

# Prob & Stats

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## 1 Introduction

Prob & Stats is Not New.

The concept of chance of uncertainty.

## 2 Sets and Elements

A “**set**” is clearly defined collection of “**elements**”.

Sets are clearly defined, but not necessarily finite.

### 2.1 Symbols

When element “ $a$ ” belongs to set “ $A$ ”, we write

$$a \in A$$

That means “ $a$  is an element of  $A$ ”.

If element “ $b$ ” is outside set “ $A$ ”, we write

$$b \notin A$$

If the elements of set  $B$  are contained within set  $A$

$$B \subset A$$

That means “ $B$  is subset of  $A$ ”.

A set containing no elements is called “**null set**” and written as “ $\emptyset$ ”.

Let's consider 2 sets  $A$  and  $B$

The set created by the elements belonging to both  $A$  &  $B$  is called the “**intersection**”.

$$A \cap B$$

The set created by all the element of  $A$  &  $B$  is called the “**union**”

$$A \cup B$$

All elements outside both  $A$  &  $B$  from the “complementary” set.

$$\overline{A \cup B} = U - (A \cup B)$$

Note

In some textbook, this symbol, “ $U$ ” means “**Everything**”.

#### Practice Exercise

$$U = \{1, 2, 4, 8, 10\}, A = \{4, 8\}$$

Note : “ $U$ ” is the “entire universe”, and  $A$  is a subset of  $U$ .

1.  $A \cap U = \{4, 8\}$
2.  $A \cup U = \{1, 2, 4, 8, 10\}$
3.  $B = \overline{A} = \{1, 2, 10\}$
4.  $A \cap B = \emptyset$
5.  $A \cup B = \{1, 2, 4, 8, 10\}$

## 2.2 Rules

For calculations with sets, the following equations “**rules**” are useful.

- Commutative Rule :  $A \cup B = B \cup A$  ,  $A \cap B = B \cap A$
- Associative Rule :  $A \cup (B \cup C) = (A \cup B) \cup C$  ,  $A \cap (B \cap C) = (A \cap B) \cap C$
- Distributive Rule :  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$  ,  $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
- De Morgan’s Rule :  $\overline{A \cap B} = \overline{A} \cup \overline{B}$  ,  $\overline{A \cup B} = \overline{A} \cap \overline{B}$

#### Practice Exercise

- Use Venn’s Diagram to show De Morgan’s Rule 1.
- Use Venn’s Diagram to show De Morgan’s Rule 2.

#### **Two Basic Rules**

$$\overline{(\overline{A})} = A, A \cap \overline{A} = \emptyset$$

## 2.3 How to count the number of elements

$n(A)$ : number of elements in finite set  $A$

$n(B)$ :number of elements in finite set B

$n(A \cup B)$ :number of elements in sets A and B

**The way to count the number of elements.**

If there is no overlap.

$$n(A \cup B) = n(A) + n(B)$$

but, in case of some counted twice,

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$A \times B$ :**“direct product”** or **“cartesian product”** means set of all possible ordered pairs.

$$A \times B = \{(a, b) | a \in A, b \in B\}$$

$$n(A \times B) = n(A).n(B)$$