







# NATURAL SELECTION: Types at single loci

Duke  
UNIVERSITY







YY 	Yy 
Yy 	yy 

# Selection and dominance







- In previous example, all adult “aa” die
  - $w(MM) = 1.00$        $w(MN) = 1.00$        $w(NN) = 0$
  - Which allele is dominant/ recessive?

YY 	Yy 
Yy 	yy 

# Selection and dominance







- In previous example, all adult “aa” die
  - $w(MM) = 1.00$        $w(MN) = 1.00$        $w(NN) = 0$
  - N is **recessive** to M, and N is detrimental (bad)
- A different example:
  - $w(MM) = 1.00$        $w(MN) = 0$        $w(NN) = 0$
  - What will this selection do differently?
  - Which allele is dominant?

YY 	Yy 
Yy 	yy 

# Selection and dominance



- In previous example, all adult “aa” die
  - $w(MM) = 1.00$        $w(MN) = 1.00$        $w(NN) = 0$
  - N is recessive to M, and N is detrimental (bad)
- A different example:
  - $w(MM) = 1.00$        $w(MN) = 0$        $w(NN) = 0$
  - N is **dominant** to M, and N is detrimental (bad)
    - With dominant detrimental, heterozygotes respond to selection
- A third example:
  - $w(MM) = 1.00$        $w(MN) = 0.5$        $w(NN) = 0$

YY 	Yy 
Yy 	yy 

# Selection and dominance



- In previous example, all adult “aa” die
  - $w(MM) = 1.00$        $w(MN) = 1.00$        $w(NN) = 0$
  - N is recessive to M, and N is detrimental (bad)
- A different example:
  - $w(MM) = 1.00$        $w(MN) = 0$        $w(NN) = 0$
  - N is dominant to M, and N is detrimental (bad)
    - With dominant detrimental, heterozygotes respond to selection
- A third example: **“no dominance”**
  - $w(MM) = 1.00$        $w(MN) = 0.5$        $w(NN) = 0$

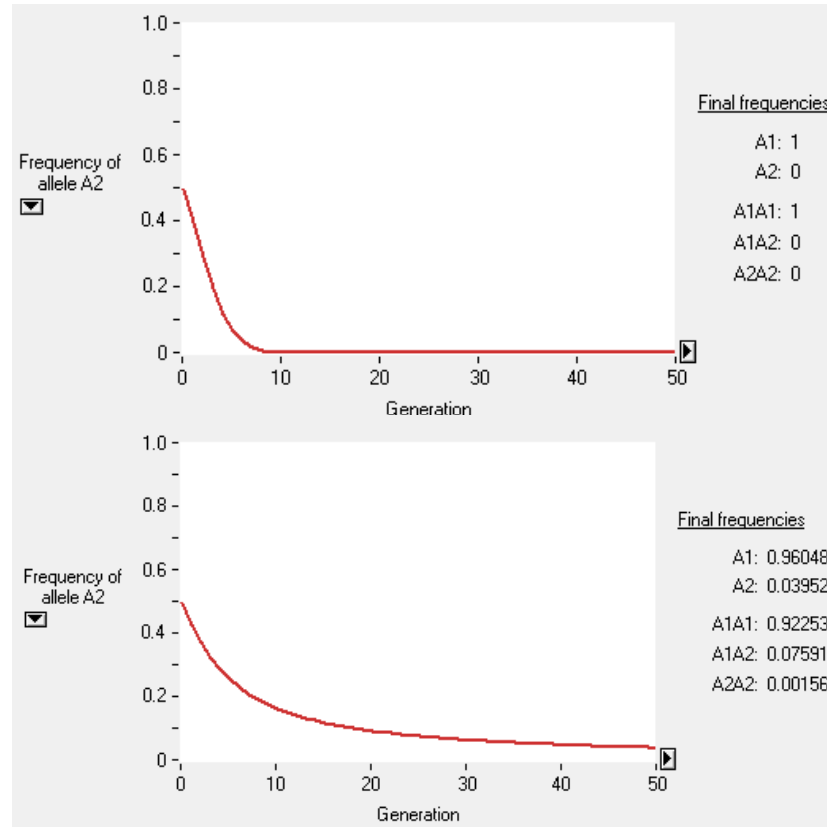
# Effect of dominance with directional selection

- **Dominant detrimental**

- $w(A_1A_1) = 1.0$
- $w(A_1A_2) = 0.5$
- $w(A_2A_2) = 0.5$

- **Recessive detrimental**

- $w(A_1A_1) = 1.0$
- $w(A_1A_2) = 1.0$
- $w(A_2A_2) = 0.5$



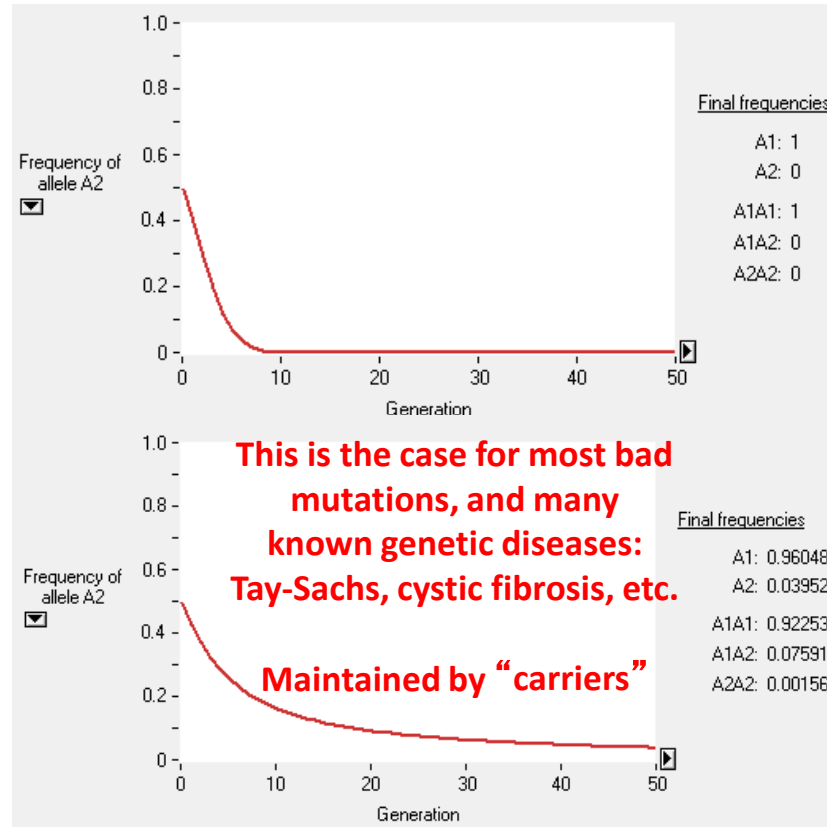
# Effect of dominance with directional selection

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- $w(A_1A_2) = 0.5$
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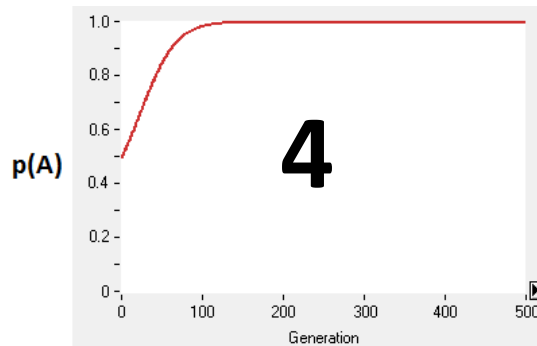
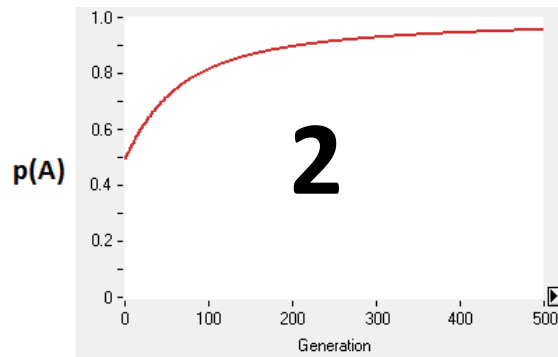
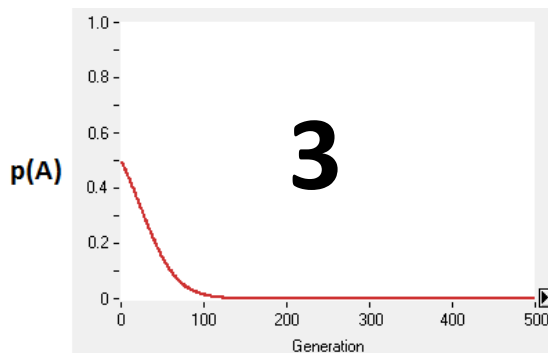
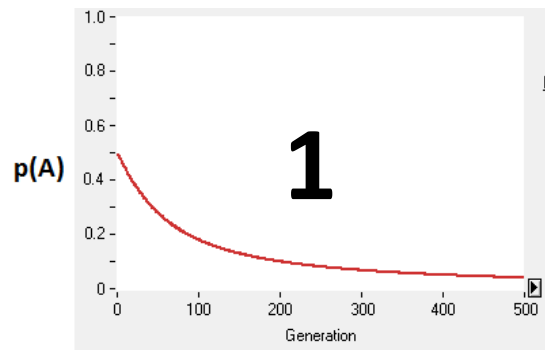
- **Recessive detrimental**

- $w(A_1A_1) = 1.0$
- $w(A_1A_2) = 1.0$
- $w(A_2A_2) = 0.5$



# Which depicts the frequency change in the lactose intolerance allele (A) by selection?

AA: 0.95 Aa: 1.00 aa: 1.00





# Types of selection on single locus:

## 1) Directional selection

- Directional selection

- One allele *eventually* replaces the other

- $w(AA) = 1.00$        $w(Aa) = 1.00$        $w(aa) = 0$

- $w(AA) = 1.00$        $w(Aa) = 0.5$        $w(aa) = 0$

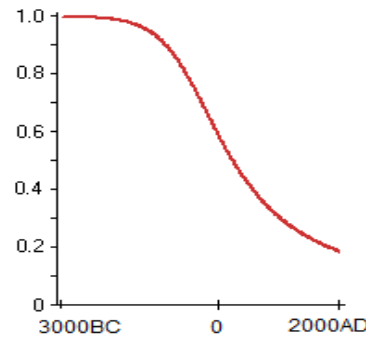
- $w(AA) = 0.1$        $w(Aa) = 0.2$        $w(aa) = 1.00$

Lactase: •  $w(AA) = 0.95$        $w(Aa) = 1.00$        $w(aa) = 1.00$

- $w(AA) \leq w(Aa) \leq w(aa)$  OR

- $w(AA) \geq w(Aa) \geq w(aa)$

Lactose  
intolerance  
allele



# Types of selection on single locus:

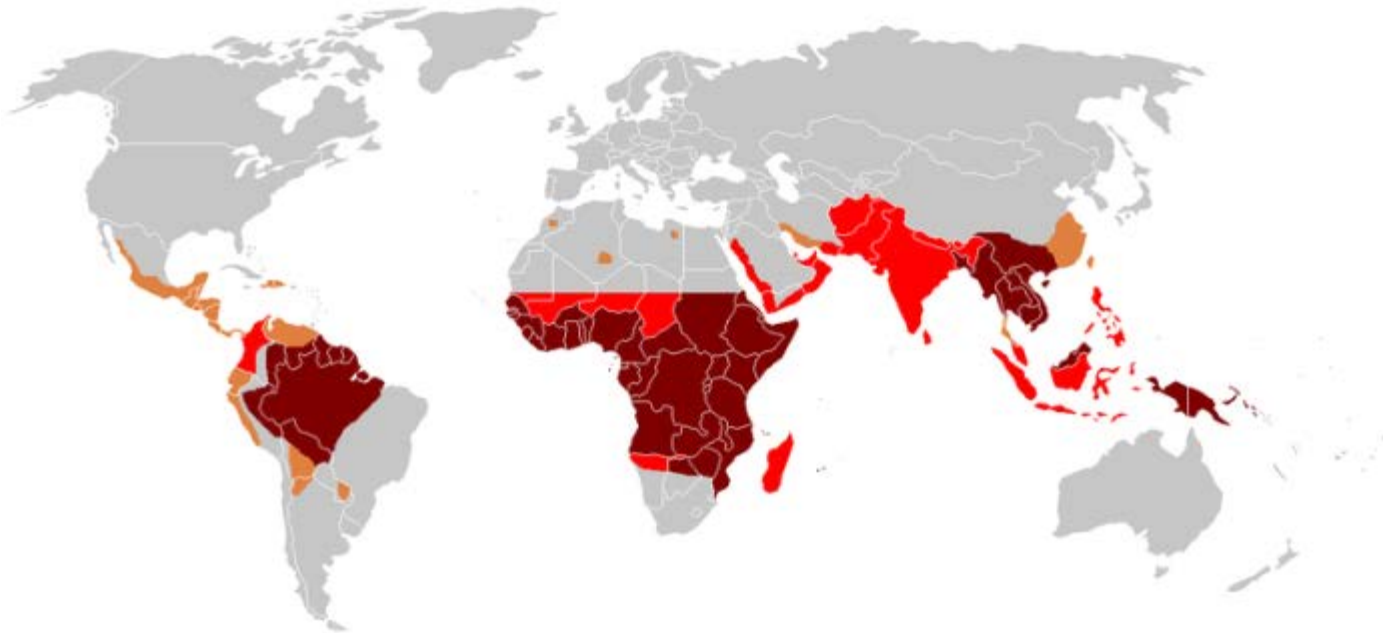
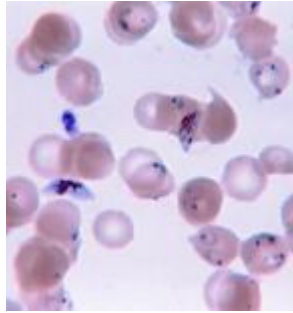
## 2) Heterozygote advantage

- Also called “overdominance”
  - Most fit genotype is the heterozygote (Aa)
    - $w(AA) = 0.85$        $w(Aa) = 1.0$        $w(aa) = 0.05$
- One allele **does not** replace the other
  - Example: Sickle cell anemia and malaria resistance



# Malaria incidence

- ~4% chance of death by malaria in sub-Saharan Africa
  - Mosquito bite transmits Plasmodium protozoa



# Sickle Cell Anemia

- Recessive genetic disease (aa)
  - Sick cells die faster than normal RBCs
  - Sick cells deliver less oxygen to cells
  - Symptoms: chronic pain & fatigue
- If heterozygote (Aa)
  - Called “Sickle cell trait”
  - Usually OK, but cells may sickle during intense physical exertion



# Intersection: Sickle Cell & Malaria

- Individuals heterozygous for sickle cell (Aa) are (more) resistant to malaria!
  - *Old thought*: Invasion, growth, & development of Plasmodium may be reduced in blood cells in Aa?
  - *Recent*: Aa more tolerant to sickle cell symptoms but retain same infection load?
  - *Recent2*: Infected Aa cells more likely to be eliminated by spleen since being Aa prevents one defense of Plasmodium



Ferreira et al (2011) *Cell* 145: 398-409

Cyrklaff et al (2011) *Science* 334:1283-6

# Sickle Cell Exhibits Heterozygote Advantage *in Some Populations*

<u>Subsaharan Africa</u>	<u>Sample Fitness</u>
AA – Susceptible to malaria	$w(AA) = 0.85$
Aa – Generally fine!	$w(Aa) = 1.00$
aa – Sickle cell anemia disease	$w(aa) = 0.05$

Fate of new “a”  
mutation in  
“A” population:

# Sickle Cell Exhibits Heterozygote Advantage *in Some Populations*

Subsaharan Africa

AA – Susceptible to malaria

Aa – Generally fine!

aa – Sickle cell anemia disease

Sample Fitness

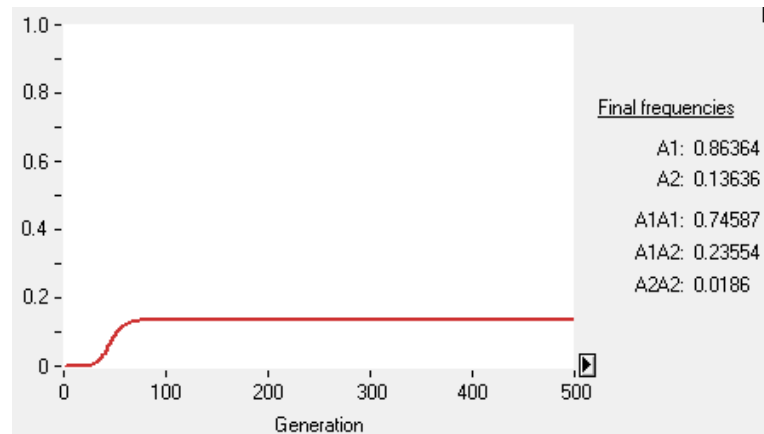
$w(AA) = 0.85$

$w(Aa) = 1.00$

$w(aa) = 0.05$

Fate of new “a”  
mutation in  
“A” population:

q (a)



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Fate of new “a” mutation in “A” population:

$$q(a) = \frac{\text{Predictable: } 1-w(AA)}{(1-w(aa)) + (1-(w(AA)))}$$



# Sickle Cell Exhibits Heterozygote Advantage *in Some Populations*

<u>Subsaharan Africa</u>	<u>Sample Fitness</u>
AA – Susceptible to malaria	$w(AA) = 0.85$
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Fate of new “a” mutation in “A” population:

$$q(a) = \frac{\text{Predictable: } 1-0.85}{(1-0.05) + (1-0.85)}$$

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<u>Subsaharan Africa</u>	<u>Sample Fitness</u>
AA – Susceptible to malaria	$w(AA) = 0.85$
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Fate of new “a” mutation in “A” population:

$$q(a) = \frac{\text{Predictable: } 0.15}{0.95 + 0.15} = 0.136$$

# Sickle Cell Exhibits Heterozygote Advantage *in Some Populations*

Subsaharan Africa

Sample Fitness

AA – Susceptible to malaria

$w(AA) = 0.85$

Aa – Generally fine!

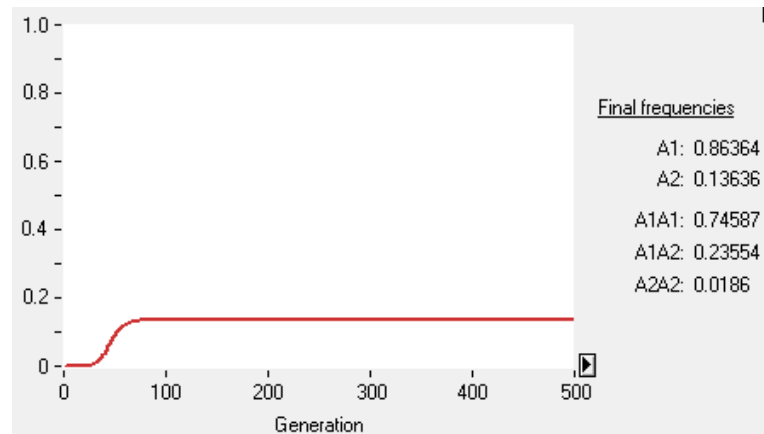
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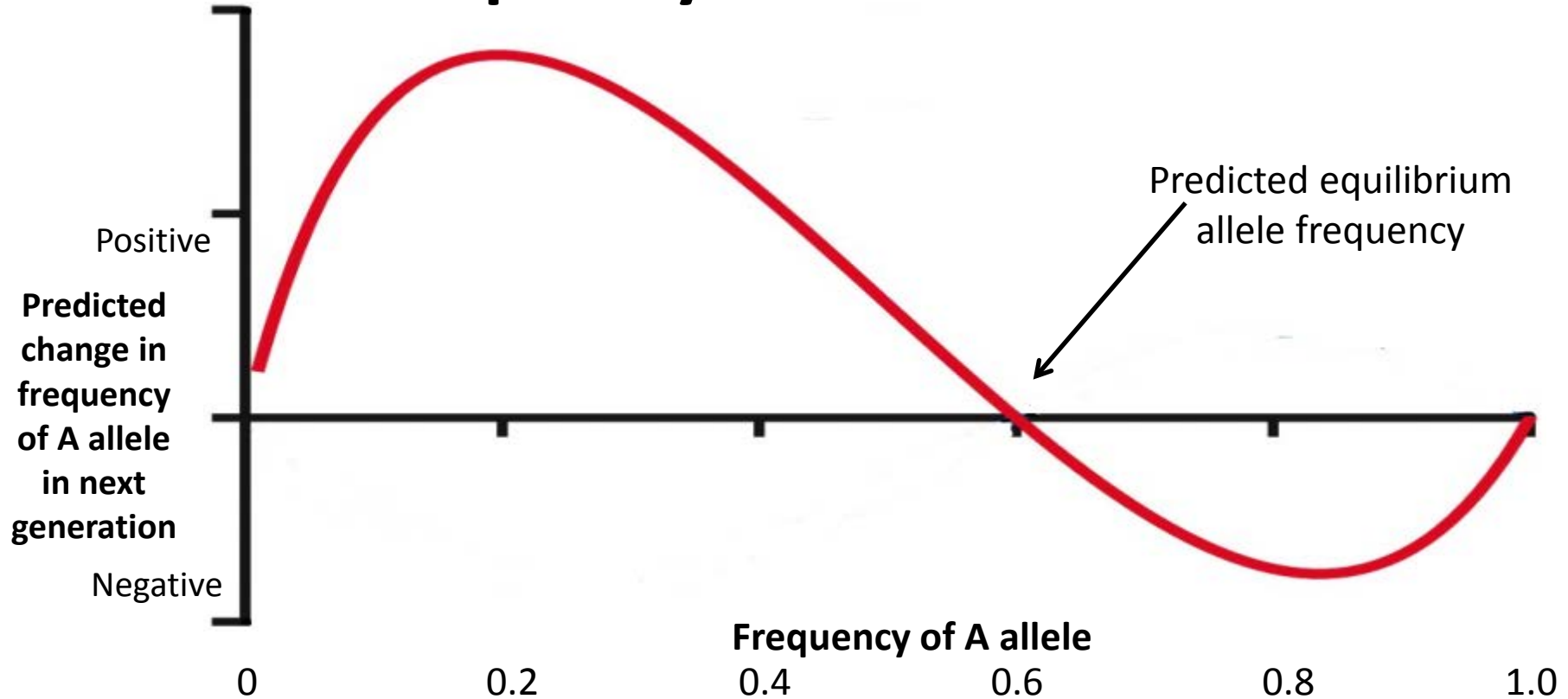
# Types of selection on single locus:

## 2) Heterozygote advantage

- Also called “overdominance”
  - Most fit genotype is the heterozygote (Aa)
    - $w(AA) = 0.85$        $w(Aa) = 1.0$        $w(aa) = 0.05$
  - Leads to a “stable equilibrium”
    - Both alleles retained in the population
    - Alleles go to “equilibrium” frequencies
    - If not at equilibrium frequency, move back to it



# Graphical representation of changes in allele frequency with overdominance



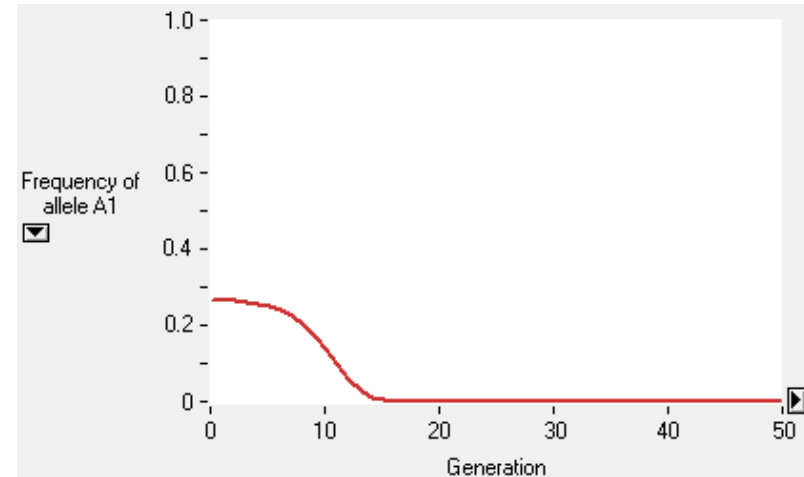
# Types of selection on single locus:

## 3) Heterozygote disadvantage

- Also called “underdominance”
  - LEAST fit genotype is the heterozygote (Aa)
    - $w(AA) = 1.00$      $w(Aa) = 0.2$      $w(aa) = 0.5$
  - Leads to a “**unstable** equilibrium” (0.272727)

If start **below** equilibrium, go to loss

- Starting  $p(A1) = 0.27$



# Types of selection on single locus:

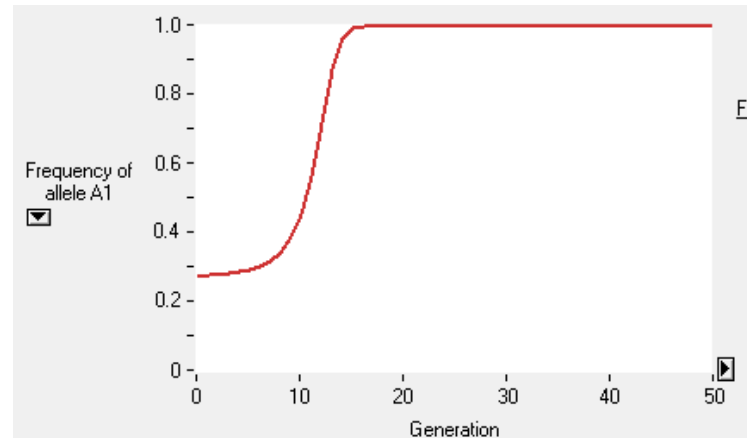
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  - Leads to a “**unstable** equilibrium” (0.272727)

If start below equilibrium, go to loss

If start **above** equilibrium, go to fixation

- Starting  $p(A1) = 0.275$



# Types of selection on single locus:

## 3) Heterozygote disadvantage

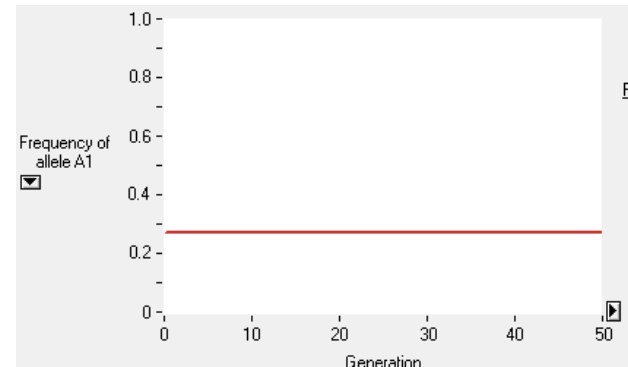
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  - Leads to a “**unstable** equilibrium” (0.272727)

If start below equilibrium, go to loss

If start above equilibrium, go to fixation

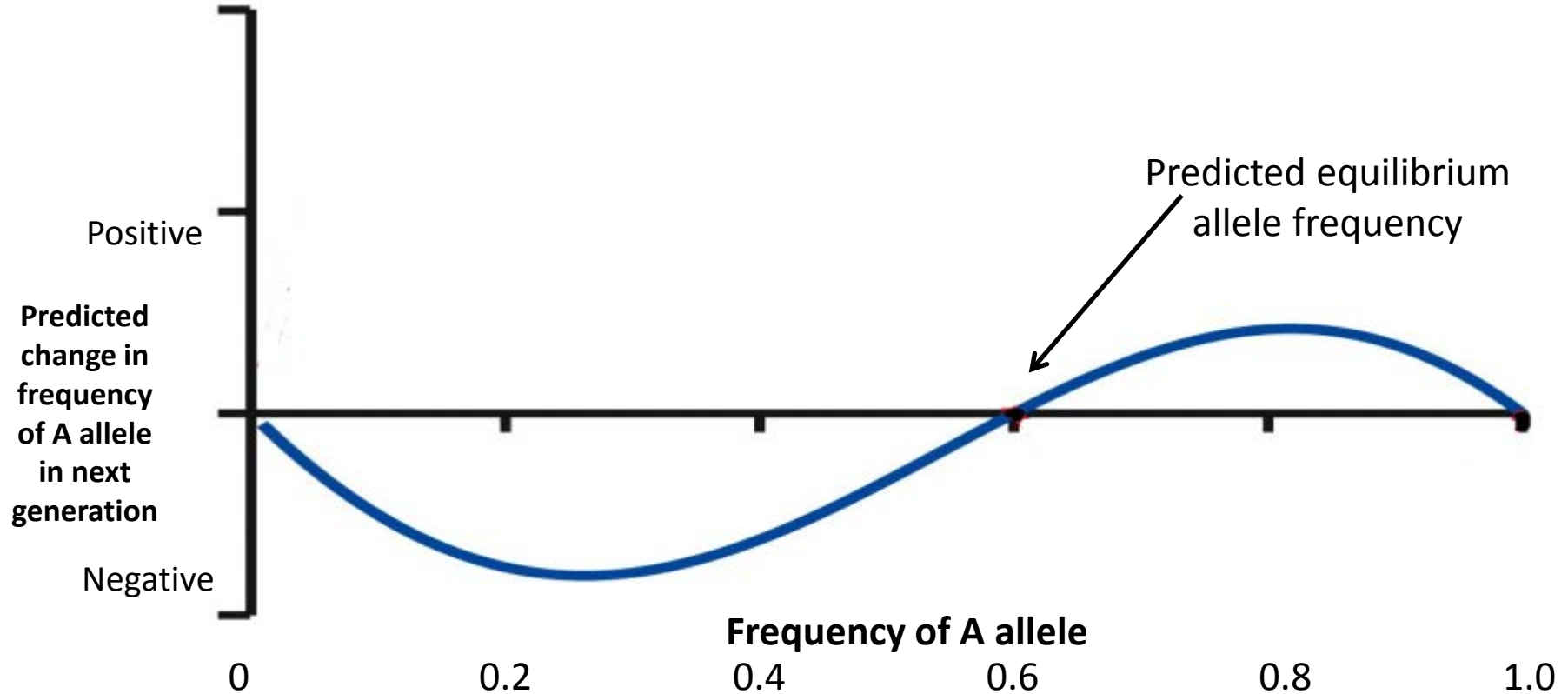
If start (and STAY) at equilibrium, alleles persist

- But very unlikely to stay...





# Graphical representation of changes in allele frequency with underdominance



# Types of selection on single locus:

## 4) Frequency dependent selection

- Previous examples assumed fitness was independent of the rest of the population
- Sometimes, it's better to be "rare" ...
- But being "better" makes you become more common
- Leads to equilibrium:
  - Negative frequency dependent selection

# Example: Sex Ratio

- In many species, sex (male vs. female) determined genetically
  - In mammals, XX vs. XY, so mostly locked in to 50-50 sex ratio by transmission
  - In other species, alleles at a gene cause individual to become male vs. female
- If females are *rare*, is it better to produce male or female offspring?
  - Would selection favor “male” or “female” allele?



# Example: Sex Ratio

- Computer science club marooned on an island
  - What is likely fitness of average guy on island?
  - What is likely fitness of the one female?





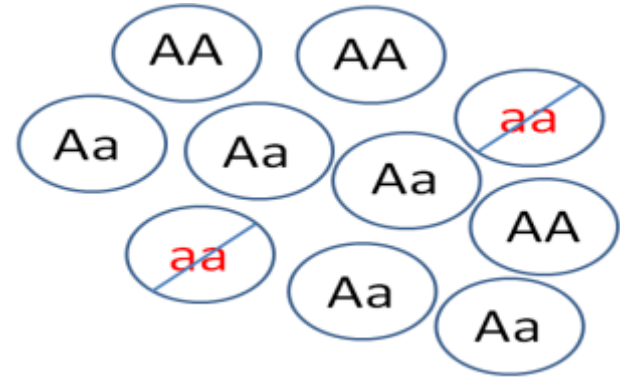
# Outcome of Negative

## Frequency Dependent Selection

- When rare, allele has advantage
- When common, allele has disadvantage
- **Genetic variation maintained in population!**
- If have 2 alleles, what do you predict the “equilibrium allele frequency” to be?
- What if a third allele is introduced into the population?

# Single locus selection discussed

- Directional selection favoring one allele
    - Effects of dominance
  - Heterozygote advantage
  - Heterozygote disadvantage
  - Frequency dependent selection
- 
- All affect genotype & allele frequencies, but act on *phenotype*



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