Compiler

x86-64 Assembly

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Credits

A large part of this course is based on the Compilation Course of J.-C. Filliâtre at ENS Ulm.

Overview of the course

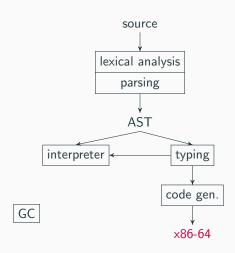


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A little bit of computer arithmetic

Reminder of computer arithmetic

An integer is represented using *n* bits, written from right (least significant) to left (most significant)

The bits b_{n-1} , b_{n-2} , etc. are said to heavy weight and the bits b_0 , b_1 , etc. are said to low weight

The number n of bits is typically equal to 8, 16, 32 or 64 When n=8 we are talking about a byte

unsigned integer

bits
$$= b_{n-1}b_{n-2}\dots b_1b_0$$

value $= \sum_{i=0}^{n-1}b_i2^i$

bits	value	
000000	0	
000001	1	
000010	2	
:	:	
111110	$2^{n}-2$	
111111	$2^{n}-1$	

Example

$$00101010_2 = 42$$

Signed integer: two's complement

the most significant bit b_{n-1} is the sign bit

bits =
$$b_{n-1}b_{n-2}...b_1b_0$$

value = $-b_{n-1}2^{n-1} + \sum_{i=0}^{n-2} b_i 2^i$

Example

$$11010110_2 = -128 + 86$$
$$= -42$$

bits	value
100000	-2^{n-1}
1 00001	$-2^{n-1}+1$
:	:
1 11110	-2
1 11 111	-1
000000	0
000001	1
000010	1
:	:
0 11 110	$2^{n-1}-2$
011111	$2^{n-1}-1$

Beware!

According to the context, the same bits are interpreted either as a signed or unsigned integer

Example

- $11010110_2 = -42$ (signed 8-bit integer)
- $11010110_2 = 214$ (unsigned 8-bit integer)

Operations

the machine provide operations such as

- logical (aka bitwise) operations: and, or, xor, not
- shift operations
- arithmetic operations: addition, subtraction, multiplication, etc.

Logical operations

operation		example
negation	х	00101001
	not x	11010110
and	x	00101001
	у	01101100
	x and y	00101000
or	X	00101001
	у	01101100
	x or y	01101101
xor	X	00101001
	у	01101100
	x xor y	01000101

Shift operation

• logical shift left (inserts least significant zeros)

(<< in Java, 1s1 in Ocaml)

logical shift right (inserts most significant zeros)

$$\rightarrow \boxed{0 \hspace{0.1cm} 0 \hspace{0.1cm} b_{n-1} \hspace{0.1cm} \cdots \hspace{0.1cm} b_3 \hspace{0.1cm} b_2} \hspace{0.1cm} -$$

(>>> in Java, 1sr in Ocaml)

arithmetic shift right (duplicates the sign bit)

$$\rightarrow \boxed{b_{n-1} \mid b_{n-1} \mid b_{n-1} \mid \cdots \mid b_3 \mid b_2} -$$

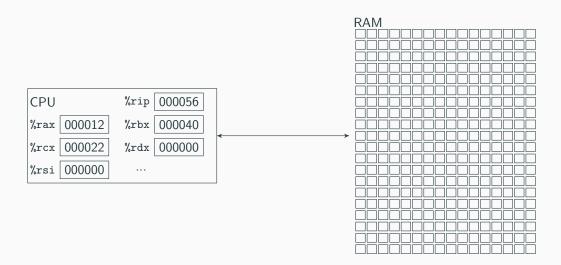
(>> in Java, asr in Ocaml)

A little bit of architecture

roughly speaking, a computer is composed

- of a CPU, containing
 - few integer and floating-point registers
 - some computation power
- memory (RAM)
 - composed of a large number of bytes (8 bits) for instance, 1 GiB = 2^{30} bytes = 2^{33} bits, that is $2^{2^{33}}$ possible states
 - · contains data and instructions

A little bit of architecture



accessing memory is costly (at one billion instructions per second, light only traverses 30 centimeters!)

A little bit of architecture

reality is more complex:

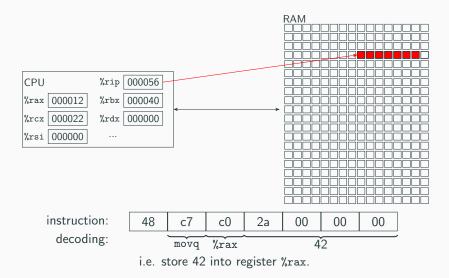
- several (co)processors, some dedicated to floating-point
- one or several memory caches
- virtual memory (MMU)
- etc.

Execution principle

execution proceeds according to the following:

- a register (%rip) contains the address of the next instruction to execute
- we read one or several bytes at this address (fetch)
- we interpret these bytes as an instruction (decode)
- we execute the instruction (execute)
- we modify the register %rip to move to the next instruction (typically the one immediately after, unless we jump)

Execution principle



Principle

again, reality is more complex:

- pipelines
 - several instructions are executed in parallel
- branch prediction
 - to optimize the pipeline, we attempt at predicting conditional branches

Which architecture for this course?

Two main families of microprocessors

- CISC (Complex Instruction Set)
 - · many instructions
 - many addressing modes
 - many instructions read / write memory
 - few registers
 - examples: VAX, PDP-11, Motorola 68xxx, AMD/Intel x86
- RISC (Reduced Instruction Set)
 - few instructions
 - few instructions read / write memory
 - many registers
 - examples: Alpha, Sparc, MIPS, ARM

we choose x86-64 for this course (and the project)

x86-64 architecture

History sketch

x86 a family of compatible architectures

1974 Intel 8080 (8 bits)

1978 Intel 8086 (16 bits)

1985 Intel 80386 (32 bits)

x86-64 a 64-bit extension

2000 introduced by AMD

2004 adopted by Intel

x86-64 architecture

- 64 bits
 - arithmetic, logical, and transfer operations over 64 bits
- 16 registers
 - %rax, %rbx, %rcx, %rdx, %rbp, %rsp, %rsi, %rdi, %r8, %r9, %r10, %r11, %r12, %r13, %r14, %r15
- addresses memory over at least 48 bits (≥ 256 TB)
- many addressing modes

x86-64 assembly

we do not code in machine language, but using the assembly language

the assembly language provides several facilities:

- symbolic names
- allocation of global data

assembly language is turned into machine code by a program called an assembler (a compiler)

Environment

in this lecture, I'm using Linux and GNU tools in particular, I'm using GNU assembly, with AT&T syntax

in other environments, the tools may differ

in particular, the assembly language may use Intel syntax, which is different

hello world

```
# instructions follow
        .text
        .globl main
                               # make main visible for ld
main:
               %rbp
       pushq
               %rsp, %rbp
       movq
               $message, %rdi # argument of puts
       movq
       call
               puts
               $0, %rax
                              # return code 0
       movq
               %rbp
       popq
       ret
                               # data follow
        .data
message:
        .string "hello, world" # 0-terminated string
```

Execution

```
assembling
```

```
> as hello.s -o hello.o
```

linking (gcc calls 1d)

```
> gcc -no-pie hello.o -o hello
```

(note: no need for -no-pie if you use older version of gcc)

execution

```
> ./hello
Hello, world!
```

disassembling

we can disassemble using objdump

```
> objdump -d hello.o
00000000000000000 <main>:
  0: 55
                                   %rbp
                            push
  1: 48 89 e5
                            mov
                                   %rsp, %rbp
  4: 48 c7 c7 00 00 00 00
                                   $0x0, %rdi
                            mov
  b: e8 00 00 00 00
                                   10 <main+0x10>
                            call
 10: 48 c7 c0 00 00 00 00
                            mov
                                   $0x0, %rax
 17: 5d
                                   %rbp
                            pop
 18: c3
                            ret
```

we note that

- addresses for the string and puts are not yet known
- the code is located at address 0

disassembling

we can also disassemble the executable

```
> objdump -d hello
00000000000401126 <main>:
  401126: 55
                                 push
                                        %rbp
  401127: 48 89 e5
                                        %rsp, %rbp
                                 mov
  40112a: 48 c7 c7 30 40 40 00
                                        $0x404030, %rdi
                                 mov
  401131: e8 fa fe ff ff
                                 call
                                        401030 <puts@plt>
  401136: 48 c7 c0 00 00 00 00
                                        $0x0, %rax
                                 mov
  40113d: 5d
                                        %rbp
                                 pop
  40113e: c3
                                 ret
```

we now see

- an effective address for the string (\$0x404030)
- an effective address for function puts (\$0x401030)
- a program location at \$0x401126

endianness

Note that the bytes of 0x00404030 are stored in memory in the order 30, 40, 40, 00

We say that the machine is little-endian

Other architectures are big-endian or bi-endian

(reference: Jonathan Swift's Gulliver's Travels)

a step-by-step execution is possible using gdb (the GNU debugger)

```
> gcc -g -no-pie hello.s -o hello
> gdb hello
GNU gdb (GDB) 7.1-ubuntu
(gdb) break main
Breakpoint 1 at 0x401126: file hello.s, line 4.
(gdb) run
Starting program: .../hello
Breakpoint 1, main () at hello.s:4
4 movq $message, %rdi
(gdb) step
5 call puts
(gdb) info registers
```

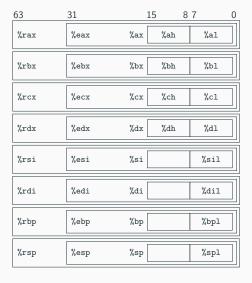
Nemiver

We can also use Nemiver (if you've installed it)

> nemiver hello

Instruction set

Registers



63	31	15	8 7	0
%r8	%r8d	%r8w	%r8b	
%r9	%r9d	%r9w	%r9b	
%r10	%r10d	%r10w	%r10b	
%r11	%r11d	%r11w	%r11b	
%r12	%r12d	%r12w	%r12b	
%r13	%r13d	%r13w	%r13b	
%r14	%r14d	%r14w	%r14b	
%r15	%r15d	%r15w	%r15b	

constants, addresses, copies

• loading a constant into a register

```
movq $0x2a, %rax # rax <- 42
movq $-12, %rdi
```

• loading the address of a label into a register

```
movq $label, %rdi
```

• copying a register into another register

```
movq %rax, %rbx # rbx <- rax
```

arithmetic

addition of two registers

```
addq %rax, %rbx # rbx <- rbx + rax
(similarly, subq, imulq)</pre>
```

addition of a register and a constant

```
addq $2, %rcx # rcx <- rcx + 2
```

particular case

```
incq %rbx # rbx <- rbx+1
(similarly, decq)</pre>
```

negation

```
negq %rbx # rbx <- -rbx
```

logical operations

logical not

```
notq %rax # rax <- not(rax)</pre>
```

• and, or, exclusive or

```
orq %rbx, %rcx # rcx <- or(rcx, rbx)
andq $0xff, %rcx # erases bits >= 8
xorq %rax, %rax # zeroes %rax
```

shift

• shift left (inserting zeros)

```
salq $3, %rax # 3 times
salq %cl, %rbx # cl times
```

arithmetic shift right (duplicating the sign bit)

```
sarq $2, %rcx
```

• logical shift right (inserting zeros)

```
shrq $4, %rdx
```

rotation

operand size

the suffix q means a 64-bit operand (quad words)

other suffixes are allowed

suffix	#bytes	
Ъ	1	byte
W	2	word
1	4	long
q	8	quad

movb \$42, %ah

when operand sizes differ, one must indicate the extension mode

```
movzbq %al, %rdi  # with zeros extension
movswl %ax, %edi  # with sign extension
```

memory access

an operand between parentheses means an indirect addressing i.e. the data in memory at this address

```
movq $42, (%rax) # mem[rax] <- 42
incq (%rbx) # mem[rbx] <- mem[rbx] + 1
```

note: the address may be a label

```
movq %rbx, (x)
```

limitation

operations do not allow several memory accesses

```
addq (%rax), (%rbx)

Error: too many memory references for `add'
```

one has to use a temporary register

```
movq (%rax), %rcx addq %rcx, (%rbx)
```

indirect addressing

the general form of the operand is

and it stands for address $A + B + I \times S$ where

- A is a 32-bit signed constant
- I is 0 when omitted
- $S \in \{1, 2, 4, 8\}$ (is 1 when omitted)

effective address

operation lea computes the effective address of the operand

note: we can make use of it to perform arithmetic

flags

most operations set the processor flags, according to their outcome

flag	meaning
ZF	the result is 0
CF	a carry was propagated beyond the most significant bit
SF	the result is negative
OF	arithmetic overflow (signed arith.)
etc	

(notable exception: lea)

using the flags

three instructions can test the flags

• conditional jump (jcc)

• computes 1 (true) or 0 (false) (setcc)

conditional mov (cmovcc)

suffix		meaning	
е	z	= 0	
ne	nz	$\neq 0$	
s		< 0	
ns		≥ 0	
g		signed >	
ge		$signed \geq$	
1		signed <	
nl		signed ≤	
a		unsigned >	
ae		unsigned ≥	
b		unsigned <	
be		unsigned ≤	

comparisons

one can set the flags without storing the result anywhere, as if doing a subtraction or a logical and

```
cmpq %rbx, %rax # flags of rax - rbx
```

(beware of the direction!)

```
testq %rbx, %rax # flags of rax & rbx
```

unconditional jump

• to a label

jmp label

• to a computed address

jmp *%rax

but also

many, many other instructions
[Enumerating x86-64 - It's Not as Easy as Counting]

including SSE instructions operating on large registers containing several integers or floating-point numbers

The challenge of compilation

the challenge of compilation

The challenge of compilation is to translate a high-level program into this instruction set

in particular, we have to

- translate control structures (tests, loops, exceptions, etc.)
- translate function calls
- translate complex data structures (arrays, structures, objects, closures, etc.)
- allocate dynamic memory

Function calls

observation: function calls can be arbitrarily nested

- ⇒ registers cannot hold all the local variables
- ⇒ we need to allocate memory

yet function calls obey a last-in first-out mode, so we can use a stack

The stack

stack	
\	
l	
dynamic	
data	
(heap)	
static	
data	
code	

the stack is allocated at the top of the memory, and increases downwards; %rsp points to the top of the stack

dynamic data (which needs to survive function calls) is allocated on the heap (possibly by a GC), above static data, and increases upwards

this way, no collision between the stack and the heap (unless we run out of memory)

note: each program has the illusion of using the whole memory; the OS creates this illusion, using the MMU

stack handling

pushing

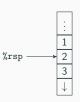
```
pushq $42
pushq %rax
```

popping

```
popq %rdi
popq (%rbx)
```

Example





function call

when a function f (the caller) needs to call a function g (the callee), it cannot simply do

jmp g

since we need to come back to the code of f when g terminates

the solution is to make use of the stack

function call

two instructions for this purpose

instruction

call g

- 1. pushes the address of the next instruction on the stack
- 2. transfers control to address g

and instruction

ret

- 1. pops an address from the stack
- 2. transfers control to that address

function call

problem: any register used by g is lost for f

there are many solutions, but we typically resort to calling conventions

calling conventions

- up to six arguments are passed via registers %rdi, %rsi, %rdx, %rcx, %r8, %r9
- other arguments are passed on the stack, if any
- the returned value is put in %rax

- registers %rbx, %rbp, %r12, %r13, %r14 and %r15 are callee-saved, i.e. the callee must save them if needed; typically used for long-term data, which must survive function calls
- the other registers are caller-saved i.e. the caller must save them if needed; typically used for short-term data, with no need to survive calls

• %rsp is the stack pointer, %rbp the frame pointer

alignment

on function entry, %rsp + 8 must be a multiple of 16

library functions (such as scanf for instance) may fail if this is not ensured

alignment

stack alignment may be performed explicitly

```
f: subq $8, %rsp # align the stack
...
... # since we make calls to extern functions
...
addq $8, %rsp
ret
```

or indirectly

```
f: pushq %rbx  # we save %rbx
...
...  # because we use it here
...
popq %rbx  # and we restore it
ret
```

calling conventions

calling conventions are nothing more than conventions

in particular, we are free not to use them as long we stay within the perimeter of our own code

when linking to external code (e.g. puts earlier), however, we must obey the calling conventions

function calls, in four steps

there are four steps in a function call

- 1. for the caller, before the call
- 2. for the callee, at the beginning of the call
- 3. for the callee, at the end of the call
- 4. for the caller, after the call

they interact using the top of the stack, called the stack frame and located between %rsp and %rbp

the caller, before the call

- 1. passes arguments in %rdi,...,%r9, and others on the stack, if more than 6
- 2. saves caller-saved registers, in its own stack frame, if they are needed after the call
- 3. executes

call callee

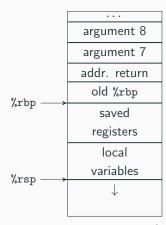
the callee, at the beginning of the call

1. saves %rbp and set it, for instance with

pushq	%rbp	
movq	%rsp,	%rbp

2. allocates its stack frame, for instance with

3. saves callee-saved registers that it intends to use



%rbp eases access to arguments and local variables, with a fixed offset (whatever the top of the stack)

the callee, at the end of the call

- 1. stores the result into %rax
- 2. restores the callee-saved registers, if needed
- 3. destroys its stack frame and restores %rbp with

leave

that is equivalent to

```
movq %rbp, %rsp
```

4. executes

ret

the caller, after the call

- 1. pops arguments 7, 8, ..., if any
- 2. restores the caller-saved registers, if needed

Exercise

Program the following function

and print the value of isqrt(17)

recap

- a machine provides
 - a limited instruction set
 - efficient registers, costly access to the memory
- the memory is split into
 - code / static data / dynamic data (heap) / stack
- function calls make use of
 - a notion of stack frame
 - calling conventions

An example of compilation

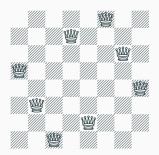
An example of compilation

```
t(a,b,c)\{int d=0,e=a\&^b\&^cc,f=1;if(a)for(f=0;d=(e-=d)\&-e;f+=t(a-d,(b+d)*2,(c+d)/2));return f ;\}main(q)\{scanf("%d",&q);printf("%d\n",t(~(~0<<q),0,0));\}
```

clarification

```
int t(int a, int b, int c) {
 int f=1;
 if (a) {
   int d, e = a & ~b & ~c;
   f = 0;
   while (d = e \& -e) \{
     f += t(a-d, (b+d)*2, (c+d)/2)
        e -= d;
 return f;
int main() {
 int n;
 scanf("%d", &n);
 printf("q(%d) = %d\n", n, t(~(~0<< n), 0, 0));
```

this program computes the number of solutions to the *N*-queens problem

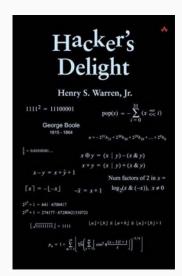


how does it work?

- brute force search (backtracking)
- integers used as sets:

e.g.
$$13 = 0 \cdots 01101_2 = \{0, 2, 3\}$$

integers	sets
0	Ø
a&b	$a \cap b$
	$a\cup b$, when $a\cap b=\emptyset$
a-b	$a \setminus b$, when $b \subseteq a$
~a	a ^c
a&-a	$\{\min(a)\}$, when $a \neq \emptyset$
~(~0< <n)< th=""><th>$\{ min(a) \}$, when $a eq \emptyset$ $\{ 0, 1, \ldots, n-1 \}$ $\{ i+1 \mid i \in a \}$, written $S(a)$</th></n)<>	$\{ min(a) \}$, when $a eq \emptyset$ $\{ 0, 1, \ldots, n-1 \}$ $\{ i+1 \mid i \in a \}$, written $S(a)$
a*2	$\{i+1 \mid i \in a\}$, written $S(a)$
a/2	$\{i-1\mid i\in a\land i\neq 0\}$, written $P(a)$



explaining a&-a

in two's complement: $-a = ^a+1$

$$\begin{array}{rcl} \mathbf{a} & = & b_{n-1}b_{n-2}\dots b_k 10\dots 0 \\ \mathbf{\tilde{a}} & = & \overline{b_{n-1}b_{n-2}}\dots \overline{b_k}01\dots 1 \\ \mathbf{-a} & = & \overline{b_{n-1}b_{n-2}}\dots \overline{b_k}10\dots 0 \\ \mathbf{a\&-a} & = & 0 & 0 \dots & 010\dots 0 \end{array}$$

Example

a = 00001100 = 12
-a = 11110100 =
$$-12 = -128 + 116$$

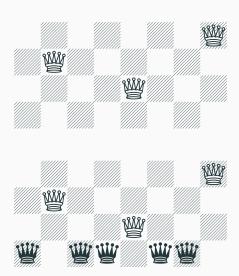
a&-a = 00000100

clarification: code with sets

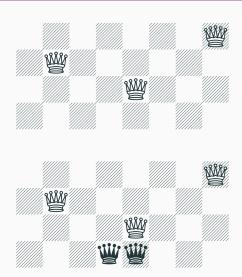
```
\begin{array}{l} \mathbf{int} \ t(a,b,c) = \\ f \leftarrow 1 \\ \mathbf{if} \ a \neq \emptyset \ \mathbf{then} \\ \\ e \leftarrow (a \setminus b) \setminus c \\ f \leftarrow 0 \\ \mathbf{while} \ e \neq \emptyset \ \mathbf{do} \\ \\ d \leftarrow \min(e) \\ f \leftarrow f + t(a \setminus \{d\}, S(b \cup \{d\}), P(c \cup \{d\})) \\ e \leftarrow e \setminus \{d\} \\ \mathbf{return} \ f \end{array}
```

int queens(n) = return $t(\{0,1,\ldots,n-1\},\emptyset,\emptyset)$

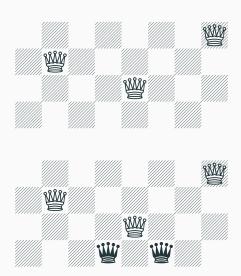




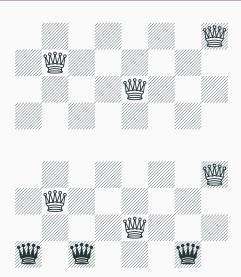
 $a = \text{columns to be filled } = 10110110_2.$



 $b = \text{unavailable columns by the left diagonals } = 00011000_2.$



 $c = \text{unavailable columns by the right diagonals } = 00010100_2.$



a&~b&~c = available positions = 10100010_2 .

why using this program?

```
int t(int a, int b, int c) {
 int f=1;
 if (a) {
   int d, e = a & ~b & ~c;
   f = 0;
   while (d = e \& -e) {
     f += t(a-d, (b+d)*2, (c+d)/2)
        e -= d:
 return f;
int main() {
 int n;
 scanf("%d", &n);
 printf("q(%d) = %d\n", n, t(~(~0<< n), 0, 0));
```

short, yet contains

- a test (if)
- a loop (while)
- a recursive function
- a few computations

and this is an excellent solution to the *N*-queens problem

compilation

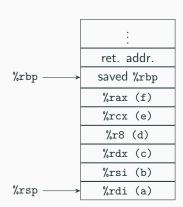
let's start with recursive function t; we need

- to allocate registers
- to compile
 - the test
 - the loop
 - the recursive call
 - the various computations

register allocation

- a, b, and c are passed in %rdi, %rsi, and %rdx
- the result is returned in %rax
- local variables d, e, and f will be in %r8, %rcx, and %rax

when making a recursive call, a, b, c, d, e, and f will have to be saved, for they are all used after the call \Rightarrow saved on the stack



compiling the test

```
int t(int a, int b, int c) {
   int f=1;
   if (a) {
       ...
   }
   return f;
}
```

```
t: movq $1, %rax
    testq %rdi, %rdi
    jz    t_return
    ...
t_return:
    ret
```

allocating/deallocating the stack frame

```
t: ...

pushq %rbp

movq %rsp, %rbp

subq $48, %rsp # allocate 6 words on the stack
...

addq $48, %rsp

popq %rbp

t return:

ret
```

when $a \neq 0$

```
if (a) {
    int d, e=a&~b&~c;
    f = 0;
    while ...
}
```

note the use of a temporary register %r9 (not saved)

```
while (expr) {
   body
}
```

```
...
L1: ...

compute expr into %rcx

...

testq %rcx, %rcx

jz L2

...

body

...

jmp L1
L2: ...
```

there are better options, though

```
while (expr) {
   body
}
```

this way we make a single branching instruction per loop iteration (apart for the very first iteration)

```
jmp loop_test
loop body:
...
loop test:
    movq %rcx, %r8
    movq %rcx, %r9
    negq %r9
    andq %r9, %r8
    jnz loop_body
t return:
...
```

```
loop body:
              %rdi, 0(%rsp)
                              # a
       movq
              %rsi, 8(%rsp)
       movq
              %rdx, 16(%rsp) # c
       movq
              %r8, 24(%rsp) # d
       movq
              %rcx, 32(%rsp) # e
       movq
              %rax, 40(%rsp) # f
       movq
              %r8, %rdi
       subq
       addq
              %r8, %rsi
       salq
              $1, %rsi
       addq
              %r8, %rdx
       shrq
              $1, %rdx
       call
              40(%rsp), %rax #f
       addq
              32(%rsp), %rcx #e
       movq
               24(%rsp), %rcx #-=d
       subq
               16(%rsp), %rdx #c
       movq
                8(%rsp), %rsi #b
       movq
                0(%rsp), %rdi #a
       movq
```

main function

```
int main() {
    int q;
    scanf("%d", &q);
    ...
}
```

```
main:
                %rbp
        pushq
                %rsp, %rbp
        movq
                $input, %rdi
        movq
                $q, %rsi
        movq
                %rax, %rax
        xorq
        call
                scanf
               (q), %rcx
        movq
        . . .
        .data
input:
        .string "%d"
q:
                0
        .quad
```

programme principal

```
main:
               %rdi, %rdi
        xorq
               %rdi
       notq
        salq
               %cl, %rdi
               %rdi
       notq
               %rsi, %rsi
        xorq
               %rdx, %rdx
        xorq
        call
               t
        movq
               $msg, %rdi
               %rax, %rsi
        movq
               %rax, %rax
        xorq
        call
               printf
               %rax, %rax
        xorq
               %rbp
        popq
       ret
```

optimization

this code is not optimal (for instance, we could save only 5 registers)

yet it is more efficient than the output of gcc -02 or clang -02

no reason to show off: we wrote an assembly code specific to this C program, manually, not a compiler!

lesson

• producing efficient assembly code is not easy

 observe the code produced by your compiler using gcc -S -fverbose-asm, or ocamlopt -S, etc.

or even better at https://godbolt.org/

now we have to automate all this

further reading

- [BO16] Computer Systems: A Programmer's Perspective (R. E. Bryant, D. R. O'Hallaron)
- its PDF appendix x86-64 Machine-Level Programming

 Notes on x86-64 programming by Andrew Tolmach and his webpage x86-64 Resources

References i



R.E. Bryant and D.R. O'Hallaron.

Computer Systems: A Programmer's Perspective.

Always Learning. Pearson, 2016.

An example of compilation

Questions?