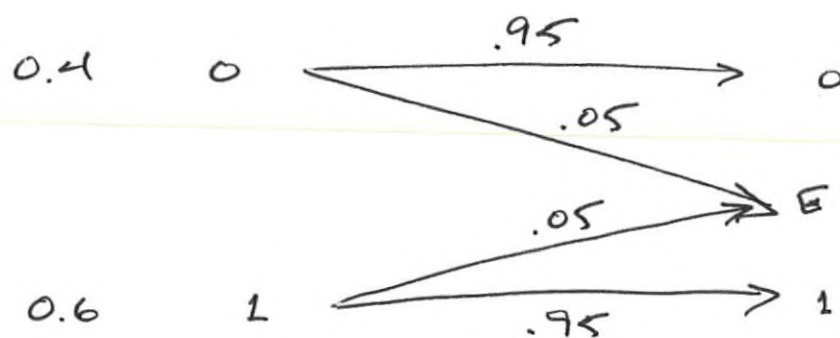


Memory

Erasure Channel

$T_e =$



output

$$P_B(0) = \vec{P}(0|0)P_A(0) = 0.95(0.4) = 0.38$$

$$P_B(E) = \vec{P}(E|0)P_A(0) + \vec{P}(E|1)P_A(1) = 0.05(0.4) + 0.05(0.6)$$

$$P_B(1) = \vec{P}(1|1)P_A(1) = 0.95(0.6) = 0.57$$

backward transition probabilities are:

$$\vec{P}(0|0) = \frac{\vec{P}(0|0)P_A(0)}{P_B(0)} = \frac{(.95)(.4)}{.38} = 1$$

$$\vec{P}(0|E) = \frac{\vec{P}(E|0)P_A(0)}{P_B(E)} = \frac{(.05)(.4)}{.05} = .4$$

$$\vec{P}(1|E) = \frac{\vec{P}(E|1)P_A(1)}{P_B(E)} = \frac{(.05)(.6)}{.05} = .6$$

$$\vec{P}(1|1) = \frac{\vec{P}(1|1)P_A(1)}{P_B(1)} = \frac{(.95)(.6)}{.57} = 1$$

entropy of the source is

i<Äsiöe^.Oc>vv \s '.

$$H(A|B) = -\sum_{i,j} P_{ij}(0) \left\{ \overleftarrow{P}(0|0) \log \overleftarrow{P}(0|0) \right\}$$

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Input Symbols: 0, 1

Input Symbol Probabilities

X_i : $P(X_i)$
0: 0.4
1: 0.6

Output Symbols: 0, E, 1

Conditional Probabilities

X_i : $P(0|X_i)$, $P(E|X_i)$, $P(1|X_i)$
0: 0.95, 0.05, 0
1: 0, 0.05, 0.95

Channel Matrix

| $X_i \backslash Y_j$ | 0 | E | 1 |
|----------------------|--------|--------|--------|
| 0 | 0.9500 | 0.0500 | 0.0000 |
| 1 | 0.0000 | 0.0500 | 0.9500 |

Joint and Marginal Distributions

| $X_i \backslash Y_j$ | 0 | E | 1 | $P(X_i)$ |
|----------------------|--------|--------|--------|----------|
| 0 | 0.3800 | 0.0200 | 0.0000 | 0.4000 |
| 1 | 0.0000 | 0.0300 | 0.5700 | 0.6000 |
| $P(Y_j)$ | 0.3800 | 0.0500 | 0.5700 | 1.0000 |

Backward Channel Matrix

| $Y_j \backslash X_i$ | 0 | 1 |
|----------------------|--------|--------|
| 0 | 1.0000 | 0.0000 |
| E | 0.4000 | 0.6000 |
| 1 | 0.0000 | 1.0000 |

Entropies

$H(X)$: 0.9710 bits/symbol
 $H(Y)$: 1.2088 bits/symbol
 $H(X|Y)$: 0.0485 bits/symbol
 $H(Y|X)$: 0.2864 bits/symbol
 $H(X,Y)$: 1.2573 bits/symbol

Mutual Information

$I(X;Y)$: 0.9224 bits/symbol