

P5.1

(1)

$$t = \frac{2L}{V} = \frac{2 \times 10^{-9}}{c} = 4 \times 10^{-9} \text{ s} = 4 \text{ ns}$$

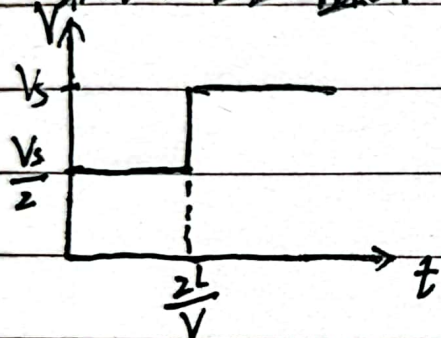
(2)

∵ 左侧, 阻抗匹配 ∴ $\Gamma_1 = 0$

∵ 右侧开路 ∴ $\Gamma_2 = 1$

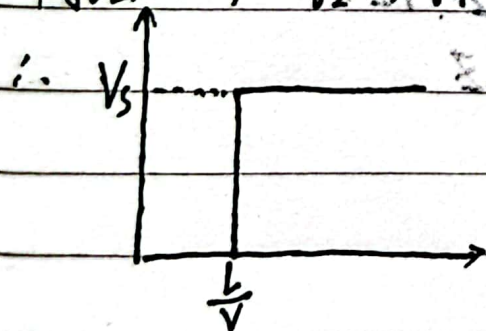
$$V = V_+ e^{-ikz} + \Gamma_2 V_+ e^{ikz} \Big|_{z=0} = 2V_+$$

∵ 最终电压值为 V_s ∴ $V_+ = \frac{V_s}{2}$



(3)

同理(2), $V_2 = V_+ + V_- = 2V_+ = V_s$



Ps. 2 (第2题)

$$(1) I_{(0)} = I_0 = \frac{1}{Z_0} (V_+ e^{-jkz} - V_- e^{jkz})$$

$$I_{(-L)} = I_0 \cos(-kL) = \frac{1}{Z_0} (V_+ e^{-jk(-L)} - V_- e^{jk(-L)}) = \frac{1}{Z_0} (V_+ e^{jkL} - V_- e^{-jkL})$$

$$\because L = 2\lambda$$

$$\therefore \text{解得: } V_+ = \frac{Z_0 I_0}{2}, \quad V_- = -\frac{Z_0 I_0}{2} \therefore \text{电压为驻波, 电流为行波}$$

2)

$$\Gamma_L = \frac{V_-}{V_+} = -1$$

(3)

$$\Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{\frac{Z_0}{Z_0} - 1}{\frac{Z_0}{Z_0} + 1} = -1$$

$$\therefore Z_L = 0$$

(4)

$$V(z) = Z_0 I_0 \cos kz$$

$$\therefore V(z, t) = \operatorname{Re} \{ Z_0 I_0 e^{-jkz} \cdot e^{j\omega t} \} = Z_0 I_0 \cos(\frac{\pi}{2} - kz) = Z_0 I_0 \sin kz$$

(5)

$$I_{(-L)} = I_0 \cos(-kL) = I_0$$

$$\therefore Z_S = \frac{V_S}{I_{(-L)}} = \frac{Z_0 I_0}{I_0} = Z_0$$



P5.3

(1) 在 $t = \frac{1.5l}{v}$ 时, 信号还未在 T_2, T_3 右侧发生反射, 只在 T_1 右侧发生反射

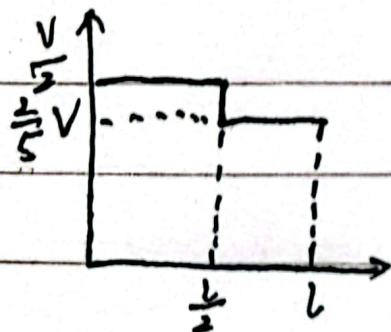
$$Z_{1L} = \frac{2Z_0 \cdot Z_0}{2Z_0 + Z_0} = \frac{2}{3}Z_0$$

$$\therefore \Gamma_{1L} = \frac{Z_{1L} - Z_0}{Z_{1L} + Z_0} = -\frac{1}{5}$$

由 P5.1, 可知开关闭合后, $V_+ = \frac{V}{2}$, 由 Z_0 分压

$$\therefore 0 \sim 0.5l, V(x) = \frac{V}{2}$$

$$0.5 \sim l, V(x) = \frac{V}{2} + \Gamma_{1L} V_+ = \frac{V}{2} - \frac{V}{10} = \frac{2}{5}V$$



(2)

$$I_1 = I_2 + I_3, V_1 = V_2 = V_3$$

由于 T_2 断路, $I_2 = 0$

由于 T_1, T_3 短路, $V_1 = V_2 = V_3 = 0$

$$\therefore Z_{in} = \frac{V_1}{I_1} = 0 \quad \therefore \text{输入阻抗为 } 0$$



5.2 (第4题)

(1)

$$H(\vec{r}) = \frac{\vec{r}}{\omega \mu} \times \vec{E} = \hat{y} \frac{k_0}{\omega \mu} e^{ik_0 x/2 + ik_0 z \sqrt{3}/2}$$

$$\therefore H(\vec{r}) = H(\vec{r})_i + H(\vec{r})_t, \quad H(\vec{r})_i = H(\vec{r})_t \big|_{x=0}$$

$$\therefore H(\vec{r}) = \hat{y} \frac{2k_0}{\omega \mu} e^{ik_0 x/2 + ik_0 z \sqrt{3}/2}$$

$$\text{在 } x=0 \text{ 处, } H(\vec{r}) = \hat{y} \frac{2k_0}{\omega \mu} e^{ik_0 z \sqrt{3}/2}$$

~~$\nabla \times \vec{H} = \vec{J}$~~ \therefore 右侧无磁场

~~由 $\nabla \times \vec{H}(\vec{r}) = -i\omega \vec{D}(\vec{r}) + \vec{J}(\vec{r})$ 得: 由环路定理知:~~

$$\therefore \vec{J}(\vec{r}) = \hat{z} \frac{2k_0}{\omega \mu} e^{ik_0 z \sqrt{3}/2}$$

(2)

记 PEC 的阻抗为 $Z=0$

$$\therefore \Gamma_x = 0-1 \text{ (x方向上)}$$

$$\therefore E_{-x} = \Gamma E_{+x} \quad \therefore E_{-} = (-\hat{x} \sqrt{3}/2 - \hat{z} 1/2) e^{ik_0 x/2} e^{ik_0 z \sqrt{3}/2}$$

\therefore 在 $x=0$ 处,

$$\begin{aligned} E_{+} + E_{-} &= (\hat{x} \sqrt{3}/2 - \hat{z} 1/2) e^{ik_0 z \sqrt{3}/2} + (-\hat{x} \sqrt{3}/2 - \hat{z} 1/2) e^{ik_0 z \sqrt{3}/2} \\ &= -\hat{z} e^{ik_0 z \sqrt{3}/2} \end{aligned}$$

\therefore x方向, 即 $x>0$ 范围内无场

