$$H(i,j) = max \begin{cases} H(i-1,j-1) + w(a_i,b_j) & \text{Match/Mismatch} \\ H(i-1,j) + w(a_i,-) & \text{Deletion} \\ H(i,j-1) + w(-,b_j) & \text{Insertion} \end{cases}, 1 \le i \le m, 1 \le j \le n$$