

# Neutral curve

$$\det A_q = \det A - q^2 (d_{uu}a_{vv} + d_{vv}a_{uu} - a_{vu}d_{uv} - d_{vu}a_{uv}) + q^4 (d_{uu}d_{vv} - d_{vu}d_{vu}),$$

$$\det A_q = a^2 - q^2 D \frac{-a^3 c + a^2 + abc - ac}{ca - a^2 - b} + q^4 D^2 \frac{c}{c - a - \frac{b}{a}}$$

We set to zero and solve for b to get:

$$b = \frac{D^2 c q^4 + D q^2 (a^2 c - a + c) - a^3 + a^2 c}{D c q^2 + a}$$

Denote  $L = D c q^2 + a$

Then

$$b = \frac{\frac{1}{c} L^2 + L \left( -2a \frac{a^3 c + c - a}{c} \right) + a^2 + a^3 c - a^3 - \frac{a^4 c + ac - a^2}{c}}{L}$$

$$\frac{db}{dL} = 0 \iff a^2 c + a^3 c^2 - a^3 c - a^4 c - ac + a^2 = L^2$$