



# **Genes vs. Environment: How much do each contribute?**



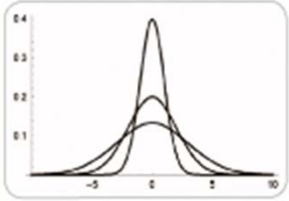


# Today's lecture

## Genes vs. Environment

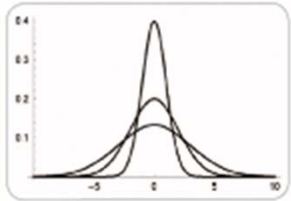


- How do we infer whether each is contributing?
  - Very often both contribute
- **How do we infer their relative contributions?**
  - “Heritability”



# “Mean” and “Variance”

- Most traits are variable
- If trait is continuously variable (ie, measurable using a continuous scale), we can calculate a “mean” and a “variance” (spread)

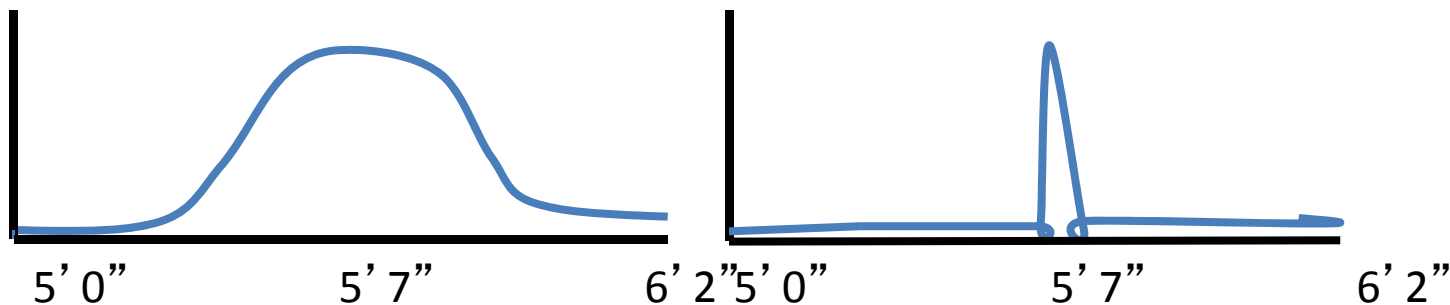


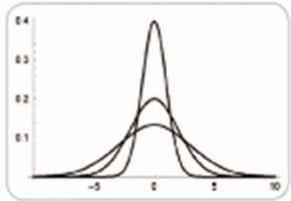
# “Mean” and “Variance”

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Height in 2 classrooms:

- 1) What is the mean?
- 2) Which has more “variance”?





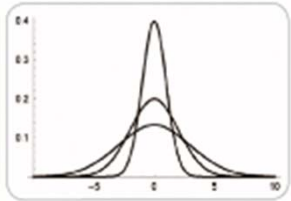
# “Mean” and “Variance”

- Mean = “average”
- Variance = how “spread out” individual measures are from the mean

– Calculated as  $\frac{\sum (X - \mu)^2}{N}$

where  $X$  is an individual measure,  $\mu$  is the mean,  
and  $N$  is the number of measures

If you had 10 individuals all with a height of 69 inches, what is the mean  
and what is the variance?



# Example

- $\frac{\sum(X - \mu)^2}{N} = \text{Variance}$

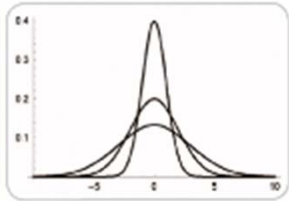
where  $X$  is an individual measure,  $\mu$  is the mean, and  $N$  is the number of measures

1. Heights in inches: 63, 65, 67, 67, 69, 71

2. Heights in inches: 65, 66, 67, 67, 68, 69

Which has greater variance: 1 or 2 or equal?

Try it with and without the math...



## Example: answer

1. Heights in inches: 63, 65, 67, 67, 69, 71

$$\text{Mean} = (63+65+67+67+69+71)/6 = 402/6 = \mathbf{67}$$

$$\text{Variance} = ((63-67)^2 + (65-67)^2 \dots)/6 = \mathbf{6.66} \quad \frac{\sum(X - \mu)^2}{N}$$

2. Heights in inches: 65, 66, 67, 67, 68, 69

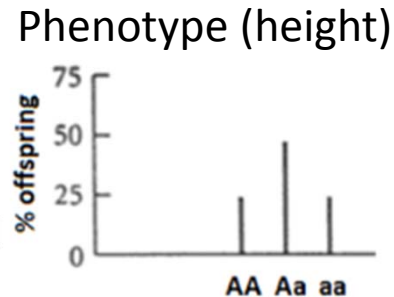
$$\text{Mean} = (65+66+67+67+68+69)/6 = 402/6 = \mathbf{67}$$

$$\text{Variance} = ((65-67)^2 + (66-67)^2 \dots)/6 = \mathbf{1.66}$$

# What causes the variance in traits like height?

- You see the variance in the **phenotype**
- Some of the variance is **genetic**
- Some of the variance is **environmental**

2 alleles at a single gene  
control height, and  
**no** effect of environment

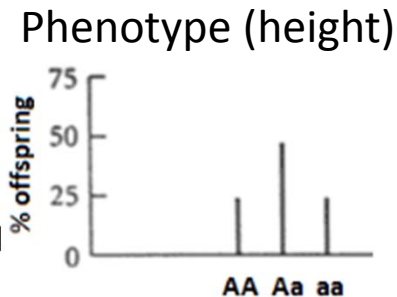




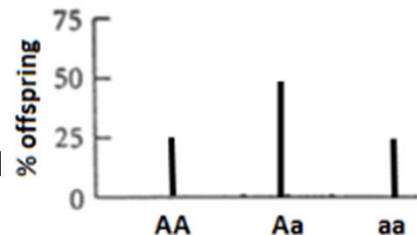
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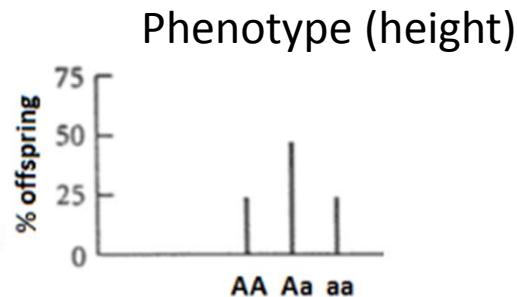


More  
genetic  
variance

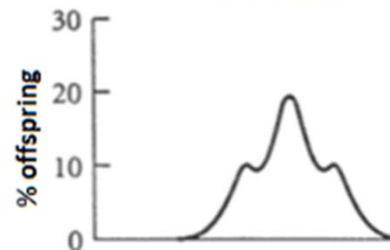
# What causes the variance in traits like height?

- You see the variance in the **phenotype**
- Some of the variance is **genetic**
- Some of the variance is **environmental**

2 alleles at a single gene control height, and **no** effect of environment



2 alleles at a single gene control height, and **some** effect of environment:



Added  
environmental  
variance

# What causes the variance in traits like height?

- You see the variance in the **phenotype**
- Some of the variance is **genetic**
- Some of the variance is **environmental**

Simple formula:  $V_P = V_G + V_E$

$V_P$  = phenotypic variance

$V_G$  = genetic variance

$V_E$  = environmental variance

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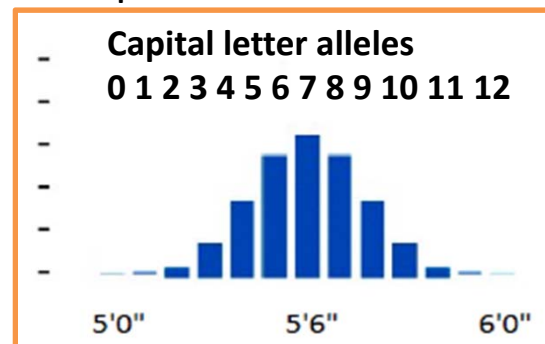
$V_E$  = environmental variance

But how to calculate???

# Genetic variation becomes apparent in F<sub>2</sub> of crosses: 6 genes for “height”

- Start with AA BB CC DD EE FF (6' tall people) having kids with aa bb cc dd ee ff (5' tall people)
- Offspring all heterozygous (5' 6" tall): Aa Bb Cc Dd Ee Ff
- What happens in F<sub>2</sub>?
  - Aa Bb Cc Dd Ee Ff x Aa Bb Cc Dd Ee Ff :
  - If unlinked, MANY possibilities

SLIDE USED EARLIER...



# Genetic variation becomes apparent in F<sub>2</sub> of crosses: 6 genes for “height”

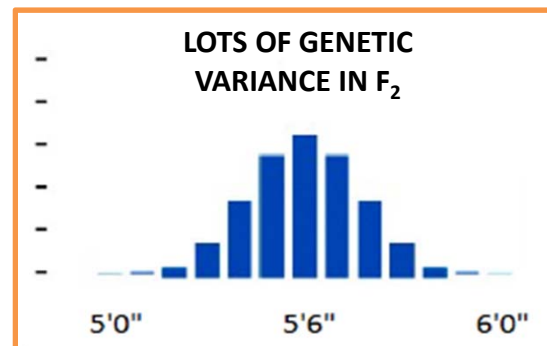
AA BB CC DD EE FF    x    aa bb cc dd ee ff



F<sub>1</sub>:    Aa Bb Cc Dd Ee Ff

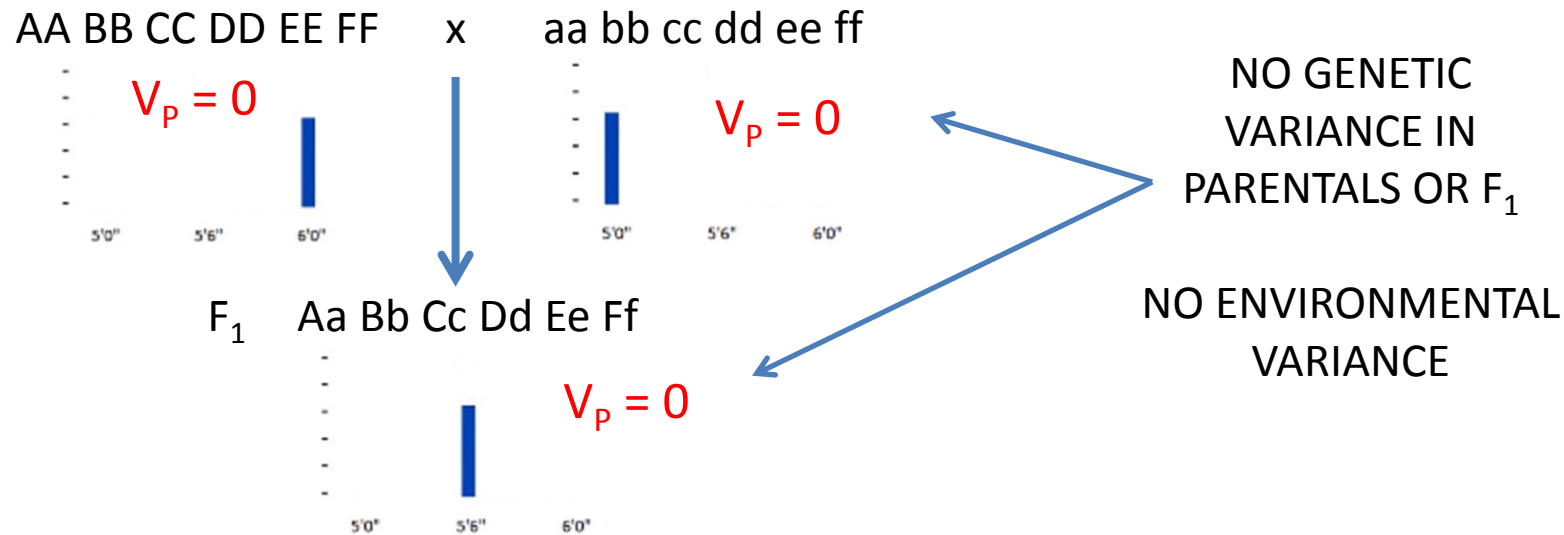
NO GENETIC  
VARIANCE IN  
PARENTALS OR F<sub>1</sub>

F<sub>2</sub>:



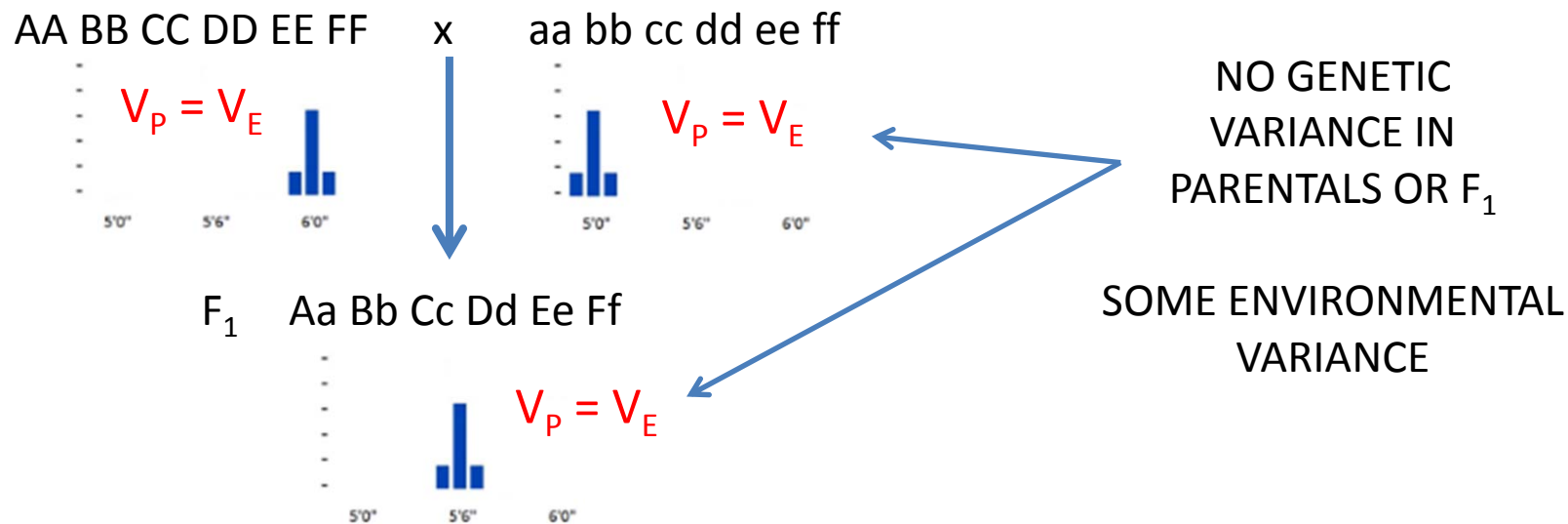
$$V_P = V_G + V_E$$

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$$V_p = V_G + V_E$$

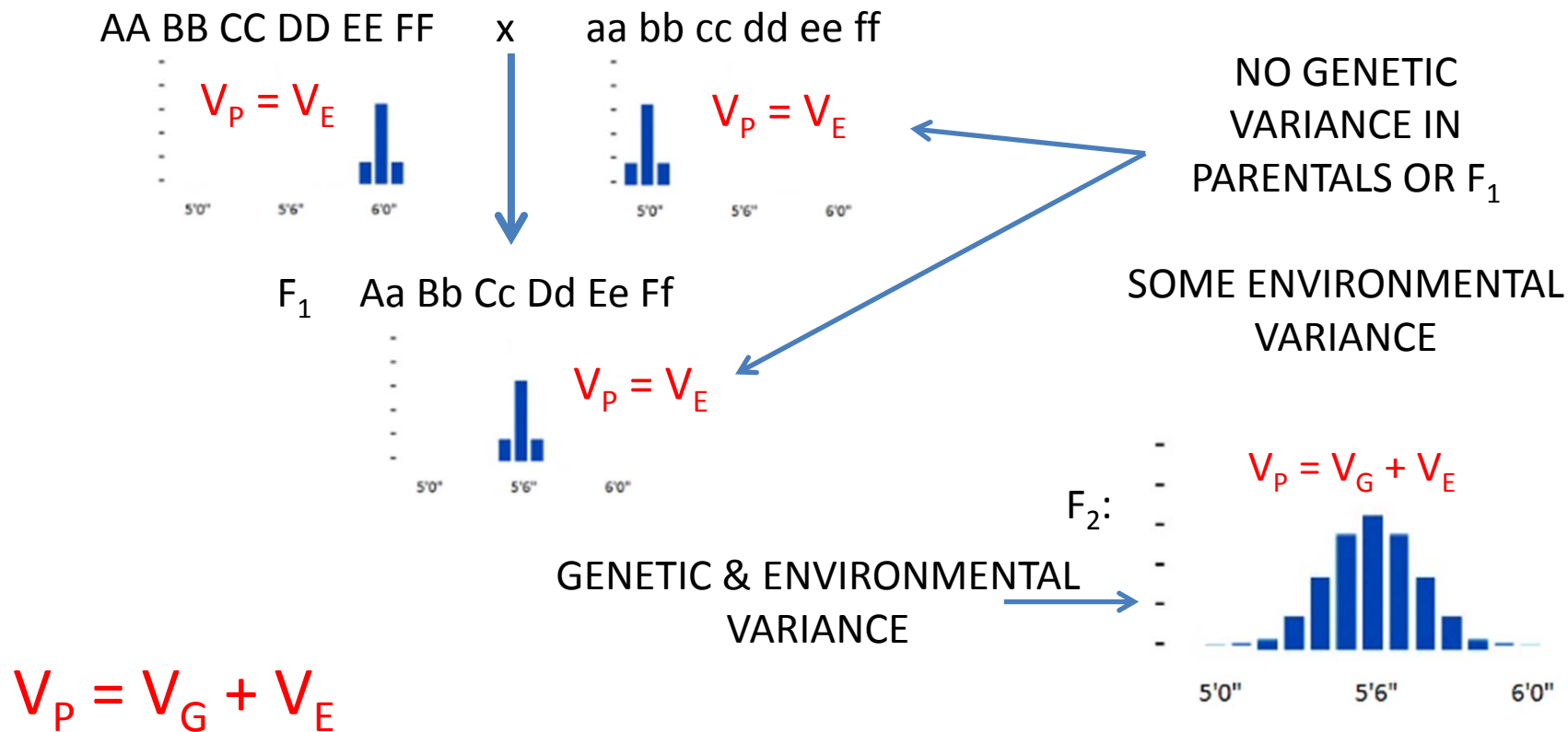
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# Variance components

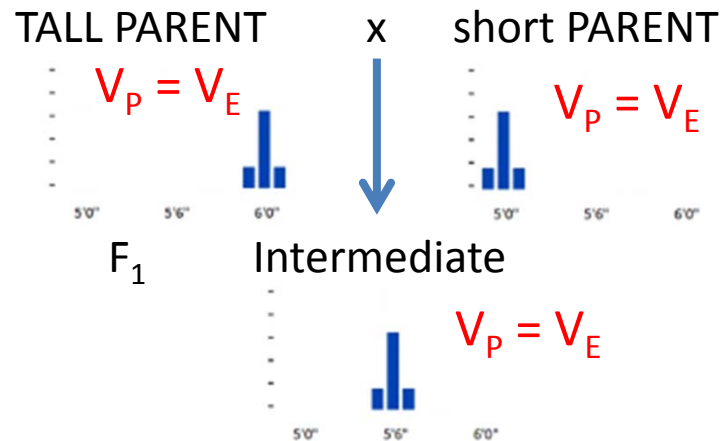
$$V_P = V_G + V_E$$

- We want to know “how much” genetics and environment contribute to phenotypic variance
- Fraction of total phenotypic variance that's genetic is called “Heritability”

$$(V_G/V_P) \text{ or } (V_G/(V_G+V_E))$$

Ranges 0 (no genetic) to 1 (all genetic)

# F<sub>2</sub> example to try



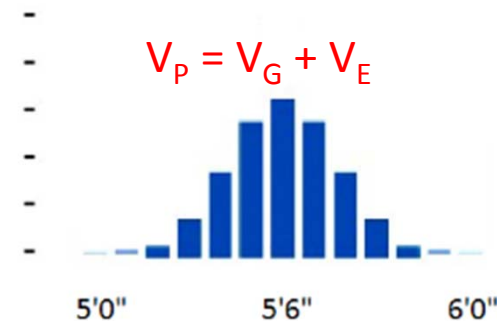
## EXAMPLE:

Manually calculate variance  
for F<sub>1</sub>s to be: 5

Manually calculate variance  
for F<sub>2</sub>s to be: 25

What is heritability???

F<sub>2</sub>:



$$V_P = V_G + V_E$$

$$\text{Heritability} = V_G / (V_G + V_E)$$