

$$(A \uparrow A) \uparrow ((A \uparrow B) \uparrow (A \uparrow B)) \uparrow ((A \uparrow B) \uparrow (A \uparrow B)) = A$$

$$\begin{array}{c} \downarrow \\ \bar{A} \end{array} \uparrow \begin{array}{c} * \\ (\bar{A}B \uparrow \bar{A}B) \end{array} \uparrow (\bar{A}B \uparrow \bar{A}B)$$

$$\bar{A} \uparrow (\bar{A}B \uparrow \bar{A}B)$$

$$\bar{A} \uparrow \bar{A}B$$

$$\underline{A + \bar{A}B = A}$$

$$\overline{(A \uparrow A) \downarrow (B \uparrow B)} \equiv \underbrace{(\bar{A} \downarrow \bar{A}) \uparrow (\bar{B} \downarrow \bar{B})}$$

$$\overline{\bar{A} \downarrow \bar{B}}$$

$$\bar{A} \bar{B}$$

$$\overline{AB}$$

$$\equiv$$

$$\bar{A} \bar{A} \uparrow \bar{B} \bar{B}$$

$$\bar{A} \uparrow \bar{B}$$

$$\overline{AB}$$

10)

A, B	TT	TF	FT	FF
$F_1(A, B)$	T	F	F	F
$F_2(A, B)$	F	T	F	F
$F_3(A, B)$	F	F	T	F
$F_4(A, B)$	F	F	F	T

$$F_1(A, B) + F_2(A, B) + F_3(A, B) + F_4(A, B) \equiv A \Rightarrow B$$

$$F_1(T, T) + F_2(T, T) + F_3(T, T) + F_4(T, T) = T$$

$$F_1(T, F) + F_2(T, F) + F_3(T, F) + F_4(T, F) = F$$

$$F_1(F, T) + F_2(F, T) + F_3(F, T) + F_4(F, T) = T$$

$$F_1(F, F) + F_2(F, F) + F_3(F, F) + F_4(F, F) = T$$

$$A \Rightarrow B$$

$$(T, T) \quad T$$

$$(T, F) \quad F$$

$$(F, T) \quad T$$

$$(F, F) \quad T$$

$$F_1(A, B) + F_2(A, B) + F_3(A, B) + F_4(A, B) \equiv A \Rightarrow B$$

11) $(A \Rightarrow B)$

$$(T, T) \quad T$$

$$(T, F) \quad F$$

$$(F, T) \quad T$$

$$(F, F) \quad T$$

$$\bar{B} \Rightarrow \bar{A}$$

$$(T, T) \quad T$$

$$(T, F) \quad F$$

$$(F, T) \quad T$$

$$(F, F) \quad T$$

$$A \Rightarrow B \equiv \bar{B} \Rightarrow \bar{A}$$