

# Linear Programming Quiz

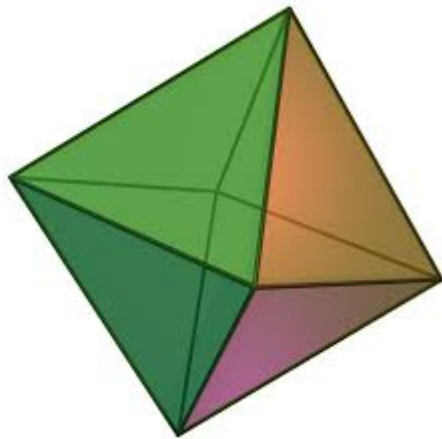
**5/5 points (100%)**

Quiz, 5 questions

**✓ Congratulations! You passed!**[Next Item](#)1 / 1  
points

1.

What is the minimum number of linear inequalities needed to define the figure pictured below?

**Correct Response**

The figure is cut out by 8 flat surfaces. Thus 8 equations are needed.

1 / 1  
points

2.

Given a solution to a linear program, one could try to show that it is optimal by finding a matching solution to the dual program. Which of the following theorems will make it easier to do so?



Separation of convex sets from outside points by hyperplanes.

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**Correct**

Correct! Complementary slackness tells you that your dual solution only uses equations that are tight in solutions to the primal.



Polytopes achieve optimum values at vertices.



1 / 1  
points

3.

Which of the following statements are true?



A system of linear equations has always 0, 1, or infinitely many solutions.



**Correct**

This statement is true. Unless there are no solutions, the solution set has some number of free variables. If there are no free variables, there is a unique solution. If there is at least one free variable, there are infinitely many solutions.



A system of  $n$  linear equations in  $n$  variables always has a unique solution.



**Un-selected is correct**



A system of linear equations has a solution unless they can be combined in some combination to give the equation  $0=1$ .



**Correct**

This statement is true. There is a solution unless the corresponding row reduced matrix has a row corresponding to this equation, this will happen only if  $0=1$  can be obtained by combining the original equations.



points

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Quiz, 5 questions

Suppose that you are trying to solve the optimization problem:

Maximize  $v \cdot x$  subject to  $Ax \geq b$  for some  $A \in \mathbb{R}^{m \times n}$  (i.e. trying to solve an optimization problem in  $n$  variables with  $m$  linear inequality constraints).

This problem can be reduced to running a solution finding algorithm on a different system of linear equations in  $k$  variables. What is the smallest value of  $k$  for which this can be done?

Preview

$$m + n$$

n+m

### Correct Response

Correct! You need to look for matching solutions to the primal ( $n$  variables) and the dual ( $m$  variables). Thus, you need a solution to a larger system with  $n+m$  variables.

Your answer,  $n+m$ , is equivalent to the instructor's answer  $n+m$ .

1 / 1  
points

5.

What is the largest possible value of  $x+y$  achievable by pairs  $x,y$  of real numbers satisfying the constraints:

- $x \leq 7$
- $y \leq 10$
- $2x+y \leq 21$
- $-x + 2y \leq 12$
- $5x-y \leq 30$

15

### Correct Response

Correct. The optimum is at  $x=6, y=9$  as shown below.

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