## Naire Bayes

y variable is usually our target, or outcome. x variable is what we observe (our dota).

$$p(y|x) = \frac{p(x|y) p(y)}{p(x)}$$

have in an event occur ing before observing any data (x).

p(x) is our <u>evidence</u>. In NLP, our endance is a value representing the probability of seing a particular combination of words together (for example, p(x,-free|x|=money) should inturtively be higher than p(x0 = tensorflow, x1 = ballad) because free and 'money' both tend to occur more frequently in the English long rage,

and tend to occur more frequently together (co-occurence). p(xly) is our likelihood. It represents the likelihood of observation the data (comments, words, documents, etc.) given we know y. In Walke Bayes, vre assure conditional independence. This means we can new the P(xly) as TIP(x;ly) when Nu the length of your observed donta. Note: we cannot make the some assumption of independence about the evidence f(x).

Likelihoods: p(x|y=ham) = p(x=free|y=ham)x p(x=morey|y=ham)p(x|y=spam)= p(x=free|y=spam)x p(x=money y=gran) =+x+=1 Note, if we only case about classifying spam/ham and not the poster is prohability, we do not need to actually cakulate p(x), our endance:

p(ylu) 
$$\propto p(x|y) p(y)$$
  
Then we simply need to  
determine if  $p(y=ham|x) > p(y=spam|x)$ .  
Evidence:  
 $p(x) = \prod_{i=1}^{n} p(x_i) = p(x=free)x$   
 $p(x) = \sum_{i=1}^{n} p(x_i) = p(x=free)x$ 

$$p(x) = \sum_{i}^{C} P(x|y_i) p(y_i) = p(x|y=ham)p(y=ham) + p(x|y=spam) p(y=spam)$$

C is the set of distinct classes (in our case, spain or ham).

$$= \frac{1}{4} \left( \frac{3}{4} \right) + \left( \frac{1}{4} \right) \left( \frac{4}{4} \right)$$

$$= \frac{1}{3} = 0.33$$

$$= .25$$

$$p(y=spam|x) = \frac{1}{1}(\frac{1}{4})$$

$$= .75$$
Notice the update from our postors:
$$p(y=ham) = \frac{3}{4} - 3$$

$$p(y=ham|x) = \frac{1}{4}$$

$$p(y=spam|x) = \frac{1}{4}$$

$$p(y=spam|x) = \frac{1}{4}$$

$$p(y=spam|x) = \frac{3}{4}$$

In this case, the posteriors should sum to 1, since the outcomes spam or hom are mutually exclusive and conditionally exclusive and conditionally exhaustive. If you had made the incorrect assumption of inspendence for the evidence, your

proterior rould be:
p(y=hamlx)= (4) (74)  $(\%4)\times(\%4)$ = 0.33 free appears twice in 4 documents p(y=span|x)=(1/)(4/4)(2/4) x(2/4) appears time in Notice these sum to >1, which is not logical.