

# 第五章 模拟运算电路

## 5.3 加法/减法电路

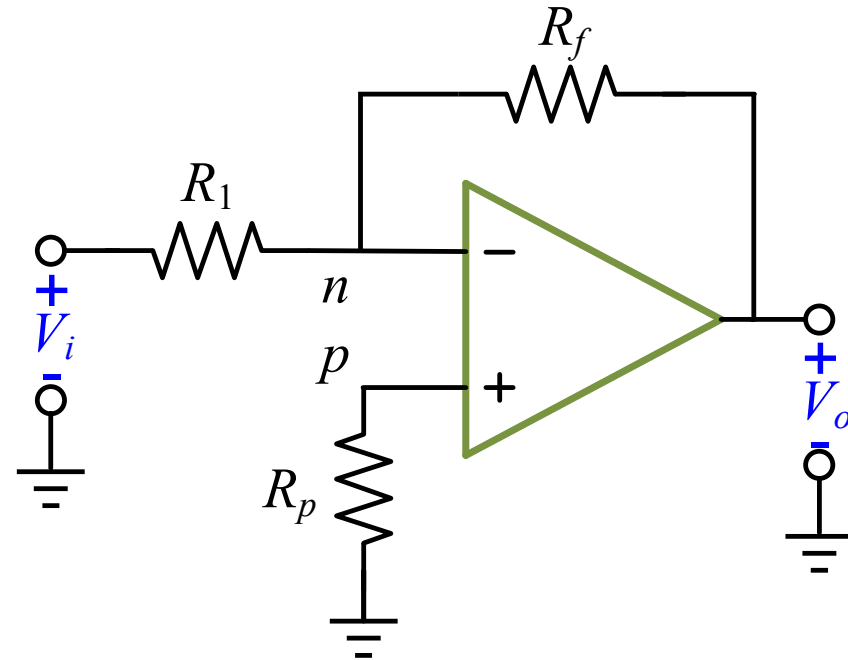
# 加法/减法电路

- 加法电路
  - 反相加法电路
  - 同相加法电路
- 减法电路

# 反相放大器

- 增益

$$A_f = \frac{V_o}{V_i} = -\frac{R_f}{R_1}$$



# 反相加法电路

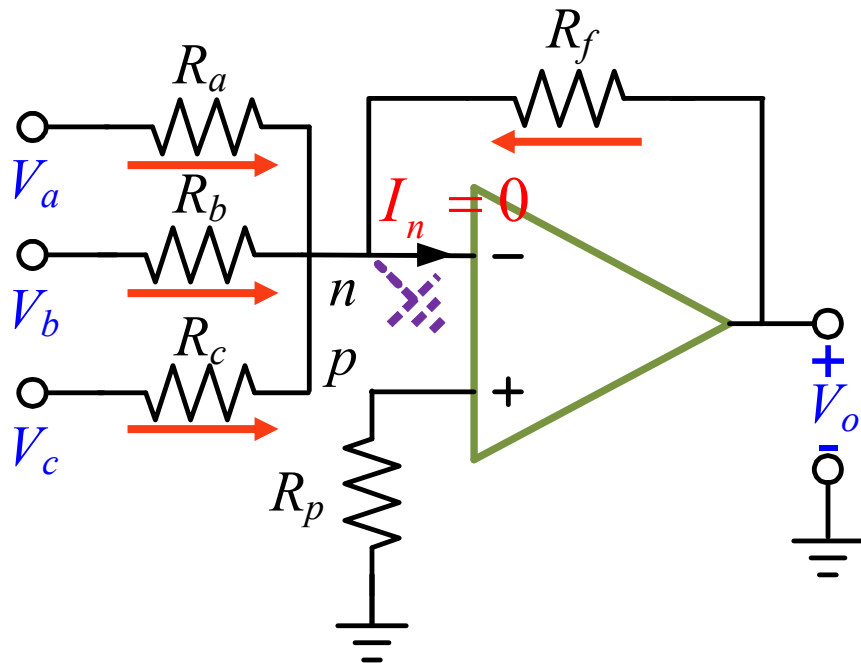
- 3个输入
- 节点n虚地, 同时  $I_n = 0$
- 围绕节点n列写KCL方程

$$\frac{V_a}{R_a} + \frac{V_b}{R_b} + \frac{V_c}{R_c} + \frac{V_o}{R_f} = 0$$

$$V_o = -R_f \left( \frac{V_a}{R_a} + \frac{V_b}{R_b} + \frac{V_c}{R_c} \right)$$

$$R_a = R_b = R_c = R_f \quad V_o = -(V_a + V_b + V_c)$$

反相加法

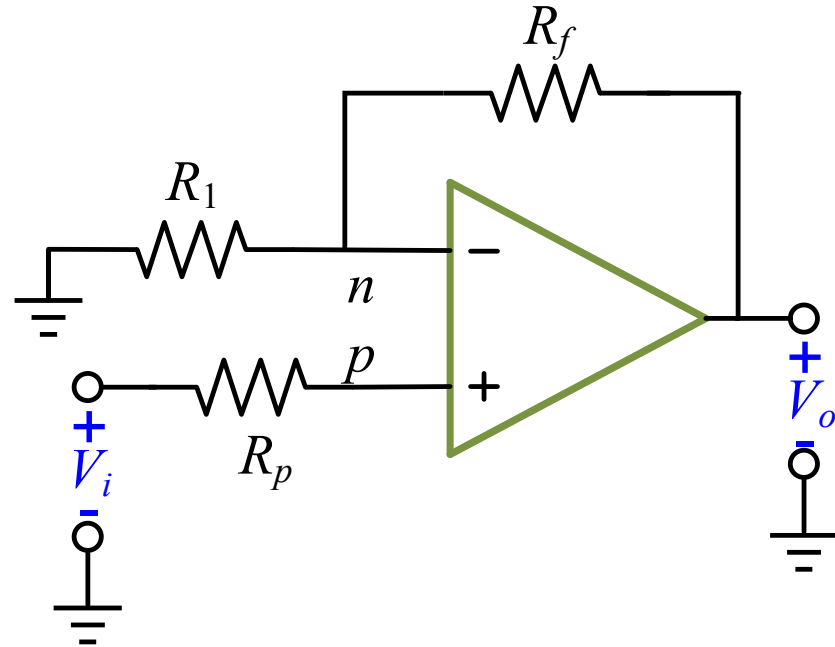


# 同相放大器

- 增益

$$A_f = \frac{V_o}{V_i} = 1 + \frac{R_f}{R_1}$$

$$V_o = \left(1 + \frac{R_f}{R_1}\right) V_i$$

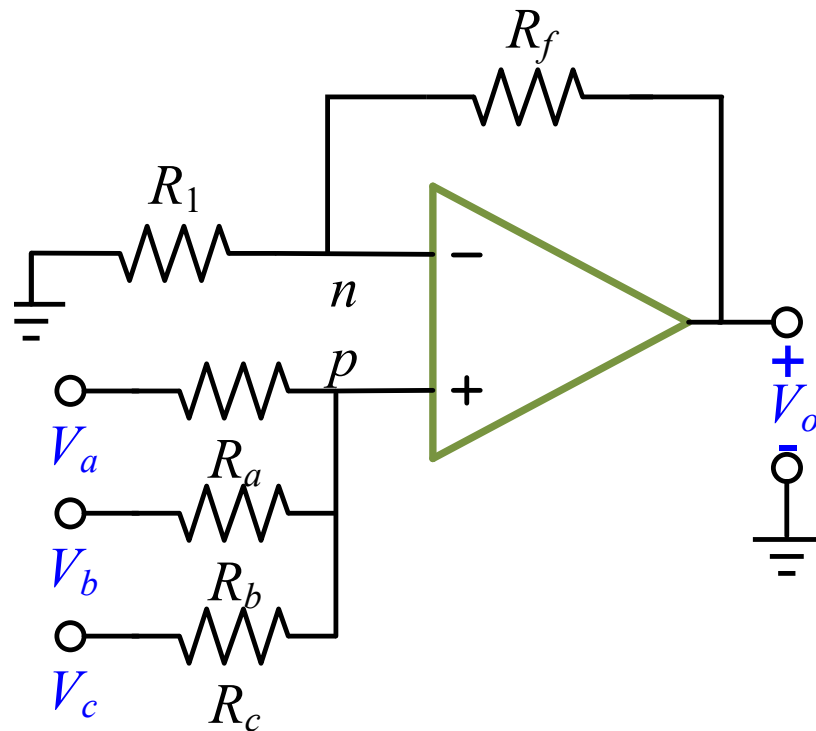


# 同相加法电路

- 3个输入

## 求解思路:

1. 分别计算 $V_a$ 、 $V_b$ 、 $V_c$ 单独作用产生的输出
2. 利用叠加原理得到总的输出

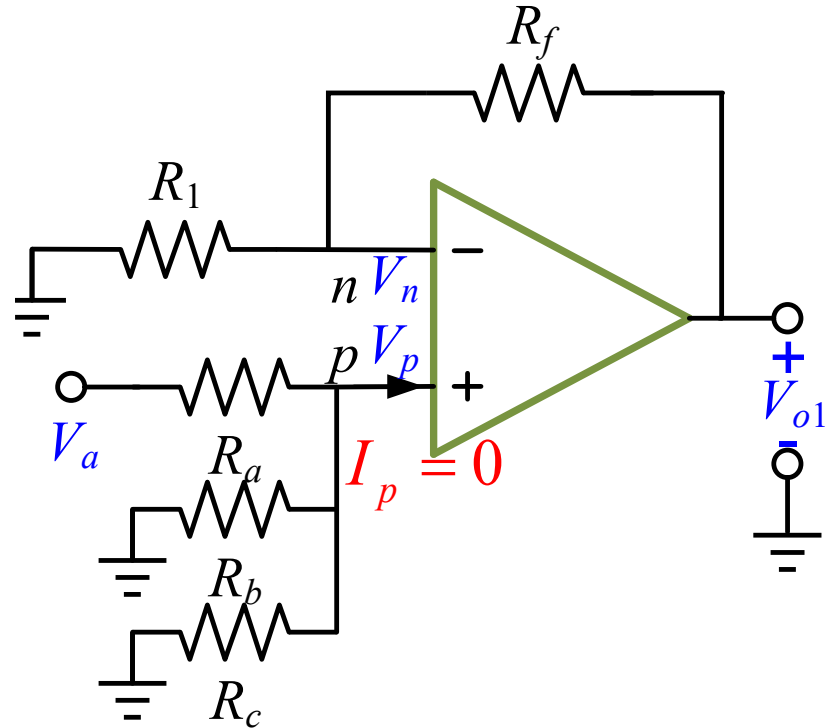


# 同相加法电路

- 假设  $V_a$  单独作用,  $V_b = 0$ ,  $V_c = 0$

$$V_p = V_a \frac{R_b \parallel R_c}{R_a + R_b \parallel R_c}$$

$$V_n = V_p$$



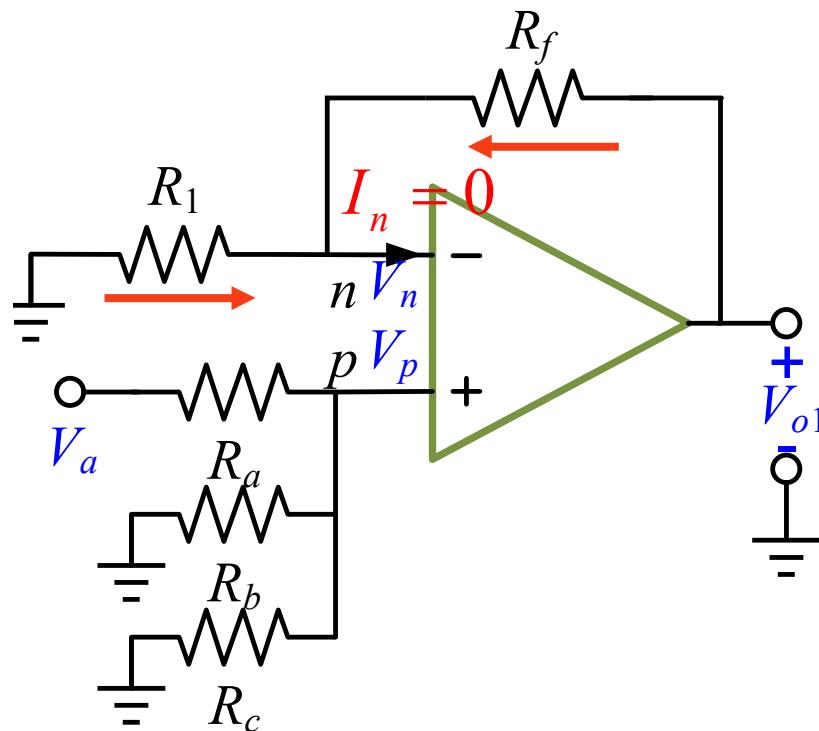
# 同相加法电路

- $V_a$  单独作用

$$V_p = V_a \frac{R_b \parallel R_c}{R_a + R_b \parallel R_c}$$

$$V_n = V_p$$

$$-\frac{V_n}{R_1} + \frac{V_{o1} - V_n}{R_f} = 0$$





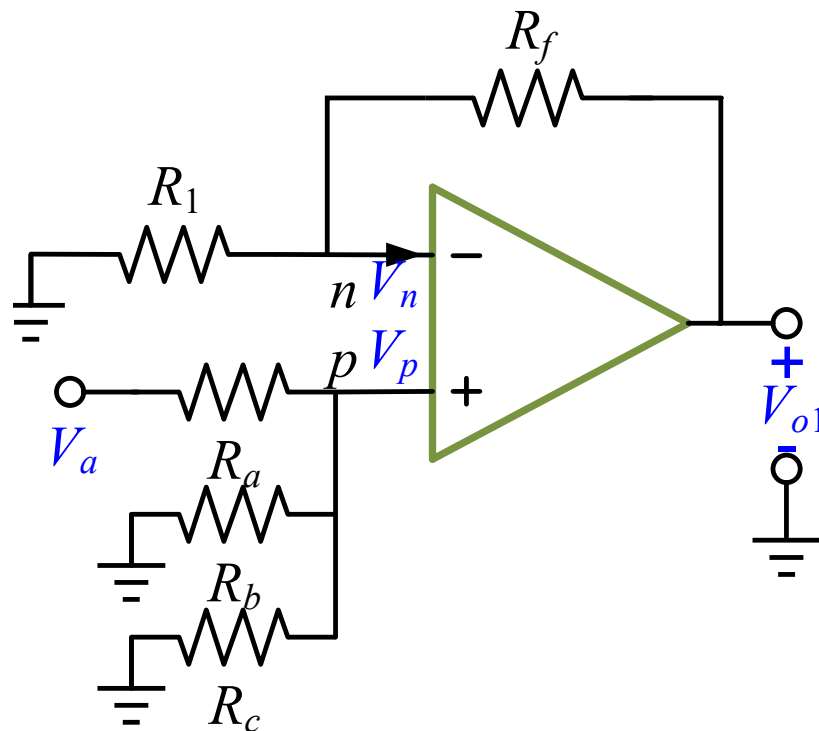
# 同相加法电路

- $V_a$  单独作用

$$V_{o1} = \left(1 + \frac{R_f}{R_1}\right) \frac{R_b \parallel R_c}{R_a + R_b \parallel R_c} V_a$$

$$R_a = R_b = R_c$$

$$V_{o1} = \frac{1}{3} \left(1 + \frac{R_f}{R_1}\right) V_a$$



# 同相加法电路

- $V_a$  单独作用

$$V_{o1} = \frac{1}{3} \left( 1 + \frac{R_f}{R_1} \right) V_a$$

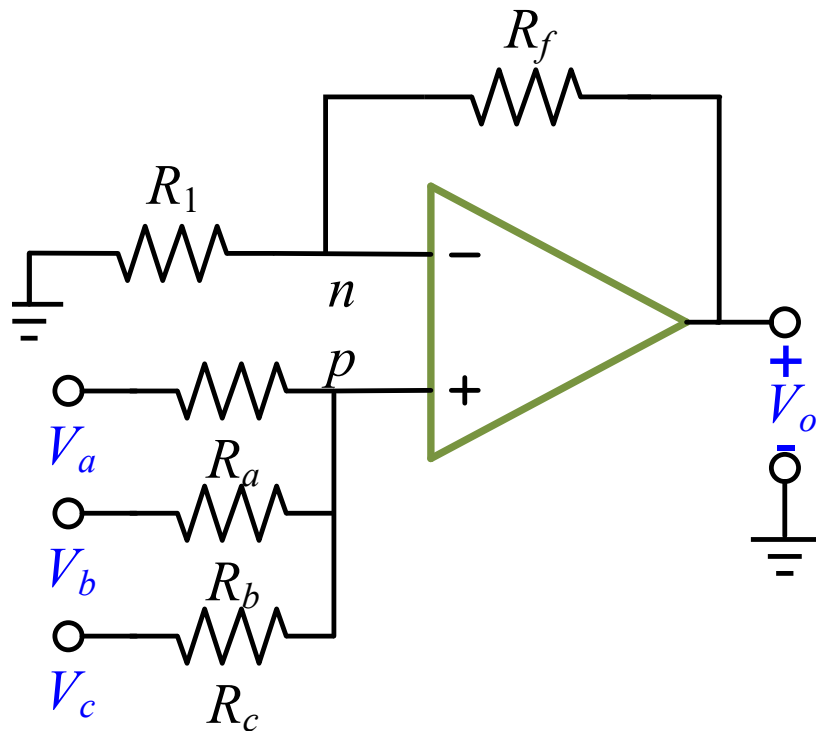
- $V_a$ 、 $V_b$ 、 $V_c$  同时作用

$$V_o = \frac{1}{3} \left( 1 + \frac{R_f}{R_1} \right) (V_a + V_b + V_c)$$

$$R_f = 2R_1$$

$$V_o = V_a + V_b + V_c$$

同相加法



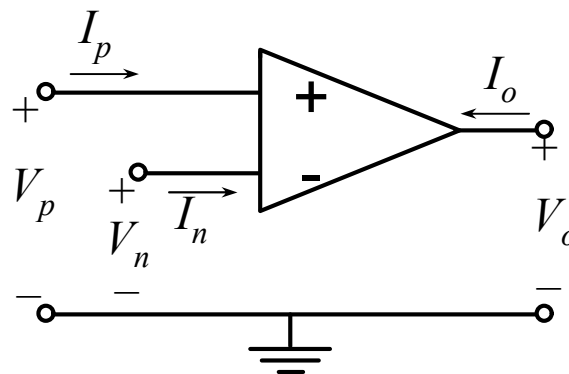
# 减法电路

理想运放就是减法放大器

$$V_o = A(V_p - V_n)$$

$$-V_{CC} \leq V_o \leq V_{CC}$$

$$-\frac{V_{CC}}{A} \leq V_p - V_n \leq \frac{V_{CC}}{A}$$

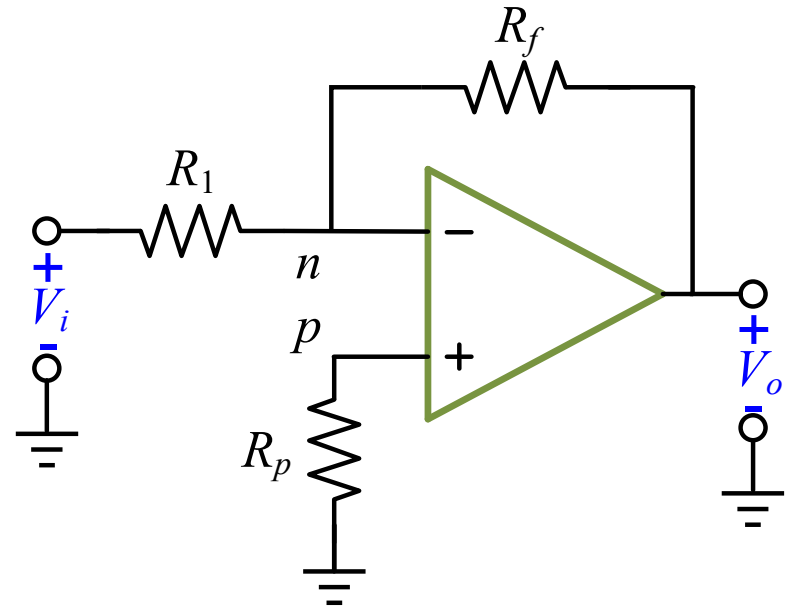


线性工作范围太小

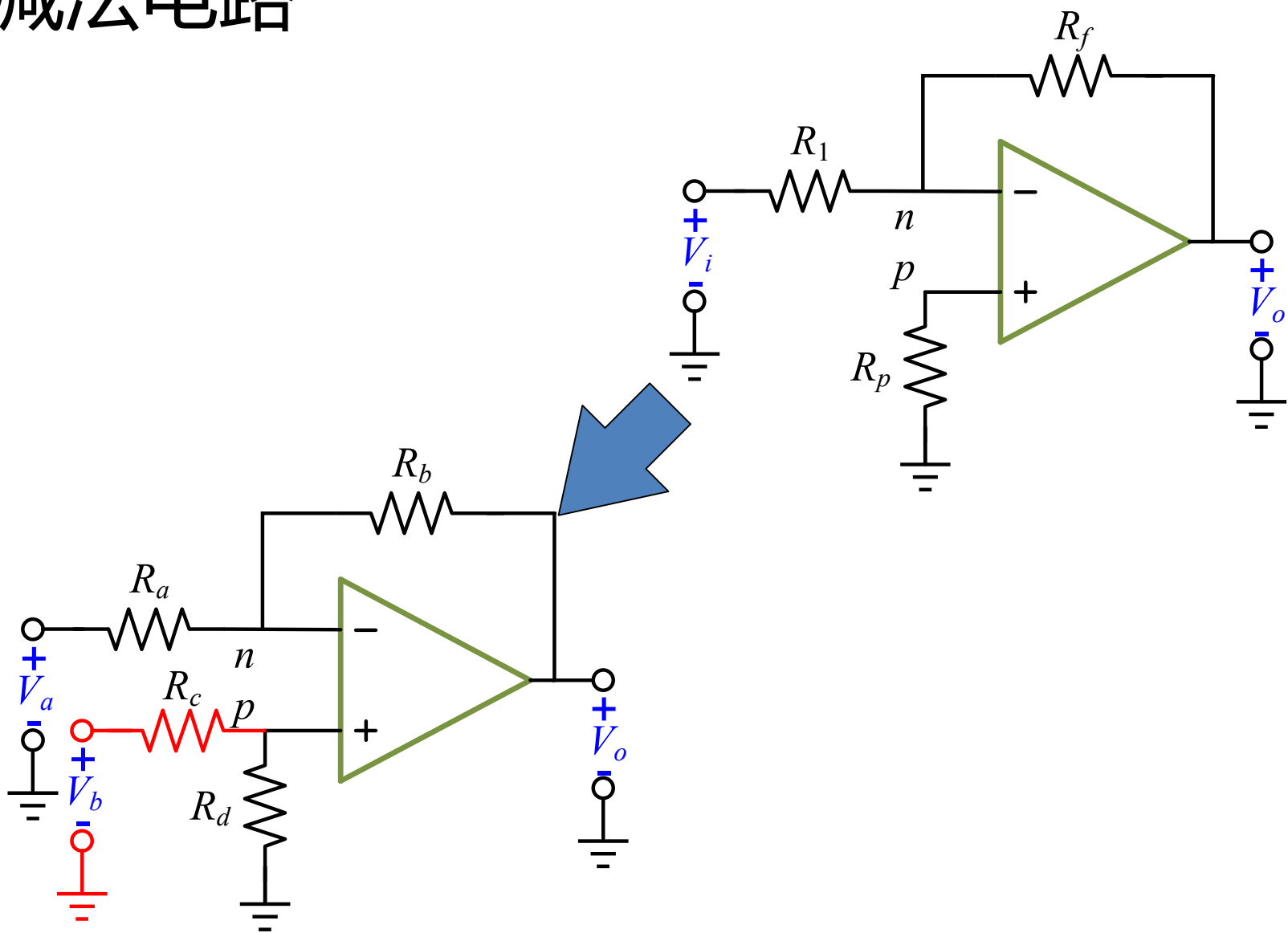
# 反相放大器

- 增益

$$A_f = \frac{V_o}{V_i} = -\frac{R_f}{R_1}$$



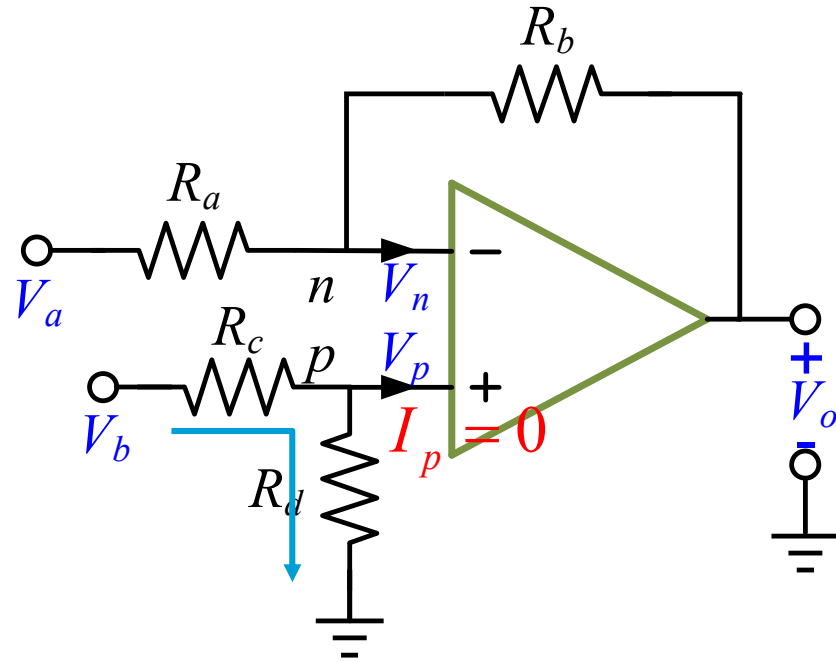
# 减法电路



# 减法电路

$$I_p = 0, \quad I_n = 0, \quad V_n = V_p$$

$$V_p = \frac{R_d}{R_c + R_d} V_b$$

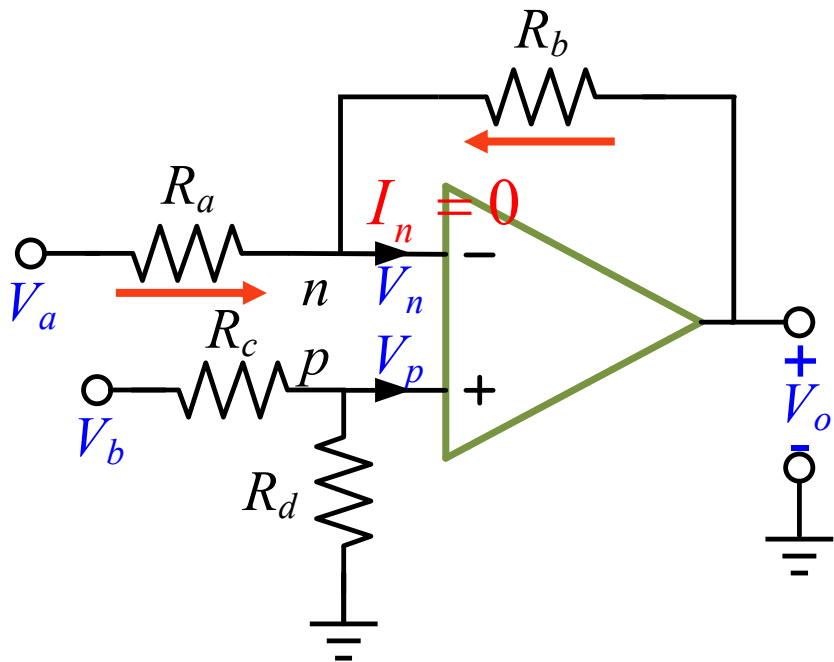


# 减法电路

$$I_p = 0, \quad I_n = 0, \quad V_n = V_p$$

$$V_p = \frac{R_d}{R_c + R_d} V_b$$

$$\frac{V_a - V_n}{R_a} + \frac{V_o - V_n}{R_b} = 0$$



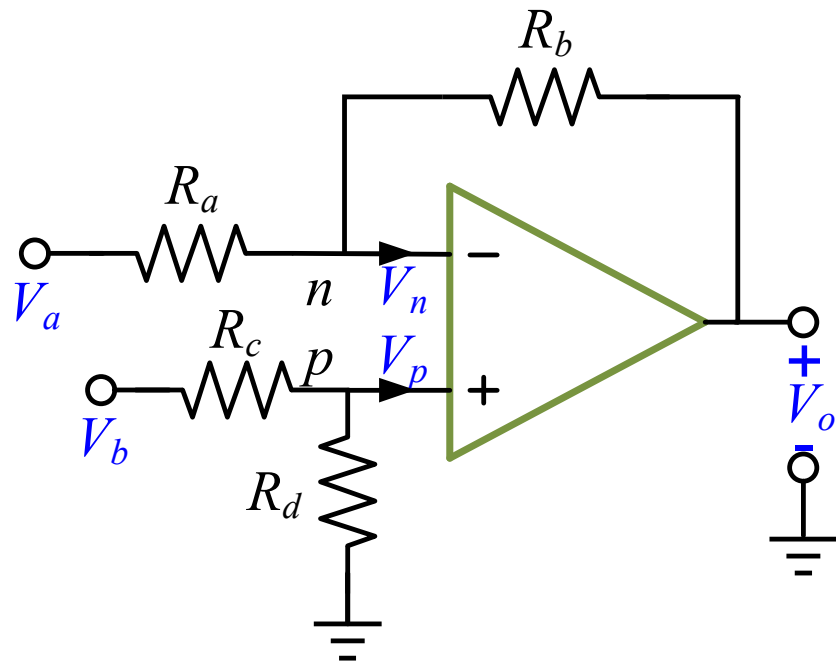
# 减法电路

$$I_p = 0, \quad I_n = 0, \quad V_n = V_p$$

$$V_p = \frac{R_d}{R_c + R_d} V_b$$

$$\frac{V_a - V_n}{R_a} + \frac{V_o - V_n}{R_b} = 0$$

$$V_o = \frac{R_d (R_a + R_b)}{R_a (R_c + R_d)} V_b - \frac{R_b}{R_a} V_a$$





# 减法电路

$$V_o = \frac{R_d (R_a + R_b)}{R_a (R_c + R_d)} V_b - \frac{R_b}{R_a} V_a$$

**减法放大：**

$$R_a = R_c, \quad R_b = R_d$$

$$V_o = \frac{R_b}{R_a} (V_b - V_a)$$

**减法：**

$$(R_a = R_c) = (R_b = R_d)$$

$$V_o = V_b - V_a$$

