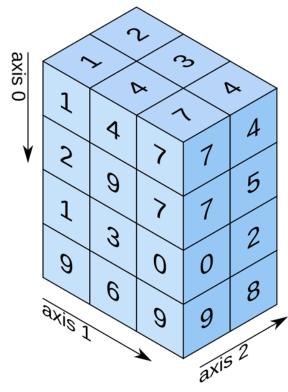


shape: (4,)



shape: (2, 3)

### 3D array



shape: (4, 3, 2)

## Reshaping

- a.reshape(shape)
  - Return an array containing the same data with a new shape

- a.resize(shape)
  - Change shape and size of array in-place
  - Same as:a.shape = shape

- a.flatten()
  - Return a flattened array

```
>>> a=np.arange(6)
>>> a.shape
(6,)
>>> a.reshape(2,3)
array([[0, 1, 2],
       [3, 4, 5]]
>>> a.resize(2,3)
>>> a
array([[0, 1, 2],
       [3, 4, 5]])
>>> a.flatten()
array([0, 1, 2, 3, 4, 5])
>>> a.shape = (1, 6)
                        # 555
```

## Reshaping (cont'd)

- One dimension can be -I in a.reshape()
  - The value is inferred from the length of the array and remaining dimensions

```
>>> a = np.arange(12)
>>> a.reshape(3, -1)
array([[ 0, 1, 2, 3],
      [4, 5, 6, 7],
      [ 8, 9, 10, 11]])
>>> a.reshape(-1, 3)
array([[ 0, 1, 2],
      [ 3, 4, 5],
      [6, 7, 8],
      [ 9, 10, 11]])
```

```
>>> a.reshape(2, 2, -1)
array([[[ 0, 1, 2],
       [ 3, 4, 5]],
      [[ 6, 7, 8],
      [ 9, 10, 11]]])
>>> a.reshape(-1, 2, 3)
array([[[ 0, 1, 2],
       [ 3, 4, 5]],
      [[ 6, 7, 8],
       [ 9, 10, 11]]])
```

## Transposing

#### a.transpose(axes)

- Return a view of the array with axes transposed
- For a I-D array, no effect
- For a 2-D array, this is a standard matrix transpose
- For an n-D array and axes are given, their order indicates how the axes are permuted. Otherwise, shapes are reversed

```
>>> a = np.arange(6)
>>> a.transpose()
array([0, 1, 2, 3, 4, 5])
>>> b = a.reshape(3,2)
>>> b
array([[0, 1],
       [2, 3],
       [4, 5]])
>>> b.transpose()
array([[0, 2, 4],
       [1, 3, 5]])
>>> c = np.arange(6).reshape(1,2,3)
>>> c.transpose().shape
(3, 2, 1)
```

## Concatenating

- np.concatenate((a1, a2, ..., an), axis)
  - Join a sequence of arrays along an existing axis
  - a1, a2, ..., an: sequence of arrays
  - axis: the axis along which the arrays will be joined. If axis is None, arrays are flattened before use. (default 0)

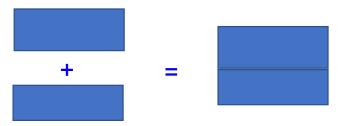
```
>>> a = np.array([1, 2, 3])
>>> b = np.array([4, 5, 6])
>>> np.concatenate((a, b))
array([1, 2, 3, 4, 5, 6])
```

## Stacking

- np.hstack(tup)
  - Stack arrays in sequence horizontally (column wise)
  - tup: tuple of arrays



- np.vstack(tup)
  - Stack arrays in sequence vertically (row wise)
  - *tup*: tuple of arrays



```
>>> a=np.arange(6).reshape(2,3)
>>> b=np.arange(6,12).reshape(2,3)
>>> np.hstack((a,b))
array([[0, 1, 2, 6, 7, 8],
      [ 3, 4, 5, 9, 10, 11]])
>>> np.vstack((a,b))
array([[0, 1, 2],
       [3, 4, 5],
       [6, 7, 8],
       [ 9, 10, 11]])
```

## Tiling

- np.tile(A, reps)
  - Construct an array by repeating A the number of times given by reps

```
>>> a = np.array([0, 1, 2])
>>> np.tile(a, 2)
array([0, 1, 2, 0, 1, 2])
>>> np.tile(a, (2, 2))
array([0, 1, 2, 0, 1, 2],
       [0, 1, 2, 0, 1, 2]])
>>> np.tile(a, (3,1,2))
array([[[0, 1, 2, 0, 1, 2]],
       [[0, 1, 2, 0, 1, 2]],
       [[0, 1, 2, 0, 1, 2]]]
```

```
>>> b = np.array([[1, 2], [3, 4]))
>>> np.tile(b, 2)
array([[1, 2, 1, 2],
       [3, 4, 3, 4]])
>>> np.tile(b, (2, 1))
array([[1, 2],
       [3, 4],
       [1, 2],
       [3, 4]])
```

## Indexing

#### Single element indexing

- Similar to Python lists
- Negative indices for indexing from the end of the array

### Multidimensional indexing

- Used for multidimensional arrays
- If you use fewer indices than dimensions, you get a subdimensional array
- x[0,2] == x[0][2]: x[0][2] is more inefficient as a new temporary array is created

```
>>> x = np.arange(10)
>>> x[2]
2
>>> x[-2]
8
```

```
>>> x.shape = (2, 5)
>>> x[0]
array([0, 1, 2, 3, 4])
>>> x[1, 3]
8
>>> x[0][2]
2
```

## Slicing

```
>>> x = np.arange(10)
>>> x[2:5]
array([2, 3, 4])
>>> x[:-7]
array([0, 1, 2])
>>> x[1:7:2]
array([1, 3, 5])
>>> x[::-1]
array([9, 8, 7, 6, 5, 4, 3, 2, 1, 0])
```

```
\Rightarrow y = np.arange(35).reshape(5,7)
>>> y[2,:]
array([14, 15, 16, 17, 18, 19, 20])
>>> y[:,2]
array([ 2, 9, 16, 23, 30])
>>> y[1:5:2,::3]
array([[ 7, 10, 13],
       [21, 24, 27]])
>>> y[-1:,-2:]
array([[33, 34]])
```

### Views

 Slices of arrays do not copy the internal array data, but only produce new "views" of the original data

```
>>> x = np.arange(6).reshape(2, 3)
>>> y = x[:,1]
>>> Y
array([1, 4])
>>> y[0] = 9
>>> Y
array([9, 4])
>>> X
array([[0, 9, 2],
       [3, 4, 5]]
```

## Index Arrays

NumPy arrays can be indexed with other arrays or lists

```
>>> x = np.arange(8, 0, -1)
>>> X
array([8, 7, 6, 5, 4, 3, 2, 1])
>>> x[np.array([3, 3, 1, 6])]
array([5, 5, 7, 2])
>>> x[[3, 3, -1, 6]]
array([5, 5, 1, 2])
>>> x[np.array([[1,1],[2,3]])]
array([[7, 7],
       [6, 5]]
```

```
\Rightarrow y = np.arange(35).reshape(5,7)
>>> y[np.array([0,2,4]),np.array([0,1,2])]
array([ 0, 15, 30])
>>> y[np.array([0,2,4]), 1]
array([ 1, 15, 29])
>>> y[np.array([0,2,4])]
array([[ 0, 1, 2, 3, 4, 5, 6],
       [14, 15, 16, 17, 18, 19, 20],
       [28, 29, 30, 31, 32, 33, 34]])
>>> y[:, np.array([0, 2])] # ???
```

## Boolean Index Arrays

Only choose the elements that satisfy the Boolean expression

```
\Rightarrow a = np.arange(1,7)
>>> a
array([1, 2, 3, 4, 5, 6])
>>> b = [True, True, False, False,
True, False]
>>> a[b]
array([1, 2, 5])
>>> c = [1, 1, 0, 0, 1, 0]
>>> a[c]
array([2, 2, 1, 1, 2, 1])
```

```
>>> x = np.arange(9).reshape(3,3)
>>> y = (x \% 2 == 0)
>>> y
array([[ True, False, True],
       [False, True, False],
       [ True, False, True]])
>>> x[v]
array([0, 2, 4, 6, 8])
>>> x[x % 2 == 0]
array([0, 2, 4, 6, 8])
```

## Arithmetic Operations

- Shape of both operands must be same!
- One operand can be a constant

```
>>> a = np.array([1, 2, 3], float)
>>> b = np.array([4, 5, 6], float)
\Rightarrow \Rightarrow a + b
array([5., 7., 9.])
>>> a - b
array([-3., -3., -3.])
>>> a * b
array([ 4., 10., 18.])
>>> b / a
array([4., 2.5, 2.])
```

```
>>> b % a
array([0., 1., 0.])
>>> b**a
array([ 4., 25., 216.])
\Rightarrow \Rightarrow a * 0.5
array([0.5, 1., 1.5])
\Rightarrow \Rightarrow h \Rightarrow 5
array([False, False, True])
>>> a + b == 5
array([ True, False, False])
```

## Operations: Python List vs. NumPy Array

#### Operator \*

- List \* n: repetition of the whole list
- Array \* n: multiply n to every element in the array

```
>>> L = [1, 2, 3]
>>> A = np.array([1, 2, 3])
>>> L * 2
[1, 2, 3, 1, 2, 3]
>>> A * 2
array([2, 4, 6])
```

#### Operator +

- List I + List 2: concatenation of two lists
- Array I + Array 2: Element-wise addition

```
>>> L + L
[1, 2, 3, 1, 2, 3]
>>> A + A
array([2, 4, 6])
```

### Iteration

Use the for loop

```
>>> a = np.arange(5)
>>> a
array([0, 1, 2, 3, 4])
>>> for i in a:
    print(i)
0
```

```
>>> b = np.arange(6).reshape(2,3)
>>> b
array([[0, 1, 2],
       [3, 4, 5]])
>>> for x in b:
       print(x)
[0 1 2]
[3 4 5]
```

## Iteration (cont'd)

One "for" loop for each dimension

```
>>> a =
np.arange(18).reshape(3,2,-1)
>>> a
array([[[ 0, 1, 2],
        [3, 4, 5]],
       [[ 6, 7, 8],
        [ 9, 10, 11]],
       [[12, 13, 14],
        [15, 16, 17]]])
```

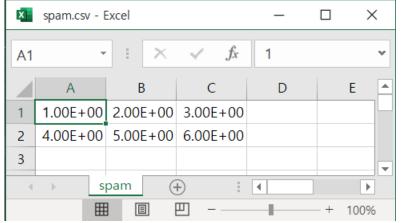
```
>>> for x in a:
   print(x)
   print('-'*10)
[[0 1 2]
 [3 4 5]]
 [ 9 10 11]]
[[12 13 14]
 [15 16 17]]
```

```
>>> for x in a:
\dots for y in x:
        print(y)
        print('-'*10)
[0 1 2]
[3 4 5]
[6 7 8]
[ 9 10 11]
[12 13 14]
[15 16 17]
```

### File I/O

- np.savetxt(fname, A[, delimiter], ...)
  - Save an array to a text file named *fname*

```
a = np.array([[1, 2, 3], [4, 5, 6]])
np.savetxt(r'C:\Users\jinsoo\Desktop\spam.csv', a, delimiter=',')
np.savetxt(r'C:\Users\jinsoo\Desktop\spam.txt', a, delimiter=' ')
```



## File I/O (cont'd)

- np.loadtxt(fname[, dtype][, delimiter], ...)
  - Load data from a text file named fname

```
b = np.loadtxt(r'C:\Users\jinsoo\Desktop\spam.csv', delimiter=',')
print(b)
c = np.loadtxt(r'C:\Users\jinsoo\Desktop\spam.txt', dtype=int,
delimiter=' ')
print(c)
[[1., 2., 3.]
[4., 5., 6.]]
```