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CSCI 4140U

CSCI 4140 Assignment One

GENERALIZING THE ALGORITHM

Modify both programs to have a parameter, n, which is the number of qubits. Note, the number of classical bits will also depend on n

```
n = 4
qbit = n
cqbit = n-1
qpen = QuantumCircuit(qbit,cqbit)
for qubit in range(cqbit):
   qpen.h(qubit)
qpen.x(cqbit)
angle = 2*math.pi/3 #alter for exact or approx.
repetitions = 1
for counting_qubit in range(cqbit):
   for i in range(repetitions):
       qpen.cul(angle, counting_qubit, cqbit);
   repetitions *= 2
qft_dagger(qpe3, cqbit)
for n in range(cqbit):
    qpen.measure(n,n)
```

ADDING NOISE

So far we have been dealing with perfect qubits, but this isn't the case in the real world. Existing quantum computers have noise, which impact gates and measurements.

Our first question is how seriously does noise effect our results?

In order to do this we need a noise model, which I provide for you.

This noise model is in the following procedure which is similar to one in the Qiskit textbook, modified for the purposes of our experiment.

This procedure is:

```
In [79]: def get_noise(p_meas,p_gate):
    error_meas = pauli_error([('X',p_meas), ('I', 1 - p_meas)])
    error_gate1 = depolarizing error(p_gate, 1)
    error_gate2 = error_gate1.tensor(error_gate1)
    noise_model = NoiseModel()
    noise_model.add_all_qubit_quantum_error(error_meas, "measure")
    noise_model.add_all_qubit_quantum_error(error_gate1, ["u1", "u2", "u3"])
    noise_model.add_all_qubit_quantum_error(error_gate2, ["cx", "cu1"])
    return_noise_model
```

The first parameter to this procedure is the noise level for measurement. This will be left at 0.01 for our experiments. The second parameter is the gate noise level, which will be varied, but will start at 0.01.

This noise model is used in the following way:

```
noise_model = get_noise(0.01,0.01)
backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
```

For the exact version of the algorithm when using "qft_dagger()"

```
In [85]: # Where n = 6
n = 6
qbit = n
cqbit = n-1
qpen = QuantumCircuit(qbit,cqbit)
                    for qubit in range(cqbit):
                    qpen.h(qubit)
qpen.x(cqbit)
                   angle = math.pi/4
repetitions = 1
for counting_qubit in range(cqbit):
    for i in range(repetitions):
        qpen.cul(angle, counting_qubit, cqbit);
    repetitions == 2
qft_dagger(qpen, cqbit)
for n in range(cqbit):
        qpen.measure(n,n)
In [82]: # Where n = 6, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                   backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[82]:
                                                                                    0.039
                         0.04
                                                                                                 0.034
0.033 0.032 0.033
0.030 0.038 0.038 0.000
                                                                                                                          0.036
                                                                0.039.036
                                        0.03535,034
                                                       0.033
                     Probabilities
0.00
                         0.01
                         0.00
In [83]: # Where n = 6, noise level = 0.05
noise_model = get_noise(0.05,0.05)
                   backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[83]:
                                                                                                   0.039 0.038
                                                     0.038
                         0.04
                                                0 03g3 03d3 3 033 033 033 033 0432
                                                                                                       0.033
                     Probabilities
0.00
                         0.01
                         0.00
```

```
In [87]: # Where n = 8
    n = 8
    qbit = n
    cqbit = n-1
    qpen = QuantumCircuit(qbit,cqbit)
                      for qubit in range(cqbit):
     qpen.h(qubit)
qpen.x(cqbit)
                     angle = math.pi/4
repetitions = 1
for counting_qubit in range(cqbit):
    for i in range(repetitions):
        qpen.cul(angle, counting_qubit, cqbit);
    repetitions *= 2
qft_dagger(qpen, cqbit)
for n in range(cqbit):
    qpen.measure(n,n)
In [88]: # Where n = 8, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                    backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[88]:
                            0.4
                                                     0.348
                            0.3
                       Probabilities
NO
                             0.1
                            0.0
In [89]: # Where n = 8, noise level = 0.05
noise_model = get_noise(0.05,0.05)
                     backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
 Out[89]:
                                                       0.045
                            0.045
                                                       0.0.937
                         Probabilities
                             0.030
                            0.015
                                                                                                       0.014
                            0.000
```

```
In [90]: # Where n = 10
n = 10
qbit = n
cqbit = n-1
qpen = QuantumCircuit(qbit,cqbit)
                      for qubit in range(cqbit):
          qpen.h(qubit)
qpen.x(cqbit)
                     angle = math.pi/4
repetitions = 1
for counting_qubit in range(cqbit):
    for i in range(repetitions):
        qpen.cul(angle, counting_qubit, cqbit);
    repetitions *= 2
qft_dagger(qpen, cqbit)
for n in range(cqbit):
        qpen.measure(n,n)
In [91]: # Where n = 8, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                    backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[91]:
                            0.100
                        Probabilities
0.050
                                                              0.060
                                                              8,639
0.032
                            0.025
                            0.000
In [92]: # Where n = 8, noise level = 0.05 noise_model = get_noise(0.05,0.05)
                     backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
 Out[92]:
                            0.012
                            0.009
                       Probabilities
00000
                            0.003
                            0.000
```

For the approximate version of the algorithm when using "qft_dagger()"

```
In [93]: #Where n = 6
                  n = 6
qbit = n
cqbit = n-1
qpen = QuantumCircuit(qbit,cqbit)
                  for qubit in range(cqbit):
     qpen.h(qubit)
qpen.x(cqbit)
                 angle = 2*math.pi/3
repetitions = 1
for counting_qubit in range(cqbit);
    for i in range(repetitions);
        qpen.cul(angle, counting_qubit, cqbit);
        repetitions == 2
qft_dagger(qpen, cqbit)
for n in range(cqbit);
        qpen.measure(n,n)
In [94]: # Where n = 6, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                 backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[94]:
                         0.45
                        0.30
                                                             0.18
                        0.15
                        In [95]: # Where n = 6, noise level = 0.05
noise_model = get_noise(0.05,0.05)
                 backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[95]:
                        0.20
                        0.15
                                                             0.12
                         0.10
                                                           0.07
                        0.05
                         0.00
```

```
In [96]: #Where n = 8
    n = 8
    qbit = n
    cqbit = n-1
    qpen = QuantumCircuit(qbit,cqbit)
                     angle = 2*math.pi/3
repetitions = 1
for counting_qubit in range(cqbit):
    for i in range(repetitions):
        qpen.cul(angle, counting_qubit, cqbit);
    repetitions == 2
qft_dagger(qpen, cqbit)
for n in range(cqbit):
        qpen.measure(n,n)
In [97]: # Where n = 8, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                    backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[97]:
                                                                        0.244
                           0.24
                      Probabilities
0.12
                           0.06
                                                                      0.046
                          0.00
In [98]: # Where n = 8, noise level = 0.05
noise_model = get_noise(0.05,0.05)
                   backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[98]:
                                                                     0.041
                           0.04
                      Probabilities
0.00
                           0.01
                           0.00
```

```
In [99]: #Where n = 10
                     n = 10
qbit = n
cqbit = n-1
qpen = QuantumCircuit(qbit,cqbit)
                      for qubit in range(cqbit):
     qpen.h(qubit)
qpen.x(cqbit)
                     angle = 2*math.pi/3
repetitions = 1
for counting_qubit in range(cqbit):
    for i in range(repetitions):
        qpen.cul(angle, counting_qubit, cqbit);
    repetitions *= 2
qft_dagger(qpen, cqbit)
for n in range(cqbit):
        qpen.measure(n,n)
In [100]: # Where n = 10, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                     backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[100]:
                            0.100
                                                                            0.093
                             0.075
                             0.050
                             0.025
                            0.000
In [101]: # Where n = 10, noise level = 0.05
noise_model = get_noise(0.05,0.05)
                     backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[101]:
                            0.016
                                                                        0.012
                             0.012
                                                                        COCCETO
                             0.008
                             0.004
                             0.000
```

For the exact version of the algorithm when using "qft_limited()"

```
In [107]: # Where n = 6
    n = 6
    qbit = n
    cqbit = n-1
    qpen = QuantumCircuit(qbit,cqbit)
               for qubit in range(cqbit):
     qpen.h(qubit)
qpen.x(cqbit)
               angle = math.pi/4
repetitions = 1
for counting_qubit in range(cqbit):
    for i in range(repetitions):
        qpen.cul(angle, counting_qubit, cqbit);
    repetitions == 2
qft_limited(qpen, cqbit)
for n in range(cqbit):
    qpen.measure(n,n)
In [108]: # Where n = 6, noise level = 0.01
noise_model = get_noise(0.01,0.01)
               backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_oounts()
plot_histogram(answer)
                     0.6
                     0.4
                           In [110]: # Where n = 8
                 n = 6
qbit = n
                 quit = n
cqbit = n-1
qpen = QuantumCircuit(qbit,cqbit)
                  for qubit in range(cqbit):
                 qpen.h(qubit)
qpen.x(cqbit)
                  angle = math.pi/4
                  repetitions *= 2
qft_limited(qpen, cqbit)
for n in range(cqbit):
                  qpen.measure(n,n)
In [111]: # Where n = 8, noise level = 0.01
noise_model = get_noise(0.01,0.01)
                  backend = Aer.get_backend('qasm_simulator')
                 backend = Aer.get_backend('qasm_simulator')
shots = 2048
results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
answer = results.get_counts()
plot_histogram(answer)
Out[111]:
                      8.0
                                        0.711
                       0.6
                       0.2
```

```
In [113]: # Where n = 10
n = 10
qbit = n = 1
qpen = QuantumCircuit(qbit,cqbit)

for qubit in range(cqbit):
    qpen.h(qubit)
    qpen.h(qubit)

    angle = math.pi/4
    repetitions = 1
    for counting qubit in range(cqbit):
        for i in range(repetitions):
            qpen.cul(angle, counting qubit, cqbit);
        repetitions = 2
    qft_limited(qpen, cqbit)
    for n in range(cqbit):
        qpen.measure(n,n)

In [114]: # Where n = 10, noise level = 0.01
        noise_model = get_noise(0.01,0.01)

        backend = Aer.get_backend('qasm_simulator')
        shots = 2048
        results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
        answer = results.get_counts()
        plot_histogram(answer)

Out[114]:
```

0.03

0.00

For the approximate version of the algorithm when using "qft_limited()*

```
In [116]: # Where n = 6
    n = 6
    qbit = n
    cqbit = n
    qpen. quantumcircuit(qbit,cqbit)

for qubit in range(cqbit):
    qpen.k(qubit)

    qpen.x(cqbit)

    angle = 2 "math.pi/3
    repetitions = 1
    for counting_qubit in range(cqbit):
        for in range(repetitions):
            respen.cult(angle, counting_qubit, cqbit);
        repen.cult(angle, counting_qubit, cqbit);
        repen.cult(angle, counting_qubit, cqbit);
        for in range(cqbit):
        for n in range(cqbit):
            dpen.measure(n,n)

In [117]: # Where n = 6, noise level = 0.01
            noise model = get_noise(0.01,0.01)

            backend = Aer.get_backend('qasm_simulator')
            shots = 2048
            results = execute(qpen, backend=backend, shots=shots, noise_model=noise_model).result()
            answer = results.get_counts()
            plot_histogram(answer)

Out[117]:

Out[117]:

Out[117]:
```

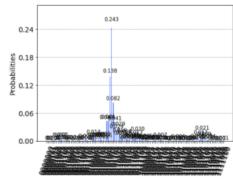
```
In [119]:  # Where n = 8
    n = 8
    qbit = n
    cqbit = n-1
    qpen = QuantumCircuit(qbit,cqbit)

for qubit in range(cqbit):
    qpen.h(qubit)
    qpen.h(qubit)

angle = 2*math.pi/3
    repetitions = 1
    for counting_qubit in range(cqbit):
        for i in range(repetitions):
            qpen.cul(angle, counting_qubit, cqbit);
            repetitions *= 2
    qtt_limited(qpen, cqbit)
    for n in range(cqbit):
            qpen.measure(n,n)
In [120]:  # Where n = 8, noise level = 0.01
            noise_model = get_noise(0.01,0.01)

backend = Aer.get_backend('qasm_simulator')
            shots = 2048
            results = execute(qpen, backend_backend, shots=shots, noise_model=noise_model).result()
            answer = results.get_counts()
            plot_histogram(answer)
```

Out[120]:



In conclusion, when using the approximate version I noticed there seemed to be and extreme outlier and that seem to prevail throughout the experiment.