

# **Population Kinetics of a Repetitively-Pulsed Nanosecond Discharge**

by

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2013

I would like to dedicate this dissertation to someone else.

## A C K N O W L E D G M E N T S

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Who is this?

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*Preface*

This is a dissertation about something; I really hope it's good.

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## **LIST OF ABBREVIATIONS**

- RPND** repetitively-pulsed nanosecond discharge  
**DBD** dielectric-barrier discharge  
**APP** atmospheric-pressure plasma  
**EEDF** electron energy distribution function  
**FIW** fast ionization wave  
**LAS** laser-absorption spectroscopy  
**LCIF** laser collision-induced fluorescence  
**MHD** magnetohydrodynamic  
**FWHM** full-width half maximum  
**FID** fast ionization dynistor  
**CCD** charge-coupled device  
**PTFE** polytetrafluoroethylene  
**PIC** particle-in-cell  
**NASA** National Aeronautics and Space Administration  
**GRC** Glenn Research Center  
**mmW** millimeter-wave  
**EMI** electromagnetic interference

# **CHAPTER 1**

## **Introduction**

### **1.1 Overview**

#### **1.1.1 Motivation**

Plasmas, commonly called the fourth state of matter, are a gas where a significant fraction of the neutral atoms or molecules have been split into pairs of electrons and positive ions. Initially, a curiosity of the laboratory, they have become a critical part of every day life. The electrically charged nature of plasmas makes them a practical means by which to convert electrical energy into electromagnetic, chemical, kinetic, or even nuclear energy. From an applications perspective, they are indispensable in lighting, semiconductor manufacturing, plastic processing, and space propulsion. On a more broad scale, virtually all observable light in the universe is the result of a plasma in some form or another [7].

Some exceptions aside, only three things are required to create a plasma: a gas, an energy source, and a means of transferring the energy to the gas. In man-made applications, the energy source is typically electricity, and the simplest transfer mechanism is via two electrodes placed on either side of the gas. The application of a potential difference to these electrodes produces an electric field as seen in figure 1.1. The field accelerates a single seed electron in the gas (often created by background cosmic radiation) until it collides with a neutral particle. The electron, having acquired a sufficient amount of energy, liberates a second electron loose from the particle, leaving behind a relatively heavy and immobile

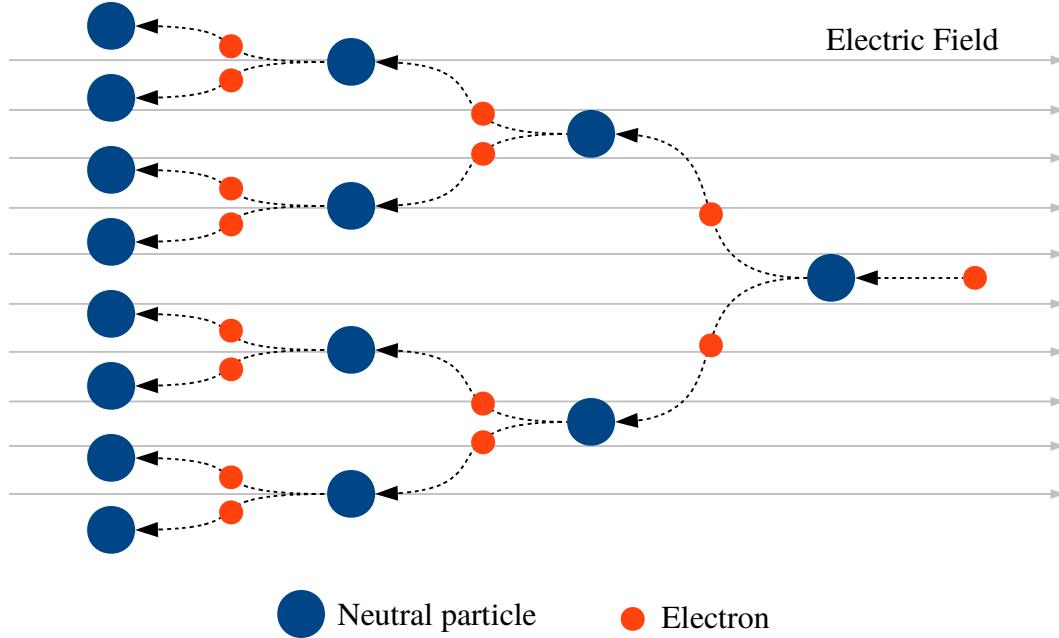


Figure 1.1: A simplified depiction of the avalanche breakdown process in a gas.

ion. Subsequently, both the first and second electron are now accelerated by the electric field. Again, they collide with two more neutral atoms, creating two new electrons. As long as the electric field persists, the number of electron and ion pairs increases exponentially. This process is generally referred to as an avalanche.

Eventually, the production of ions and electrons in the gap balances out with the rate at which they leave the system, whether by collection at the electrodes or some other process. The resulting ionized gas may be referred to as a plasma if it meets certain criteria. Simply put, there must be a high enough density and number of charged particles for their electromagnetic interaction to dominate over random collisions with neutral gas particles.

Despite this relatively simple recipe, the physical characteristics can vary greatly depending on what gas is used, what pressure it is at, what voltage is used, whether the electricity is applied constantly or varied over time, what kind of electrodes are used, etc. As a result, man-made plasmas are generally produced under very specific conditions. For example, a plasma etcher used in semiconductor manufacturing may need to operate oper-

ate at pressures that are one-thousandth of atmospheric pressure with ultra-pure (99.999%) gases [8].

Plasmas like those which occur in plasma etchers, feature ions and neutral gas particles with temperatures that are below 1,000 K, or roughly 1,340° F. Though this temperature is relatively high compared to room temperature, it is well below the temperature of the electrons which may be in excess of 20,000 K. Plasmas which exhibit this disparity in temperatures are often called nonequilibrium or “low-temperature” plasmas.

Conversely, there exists another class of plasmas where the electrons, ions, and neutral particles are all at the same temperature. These are called thermal plasmas. Generally speaking, the closer the gas pressure is to atmosphere, the more thermal a plasma is owing to the rapid increase in the frequency of collisions between neutral and charged particles [9]. Additionally, the temperatures in a thermal plasma can be quite high and, in many cases, can easily melt all metals assuming that the total energy content of the plasma is high enough. For example, the arc of an arc welder is a thermal plasma. Similar high temperature plasmas, have a number of other applications which include a variety of high-intensity lamps, metal cutting, and surface coating.

There are, however, a number of applications which would benefit from operation at higher pressures, but with low-temperature ions and neutrals so as to avoid heat damage. This has spurred a substantial amount of research on nonequilibrium atmospheric-pressure plasmas (APPs) in recent years [10]. Ideally, such a plasma could be generated at or near atmospheric pressure with hot electrons, but minimal heating of surrounding gas. Though this field of research is still relatively young, it has produced a variety of new plasmas and capabilities. One of the more ubiquitous examples is use of plasmas to process the surface of plastics so that ink can adhere. Separately, nonequilibrium APPs are the technology which drives plasma televisions [11].

As mentioned, these applications promise to be the first of many for such plasmas. More recently, there have been innovative proposals to use these plasmas in water purification

[12], wound sterilization [13], improved combustion engines [14], nanoparticle production [15], and more. However, each situation has its own challenges when it comes to the design and development of a plasma source, particularly at these elevated pressures. Particularly problematic is the tendency of APPs to develop instabilities which can cause them to rapidly transition to thermal plasmas in a matter of nanoseconds.

There exist a few ways of getting around these instabilities. One example is the dielectric-barrier discharge which passively regulates the amount of power which can be deposited into the plasma [16]. Another example includes split-ring resonators which use natural feedback mechanisms to damp out potential instabilities [17]. The technique considered here, referred to as the repetitively-pulsed nanosecond discharge, or RPND, uses high voltage pulses which are so short that the instability does not have time to develop [18]. The RPND is a nonequilibrium plasma which can operate at pressures ranging from approximately  $10^{-3}$ –1 atmospheres [19]. At atmospheric pressure the RPND can produce a uniform plasma in volumes on the order of 10 mL [20]. As the pressure is reduced, the plasma volume can reach the order of liters [21].

The importance of large-area, uniform, high-pressure plasmas such as the RPND was highlighted in the National Academies' most recent decadal survey of plasma science [7]. However, there is still much that is not known about such plasmas. From the same survey, it is said that “the full promise of APPs will be known only if they can be understood and managed based on fundamental scientific principles at two extremes—the nanoscopic kinetic level, where selective chemistry occurs, and the global stability level.” It is this challenge, specifically the investigation of the nanoscopic kinetic level, which drives the research presented here.

### 1.1.2 History

Historically, the study of low-temperature APPs has been almost indistinguishable from the study of plasmas as a whole. However, this was not necessarily a matter of reasoned choice.

Plasma generation at atmospheric-pressure obviates the need for an effective vacuum pump. Additionally, prior to the creation of large battery banks, early sources of electrical energy had relatively small capacities. This precluded the generation of thermal atmospheric plasmas which required large amounts of energy.

Indeed, the requirements for a low-temperature APP are sufficiently rudimentary that the first man-made one (and likely the first man-made plasma), was probably a spark generated by rubbing fur against amber. This is commonly attributed to Thales of Milêus from around 600 B.C. Following Thales, electrical sparks came to intrigue many scientists including Gottfried Liebniz, Benjamin Franklin, and Charles Wheatstone. By the mid-1800s, Plücker, Geißler, and Hittorf began some of the first work on low-pressure plasmas though it was Crookes who would later identify plasma as a separate state of matter. Later, J.J. Thomson's discovery of the electron and discretized charge in 1897 marked the beginning of modern plasma research.

By this time, the necessary tools and techniques existed to create steady plasmas in pure, rarified gases. The behaviors of which were dominated by the motion and interaction of the charged electrons and ions. Critically, the effects of the neutral particles were negligible, thus isolating the electrical properties of the plasma. These carefully controlled systems were ideal for basic studies of plasma behavior and were used to great effect by individuals such as Lewi Tonks and Irving Langmuir [22]. In fact, many modern concepts in plasma physics can be traced back to their work.

In contrast, the pulsed APPs, characteristic of the earliest man-made plasmas [23], were easy to create, but notoriously difficult to work with. It could take them only a few nanoseconds to form, and less than a millisecond to decay away. For many years, there were simply no instruments capable of taking measurements this quickly. Furthermore, the neutral particles which were of no consequence in the low-pressure plasmas, could not be ignored. The neutral particles were present in such quantities that they could confound or obscure otherwise simple measurements.

As a consequence, there is still a great deal that is not known about pulsed APPs, particularly lightning, streamers, and a type of plasma which Thomson referred to as a “luminous front.” By the 1970s, this latter plasma had come to be called the fast ionization wave, or FIW [19]. It was generated by a single voltage pulse lasting around 100 nanoseconds and peaking at 10s or 100s of kilovolts. For the right pressure and gas, the FIW could fill volumes of nearly 40 L with a relatively uniform plasma, but with little heating of the gas.

These properties were attractive for a number of uses, but the FIW faced a number of implementation-related challenges. The switches used to trigger the FIW could only operate up to 100 times each second [24]. Unfortunately, the lifetime of a plasma at elevated pressures is relatively short, and the plasma generated by the FIW would decay away quickly after each pulse. This meant that the FIW-generated plasma had a relatively low duty cycle; the ratio of the time the plasma spends on to the time it spends off. This was disadvantageous for plasma-processing applications where low duty cycles are equivalent to long processing times. The low duty cycle also necessitated so-called preionization of the gas with UV lamps or a secondary plasma generator, adding to the cost and complexity of the system [3]. Finally, the pulse generators used for FIWs were not considered reliable enough for long operational lifetimes.

Recent advances in solid-state switching technology has largely solved these issues. At present, switches exist which can reliably operate 100,000 times a second; sufficiently fast that the plasma duty cycle approaches 100% [25]. This has the additional benefit of obviating the need for a preionization stage, as a sufficient number of electrons persist between pulses. The discharge produced by the use of these new switches is what we refer to as the RPND.

### 1.1.3 Questions

The large pedigree of pulsed plasma research belies the fact that they are still not well-understood. This remains especially true for RPNDs which present significant experimental challenges. A major component of this has to do with the time scales associated with the RPND. The formation of a RPND often requires no more than a few nanoseconds. Very sensitive equipment is required in order to measure changes which occur during this period. Unfortunately, such equipment is particularly susceptible to the broadband electronic noise generated by both real and displacement currents of the fast pulses. There is a plethora of other problems that can be traced back to topic of timing. For example, the length and insulators of detector cables can introduce substantial delays, and must be considered in order to synchronize different measurements.

Consequently, the majority of RPND studies focus on measurements after the discharge has occurred, when changes happen at a much slower rate. A great deal of information is available for this period of time, including chemical compositions, atomic densities, electron densities, gas temperatures, and more. While undoubtedly important, these measurements provide limited insight on what is happening *while* the plasma is forming. It is natural, then, to ask, what are the RPND plasma properties during formation?

Additionally, most studies have used a limited range of gases: oxygen, nitrogen, air, hydrogen, or some mixture thereof. The choice of these gases is deliberate and reflects specific applications in combustion and aerospace. However, the use of rare gases (such as helium) and rare gas mixtures has become popular because they provide for a wider range of stable operating conditions. Notably, it has been found that the unique internal electronic structure of rare gases can produce very different discharges. Given this, there is the question of how rare gas RPNDs compare to more conventional ones.

Finally, the persistence of the plasma between pulses makes the development of a RPND very different from a FIW.

Finally, though the RPND and FIW are qualitatively similar, there are some fundamental

differences between the two. These largely stem from the persistence of the plasma between pulses. It is this plasma which guarantees uniform breakdown in the case of RPND, while the FIW is largely dependent on very high energy electrons. At the same time, if the plasma is too dense at the beginning of the voltage pulse, it can limit the final density of the electrons and excited atoms. Because plasma-induced chemistry is a product of these particles, this pre-pulse plasma plays a decisive role in the number of reactions a RPND can produce. Therefore, one must ask how the properties of a RPND compare to those of a FIW and how they vary with the operating conditions.

#### **1.1.4 Approach**

The dissertation presented here represents efforts to either answer or provide a foundation to answer these questions. In order to develop the appropriate context for this work, the next section will be a comprehensive review of the RPND literature. It begins with the first reported pulsed APPs and concludes with contemporary studies.

The following two chapters set the basis for the experimental and numerical studies. Chapter 2 presents the theory necessary to understand RPNDs including streamer discharges, atomic spectroscopy, and collision processes. Subsequently, Chapter 3 describes the design of the helium RPND discharge apparatus used for the experimental studies and as the basis for the simulations. Also included in this chapter are several measurements of the basic discharge properties.

Chapters 4 through 5 provide more detailed measurements and analysis of the RPND dynamics. In Chapter 4, the measurements of the helium metastables in a RPND are presented and analyzed as a function of pressure and axial location in the discharge apparatus. Chapter 6 presents and analyzes similar measurements of the spontaneous plasma emissions. Finally, Chapter 5 discusses the development of a global model for a helium plasma and its use with the experimental data to infer the plasma properties of the RPND. The dissertation concludes with a summary of the results and suggestions for further avenues of

research.

## 1.2 Literature Review

RPNDs are only a recent invention which resulted from advances in fast-switching semiconductors. However, the physics of their formation is related to a much more broad category of plasmas which includes lightning, streamers, and even some transient phenomena in DC glows [26]. These plasmas are unique in that their spatial structure develops at speeds much faster than can be accounted for by the conventional Townsend mechanism. Loeb refers to this phenomena as “ionizing waves of potential gradient.”<sup>1</sup>.

### 1.2.1 Early History of Pulsed Discharges

In 1835 (as reported by Thomson [1]), Charles Wheatstone attempted to measure what he thought to be the speed of electricity in a six-foot long discharge tube of unspecified pressure [27]. It is now known that he was actually measuring the speed with which a plasma formed between the two electrodes. He accomplished this by the use of a rotating mirror which allowed him to see images of two sections of the tube, slightly displaced. The displacement between the images was proportional to the speed with which the plasma traveled between them. Wheatsone estimated this speed to be at least  $8 \times 10^7$  cm/s.

Interestingly, von Zahn later noted that this was *not* the speed of the emitting particles [28]. The visible light did cross the gap at an appreciable speed, but there was no detectable Doppler shift in the light emitted parallel to the propagation. As a result, it was concluded the light-emitting particles could not be traveling at the same speed as the light.

Later, Thomson revisited this work with an improved apparatus [1]. This included a tube that was now 15 m in length and five mm in diameter, as seen in figure 1.2. Also

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<sup>1</sup>It should be noted that the phrase wave does not indicate any kind of periodic motion or spatial arrangement. Simply put, it describes a boundary which separates ionized and unionized gas which travels from one electrode to another.

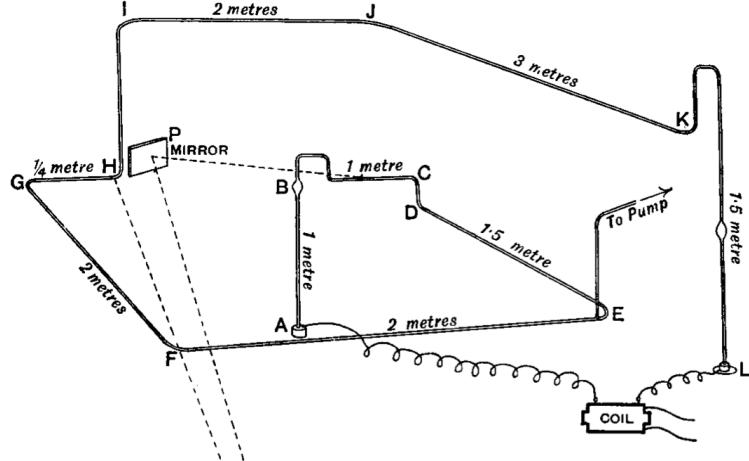


Figure 1.2: A sketch of J.J. Thomson’s early experiments on pulsed plasmas in long vacuum tubes [1].

using the rotating mirror apparatus, Thomson was able to greatly improve on the estimates of Wheatstone. He estimated that the so-called “luminous front” had a speed that was more than  $1.5 \times 10^{10}$  cm/s, or in excess of half of the speed of light. Furthermore, Thomson determined that the luminous front always appeared to travel from the positively pulsed electrode (anode) to the ground electrode (cathode).

The study of these luminous fronts was revisited by several researchers in the wake of Thomson [29–31], but their attempts to duplicate the measured speeds were met with varied success. In 1930, Beams confirmed definitively those of Thomson. He also found that the front always initiated at the electrode with the highest, absolute potential, relative to ground. Beams hypothesized that the rapid motion of the front was a result of a self-propagating region of high space charge, quote:

In the neighborhood of the electrode . . . the field is very high and intense ionization should take place. This ionization due to the large difference in mobilities of positive ions, negative ions and electrons respectively should result in the establishment of a space charge. This space charge, once formed near the high potential electrode . . . must move down the tube regardless of the polarity of the applied potential because of the changes it produces in the field near its edges.

At about the same time, Schonland and Collens reported on their observations of lightning [32]. Though the general structure and length scale of lightning is substantially different from the luminous fronts observed by Beams and Thomson, the two phenomena would later prove to be very similar. In their work Schonland and Collens noted that lightning would usually occur in a two-step process. Based on the images they obtained, they suggested that the leader was generated by a relatively small “dart” with a mean vertical velocity of  $7.2 \times 10^8$  cm/s. The dart moved in a random manner, changing directions at random intervals, but always moving toward the ground.

The second step began when this dart reached the ground. Once there, a bright return stroke would occur along the same path that the leader had traced out. In contrast to the leader stroke, the return stroke had a velocity of  $5 \times 10^9$  cm/s. Schonland and Collens hesitantly attributed the leader stroke to an extended electron avalanche, and the return stroke to thermal ionization along the conductive path generated by the dart. However, calculations by Cravath and Loeb showed that the speeds of the proposed avalanche was inconsistent with the fields at the head of a lightning stroke [33]. Instead, they suggested that the dart was actually a moving region of space charge which locally accelerated electrons to ionizing energies. This was similar to the mechanism earlier proposed by Beams.

### 1.2.2 The Streamer Model

It was long known that sparks in air were similar to lightning. Advances in technology during the 1930’s led to experiments which reinforced this similarity. In response to the measurements of Schonland and Collens; Snoddy, Beams, and Dietrich studied the breakdown of gas in a long tube with both positive and negative applied potentials [34]. Using an oscilloscope, they observed both the leader and a return stroke in both cases. However, the propagation of the plasma wave toward the cathode required a source electrons ahead of the wave. The authors proposed that photoionization might provide these necessary electrons.

Around the same time, Flegler and Raether had come to a similar conclusion regarding

the importance of photoionization. This led them to develop a more thorough theoretical model for these waves [35] which came to be known as the streamer theory. This was followed by a similar treatment by Loeb and Meek [36–38]. The streamer theory divided the initial plasma formation into two steps. In the first step, an electron avalanche is initiated between two electrodes. The avalanche travels toward the anode and leaves behind a region of positive space charge. In the second step, the return stroke begins at the anode and travels along the conductive path generated by the initial avalanche toward the cathode.

The streamer model proved relatively successful in describing the development of sparks and lightning. Theoretical estimates of the speed matched the velocity measurements that were acquired with photographs and oscillographs. Additionally, the theory was able to account for the branching manner in which lightning was formed as well as the constriction in space.

Following the initial work of Flegler, Raether, Loeb, and Meek, a number of researchers began to explore the boundary between the Townsend mechanism and the streamer mechanism. Most notable was Fisher and Bederson’s work in 1951 [39], which was later extended to nitrogen [40] and argon [41]. These studies suggested that the streamer theory was incomplete. Furthermore, the reliance of the streamer theory on photoionization would later prove very contentious [42]. Finally, there was a whole class of discharges that it did not readily explain.

### 1.2.3 Diffuse Streamers

As noted by Chalmers [43], Rogowski and Buss [44, 45] observed a fast, diffuse, glow discharge immediately prior to the filaments of a streamer discharge. Allibone and Meek, noted similar diffuse discharges in air based on oscillographs and photographs [46–48]. However, the Boys apparatus [49] which was employed in these studies (an ancestor to the modern streak camera) was unable to capture the evolution of the diffuse glow, given its large spatial extent.

This was first noted by Allibone who attempted to use Lichtenberg figures<sup>2</sup> to definitively capture this diffuse glow [50]. Later, Saxe and Meek used the recently invented photomultiplier tube to record the evolution of the light emissions in the brief, diffuse glow [51] as a function of space. Both studies agreed in the existence of the diffuse glow, despite some disagreement on the nature of its geometry and propagation.

By 1968 (according to Kunhardt and Byszewski [4]), Stankevich and Kalinin had provided the most firm evidence yet of a diffuse discharge in a dense gas [52]. This was later confirmed by experiments with a pulsed nanosecond discharge by Mesyats, Bychkov, and Kremnev [53]. In their analysis, they concluded that photoionization could not play a role in such short-lived discharges. The formation of their discharge only required several nanoseconds, much shorter than the lifetimes of the excited states responsible for photon emission. They suggested that the streamer model required some extension.

In addition to the diffuse discharge, Stankevich and Kalinin also noted the detection of x-rays with each pulse. This suggested the presence of high-energy electrons impinging on the surface of the electrodes, despite the high collisionality of the dense gas. Not only that, but the electron energies could even exceed what would be expected from the vacuum electric fields [54]. The eventual conclusion was that the electric field associated with the space charge at the head of the streamer produced very energetic electrons which deposited their energy far from the streamer tip [4,55], allowing the streamer to spread out beyond the diffusive region of the electrons.

It was based on the studies of the fast electrons in these discharges that Mesyats, Bychov, and Kremnev proposed the use of a fast electron beam for pumping high-pressure gas lasers. Similar work was conducted simultaneously by Fenstermacher et al. [56]. Palmer [57], and Levatter and Lin [3] determined that there was a threshold amount of preionization required to ensure homogeneity of the discharge. Hunter [58], and Koval'chuk and Mesyats [59] later proposed that such discharges be used for fast-closing switches. Gas lasers and fast

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<sup>2</sup>Such figures directly exposed photographic emulsions to the electrical discharge. The developed image was a time-integrated representation of the discharge.

switches would drive much of the later research on fast, pulsed discharges.

Eventually these discharges came to be referred to as fast ionization waves (FIWs). A large body of Russian literature developed around their study, though much of it has remained untranslated. In 1994, Vasilyak produced an extensive review of these studies [19]. The data include wave velocities for a variety of gases and pressures. Other parameters such as attenuation coefficients for the waves, high energy electron currents, electric field measurements, and a circuit model of the FIW are also included.

#### **1.2.4 Repetitively-Pulsed Nanosecond Discharges**

The type of discharge originally studied by Babich, Loika, and Tarasova came to be known as the fast ionization wave (FIW). In the years following its discovery, a substantial effort was made to document the properties of the FIW over a wide range of conditions. In these studies, the wave velocity, current, and attenuation were the most frequently measured quantities. Much of this work is summarized in a review by Vasilyak [19]. Also reviewed are Slavin and Sopin's work which was the first to attempt a computation of the electron energy distribution function EEDF in FIWs [60].

The experimental measurements and computational work reported by Vasilyak were expanded on by a series of studies conducted at the Moscow Institute of Physics. These are reviewed by Starikovskaia et al. [24] and included measurements of the electron density, electric field, and energy coupling for FIWs in air, nitrogen, and hydrogen. The computational work by Starikoskaia and Starikovskii [61] still represents the most detailed study of the EEDF in nitrogen FIWs.

However, Starikovskaia et al. noted that the usefulness of FIWs were limited, in part, by their repetition rates. The power supplies for FIWs were capacitor banks, charged in parallel, and discharged in series (also referred to Marx banks). Unfortunately, the spark gaps used to trigger these capacitor banks would not operate above a few hundred Hz. This changed in the late 1990's with the development and commercialization of fast, solid-state

switches. Specifically, with the fast ionization dynistor it was possible to achieve repetition rates of 100 kHz [25].

This led to a new class of repetitively-pulsed discharges, or the RPND. These discharges operated at sufficiently high rates such that the electrons and ions would persist in significant quantities between pulses. This meant that the plasma duty cycle was increased by a significant amount. These improved qualities of the RPND over the FIW inspired a number of novel, application-driven studies. This included:

- Plasma-assisted combustion [18, 62, 63]
- Magnetohydrodynamic energy bypass engines [18, 64, 65]
- Plasma actuators [66, 67]
- High-pressure xenon lamps [68]
- Plasma medicine [13, 69]
- Water treatment [70]

Though not specific to the RPND, Becker et al. [10] provide an extensive discussion of the potential uses for non-equilibrium air plasmas.

As a result, contemporary researchers have produced a wealth of literature on the operation of RPNDs. More recently, there have been detailed measurements of the gas temperatures [62, 71–77], chemical composition [73–75], electric fields [78–80], and energy coupling [62, 81]. Notably, these studies have been generally restricted to molecular gases; air, nitrogen, and occasionally, hydrogen.

The first such study was the work of Laroussi and Lu who examined a RPND excited in a stream of helium flowing from a tube into air [82, 83]. The resulting plasma had the appearance of a jet, emitted from the open end of the tube. Using fast photography they observed that the jet was actually a series of plasma “bullets” formed with each pulse. Measurements of the bullet velocities showed that their speed greatly exceed what would be expected purely from electrons drifting under the applied electric field. They described the bullet as a classic cathode-directed streamer propagated by photoionization.

The plasma bullets of Laroussi and Lu spawned a great deal of interest in RPND helium plasma jets<sup>3</sup> For example, Walsh et al. studied the atomic oxygen production for helium-oxygen mixtures with the use of emission spectroscopy and a global plasma chemistry model [84]. Urabe et al. employed a variety of laser diagnostics to measure the radial density profiles of helium metastable atoms and molecular nitrogen ions in a similar jet. This work was supported by a number of two-dimensional plasma simulations such as those by Naidis [85] and Breden, Miki, and Raja [86].

Simultaneously, there has been a decline in the study of FIWs, and relatively little on large-volume RPNDs. One of the most recent FIW studies was produced by Takashima et al. [87]. In it, the authors reported on FIWs in helium and nitrogen which were studied using capacitive probes and voltage-current characteristics. The results were compared to extensive two-dimensional fluid simulations and an analytic, one-dimensional drift model. In most cases, the measurements and simulations showed good agreement.

### 1.3 Summary

Contemporary RPND studies have mostly focused on measurements in the afterglow plasma or of time-integrated quantities. This has limited the understanding of how RPNDs develop as only so much can be inferred from these measurements. Particular issues, such as the electron energetics in the wave front are not firmly known. Relatedly, the relative importance of photoionization and nonlocal electrons is still under debate. Even measurements of common plasma parameters such as electron densities and temperatures are in short supply. Each of these issues is important in the development of a thorough theoretical understanding of RPNDs, as well as the validation of simulations, and optimization for real world applications.

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<sup>3</sup>A distinction should be made between plasma jets, excited by sinusoidal power supplies, similar to the well-known dielectric-barrier discharge [16], and those produced by nanosecond pulses. Differences between the two were reported by Walsh, Shi, and Kong [20].

Relatedly, the study of RPNDs has generally been limited to molecular gases such as air, nitrogen, oxygen, or combustion-related mixtures. Consequently, little information has been published on rare gas RPNDs, in spite of the fact that their unique physics makes them ideal for certain uses. For example, rare gas discharges exhibit very little gas heating, making them desirable for the treatment of highly sensitive materials. Additionally, the radiative emissions of rare gases have a range of uses from commercial lighting to gas lasers. Finally, the large degree of Penning ionization resulting from rare gases may make them useful in RPND gas mixtures as a means of optimizing discharge properties.

In order to address these issues, this work will use a combination of experiments and modeling to examine the plasma dynamics of a helium RPND on time scales ranging from 5 ns to 100  $\mu$ s and at pressures from 0.3 to 16.0 Torr. The nanosecond time scale results will be one of a very few datasets available on the evolution of the RPND during its formation. This will provide new insight on the dominant physical processes in the wave front. To complement this, the microsecond time scale measurements will reveal the dominant loss mechanisms in between pulses as well as the time-averaged characteristics of the RPND. Lastly, the parameterization with pressure will offer the chance to examine how the physics of the discharge is altered by the collisionality.

Experimentally, the RPND will be studied by its current and voltage characteristics, optical emissions, and with laser absorption spectroscopy. The current and voltage characteristics will be used to determine the energy absorbed by the plasma with each pulse. The optical emissions will provide information about the excited state dynamics and the wave velocity. Finally, the laser absorption spectroscopy will be used to resolve the short time scale dynamics and as a benchmark for the numerical modeling. The modeling will focus on the development of a detailed global model of a helium discharge. This model will be informed by additional particle-in-cell simulations, and solutions of the Boltzmann equation. Using the metastable measurements as a baseline, the global model will be used to predict the electric field, electron temperature, electron density, excited state densities, and

emissions of the RPND.

## CHAPTER 2

# Theory

In order to properly understand the RPND—the experimental measurements, and the models, it is necessary to develop a theoretical underpinning. The RPND is an ionized gas, and, dependent on its characteristics, a plasma. Therefore, we begin with a review of the statistical description of an ionized gas, equilibrium solutions, and several approximations. Subsequently, the discharge initiation process is considered from the perspective of a single avalanche. The Townsend model is briefly reviewed, followed by a more detailed explanation of the streamer model. This naturally leads to the development of a homogeneous discharge condition based on the preionization density—the basis for the RPND. Following this, a qualitative introduction to atomic structure is provided in order to introduce spectroscopic concepts such as energy levels, transitions, lineshapes, and absorption cross sections.

### 2.1 Ionized Gas

An ionized gas is a volume of gas in which some fraction of the neutral atoms and/or molecules have been separated into electron and ion pairs. For a sufficiently large number of particles and collision rate, the behavior of each species in the ionized gas can be described by a continuous distribution function.

This function is an expression of the likelihood of finding a particle within a specific range of velocities in a specific volume, as a function of time. This function is denoted as

$f_\alpha(\vec{r}, \vec{v}, t)$ , where the subscript  $\alpha$  denotes the species,  $f$  is the distribution function,  $\vec{r}$  is the position,  $\vec{v}$  is the velocity, and  $t$  is the time.

The behavior of  $f_\alpha$  can be shown [88] to be governed by the Boltzmann equation,

$$\frac{\partial f_\alpha}{\partial t} + \vec{v} \cdot \nabla f_\alpha + \frac{q_\alpha}{m_\alpha} (\vec{E} + \vec{v} \times \vec{B}) \cdot \nabla_v f_\alpha = \left( \frac{\partial f_\alpha}{\partial t} \right)_{\text{coll}}. \quad (2.1)$$

Here,  $m$  is the particle mass,  $q$  is its charge,  $\vec{E}$  is the electric field,  $\vec{B}$  is the magnetic field, and  $(\partial f_\alpha / \partial t)_{\text{coll}}$  is a term which represents changes to the distribution function as a result of collisions. Coupled with Maxwell's equations, equation 2.1 provides a complete description of the behavior of the fields and particles in a plasma.

For a species in equilibrium in the absence of external forces and  $(\partial f_\alpha / \partial t)_{\text{coll}} = 0$ , it can be shown [89] that the distribution of energies is

$$f_\alpha(\epsilon) = C \epsilon^{1/2} \exp\left(-\frac{\epsilon}{k_B T_\alpha}\right) \quad (2.2)$$

where  $C$  is a normalizing constant,  $\epsilon$  is the energy,  $k_B$  is Boltzmann's constant, and  $T_\alpha$  is the temperature of the species. This is referred to as the Maxwell-Boltzmann distribution. It should be emphasized that this solution only applies when the classical species can be considered to be in equilibrium. Gradients and electromagnetic fields can both significantly alter the distribution function of a species. This can be of particular importance in the calculation or reaction rates, or the measurement of temperatures.

Additionally, the Boltzmann equation may be solved for electrons in equilibrium constant electric field, provided that a constant current density, and only elastic collisions. This is generally valid if the electric field strength is sufficiently small such that the mean energy of the electrons does not become comparable to the threshold energies for inelastic collisions. This result was originally presented by Druyvesteyn and Penning [89] and has come

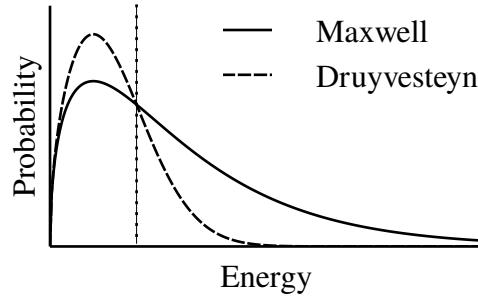


Figure 2.1: Comparison of the Maxwell-Boltzmann energy distribution and the Druyvesteyn distribution for the same average energy (illustrated by the dotted line).

to be known as the Druyvesteyn distribution. It is defined as,

$$f_\alpha(\varepsilon) = C \varepsilon^{1/2} \exp\left(-\frac{\varepsilon^2}{\langle \varepsilon \rangle^2}\right) \quad (2.3)$$

where  $\langle \varepsilon \rangle$  is some mean energy, determined by the gas properties. This solution tends to suppress the probability of higher and lower-energy electrons in favor of more intermediate values. Figure 2.1 compares the probability distributions from equations 2.2 and 2.3 for the same temperature  $T_\alpha$ . The dotted line illustrates the average energy for the two distributions, which is not the same as the most probable energy.

Additional solutions of equation 2.1 in anything but these simple cases can be very challenging (c.f. Chapter 18 of [90]). Even computational approaches can be stymied by the seven-dimension phase space and high dynamic range. In most situations, the Boltzmann equation is reduced to more tenable expressions by integrating over velocity-space (leaving  $f$  as a function of space and time). The first so-called moment is the conservation equation or continuity equation [90],

$$\frac{\partial n_\alpha}{\partial t} + \nabla \cdot (n_\alpha \vec{u}_\alpha) = G_\alpha - L_\alpha. \quad (2.4)$$

In this case, there is now a mean velocity  $\vec{u}$ , as well as gain ( $G$ ) and loss ( $L$ ) terms which

replace the collision operator. The gain and loss terms are generally expressed as the product of the densities of the interacting species, and a rate coefficient. For an electron-impact interaction where the target is relatively stationary, the rate coefficient is

$$K = \int_0^\infty f_e(\varepsilon) \sigma(\varepsilon) \sqrt{\frac{2\varepsilon}{m_e}} d\varepsilon, \quad (2.5)$$

where  $\sigma$  is the energy-dependent cross section.

The definition of the mean velocity,  $\vec{u}$  can be obtained by multiplying equation 2.1 by  $v$  and integrating over velocity-space, to obtain the second moment [90],

$$m_\alpha n_\alpha \left[ \frac{\partial \vec{u}_\alpha}{\partial t} + (\vec{u}_\alpha \cdot \nabla) \vec{u}_\alpha \right] = q_\alpha n_\alpha (\vec{E} + \vec{u}_\alpha \times \vec{B}) - \nabla \cdot \vec{\Pi} + \vec{f}_{\text{coll}}. \quad (2.6)$$

This expresses the conservation of momentum by the plasma. It provides a means by which to solve for the mean velocity of the system, however it also introduces two additional terms.  $\vec{f}_{\text{coll}}$  deals with the forces transferred to  $\alpha$  via collisions. This is often approximated as the Krook collision operator, which is only dependent on known quantities:  $m$ ,  $n$ ,  $\vec{u}$ ,  $G$ ,  $L$ , and the momentum transfer frequency,  $\nu_m$ , for the species  $\alpha$  and all species it interacts with. The second term,  $\vec{\Pi}$ , is the pressure tensor and can only be defined by the third moment of the Boltzmann equation. In fact, each additional moment introduces a new term requiring a higher order moment, *ad infinitum*. In most situations, this chain of equations is terminated after the first two or three moments by the use of an additional assumption such as an equation of state. One common example of an equation of state is the isothermal relation,  $p = nk_B T$ , which can be used to remove the pressure tensor.

For the purposes of this paper, one more moment will suffice. Assuming that the pressure is isotropic, one can multiply equation 2.1 by  $mv^2/2$ , and integrate over velocity-space to find the energy conservation equation,

$$\frac{\partial}{\partial t} \left( \frac{3}{2} p_\alpha \right) + \nabla \cdot \frac{3}{2} (p_\alpha \vec{u}_\alpha) + p_\alpha \nabla \cdot \vec{u}_\alpha + \nabla \cdot \vec{q}_\alpha = \frac{\partial}{\partial t} \left( \frac{3}{2} p_\alpha \right) \Big|_{\text{coll}}. \quad (2.7)$$

In this case,  $p$  represents the isotropic pressure, and  $\vec{q}$  is the heat flow. The first term on the LHS represents the total energy contained by the species, the second term is the energy flux in and out of the volume, and the third term accounts for changes due to compression or expansion. The RHS is the collision operator which describes energy added or removed from the system as a result of collisions.

Equations 2.4 and 2.7 are particularly important for this study. As will be detailed in Chapter 5, the two can be used to create a global model of the plasma. Such a model assumes spatial homogeneity of the plasma in order to reduce the associated computational costs. This allows the model to address large numbers of species over long periods of time as will be required in the case of the RPND.

## 2.2 Plasma Criteria

Though the Boltzmann equation describes both an ionized gas and a plasma, the two are distinct as a plasma is necessarily an ionized gas, but not vice versa. A plasma is unique in that its dynamics are governed by long range electromagnetic forces, unlike gases in which short-range collisions dominate. As a result, plasmas frequently exhibit large scale structure and organization. Examples of these structures are ubiquitous in astronomy where phenomena such as the aurora borealis, coronal mass ejections, and even interstellar media are all plasmas [91]. There are three criteria which form a more exact definition of what constitutes a plasma.

### 2.2.1 Debye Length

If an electrical perturbation is introduced into an ionized gas, the charged particles will tend to rearrange themselves to shield it out. A plasma is an ionized gas which is large enough for this shielding effect to occur. The characteristic length scale for this shielding effect to take place is referred to as the Debye length, denoted  $\lambda_D$ . It can be shown to be equal to

$\sqrt{\epsilon_0 T_e / (en_0)}$ , where  $\epsilon_0$  is the vacuum permittivity,  $T_e$  is the electron temperature, and  $n_0$  is the plasma density. If the characteristic length scale of the ionized gas is  $L$ , then  $\lambda_D < L$  for it to be considered a plasma.

## 2.2.2 Debye Sphere

However, the above condition by itself is not sufficient for shielding to occur. It is possible that an ionized gas may have a relatively small Debye length, but also lack enough charged particles for shielding to occur. More simply put, it would be impossible for a single electron to shield out even the smallest of perturbations. For that reason, the number of particles in a Debye sphere must be greater than unity in a plasma, or  $n_0(4\pi\lambda_D^3/3) \gg 1$ .<sup>1</sup>

## 2.2.3 Plasma Oscillations

Finally, a plasma may exhibit Debye shielding, but lack the collective behavior of a plasma. This can occur when the collision frequency with neutral particles is too high. In this case, the behavior of the ionized gas would be determined more by the random collisions. Therefore, the characteristic response frequency of a plasma, commonly called the plasma frequency, must be greater than the neutral collision frequency, or  $\omega_p > \nu$ . The plasma frequency can be shown to be  $\omega_p = \sqrt{e^2 n_0 / (\epsilon_0 m_e)}$ .

There are many natural and man-made plasmas of varying size and quality. Figure 2.2 shows several categories of plasma, plotted as a function of their electron density and temperature. As can be seen in this example, the electron densities span seven decades, and the densities cover in excess of 20. This broad range of conditions presents a particularly challenging problem for both simulations and experimental measurements. Also highlighted in the figure is the range spanned by the RPND.

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<sup>1</sup>This condition is also implied in the derivation of the Debye length.

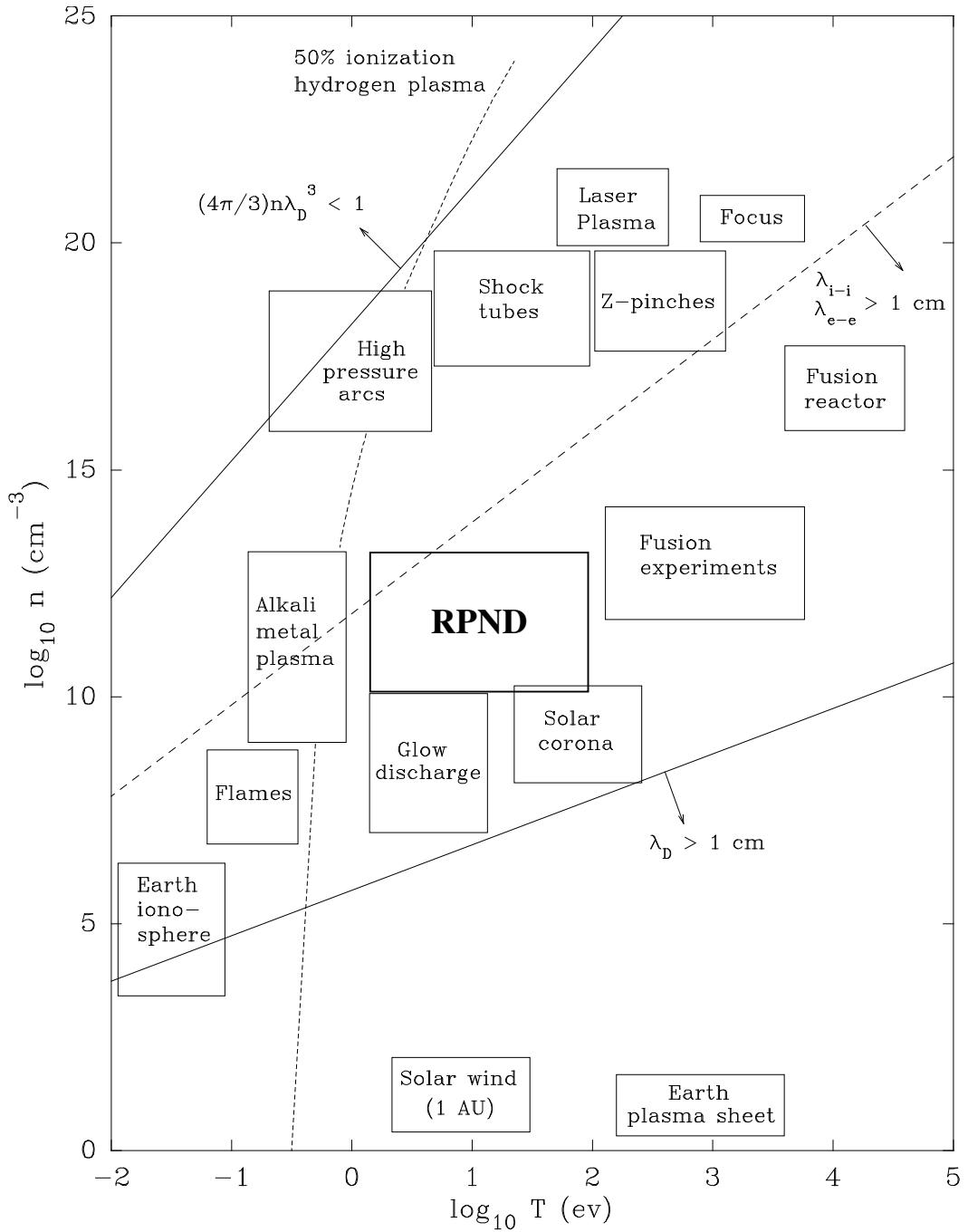


Figure 2.2: Illustration of the various regimes of plasma in terms of electron temperature and density with the RPND regime highlighted, adapted from [2].

## 2.3 Discharge Initiation

The Boltzmann equation is a continuous, statistical description of a plasma. By comparison, the initial breakdown of a plasma is a highly discontinuous process marked by its stochasticity. The initiation of a discharge is typically the result of electron avalanches which occur randomly throughout a volume of gas [89]. Often, the seed electrons for a plasma are the products of ionizing cosmic rays. At sea level this results in a few electrons per cubic-centimeter. As a result, it is necessary to consider the initiation of a discharge separately from a pre-existing plasma.

### 2.3.1 Townsend Mechanism

Classically, plasmas are created by two different mechanisms, the applicability of which depends on primarily on the strength of the electric field relative to the neutral gas density, a value called the reduced electric field [92]. At lower reduced fields, the Townsend mechanism is responsible for the formation of a plasma. Consider two electrodes separated by a gap filled with some gas. An electron starting near the cathode will drift toward the anode. For a large enough electric field, the electron will gain sufficient kinetic energy to ionize a neutral atom, producing a second electron. The two electrons are now accelerated by the field, instigating further ionization of the background gas. The population of electrons quickly grows, thus the process is referred to as an electron avalanche. Eventually, the avalanche electrons are collected at the anode.

In their wake are ions which slowly drift toward the cathode. As the ions impact the surface of the cathode, they occasionally cause a secondary electron to be emitted. This secondary electron initiates a new avalanche and helps to sustain the discharge. A steady state electric discharge occurs when the current of the ion collection at the cathode matches the current of the electron collection at the anode. The time scale of the Townsend discharge is usually determined by the positive ions, as their large mass results in slow drift velocities.

For an electric field of 50 V/cm at 200 mTorr, the drift velocity of a helium ion in helium is about  $7 \times 10^4$  cm/s [93]. For a gap of 10 cm, this gives a drift time on the order of 10–4 s.

The Townsend mechanism is characterized by two parameters:  $\alpha$  and  $\gamma$ , the first and second Townsend coefficients.  $\alpha$  is the number of ionization events that occur per unit length, often expressed as a function of the reduced field [89]. The second Townsend coefficient is the probability that an ion impinging on the cathode produces a secondary electron. The values for  $\gamma$  can vary widely and depends on the type of ion, its energy, the cathode material, contamination of the surface, and many other factors. That said, typical values are around 0.01-0.1 [90].

### 2.3.2 Streamer Mechanism

In contrast, the streamer discharge which occurs for larger values of the reduced field does not depend on secondary emission. Additionally, streamer discharges can develop in time periods as short as 1 ns, much less than the time required for Townsend breakdown. In order to describe the streamer mechanism, again consider an electron between two electrodes, as seen in (a) of figure 2.3. As with the Townsend discharge, this electron initiates an avalanche which moves toward the anode. As the electrons travel toward the anode, they randomly collide and diffuse, leaving behind a cone of ions, as seen in part (b). However, the higher reduced field drastically increases  $\alpha$ . This causes the space charge of the avalanche to create an electric field comparable to the one that is applied, slowing the propagation of the avalanche.

At this point the avalanche can be considered a streamer as it begins to increase its extent by several additional processes. The large internal fields of the avalanche can accelerate individual electrons and “inject” them in the direction of the anode [4]. In addition, as the excited atoms in the wake of the avalanche begin to radiate, they can cause photoionization throughout the volume. Photoelectrons generated close enough to the negative head, or positive tail of the streamer will initiate secondary avalanches which eventually connect

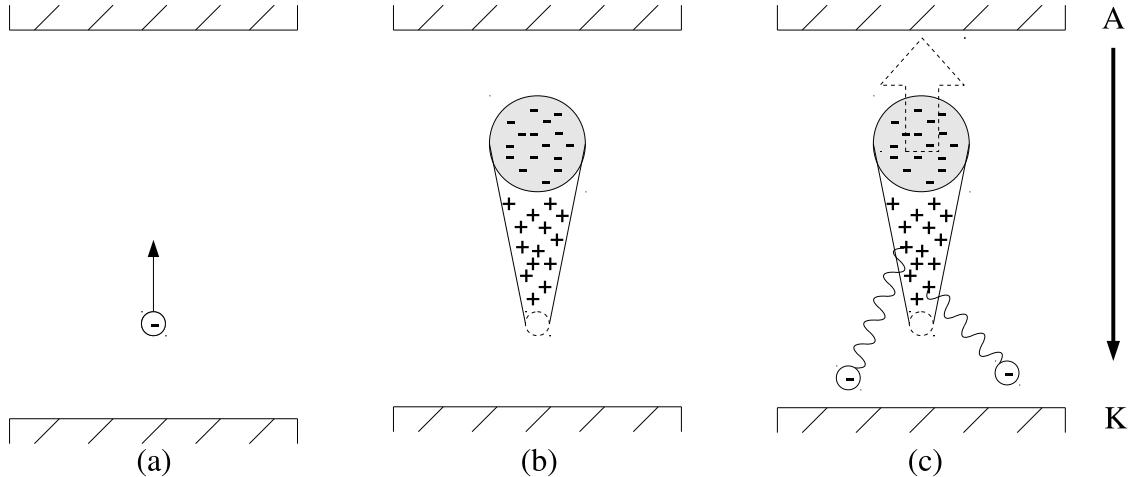


Figure 2.3: An illustration of the development of a single streamer. (a) A seed electron is accelerated by the applied electric field. (b) The initial electron develops into an avalanche which leaves a large region of positive space charge, slowing further advance. (c) The streamer propagates toward the cathode via photoionization and the anode via nonlocal electrons and photoionization. Adapted from [3] and [4].

to the primary one. While photoelectrons may cause some additional broadening of the streamer, the injection of electrons toward the anode is aligned with the direction of the internal field of the avalanche. As a result, the ionization caused by these electrons do not appreciably increase the radius of the streamer.

### 2.3.3 Homogeneity Condition

However, these processes are not critical in the formation of a large-volume discharge by an RPND. This description of a streamer only considers an avalanche generated by a single electron. In reality, many can form simultaneously assuming that there is more than one seed electron in the volume. With moderate preionization of the volume, the strong fields of the individual avalanches can begin to overlap<sup>2</sup>. This smoothes out the field gradients which would otherwise radially constrict the streamers. Instead, ionization progresses homogeneously throughout the volume.

In order to determine the necessary preionization density, we refer to the work done by

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<sup>2</sup>If the preionization of the volume is too large, it can effectively short out the electric field.

Levatter and Lin on gas laser discharges [3]. First, the electron drift velocity in an applied field can be expressed as the product of the field and the electron mobility  $\mu$ . The electron mobility multiplied by the electric field is the steady-state drift velocity for an electron in that field and represents the balance between the frictional force of the neutral gas collisions and the electric field. Consequently, the mean velocity of electrons drifting in a time-varying field  $E(t)$  can be expressed as

$$u(t) = \mu(E)E(t). \quad (2.8)$$

The length of the avalanche can be written as a time-integrated function of the electron drift velocity,

$$\xi = \int_{t_0}^t u(t)dt. \quad (2.9)$$

Here,  $t_0$  is the time at which  $E(t)$  becomes high enough that the first Townsend coefficient,  $\alpha$ , exceeds 0. Because no electron multiplication occurs while  $\alpha < 0$ , this effectively represents the beginning of the avalanche.

The electric field in the head of the avalanche depends on its radius, which is dependent on the diffusion of the electrons as they cross the gap. This is governed by the free diffusion coefficient,  $D$ . For a fixed diffusion constant, the final avalanche radius would simply be  $R = \sqrt{2D\Delta t}$ , where  $\Delta t$  is the time after breakdown. As the diffusion coefficient typically varies with the applied electric field, the final avalanche radius will be assumed to be equal to  $R = \sqrt{2\bar{D}\Delta t}$ , where  $\bar{D}$  is the time-averaged diffusion coefficient.

Levatter and Lin assume that the avalanche slows when the peak field of the avalanche is equal to the applied field. Assuming that the electrons diffuse equally in all directions, the electric field of the avalanche head can be expressed as

$$E_a(r) = \frac{eN_e}{4\pi\epsilon_0 R^2} F(r/R), \quad \text{where} \quad (2.10)$$

$$F(r/R) = \frac{1}{R^2} \left[ \operatorname{erf}(r/R) - \frac{2}{\pi^{1/2}} (r/R) \exp(-r^2/R^2) \right], \quad (2.11)$$

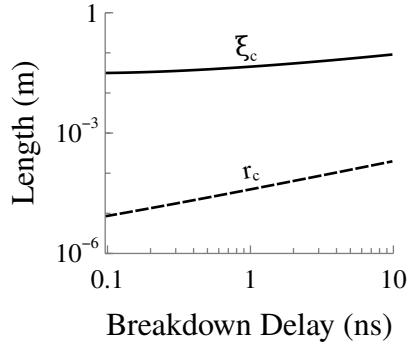


Figure 2.4: Numerical calculations of the avalanche length and avalanche radius for in helium at a pressure of 4.0 Torr as a function of the slope of the electric field,  $dE/dt$ .

where  $r$  is the radius with respect to the center of the avalanche,  $N_e$  is the number of electrons in the avalanche,  $\text{erf}$  is the error function.  $F$  is a dimensionless function which has a peak value of 0.428. Provided  $\alpha$  as a function of reduced field, the number of electrons in the avalanche is equal to

$$N_e = \int_0^\xi \alpha(\xi') d\xi'. \quad (2.12)$$

Here, Levatter and Lin make a number of assumptions in order to develop an analytic and dimensionless solution for  $E_{a,\max}(t) = E(t)$ . However, it is possible to numerically integrate equations 2.9 and 2.12 to determine the time required for the avalanche to slow. This should provide a more accurate, but less general result. Assuming a linearly increasing electric field, figure 2.4 shows the results of such calculations for an avalanche in 4.0 Torr of helium, as a function of various breakdown delays. The breakdown delay is defined as the time it takes for  $\alpha > 0$ . The mobilities, diffusion coefficients, and Townsend coefficients were interpolated from solutions of the Boltzmann equation provided by the BOLSIG+ code with Phelps' cross sections [94]. For this range of breakdown delays, the avalanche was able to develop up to nearly 10 cm in length before it slowed. The times required for the avalanche to slow ranged from around 23 ns for the shortest breakdown delay, and 389 ns for the longest.

From this, a criteria for homogeneous breakdown of the gas can be developed. In order

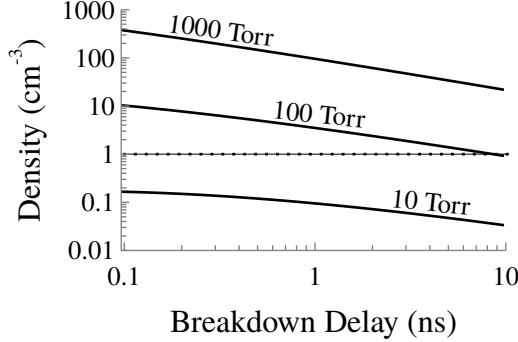


Figure 2.5: Minimum preionization densities required at a variety of pressures and breakdown delays. The dotted line indicates the background ionization level as a result of cosmic radiation.

for the field gradients to be smoothed out, the individual avalanche heads should roughly overlap by the time they have slowed. Assuming that all seed electrons in the volume initiate avalanches, this can be approximated as  $n_{e,c} > r_c^{-3}$ , where  $n_{e,c}$  is the critical electron density, and  $r_c$  is the avalanche radius when it has slowed. As seen in figure 2.5, the required preionization density depends on both the breakdown delay and the operating pressure. Generally, the preionization density increases with pressure and decreases with breakdown delay. The dotted line in the figure indicates the anticipated background electron density from cosmic radiation. This suggests that, for the breakdown delays in question, the discharge will almost always be homogeneous at pressures below 100 Torr. While the plot suggests that large values of  $dE/dt$  might guarantee homogeneous breakdown at near-atmospheric pressure, the increasing likelihood of ionization instabilities [95] will preclude homogeneous discharge development.

## 2.4 Atomic Spectroscopy & Notation

As described, much of the experimental work presented will concern the use of spectroscopic techniques. Careful measurements of the light emitted from excited atomic states can yield electron densities and temperatures, excited state densities and temperatures, elec-

tric fields, and magnetic fields [96]. The topic of spectroscopy is extensive and it is neither necessary nor desirable to cover it in full. Instead we will only consider what is necessary to understand the emissions from a singly-excited, multi-electron atom.

An atom is composed of a small, positively charged nucleus, orbited by negatively charged electrons. The actual position of any single electron is probabilistic and described by a wavefunction—solutions of the Schrödinger equation for the atom in question. Each wavefunction is associated with a number of eigenvalues which quantize aspects of the state of bound electrons. In simple atoms, four such quantum numbers are of interest [97],

- $n = 1, 2, \dots$ : the principal quantum number,
- $l = 0, 1, \dots, n - 1$ : the orbital angular momentum number,
- $m_l = -l, \dots, l$ : the projection of  $l$ , and
- $m_s = \pm 1/2$ : the projection of the spin quantum number.

The quantum numbers are hierarchical such that each  $n$ , or shell, possesses a series of subshells,  $l$ , while each subshell possesses a number of individual orbital,  $m_l$ , and each orbital possess one of two spins. As a result of the Pauli exclusion principle, the wavefunction of each electron around an atom is described by a *unique* set of quantum numbers. This means, that any particular subshell can only contain  $2(2l + 1)$  electrons. The subshells are often referred to using the nomenclature  $0, 1, 2, 3, \dots = s, p, d, f, \dots$

As a result of their separation from the nucleus, the electrons in an atom possess some degree of potential energy. As the  $n$  and  $l$  of an electron increase, so does its potential energy. In the absence of electric and magnetic fields,  $m_l$  and  $s$  do not affect the potential energy of an electron. As an example, an electron in the  $1s$  ( $n = 1$  and  $l = 0$ ) subshell has the lowest possible potential energy.

Absent from external influences, the individual states are populated with electrons so as to minimize the total potential energy of the system. This natural arrangement is referred to as the ground state configuration. Often, but not always, the subshells are filled sequentially and in order from lowest to highest  $l$  [97]. Provided some input energy in the form of a

collision or a photon, one or more of the electrons surrounding the atom may transition to another state, increasing the potential energy of the system. In low-temperature plasmas it usually one of the electrons from the outermost or partially filled subshell to be excited.

The potential energies of the electron configurations for multi-electron atoms are determined by the collective effects of all the surrounding electrons.

It is the collective effects of all electrons surrounding an atom which determine its potential energy. This results in a single set of total angular momenta which can be used to describe the atom. In lighter atoms [97], the contributions of the individual electrons are combined assuming a condition called L-S coupling. Under this assumption, the total angular momentum of the atom can written as  $\vec{L} = \sum \vec{l}_i$ , where  $i$  is each electron in a partially filled subshell (filled subshells sum to zero). Likewise, the total spin can be written as  $\vec{S} = \sum \vec{s}_i$ . These can be combined to form the total angular momentum of the atom,  $\vec{J} = \vec{L} + \vec{S}$ . Finally, the each atom is said to have an even or odd parity, defined as  $(-1)^{\sum l_i}$ , where  $-1$  is odd, and  $1$  is even.

These quantities can be used to write a “term symbol” for the atom, of the form  $^{2S+1}L_J^p$ , where  $p$  is ‘o’ if the parity is odd, and omitted if it’s even. The term symbol can be augmented by prepending additional terms which address the subshells in which electrons can be found. This is typically written as  $nL^N$ , where  $N$  is the number of electrons in a given subshell (omitted if  $N = 1$ ). For example,  $1s2s^3S_1$ , describes the triplet helium metastable state. In this case, there is a single electron in the  $1s$  subshell and a second atom in the  $2s$  subshell. The configuration has a total orbital angular momentum of 0 (denoted by the ‘S’), an even parity (denoted by the absence of a superscript ‘o’), a total spin of 1 (the superscript 3 is equal to  $2S + 1$ ), and a total angular moment of 1.

Excited atomic states usually have finite lifetimes. Normally, electrons will undergo transitions to lower the potential energy of the system. This can also occur spontaneously, through the emission of a photon, or through a superelastic collision with another particle. In the case of spontaneous transitions, only certain states can transition to others, as defined

by a series of selection rules [97]:

- $\Delta S = 0$
- $\Delta L = \pm 1$  or 0
- $\Delta J = \pm 1$  or 0
- $L = 0$  cannot transition to  $L = 0$
- $j = 0$  cannot transition to  $J = 0$

These rules are determined from a lower order approximation, and thus are not strict. As a result, forbidden transitions can occur, however these generally take place at much lower rates.

Figure 2.6 is a Grotrian diagram of the energy levels in neutral helium and the allowed transitions. In this case, the atomic states are separated into the singlet ( $S = 0$ ) and triplet ( $S = 1$ ) manifolds. The singlet manifold is composed of excited states where the electron spins are anti-parallel, and the triplet manifold represents excited states where the electron spins are parallel. As indicated by the first selection rule, transitions between these two manifolds is forbidden, thus each is something of a self-contained system [98].

Also observable in the diagram are two “metastable” states. These are the 2s states at the bottom of the singlet and triplet manifolds. An electron in either state cannot spontaneously transition to a lower energy state. As a result, an electron in either state can be extremely long-lived. In addition, they are also the lowest-lying excited states of helium. For these reasons, helium plasmas tend to have high densities of metastable atoms. This makes them a good candidate for spectroscopic study as will be seen in Chapter 4.

#### 2.4.1 Spectral Lineshapes

Electrons which transition to lower energy states emit photons which can be detected. Conversely, if an atom is exposed to a photon with an energy matching a transition, the atom may absorb the photon. Both processes are useful in determining the prevalence and dynamics of the excited states. This, in turn, can be used to infer various plasma properties.

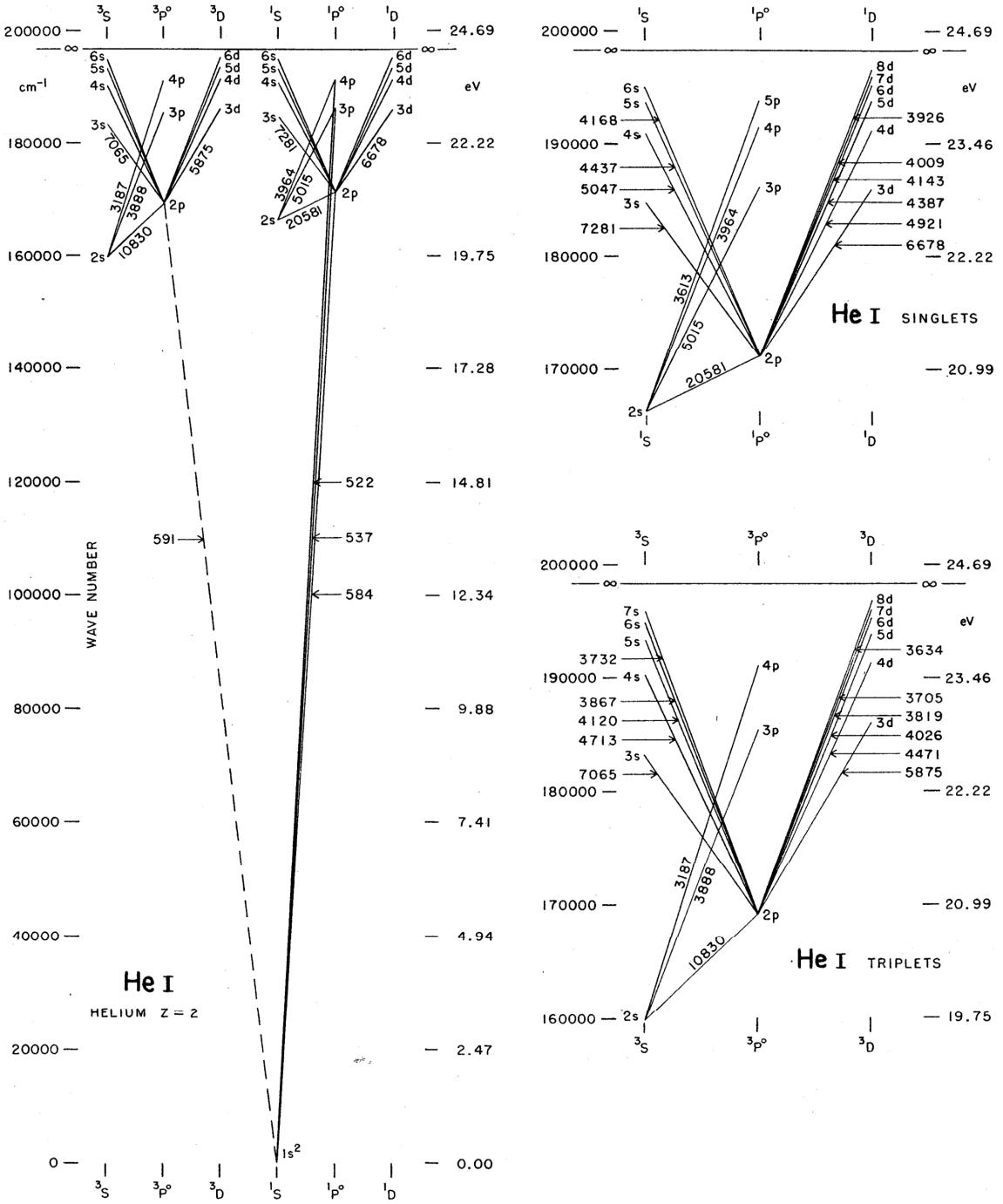


Figure 2.6: A partial Grotrian diagram of neutral helium, from [5].

Conservation of energy requires that the energy of the absorbed or emitted photon match the energy difference between the two states. However, the finite lifetime of excited atomic states implies, via the time-energy formulation of the uncertainty principle, some uncertainty in the actual energy difference between the states. As a result, the emitted photon will possess an energy selected from a distribution of energies.

This distribution is referred to as the spectral lineshape. The narrowest permissible lineshape, or natural lineshape, of an atomic transition can be shown [99] to be a Lorentzian of the form,

$$g(\omega) = -\frac{1}{4\pi^2} \frac{A\lambda^3}{\Delta\omega_a} \frac{1}{1 + [2(\omega - \omega_a)/\Delta\omega_a]^2}, \quad (2.13)$$

where  $\omega$  is the photon frequency,  $A$  is the Einstein coefficient for the transition,  $\lambda$  is the wavelength of the transition,  $\omega_a$  is central frequency of the transition, and  $\Delta\omega_a$  the full-width half maximum (FWHM) of the transition. In the ideal case, where the atoms motionless and unaffected by external perturbations,  $\Delta\omega_a = A$  [99]. This is known as the natural linewidth.

Other processes can act to broaden or alter the spectral lineshape [100]. For example, inter-atomic collisions can reduce the lifetimes of excited states. This results in additional broadening of the line, though it retains its Lorentzian nature. As the frequency of inter-atomic collisions increases linearly with pressure, this phenomena is referred to as pressure broadening. It can be included in equation 2.13 by using  $\Delta\omega_a = A + BP$ , where  $B$  is a measured or calculated broadening coefficient, and  $P$  is the pressure [99].

Atomic motion can also play a role in the spectral lineshape. If an atom is moving toward or away an observer as it emits a photon, the emitted photon will be blue or red shifted. Likewise, if the atom is moving toward or away an incident photon, the energy of that photon will be shifted [99]. If this effect is averaged over the random motion of atoms in a gas, the result is an additional broadening of the lineshape, called Doppler broadening. Unlike pressure broadening, Doppler broadening introduces a Gaussian component to the

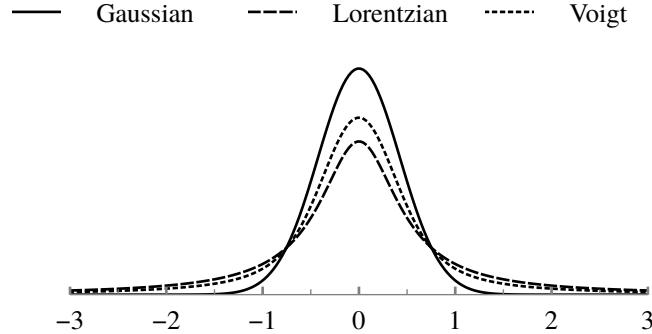


Figure 2.7: A comparison of the three primary spectral lineshapes, each with the same full width.

lineshape such that,

$$g(\omega) = \sqrt{\frac{2 \ln 2}{\pi^3} \frac{\Delta\omega_a}{\Delta\omega_d}} \int_{-\infty}^{\infty} \frac{1}{[(\omega - \omega_a) - \omega']^2 + 4\Delta\omega_a^2} \times \exp \left[ 4 \ln 2 \left( \frac{\omega'}{\Delta\omega_d} \right)^2 \right] d\omega'. \quad (2.14)$$

Here,  $\Delta\omega_d = \omega_a \sqrt{\frac{8k_B T_g \ln 2}{Mc^2}}$ , is the width of the Doppler broadening, where  $T_g$  is the gas temperature,  $M$  is the particle mass, and  $c$  is the speed of light. This form of the spectral lineshape is known as the Voigt profile, and it must be numerically integrated. In the case that  $\Delta\omega_d \gg \Delta\omega_a$ , equation 2.14 can be simplified to a standard Gaussian distribution,

$$g(\omega) = \sqrt{\frac{4 \log 2}{\pi \Delta\omega_d^2}} \exp \left[ -(4 \log 2) \left( \frac{\omega - \omega_a}{\Delta\omega_d} \right)^2 \right]. \quad (2.15)$$

The effect of the various broadening mechanisms is most apparent in the wings of the lineshape, far from the peak. Figure 2.7 illustrates the three major lineshapes with equivalent full widths. The Voigt profile is composed of equally broad Lorentzian and Gaussian distributions. As can be seen, the wings of the Gaussian distribution fall off very quickly. In comparison, the Lorentzian component is observable well out to the edges of the figure.

The spectral lineshape can be altered by a number of other processes. Electric fields can

influence the emissions via the Stark effect, while magnetic fields can split up degenerate states via the Zeeman effect. The fields of electrons and nearby molecules can also alter the lineshape of a transition. While not used in this study, such effects can be used as effective diagnostic tools in the measurement of field strengths, and charged particle densities in plasmas.

## 2.4.2 Absorption

As has been mentioned, a photon which closely matches the energy between two states can be absorbed by an atom. This property forms the basis for absorption spectroscopy where light with a known spectrum is used to illuminate a sample. The spectrum of the light that passes through the sample is measured and used to infer properties of the sample. In contrast to the emission processes occur spontaneously with a characteristic lifetime, often 10s of nanoseconds or more, absorption is almost instantaneous. This makes absorption-based spectroscopic methods desirable for fast phenomena, such as the RPND [101].

The cross section for a single atom to interact with a photon can be shown [99] to be,

$$\sigma(\omega) = A \frac{\lambda^2}{8\pi} \frac{g_1}{g_2} g(\omega). \quad (2.16)$$

where  $g_1$  and  $g_2$  are the number of degenerate configuration for the lower state and upper state respectively.  $g(\omega)$  is the appropriate spectral lineshape, determined from the operating conditions.

It is important to recognize that absorption spectroscopy can also perturb the system it is measuring. Suppose two consecutive photons were incident on the atom. If the first was absorbed, the likelihood that the second photon would be absorbed is zero. The cross section for absorption has not changed, there are simply no atoms available for the second photon to interact with. Therefore, if a photon field is incident on a volume of atoms susceptible to absorption, the degree to which the field is absorbed will depend on its intensity. The more

intense the photon field is, the more it reduces the number of atoms available to interact with.

Eventually, this effect is balanced by a process called stimulated emission. In this process, an atom is already in an excited state with one or more lower states. If an photon is incident on the atom and matches the energy difference between its current state and a lower one, the photon may induce a transition to the lower state. This results in the emission of a second photon with the same energy and phase as the first. The cross section for stimulated emission is identical to that for photon absorption.

This feedback process where the absorption and emission processes balance with each other is known as saturation. The saturation of a volume of gas is a continuous process, and depends on the atomic states in question and areal density of the incident photons, or intensity. From a practical standpoint, absorption measurements require that the interrogating photon field remain below a threshold value. This saturation intensity can be shown [99] to be,

$$I_s = \frac{2\sqrt{2}h\nu_0A}{\lambda^2}, \quad (2.17)$$

where  $h$  is Planck's constant, and  $\nu_0$  is the nominal frequency of the transition [99].

In this report, absorption and spontaneous emission diagnostics provide the experimental basis on which the RPND analyzed. Both are direct measures of the excited states that exist within a RPND. However, neither provides any direct measurement of the quantity or energies of the electrons. In the RPND, as with all plasmas, the electrons play a fundamental role in how the discharge behaves and develops. At the most basic level, it is the electrons which are accelerated by the electric field and collide with the gas atoms to produce the aforementioned excited states. Consequently, it should be possible for a sufficiently detailed model to use measurements of the excited states in order to infer the properties of the electrons, as will be seen in Chapter 5.

## CHAPTER 3

# Experiment

### 3.1 Discharge Apparatus

The RPND apparatus used in the forthcoming experiments was similar in design to the coaxial geometry used by Vasilyak and others used in FIW studies [19]. As depicted in figure 3.1, it is essentially a cylindrical inner conductor, surrounded by a dielectric, covered by an outer conductor. An electrode, connected to the transmission line, and the RPND serve as the inner conductor. The dielectric took the form of a glass tube and an air gap. Finally, the outer conductor consisted of a series electrically connected metal shells which served as the current return path. Following from right to left, the inner conductor was composed of a vacuum window, a nipple, a double-sided flange tapped for an NPT connection, and the discharge tube containing the RPND. Unless otherwise noted, all vacuum components featured DN35 CF flanges with copper gaskets.

The tube was composed of borosilicate glass with metal vacuum flanges on both ends. The flanges of the tube also acted as the electrodes for the generation of the RPND. The glass tube had an inner diameter of 3.3 cm, an outer diameter of 4.0 cm, and a length of 22.9 cm. The overall length of the tube including the flanges was 30 cm. In the figure shown here, the right electrode served as the anode, and the left electrode was the cathode.

The dielectric surrounding the inner conductor was composed of several components. The vacuum window, nipple, double-sided flange, and anode were separated from the outer

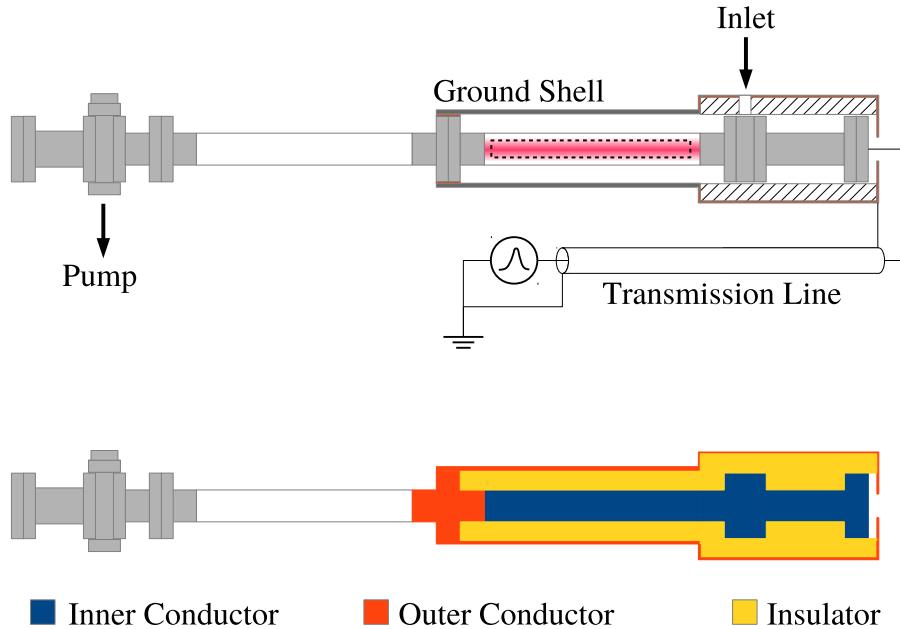


Figure 3.1: Two illustrations of the RPND apparatus. The upper version is an annotated sketch of the device, and the bottom version simplifies the geometry into its three electrical components.

conductor by an air gap and a polytetrafluoroethylene (PTFE) tube, 20 cm in length with an inner diameter of about 7.5 cm, and an outer diameter of 10 cm. The RPND portion of the inner conductor was separated from the outer conductor by the glass tube and an air gap of about 2.54 cm.

The left side of the discharge tube, or cathode, connected to the outer conductor and served as part of the current return path. Directly attached to the cathode was an aluminum tube, held in place by an acetyl resin shaft collar and a copper shim. Radial optical access to the discharge was provided by two slots milled into the ground shell. The slots were positioned on opposite sides of the shell and were 3.8 by 25.4 cm in length. The tube itself was 30 cm in length.

The end of the aluminum tube nearest the anode was affixed to a copper sheet which was oriented perpendicular with respect to the tube's axis of rotation. The sheet was 10 cm square, and was attached to the tube with conductive copper tape. A 5 cm diameter

hole was cut into the copper sheet to allow the discharge tube to pass through it. The sheet was secured to the edge of the PTFE tube by nylon screws. Surrounding the PTFE tube was a second shell, made of rolled copper sheet. This was electrically connected to the aluminum tube by a braided copper strap. The right end of the PTFE tube was covered by a second copper sheet, 10 cm square. Again, the sheet was secured to the PTFE tube by nylon screws and in electrical contact with the copper shell. In the center of the copper sheet was a HN bulkhead adapter for connection to the transmission line. The inner conductor of the bulkhead adapter was connected by a straight run of 5 cm of silicone-coated wire to the vacuum window flange. The outer conductor of the bulkhead adapter provided the ground connection for the discharge apparatus.<sup>1</sup>

The voltage pulse was generated by a FID power supply, supplied by ANVS, Inc. (model PT510NM). The amplitude of each pulse was fixed at 6.4 kV with a repetition rate of 1.0 kHz. Each pulse had a fixed width of 25 ns, required approximately 4 ns to rise from 10% of its peak to 90% of its peak, and was roughly Gaussian in shape. A SRS DG645 delay generator was used to trigger the power supply output for all experiments and provided a reference time base for all measurements.

Preliminary experiments revealed multiple reflections between the power supply and the anode. A long run of RG 213 coaxial cable was used to temporally separate the reflections. This made it possible to study the effects of individual pulses. Based on the length of the cable (about 13.7 m), the delay was predicted to be 69.2 ns. As the reflection would have to cross the length of the transmission line twice before it reached the anode again, the total separation time between the initial pulse and each subsequent reflection was predicted to be 138.4 ns. This calculated delay was found to closely match the measured time period between the incident and reflected pulse.

A simplified version of the gas flow system can be seen in figure 3.2. The gas supply

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<sup>1</sup>Measurements confirmed that the entirety of the outer conductor had a low DC impedance to ground. However, it is likely that at frequencies relevant to the RPND, the impedance is not negligible. As a result, the outer conductor likely floats to a finite voltage during operation.

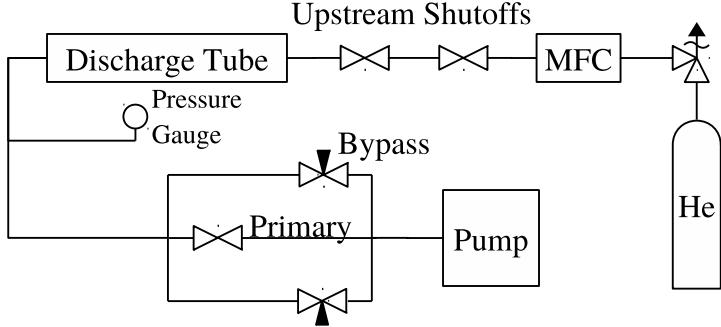


Figure 3.2: Simplified diagram of the gas flow path and pumping system.

was provided by a bottle of ultra-high purity helium. Following the regulator, the helium passed through a digital flow controller which was set at 25.0 sccm for all experiments. The helium then entered a gas distribution manifold, followed by a shutoff valve, a short run of 1/4" stainless steel tubing, another shutoff valve, about 2 m of 1/4" polyethylene tubing, and then the discharge tube via the double-sided flange.

The gas exited the discharge tube via an identical tube, on the side opposite the inlet, see figure 3.1. This second tube was intended to electrically isolate the discharge portion of the apparatus so that only a single conductive path to ground existed. The pressure was monitored downstream of the second tube with two capacitance manometers (one with a full scale range of 10 Torr, the other with a range of 100 Torr). The gas exhaust of the second tube was connected to an oil-seal roughing pump via three independent paths. The primary pump path had the highest gas conductance and was controlled by a bellows valve. However, this path was typically closed in favor of two needle valve bypasses. The needle valves were used to control the pumping speed and obtain the desired operating pressure. Immediately upstream of the roughing pump was a zeolite trap in order to limit oil backstreaming.

The base pressure of the system was measured to be approximately 15 mTorr. The leak rate was measured several times by evacuating the apparatus and then sealing it from the pump by all three pump paths. The leak rate was found to be  $2.0 \times 10^{-3}$  sccm. Given a constant flow rate of 25.0 sccm, the fractional impurity can be conservatively estimated to be 80 ppm.

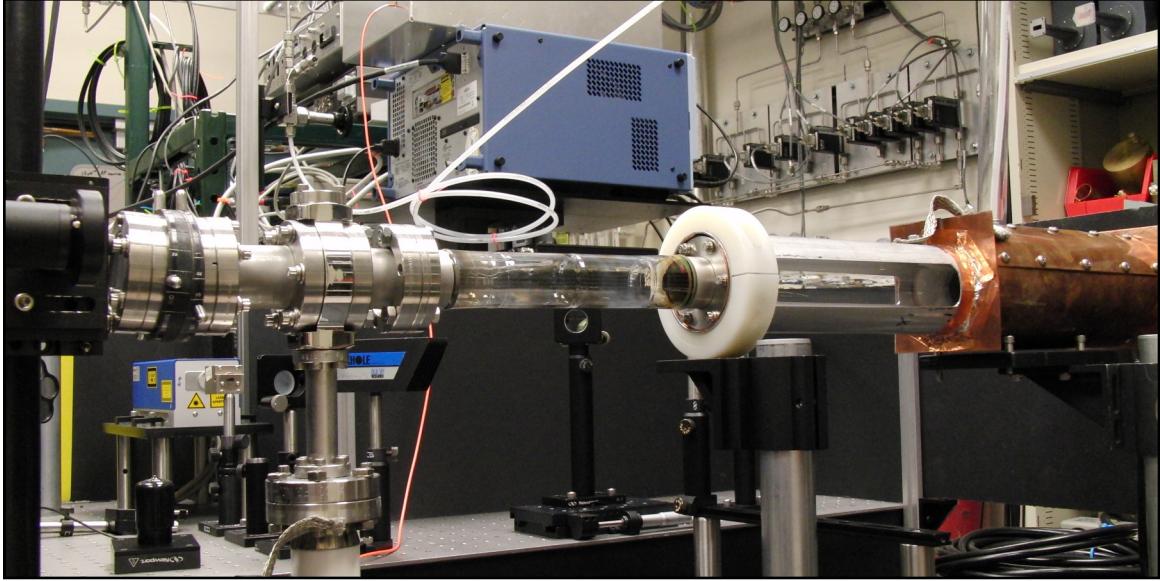


Figure 3.3: Photograph of the discharge apparatus.

The assembled discharge apparatus can be seen in figure 3.3. The RPND apparatus was supported two 1.5 in mounting posts with angle brackets. The mounting posts attached to a 122 cm by 76 cm optical breadboard, supported by urethane shock absorbers, and a rigid frame. The roughing pump was attached to the apparatus with flanged bellows in order to reduce mechanical vibrations.

All electrical measurements were made with a LeCroy 6100A WaveRunner oscilloscope which had a bandwidth of 1.0 GHz. Electrical connections to the oscilloscope were made with RG 50/U coaxial cable and standard BNC connectors. All connections were terminated at  $50\ \Omega$  unless otherwise noted. The voltage of the pulses was monitored from a 1 : 1000 divider built into the power supply. The current was measured from a current shunt which crossed a small electrical break in the outer conductor of the transmission line. The shunt was built into the transmission line as close as possible to the power supply, about 3 cm from the output connector.

The current shunt was composed of nine, low inductance,  $1.0\Omega$  resistors connected in parallel. As illustrated in figure 3.4 the resistors were soldered to two strips of copper foil. This assembly was then wrapped around the electrical break in the transmission line, bridg-

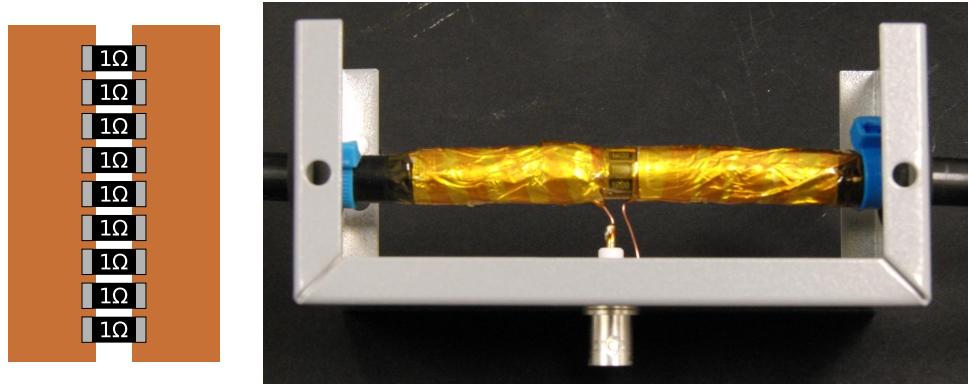


Figure 3.4: Sketch of the unassembled back-current shunt, and a photograph of it assembled around the transmission line.

ing it. Two short lengths of No. 18 copper wire were soldered to each side of the shunt assembly. These were then attached to a BNC bulkhead connector, fitted to a metal project box. The voltage across the resistors was used to measure the current traveling through the outer conductor of the transmission line. The copper foil was then secured to the outer conductor with several wraps of aluminum foil, followed by a layer of polyimide tape.

Data were retrieved from the oscilloscope with a desktop computer via the GPIB interface. Instrument control, data acquisition, and data storage were all managed by a LabView program. Analog input and output was handled with the auxiliary input and output ports of a SRS SR850 DSP lock-in amplifier.

## 3.2 Field Calculations

The electric field characteristics of the discharge apparatus were analyzed using Ansoft Maxwell 9, a two-dimensional, electrostatic solver. At the top of figure 3.5 is a logarithmic heatmap of the electric field magnitudes within the device. Overlaid are the electric field vectors in magenta. Below this is a plot of the electric field on a linear scale, across the central axis of the apparatus and along the outer edge, adjacent to the glass tube. It is apparent that the field strength is the strongest at the triple point which occurs near the glass-metal seal. Also noticeable is the fast fall off of the electric field with distance from the anode.

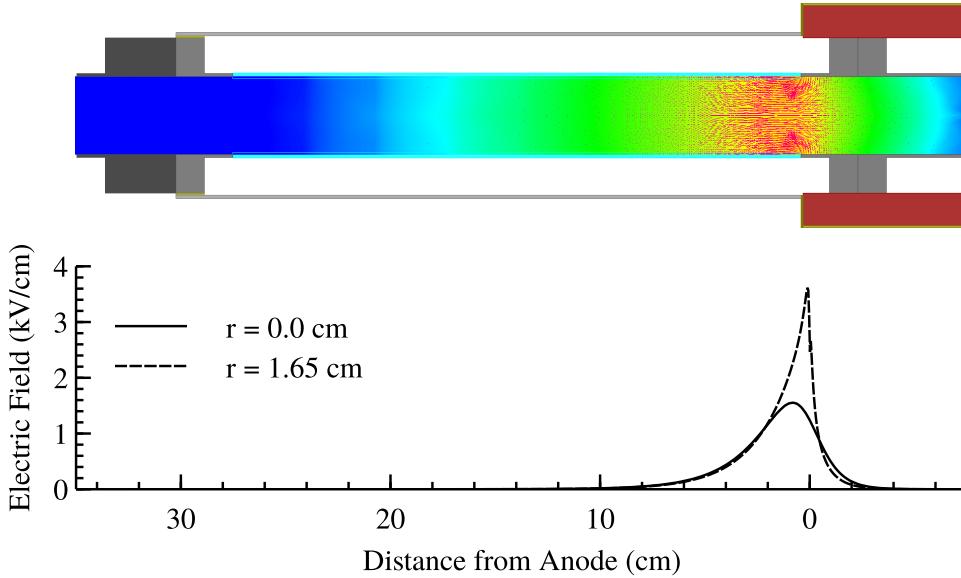


Figure 3.5: Heatmap and vector plot of the electric field in the RPND discharge apparatus.

The presence of the external ground shield produces an electric field contour vastly different from that of two parallel plates. This is also reflected in the electric field vectors. Specifically, the many locations possess fields with strong radial components, especially those near the anode.

These static fields are only valid in the absence of free charge within the system. However, these characteristics suggest that the discharge formation will be somewhat different than the one-dimensional description of a streamer in Chapter 2. First, assume that the electrons are distributed uniformly throughout the discharge tube, prior to the pulse. As a pulse is applied, ionization would preferentially take place near the anode. As the electrons would be drawn toward the anode, and leave behind some amount of positive space charge. However, as the positive space charge builds up, it would begin to act as a virtual anode, increasing the electric field further from the physical anode. The virtual anode would then begin to draw its own electron current, predominantly from around the edges, near the wall. In this manner, the discharge would propagate away from the anode, leaving a quasineutral ionized gas in the center of the discharge tube and a positive space charge region along the wall.

### 3.3 Operating Procedures

One of two operating procedures for the RPND was used depending on how recently the discharge had last been turned on. If the discharge was inactive for over one hour, then a full startup procedure was used. Otherwise, an abbreviated process was used.

In the case that the discharge had not been operated for over an hour, the roughing pump was turned on and the primary pump path valve was opened as was the first shutoff valve upstream of the discharge chamber, seen in figure 3.2. The system was then allowed to pump down to its base pressure. Afterward the second upstream shutoff valve was opened and the system was again allowed to reach base pressure. At this point the helium flow was turned on and set to 25.0 sccm. The primary pump path was then closed and the needle valve bypasses were used to adjust the system pressure to 3.0 Torr.

Next, the delay generator was turned on and the output for triggering the power supply was activated. Then, the FID power supply was turned on. This would produce an easily visible discharge within the discharge tube. The system was allowed to operate at this condition for one hour in order to remove potential contamination on the walls and electrodes. At the end of this period, the voltage waveform was checked to ensure that it was consistent with previous experiments. Once this was confirmed, the pressure was adjusted to the desired operating condition.

The discharge was shutdown by first shutting off the power supply, followed by the delay generator. Then, the helium flow was shut off, and the primary pump path was opened. The system was allowed to come to base pressure before the two upstream shutoff valves were closed, after which the primary pump path was closed. The roughing pump was then shut off.

In the cases that the discharge had been operated within the last hour, it was possible to use an abbreviated startup procedure. This process was fundamentally the same as the previous one, however once the pump-related procedures were complete the discharge only required five minutes to reach a steady state. This was verified with multiple measurements

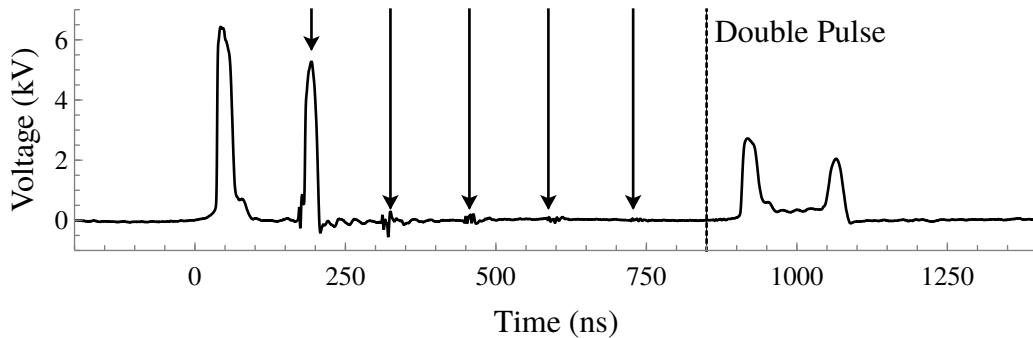


Figure 3.6: Typical voltage waveform of the RPND. Arrows indicate reflections back to the power supply. The dotted line delineates the time at which the power supply begins to exhibit double pulsing.

of the current and voltage characteristics as well as the discharge emissions. At times prior to this five minute equilibration period, the reflected pulse energy was noticeably higher, and the delay between the trigger pulse and the output pulse was variable.

It seems likely that the increased reflected pulse energy during the equilibration period is due to poor matching between the output impedance of the power supply and the plasma load [62]. When the pulse train is initiated, the first series of pulses perceive an almost open load. During this time, the plasma density tends to increase more with each pulse than is lost between pulses. This increase in plasma density, reduces its impedance and improves energy coupling to the plasma. At the same time, the increasing plasma density results in an increasing shielding effect of the applied voltage. Eventually, these effects balance out and the density increased caused by each pulse equals the density decrease which occurs between pulses. At this point the energy coupled into the plasma with each pulsed remains essentially fixed.

### 3.4 Electrical Characteristics

The typical voltage waveform, as seen in figure 3.6, exhibited a number of features. It begins with an incident pulse at  $t = 0.0$ . 138 ns later, it is followed by the pulse that has

been reflected from the anode. The reflected pulse is somewhat smaller, proportional to the energy deposited in the discharge. Additional reflections are visible at integer multiples of 138 ns. These subsequent reflections are much smaller than the initial one, suggesting that much of the remaining pulse energy was dissipated after the first reflection reached the anode. Curiously, a second pulse appears at 800 ns. This is believed to be a peculiarity of the power supply. For the most part, analysis of the RPND will focus on the times which precede 280 ns (the incident pulse and first reflected pulse).

The properties of the RPND were examined at: 0.3, 0.5, 1.0, 2.0, 3.0, 4.0, 8.0, and 16.0 Torr. The appearance of the discharge varied with the pressure in a continuous fashion, however it was apparent that there were three regimes of operation. At the low pressures, 0.3 and 0.5, it was difficult to initiate the discharge. Often, it would be necessary to increase the pressure to initiate the discharge, and then reduce the pressure to the desired conditions. The discharge appeared dim and relatively constricted about the central axis of the discharge tube, with a radial extent of approximately 1 cm. Accompanying these pressures was a large degree of electronic noise. This manifested primarily in the current waveforms, as seen in figure 3.7, as well as a number of equipment malfunctions.

As the pressure was increased (from 1.0-4.0 Torr), the electrical noise was observed to subside. The current waveforms showed significant reductions in the ringing that was particularly prominent at lower pressures. In addition, the visual extent of the discharge increased substantially, to the point where it could be considered volume-filling. The discharge also increased its axial extent as well, eventually reaching well past its intended limit at the cathode. This occurred despite attempts to isolate the downstream pump sections from the discharge.

Such behavior is similar to that observed in plasma bullets [83] where the discharge is able to continue far past the cathode. This suggests that development of the RPND along the discharge tube led by a large region of positive space charge, as suggested in the discussion of the field characteristics. The ions that produce this positive space charge are eventually

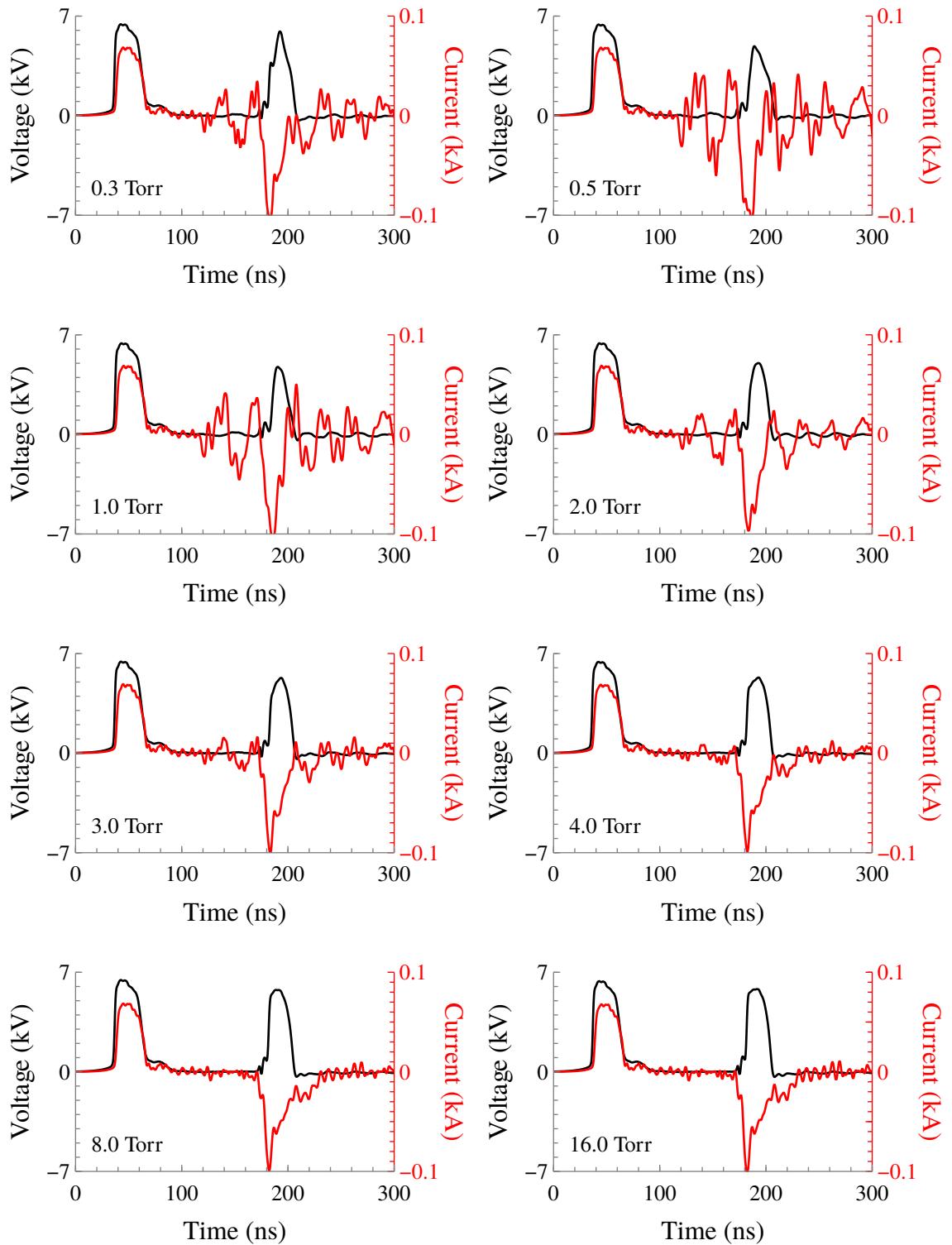


Figure 3.7: High resolution views of the voltage and current waveforms for the first incident and reflected pulse, at each of the operating pressures.

collected at the cathode or neutralized at the walls, however their low mobility (as noted in Chapter 2) prevents this from happening on time scales relevant to the RPND formation.

At higher operating pressure (8.0 and 16.0 Torr), the discharge receded back toward the cathode. This was accompanied by a decrease in the apparent brightness of the discharge to levels similar to that of the low pressure conditions. In contrast, the discharge appeared to remain volume-filling. While discharge initiation was difficult at the higher pressures, it was not accompanied by the electrical noise observed at lower pressures.

## 3.5 Energy Coupling

The product of the voltage and current waveforms, as seen in figure 3.7, gives the power deposited in the discharge as a function of time. Subsequently, the power integrated over time gives the total energy deposited in the discharge. However, this approach is somewhat complicated by several features of the RPND. As previously mentioned, the pulses produced by the power supply are not completely absorbed by the discharge. Therefore, the integration must be carried out over both the incident and the reflected pulse. Additionally, there is the concern that the oscillations in the current measurements could introduce fluctuations in the calculated energy deposition. However, the small voltage signal limits the error introduced by these fluctuations to less than 1%.

Figure 3.8 gives the total energy deposited for the first pulse at each of the operating conditions. The energy coupled to the discharge peaks at an energy of 5.5 mJ (out of a total incident energy of 8.8 mJ) at a pressure of 1.0 Torr, after which it slowly decreases. This peak in the coupled energy is coincident with the peak brightness of the discharge. Together, these suggest that the density of excited states will be optimized at intermediate pressures.

Though there appear to be no direct comparisons available in the literature, several papers report on energy coupling for similar systems. Macheret, Schneider, and Murray studied a parallel plate RPND in air, at 1-10 Torr and reported a total energy deposition of

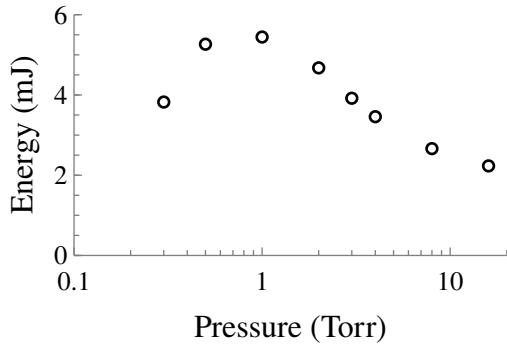


Figure 3.8: Plot of the energy coupled into the discharge with the first pulse as a function of pressure.

0.30-0.36 mJ, increasing with pressure [81]. Nishihara et al. recorded values of 1-2 mJ in a nitrogen RPND [72]. Pancheshnyi et al., in the study of an air-propane mixture at 750 Torr, found that each pulse deposited about 1.9 mJ of energy. Overall, the measured values for the deposited energy appear to be in comparable with those previously measured.

From an applications standpoint, the potential existence of a condition which optimizes the production of excited states is an interesting one. This behavior is also compelling from a physical standpoint as it suggests a phase change in the competition of two or more processes. Though this kind of competition is reminiscent of Paschen's law, the duration of the pulse is too short for appreciable ion drift to occur (an estimated maximum of 3 mm), therefore secondary electron emission is not important. These observations provide further impetus for a close examination of the RPND properties, particularly the excited state dynamics.

## CHAPTER 4

# Metastable Measurements

As was noted in Chapter 1, measurements of the RPND have been mostly limited to the afterglow plasma or time-integrated quantities. Electric field measurements, either with capacitive probes or nonlinear wave-mixing, thus far provide the only insight on the development of the RPND [79, 80, 87]. Though the electric field can be used to estimate electron densities and reaction rates in the plasma, this requires a number of additional assumptions regarding electron locality, and equilibrium with the applied field.

As a result, there is a lack of reliable information on particle properties of the RPND during its development. That said, such information is necessary to confirm the present understanding of how these discharges develop, how they may be optimized for specific applications, and how to improve existing numerical simulations. Therefore, a clear need exists for direct measurements of the RPND particle properties.

Unfortunately, this presents a significant challenge for most traditional plasma diagnostics. In most situations, the obvious choice would be the Langmuir probe given its simplicity and ease of implementation. However, the fast variations in the plasma potential, slow response of the ions, and high collisionality all preclude this approach [90]. Furthermore, any physical probe could potentially act as a large perturbation to the very system it is measuring.

The logical alternative to physical probes is the use of optical diagnostics, however these have their own associated difficulties. Electrons cannot be studied by their light emissions because, with the exception of bremsstrahlung and cyclotron radiation, they do not emit.

This leaves the light emitted from excited atoms. Atomic emission spectroscopy can be used to measure many different plasma quantities, from electron density, to local electric field strength [96]. Unfortunately, spontaneous emission can be a slow process compared to the development of the RPND. For example, the fastest neutral helium transition in visible wavelengths ( $3^3D_3$ - $2^3P_2$ ) has a decay rate of 14 ns [102].

This suggests that instead of waiting for spontaneous emission to occur, it may be better to use some form of active spectroscopy. Though the added complexity of a well-characterized light source is undesirable, it allows for several interesting opportunities. For example, a sufficiently intense laser can be used to directly interact with the electrons through Thomson scattering. It has a high spatial and temporal resolution and is able to measure the electron density and temperature simultaneously [103]. However, the RPND may have densities well below the interaction limit of  $5 \times 10^{12} \text{ cm}^{-3}$  [75].

If it is not possible to directly interact with the electrons, the next alternative is interact with the atomic population. Probing of the ground state is difficult given its large separation from any excited state. Furthermore, the high densities of the neutral states would completely absorb all incident radiation, even over short pathlengths (leaving nothing to measure). Instead it makes more sense to probe an excited atomic state. The lowest lying one is the triplet metastable ( $2^3S$ ), which resides at 19.82 eV above ground [102]. This relatively large energy gap assures that no such states will be naturally present at room temperature. The triplet metastable (and all higher-energy states in helium) will be populated almost exclusively by energetic electrons. Therefore, the triplet metastable density is a useful indicator of the electron energetics in the RPND as it develops. With a sufficiently complex model, it may even be used to infer properties of the electron population.

Perhaps the most straightforward means by which to measure the triplet metastable density is with absorption spectroscopy. This approach has a long history in the study of gas discharges, going back at least six decades [104]. At its most basic, the technique involves illuminating a plasma with light matching a transition between the metastable, and some

upper level. The amount of transmitted light is then measured with a detector on the opposite side of the plasma. The amount of transmitted light is proportional to the metastable density, integrated along the path of the light. As the temporal bandwidth of this technique is only limited by the time required for the light to traverse the plasma, it presents a promising approach for particle measurements during the development of the RPND.

## 4.1 Setup

Traditionally, the light used in absorption spectroscopy has been supplied by discharge tubes of same gas as the system under study. Though straightforward, this approach is limited by the luminosity of the discharge tube, and the fact that the emitted radiation is isotropic. More recently, Millard et al. noted that diode lasers provide a greatly improved light source for absorption experiments [105]. The laser light is easily directed and collimated for spatial selectivity, and has more than sufficient intensity [105]. Therefore, it was decided to use a diode laser in the measurement of the triplet metastable level.

As with the study by Millard et al., the decision was made to study the transition from the triplet metastable to the  $2^3P_{0,1,2}^o$  state (a transition wavelength of approximately 1083 nm). This was done for several reasons. For one, the closest helium transition is over 7 nm away, making it relatively isolated. In addition, the different levels or values of  $J$  are all within the tuning range of a single diode. As each level has a different degeneracy,  $g$ , the strength of absorption varies depending on the selected level. Thus, the absorption strength can be increased for low densities, or decreased at high densities, improving the dynamic range of the diagnostic.

The laser used was a distributed feedback laser diode, produced by Toptica, model LD-1083-0070-DFB-1. The specified linewidth of the laser was 3 MHz, well below the natural linewidth of the transition at 10.2 MHz. This can be exploited to directly measure the gas temperature of the system, as will be seen in the next section. The diode was rated for a total

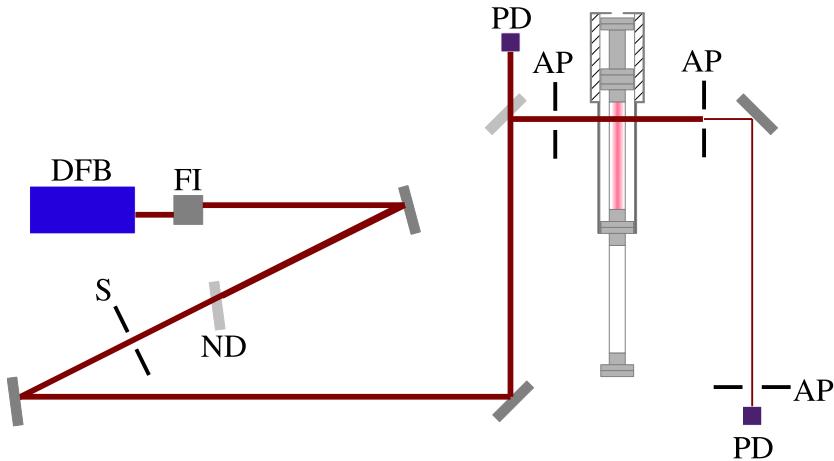


Figure 4.1: Optical beam path of the laser in the absorption spectroscopy experiment. DFB - Distributed feedback laser diode; FI - Faraday isolator; ND - neutral density filter; S - shutter; PD - photodiode; AP - aperture.

output power of 70 mW, with a beam size of 1 mm by 3 mm and vertical polarization. The diode was housed in a Toptica DL DFB housing which incorporated the collimating optics. A Toptica DCC 110 was used to provide current control for the diode laser, and a Toptica DTC 110 was used to control the thermoelectric cooler for the diode.

The layout in figure 4.1 reflects the optical beam path used in the absorption experiment. The laser light is produced by the distributed feedback laser diode (DFB). It then enters an Electro-Optics Technology, Inc. Faraday isolator (FI) which prevents back-reflections from entering the diode. Without the isolator in place, such back-reflections can cause mode-hopping, resulting in unreliable tuning. The laser intensity is then reduced by a neutral density filter (ND). After which, the laser passes through a Vincent Associates electronic shutter (S). Then, the beam is split by a Thorlabs BSF10-C beam sampler at a  $45^\circ$  angle. This reduced the laser intensity below the saturation intensity ( $0.45 \text{ mW/cm}^2$ ) of the transition. The beam was collimated with two apertures (AP) on both sides of the discharge apparatus. The beam exiting the apparatus was then sent through a final aperture to filter nearly-colinear plasma emissions before it was coupled into an optical fiber by a Thorlabs F240SMA-780 collimation package.

Behind the beam sampler was a Thorlabs DET300 germanium photodiode. The signal from this photodiode was terminated at  $1\text{ M}\Omega$  and used to monitor the beam. The opposite end of the optical fiber was affixed to a Thorlabs DET410 InGaAs photodiode. The photodiode signal was amplified by a Femto HVA-200M-40-B voltage amplifier before being sent to the oscilloscope. The time resolution of the metastable measurements was determined by the InGaAs photodiode which had a specified rise time of 5 ns.

In order to measure the absorption of the laser, it was first necessary to tune the laser to the correct wavelength. This matter was complicated by the lack of a wavemeter with sufficient precision and accuracy. As a result, a signal generator was used to sweep the laser current so as to cover a frequency range of 40 GHz while the plasma was operating. The temperature of the diode was then slowly adjusted until absorption peaks corresponding to the  $2^3S_1 - 2^3P_{0,1,2}^o$  transition were observed in the output of the InGaAs photodiode. This allowed the laser current to be tuned to coincide with the desired transition and provided a rough conversion between changes in the diode current and changes in the laser wavelength. A more accurate measurement of this relation was made with a CVI Melles Griot ET-25.4-10.00-30, solid dielectric etalon. It was found that a temperature of  $36^\circ\text{ C}$  and a current of 63 mA produced resulted in an output wavelength of approximately 1082.9 nm and the conversion between diode current and wavelength was 0.6067 mA/GHz.

As described in Chapter 3, data acquisition was handled by a LabView program, connected to the oscilloscope by a GPIB cable. The auxiliary outputs of the SRS SR850 lock-in amplifier were used to adjust the diode laser current (via the DCC 110 module), and to trigger the electronic shutter. One of the auxiliary inputs of the lock-in amplifier was used to read out the pressure from the pressure controller.

Data were acquired for a range of pressures from 0.3-16.0 Torr, and at three axial locations: 5.08, 12.7, and 20.32 cm, relative to the glass-metal seal of the anode. In reference to their location relative to the gas inlet these will be referred to as the ‘upstream’, ‘midstream’, and ‘downstream’ locations, respectively. For each combination of location and pressure,

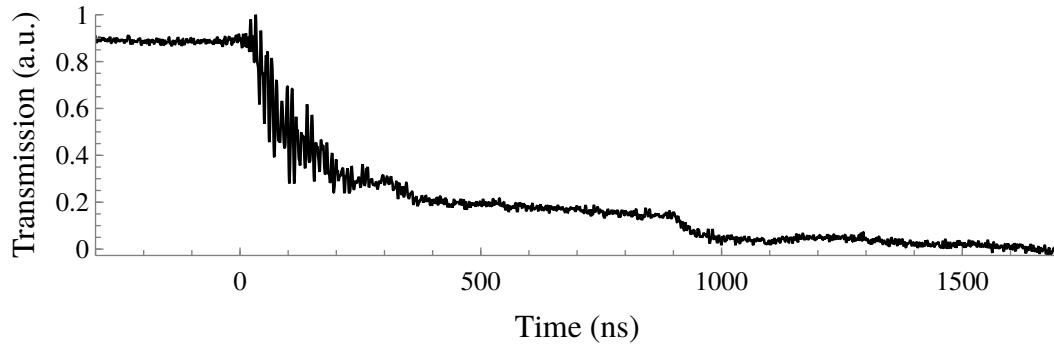


Figure 4.2: Measurement of the transmitted laser light at the nominal transition wavelength at 4.0 Torr of helium.

absorption spectra were measured over  $\pm 3.85$  GHz relative to the nominal transition frequency of the  $2^3S_1$ - $2^3P_0^o$  transition at intervals of 154 MHz. The absorption spectra were measured for time domains of  $-300$ - $1700$  ns relative to the voltage pulse. Additional measurements were made at the midstream position of the metastable densities from  $-88$ - $700$   $\mu$ s in order to investigate the loss mechanisms of the metastables.

The broadband electronic noise emitted by the fast pulses was a persistent issue and presented one the greatest challenges in the acquisition of accurate measurements. In order to reduce the noise present in the detector signal, the InGaAs photodiode was removed from the immediate area surrounding the discharge by the use of an optical fiber. The optical fiber was routed through a small opening in a grounded metal box where both the photodiode and the voltage amplifier resided. In addition, the DC power supply of the voltage amplifier was connected to an outlet on a Tripp-lite Isobar intended to provide isolation for the power input. The photodiode was connected directly to the input terminal of the amplifier minimizing the length between the two. Likewise, the amplifier was connected to a BNC bulkhead adapter by a 10 cm length of RG 50/U. The final connection to the oscilloscope was made by an additional 10 cm length of RG 50/U, running from the BNC bulkhead connection.

Figure 4.2 shows the transmission signal measured at the nominal transition wavelength while the plasma was active in 4.0 Torr of helium. The signal is an average of 200 indepen-

dent pulses. Further sampling had no appreciable effect on the waveform. As can be seen, despite the efforts to limit the electrical interference, there is still a substantial amount of noise present in the transmission signal. This is most noticeable in the large ringing which occurs for the first 200 ns after the voltage pulse. Without any kind of compensation for this noise it would be impossible to obtain reliable measurements of the transmission signal.

## 4.2 Noise Suppression & Absorption Analysis

The noise produced by the RPND was relatively consistent between pulses as well as over the duration of each experiment. As a result, it was possible to correct for the electrical noise and emissions from other transitions by measuring the signal from the photodiode in the absence of the laser and subtracting this from the signal with the laser. The acquisition process proceeded as follows:

1. Set desired laser wavelength.
2. Wait 5 s for laser output to settle.
3. Acquire 200 waveforms from photodiode.
4. Close shutter.
5. Acquire 200 waveforms from photodiode.
6. Repeat

The effect of this subtraction can be seen in figure 4.3 where the top heatmap shows the initial set of acquisitions with the laser on, and the middle heatmap shows the transmitted signal with the noise subtracted.

As the wavelength of the laser diode changed, so did the output power. This led to the gradient-like appearance of the top two plots in figure 4.3. In order to correct for this a measurement was made of the unattenuated laser power as a function of diode wavelength. This was done by deactivating the plasma and repeating the above acquisition procedure. The intensity of each point in the transmission spectra was then divided by the unattenuated laser power, producing the properly normalized transmission spectra.

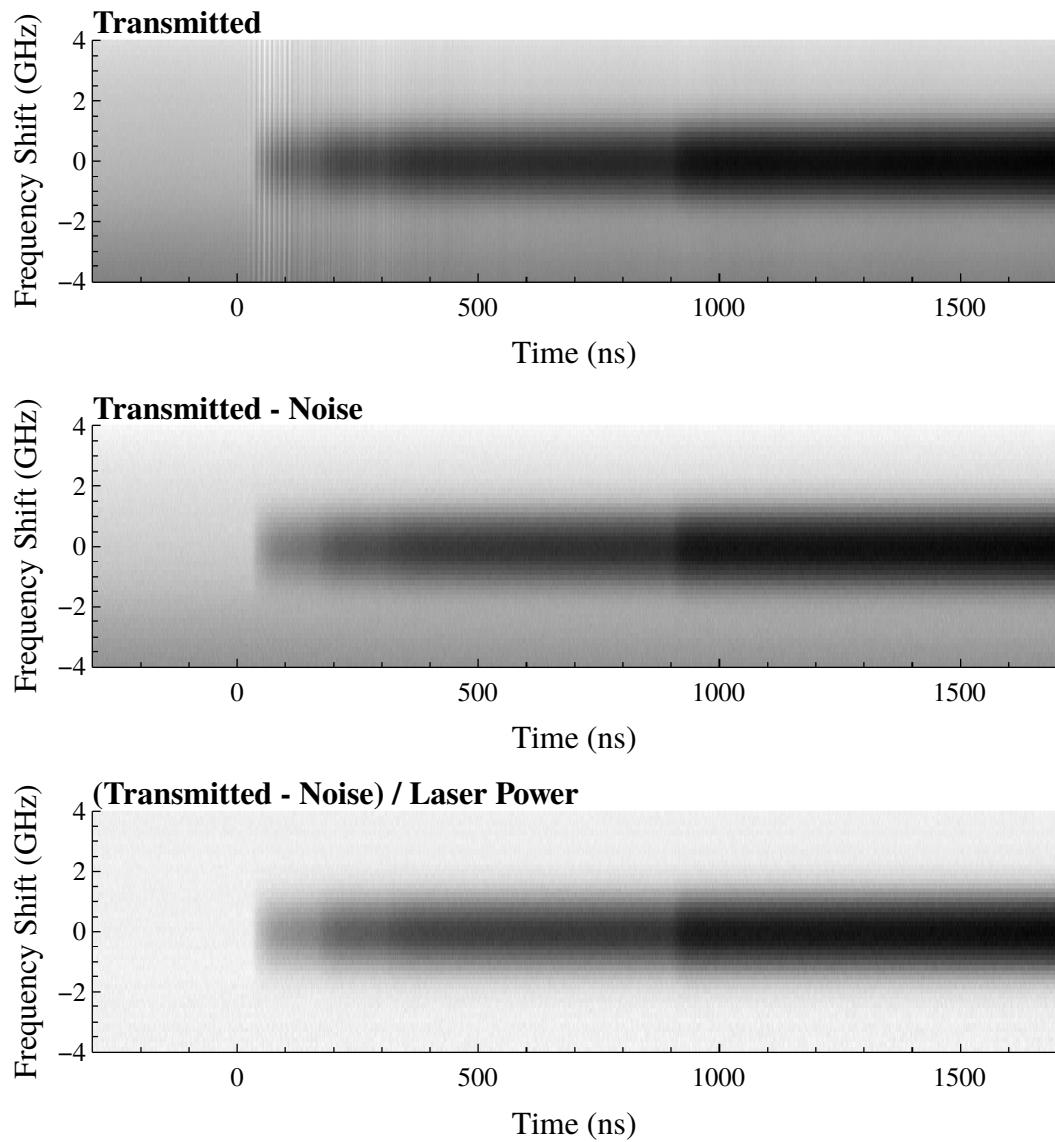


Figure 4.3: Heatmaps of the transmitted laser signal for the 4.0 Torr condition at various stages of post-processing.

These spectra were then analyzed using a transmission model based on the absorption cross sections described in Chapter 2. In a one-dimensional system, the change in intensity of an incident photon field (below the saturation limit), can be expressed as

$$\frac{dI(x, \omega)}{dx} = -\sigma(\omega)N(x)I(x, \omega) \quad (4.1)$$

where  $I$  is the intensity of the photon field as a function of distance  $x$ ,  $\omega$  is the frequency of the photons,  $N$  is the density of the interacting species, and  $\sigma$  is the interaction cross section. This equation has the simple solution,

$$T(\omega) = \frac{I(x, \omega)}{I_0(\omega)} = \exp \left[ -\sigma(\omega) \int_0^x N(x') dx' \right], \quad (4.2)$$

where  $T$  is the transmitted intensity fraction, and  $I_0$  is the initial intensity of the photon field. The absorption can be trivially obtained from the relation  $A(\omega) = 1 - T(\omega)$ .

For the purpose of analyzing the absorption spectra, a quantity called the line-integrated density will be defined. This is simply,  $\langle N \rangle = \int_0^x N(x') dx'$ . While equation 2.16 can be used to determine the absorption cross section it requires that a lineshape be specified. In general, it is preferable to select either a purely Gaussian or purely Lorentzian lineshape. This reduces the computational cost of spectral calculations in comparison to the use of the Voigt profile (equation 2.14). Whether the Voigt profile is necessitated or not can be determined by a comparison of the relative widths of the different broadening mechanisms. For a temperature of 300 K and a pressure of 8.0 Torr, it is found that  $\Delta\omega_d = 1.7$  GHz and  $\Delta\omega_a = 0.21$  GHz. Because neither broadening mechanism appears dominant, the choice was made to analyze the data with a Voigt profile, despite the added computational cost.

Equations 4.2, 2.16, and 2.14 can be combined to form a model equation for the absorption spectrum. It can be seen that only two unknowns exist: the gas temperature,  $T_g$ , and the line-integrated density,  $\langle N \rangle$ . The model equation was matched to the measured spectrum at each time point using the Levenburg-Marquardt algorithm [106], as implemented by the

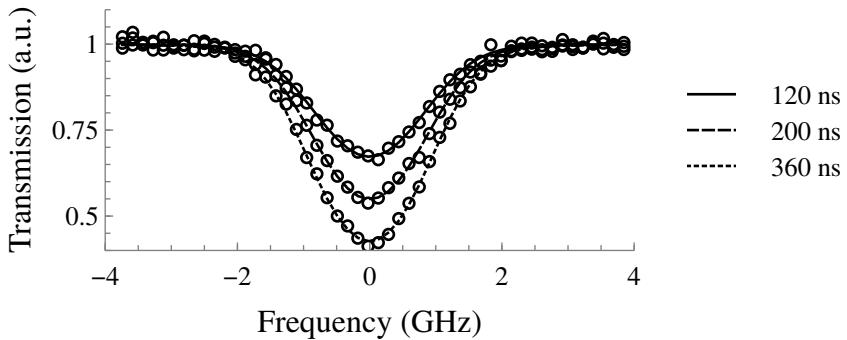


Figure 4.4: Comparison of the measured transmission profile (open symbols) and the computer-generated matches for at several different times for the 4.0 Torr operating condition.

SciPy library [107]. During the matching process, small variations in the center frequency of the laser diode were observed. This was assumed to be the result of long-term variations in the diode temperature that were not adequately compensated for by the temperature control system. The magnitude of these drifts were on the order of  $\pm 60$  MHz between experiments. This fluctuation in center frequency was measured for each experiment and used to correct the wavelengths in the post-processing.

### 4.3 Results

The matching algorithm proved robust enough to automatically match the transmission spectrum at each time step with no user intervention. Figure 4.4 shows three examples of the measured transmission spectra along with the computer-generated matches. The measured data cleanly coalesce to complete transmission far from the peak. In addition, the spectra show no evidence of the noise caused by the discharge. This suggests that the compensation described in the previous section was adequate for these conditions. Across all cases, the total variation in the baseline transmission signal was approximately 0.02. This set a minimum line-integrated detection limit of approximately  $3.0 \times 10^{14} \text{ m}^{-2}$ , though the actual value varied with respect to the pressure and temperature.

### 4.3.1 Temperatures

The temperatures calculated for the metastables from the laser-absorption spectroscopy diagnostic are shown in figure 4.5. Prior to the pulse, the temperature estimates are subject to large variations. This is a result of the low metastable densities which precede the pulse. Without a substantial metastable population, the matching algorithm had difficulty discriminating between a combination of low temperatures and low densities (a small, narrow absorption spectrum) versus high temperatures and high densities (a very broad absorption spectrum).

Though it is not possible to provide an exact value of the errors in the calculated temperatures, the algorithm does provide an estimate of the standard deviation in its results. In all cases, the estimated standard deviation was less than 10 K by the end of the measurement period. Given this value, there appear to be no meaningful trends throughout the measurement period, and between the measurement locations.

In order to more clearly compare the temperatures at the different operating conditions, the results for each location were combined and averaged over the final 200 ns. This was then plotted with respect to the energy deposition calculations from Chapter 3, divided by the gas density. If the discharge was appreciably heating the helium, the temperature would be expected to increase with respect to the density-normalized energy deposition. As seen in figure 4.6 this does not appear to be the case. Indeed, most of the operating conditions show little to no statistical difference between each other and room temperature. The only exception to this is the 16.0 Torr operating condition with a mean temperature of 255 K. As no effort was made to cool the discharge tube, this appears to be an erroneous result. A comparison of the calculated spectra and the original absorption spectra revealed no obvious errors. However, as will be seen later, the metastables were the least dense at 16.0 Torr. This, along with the large variation of the temperatures between time points suggest that the standard deviation in the calculations is higher than estimated.

Only a limited number of similar direct temperature measurements exist within the lit-

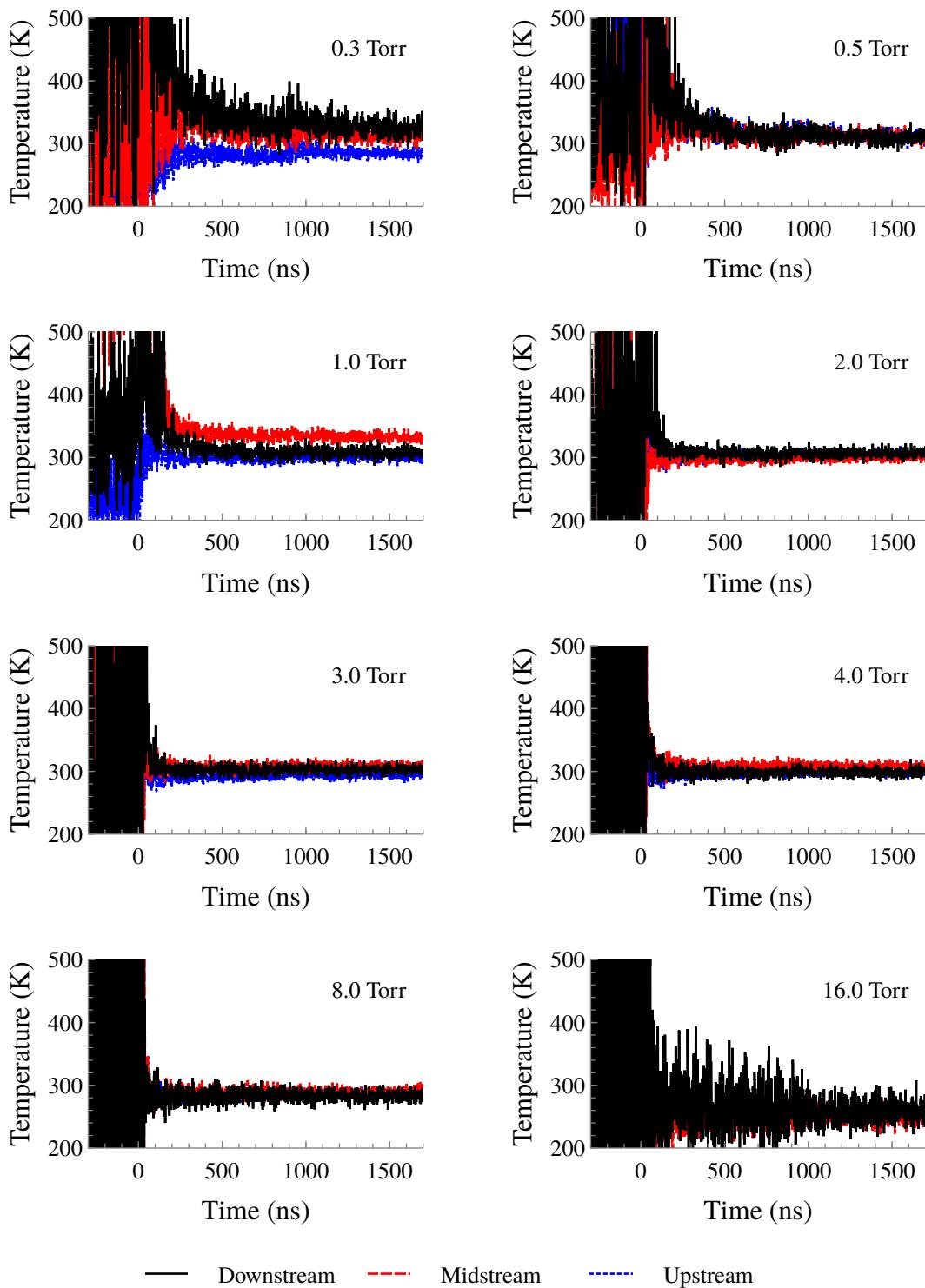


Figure 4.5: Plot of the gas temperatures at each of the operating pressures and each axial location as a function of time.

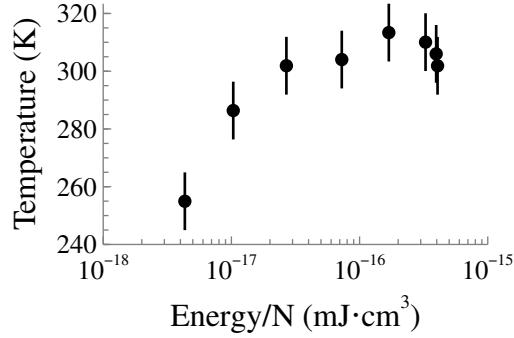


Figure 4.6: Plot of the average gas temperature as a function of deposited energy.

erature. The work of Walsh et al. [84] provides the most direct comparison. In their study, they measured the heating in a planar discharge with helium and a small admixture of oxygen as the working gas. The system was held at atmospheric pressure and had a gas flow rate of 5 slm. Instead of absorption spectroscopy, the rotational spectra of the oxygen was used to determine the temperature. Temperatures ranged from 300-340 K, depending on the average power dissipated in the plasma. Walsh et al. suggested that the observed temperature increase was a result of Joule heating, that is, heating of the gas as a result of electrons colliding with neutral particles. As this process scales with temperature, it would not be expected to be present in the trends from figure 4.6. The presence of a measurable fraction of a molecular gas (oxygen) allows for several other heating mechanisms to occur. Dissociation of the oxygen can impart translational energy to the daughter particles, heating the gas. Additionally, excited the energy contained in rotational and (to a lesser extent) vibrational states can be converted to translational energy in collisions [108].

Other experiments have demonstrated minimal gas heating for RPNDs. Plasma bullets, like those of Laroussi and Lu [82, 83], tend to be associated with minimal heating. However, others have observed measurable heating with temperatures ranging from 400-1000 K [75, 76, 109, 110] (see appendix A for detailed study in air at NASA Glenn Research Center). A comparison of the experimental conditions shows that heating was only observed in molecular gases, though there were cases in which no heating was observed [111], likely

a result of the low repetition rate and energy deposition. These similarities emphasize the importance of the additional heating pathways linked to molecular gases.

For comparison recent simulations and rate calculations [87, 112] have provided estimates of the electron temperature in the range of 10-20 eV. As a result, all of the discharges mentioned are very much nonthermal in nature. That said, the negligible heating in the helium RPND studied here may provide a significant advantage in some applications, as even the moderate temperature increases in molecular discharges can threaten material integrity. For example, most commercial polymers are only rated to 300° C, making them susceptible to damage without careful thermal management.

### 4.3.2 Line-integrated Densities

As described in the analysis section, the laser-absorption spectroscopy also yielded the line-integrated metastable densities. Figure 4.7 shows the metastables dynamics for each operating pressure and at each location. Similar to the temperature measurements, there is a substantial uncertainty during the pre-pulse period for pressures greater than 1.0 Torr. However, for 1.0 Torr and below, there are detectable populations of triplet metastables, around  $7 \times 10^{14} \text{ m}^{-2}$ . These excited atoms are the remnants of the previous pulses which have not been destroyed or left the system. Despite the efforts made to limit the noise in the signals, there is a significant number of erroneous data points in the downstream measurements for pressures below 3.0 Torr. It is not clear why this measurement location was particularly susceptible to plasma-related noise. In all cases, the photodiode remained in the grounded enclosure and only optical components were moved.

In each case, the metastable population exhibits two short bursts at 140 and 280 ns. This is shown in more detail in figure 4.8. The timing of these bursts correlate with the arrival of pulse reflections. This suggests that the even after the plasma has formed, additional pulses are still able to deposit a significant amount of energy in the plasma. This appears to contradict the predictions made by the one-dimensional drift models of Adamovich et

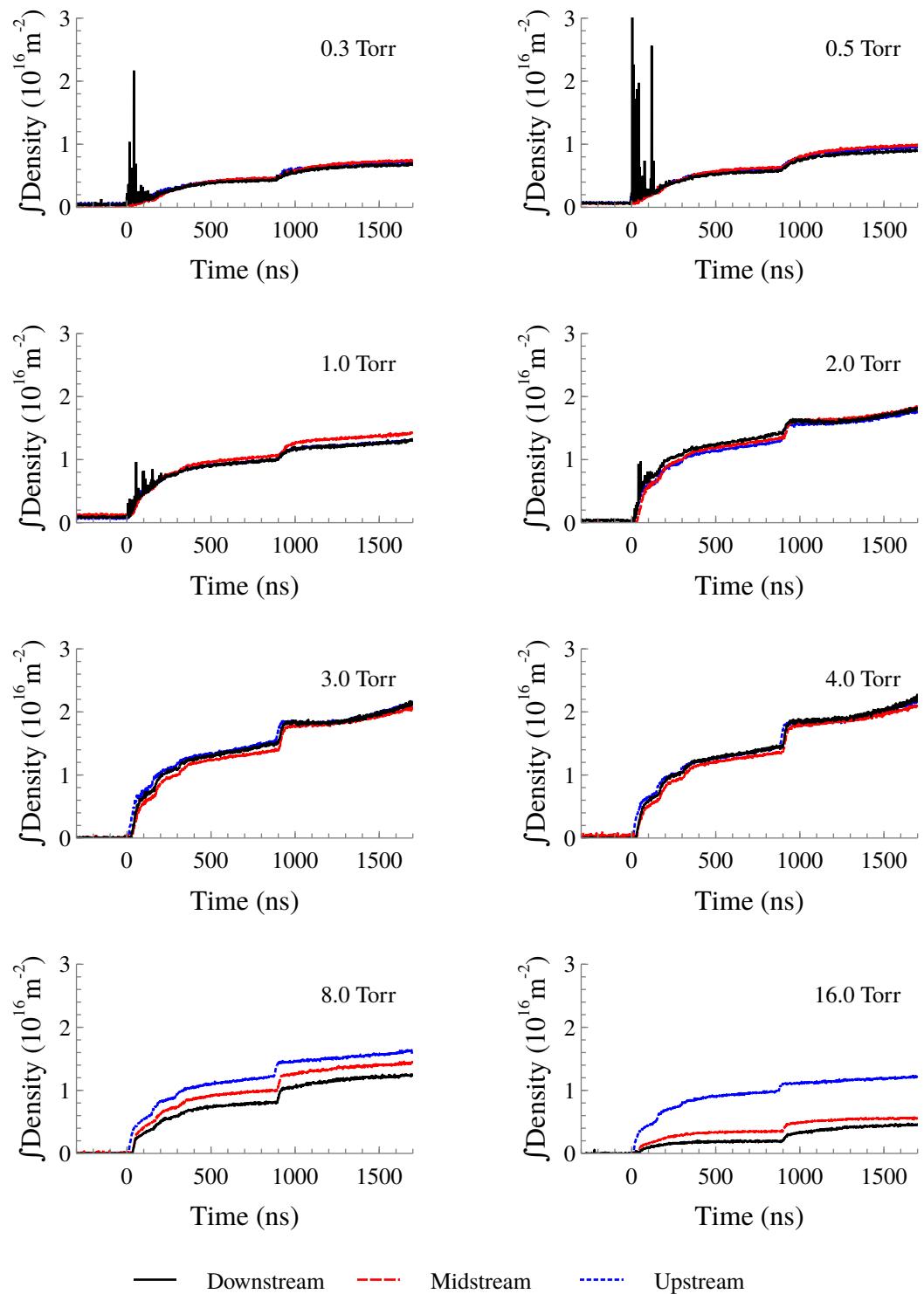


Figure 4.7: Plots of the line-integrated metastable densities at each of the operating pressures and each axial location as a function of time.

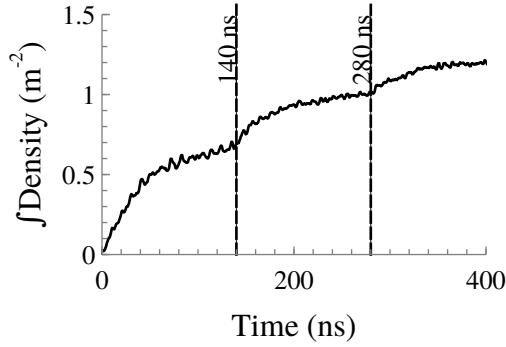


Figure 4.8: Zoomed in view of the increases in metastable density as a result of pulse reflections.

al. [67] and Nikandrov et al. [68] which stated that little energy is coupled into the plasma after breakdown occurs. In addition to the smaller bursts in density, another can be noted at about 900 ns which corresponds to the double-pulsing observed in the current-voltage characteristics of Chapter 3.

By 200 ns after the pulse, the estimated standard deviation in all cases is approximately  $2 \times 10^{14} \text{ m}^{-2}$ . Based on this, it can be concluded that the metastable populations had no significant axial dependence below 8.0 Torr. However, both 8.0 and 16.0 Torr conditions showed notable differences in the metastable population as a function of distance from the anode. As might be expected, the upstream location (closest to the anode) has a high metastable population than the other two. At 16.0 Torr, the line-integrated density at the upstream location was over twice that of either location.

This behavior is reminiscent of that observed by Vasilyak et al. [19] in FIW devices. It was noted that the electric field of the wave would attenuate with distance. In order to interpret this, they considered the wave to consist of two components: a moving ionization front with a finite width, and the plasma left in its wake. They state that the plasma, with its finite conductivity, will have some voltage drop across it, and as it grows, this drop increases. As a results the voltage drop across the ionization front can never be greater than the overall potential applied to the system and is constantly diminishing as it moves away from the

energized electrode. If true, this behavior would be associated with a reduction in the rate of metastable generation in the front, thus explaining the high pressure data in figure 4.7.

In order to compare the metastable measurements to other results, it's necessary to know the density as opposed to the line-integrated value. In this case, it shall be assumed that the metastable atoms are distributed uniformly along the beam path through the plasma. This suggests that the metastable densities in the RPND lie in the range of  $0\text{-}1 \times 10^{12} \text{ cm}^{-3}$ . This is significantly less than the measurements of Stevefelt, Pouvesle, and Bouchoule [113], however their system involved an atmospheric-pressure discharge and energy deposition of up to 0.2 J (compared to a maximum of 5.5 mJ in this experiment). Urabe et al. [114] measured metastable densities of up to  $4 \times 10^{11} \text{ cm}^{-3}$  with laser-absorption spectroscopy in a helium jet at atmospheric pressure. Nersisyan, Morrow, and Graham made measurements suggesting a metastable density of about  $1.5 \times 10^{10} \text{ cm}^{-3}$  in a DBD [115]. Though the discharge was not pulsed, Millard et al. measured densities from  $5 \times 10^9$  -  $1.2 \times 10^{11} \text{ cm}^{-3}$  in helium glow at 2.0 and 5.0 Torr [105]. While none of these experiments are a direct comparison, they do suggest that the results obtained above are within reason.

### 4.3.3 Metastable Destruction

In addition to the fast metastable dynamics, measurements were made of the long-term trends of the metastable populations. Afterglow measurements such as these are less subject to the noise and bandwidth limitations of the short timescale measurements. This makes it possible to obtain relatively clean and precise values for the metastable densities. However, without the applied electric field, the nonequilibrium dynamics of the system rapidly disappear. Therefore, while these measurements provide some insight on the initial conditions, they cannot describe the dynamics of the RPND alone.

That said, a large body of work has been conducted on helium afterglow discharges, which makes this regime attractive as a point of comparison. Furthermore, these measurements include the peak metastable populations for each operating pressure (which are

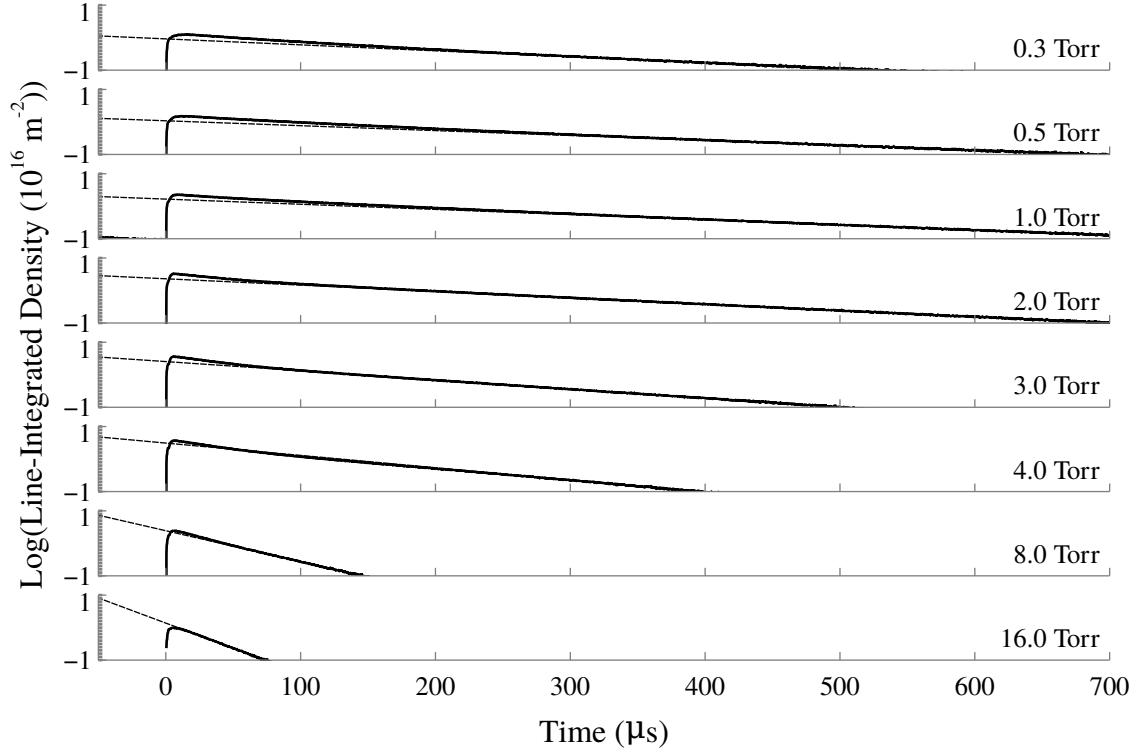


Figure 4.9: Measurements of the long-duration metastable density trends. Exponential fits are indicated by the dotted lines.

missing from figure 4.7). The peak metastable densities and the lifetime of the metastable populations are of interest as they can produce charged particles through Penning ionization of each other or impurities [115]. This extends the ionization period in rare gas RPNDs well past the voltage pulse itself. Also, as seen in figure 2.6, all excited states in the triplet manifold will eventually decay to the triplet metastable level. Thus, a substantial portion of the energy deposited in the plasma is contained in this one level.

Figure 4.9 contains logarithmic plots of the metastable populations for each operating condition, all measured at the midstream location. In addition, an exponential function was fit to the tail of each trend, represented by the dotted line. On these time scales, the destruction of metastables in the RPND apparatus can be described by four different mechanisms: diffusion, Penning ionization of impurities, Penning ionization between metastables, and three-body collisions resulting in helium dimer formation. All processes with the exception

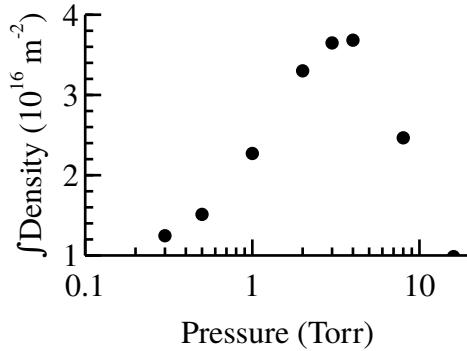


Figure 4.10: Peak line-integrated metastable densities as a function of pressure.

of the Penning ionization between metastables have an exponential dependence, thus any deviation from an exponential decay is likely a result of Penning ionization [116].

As can be seen, a number of the decay curves deviate from a strictly exponential decline. This deviation appears to be more substantial at the lower pressures. For example, the decay at 16.0 Torr appears strictly exponential. Initially, this deviation was believed to be the result of Penning ionization between metastables. The rate at which this takes place is proportional to the square of the metastable density. Therefore, if this is the process responsible for these deviations, it should be most severe for the highest metastable densities. However, per figure 4.10, this is not the case. If Penning ionization between metastables were the dominant loss mechanism, it would be reduced at the lower pressure conditions, contrary to what was observed.

Ultimately, the behavior of the metastable populations in the afterglow can be best understood by a comparison of the depopulation rates for each process. Figure 4.11 illustrates the aforementioned decay processes at 0.3 Torr, for a variety of metastable densities. The rate constants for these processes were obtained from the study by Deloche et al. [116] and the work of Pouvesle et al. [113] (specifically for the rate of Penning ionization of nitrogen impurities). The gas impurities were assumed to be nitrogen, and the mole fraction was assumed to be 80 ppm, as was estimated in Chapter 3.

As can be seen, the dominant loss mechanism above metastable densities of  $2 \times 10^{17} \text{ m}^{-3}$

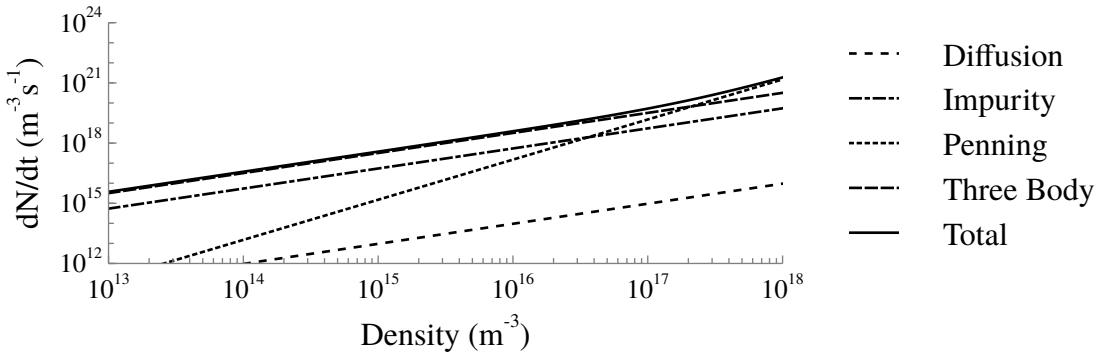


Figure 4.11: Comparison of the decay rates for various processes at 0.3 Torr as a function of metastable density.

was Penning ionization between two metastable atoms. Below this density, the three-body process responsible for dimer formation was dominant. However, the three-body process scales with the square of the neutral gas pressure. As a result, as the pressure is increased this mechanism quickly overtakes all the others. Therefore, the exponential dependence of the decay at higher pressures is not representative of any change in the importance of Penning ionization between metastables, but rather the increasing importance of three-body collisions. This severely restricts the longevity of the metastable states at higher pressures, and reduces their ability to prolong the charged particle population.

From figures 4.11 and 4.9, it can be seen that, aside from the deviations at lower pressures, the decay curves are well-matched by the exponential functions. As a result, it is possible to use the fitting functions to estimate the pre-pulse metastable densities as a function of pressure. These estimates are consistent with the short-scale measurements from figure 4.7. The estimated values of the pre-pulse metastable densities are compiled in table 4.1. along with the decay constants. These results show reasonable agreement with the earlier pre-pulse metastable densities, and are within a factor of two or less. This supports the previous measurements, and provides some confidence that the other extrapolations are also accurate representations of the pre-pulse metastable densities.

The decay constants are about an order of magnitude larger than those recorded by

Table 4.1: Listing of the extrapolated, pre-pulse line-integrated metastable densities, and decay coefficients as a function of pressure.

Pressure (Torr)	Integral Density ( $\text{m}^{-2}$ )	Decay Constant ( $\text{s}^{-1}$ )
0.3	$1.34 \times 10^{14}$	$4.23 \times 10^3$
0.5	$3.36 \times 10^{14}$	$3.47 \times 10^3$
1.0	$4.29 \times 10^{14}$	$3.65 \times 10^3$
2.0	$2.60 \times 10^{14}$	$4.48 \times 10^3$
3.0	$3.94 \times 10^{13}$	$6.47 \times 10^3$
4.0	$5.04 \times 10^{12}$	$8.73 \times 10^3$
8.0	$7.08 \times 10^6$	$2.20 \times 10^4$
16.0	$4.74 \times 10^0$	$3.56 \times 10^4$

Phelps and Molnar [104] at similar pressures. This almost certainly reflects the presence of the impurities in the system. Figure 4.11 shows that impurities are a moderate contributor to the decay of the metastable atoms even at low pressures. Similar measurements and calculations by Deloche et al. [116] confirm the lower decay constants of Phelps and Molnar. In addition, their results showed a relatively consistent proportionality between the electron density and metastable density (on the order of one for every ten). Therefore, these density values may be read as a rough approximation of the electron densities within the RPND.

## 4.4 Summary

A laser diode-based absorption spectroscopy experiment was set up to observe the development of the RPND on short (0-1700 ns) and long (0-700  $\mu\text{s}$ ) time scales. The measurements on the short time scale provide some of the only detailed measurements of the RPND during its development. The design of the system and post-processing software carefully accounted for plasma-related noise, background emissions, and laser drift. The absorption spectra model showed excellent agreement with the measured spectra and the matching algorithm produced consistent and reliable results almost all cases.

Temperature measurements from the Doppler broadening of the absorption spectra showed no appreciable gas heating at any operating pressure. These results contrast with some mea-

surements made in molecular RPNDs where a variety of additional mechanisms are available to transfer kinetic energy from electrons to heavier species.

The line-integrated density results indicate that the plasma is axially uniform across the tube at lower pressures. The 8.0 and 16.0 Torr conditions show significant attenuation in the metastable densities as a function of distance from the anode. This may present a geometric limit to the use of similar RPNDs in material processing. The dominant metastable loss mechanism at low pressures and short time periods is Penning ionization between metastables. However, losses are eventually dominated by three-body dimer formation for all cases. Peak metastable generation is optimized at 4.0 Torr. However, the peak pre-pulse metastable densities, and possibly the electron densities, are optimized at 1.0 Torr. Interestingly, this corresponds with the maximum measured energy deposition from Chapter 3.

These measurements provide an important foundation upon which to develop a more encompassing perspective of how the RPND develops. Specifically, the generation of the metastable atoms is related to a number of other plasma parameters, including: electron density, electron temperature, EEDF, and electric field. Provided a sufficiently detailed model, it should be possible to capture these relationships, and use the measured metastable densities to infer the evolution of these quantities as well as other excited states in the system.

## CHAPTER 5

### Modeling

Though the metastable density measurements appear to be one of only a few diagnostics conducted during the development of the RPND, they only provide a limited view of what is happening. Other quantities, such as the ions, electrons, additional excited states, and fields are all evolving with the metastables. However, these are all closely related and, provided a sufficiently detailed model, it should be possible to infer some or all of these parameters during the development of the RPND. The ideal model would solve equation 2.1, the Boltzmann equation for each species, over the entire geometry, for all velocities, for as long as was required to reach equilibrium.

Unfortunately, these requirements are somewhat problematic. Solutions to the Boltzmann equation alone are difficult [90], let alone for the dozens of species which may be present in the RPND. The spatial discretization can be estimated as the cube of the largest length scale (the discharge apparatus length, about 30 cm) divided by the smallest length scale (on the order of the Debye length, about 20  $\mu\text{m}$ ). This calculation reveals the need for nearly  $2 \times 10^{12}$  spatial cells. Similar calculations can be performed for the time scale (from nanoseconds to minutes) and velocity scale (from thermal to 100s of eV). It quickly becomes apparent that no existing computer could handle such a simulation.

## 5.1 Model Development

Therefore, some approximations of the Boltzmann equation were required in order to obtain a computationally tractable problem. As discussed in Chapter 2, the most common approach, and the one applied here, is the use of *moments* of the Boltzmann equation. These moments average out the velocity dependence of the Boltzmann equation in favor of macroscopic properties such as particle densities and mean velocities. They are often used to develop various fluid approximations for plasmas [91] (e.g. the two fluid model and the magnetohydrodynamic equations). Fluid models have been tremendously successful in the description of everything from plasma display panels [117] to interstellar plasmas [118].

The use of moments of the Boltzmann equation does introduce some additional problems. Reaction rates, such as ionization and excitation, are sensitive to changes in the distribution of particle velocities. This presents a problem when the velocity dependence has been averaged out, as in the case of the fluid models. As a result, a distribution function must be assumed or calculated in order to determine the reaction rates. The Maxwell-Boltzmann and Druyvesteyn distributions from Chapter 2 are often used for this purpose. However, they require a number of assumptions which are not necessarily true for most plasmas. In cases where these distributions cannot be applied, approximate solutions of the Boltzmann equation are often used [119] which employ detailed reaction cross sections to obtain more accurate solutions. The choice of which approach to use is not easy as the EEDF is rarely known *a priori*. Consequently, this topic is considered more thoroughly in section 5.1.2.

From another perspective, fluid models include some or all spatial dimensions. This can lead to simulations that are still computationally demanding depending on the length scales involved. In some cases, the number of species and reactions must be limited in to order to speed up the solution process [90]. For this reason, simulations may only include one or a few excited states. Careful choices of the excited states and reactions can produce excellent results, however this approach can prevent detailed comparisons to spectroscopic data which can reveal information about the degree of equilibrium in the plasma and

the electron temperatures, both of interest in the RPND. Therefore, the model developed here makes additional simplifications in order include additional a large number of excited states and reactions.

As simplifications had already been made to the velocity space, the next logical approach was a simplification of the geometric dependence of the model. Several FIW studies were found to have successfully applied “global models” to their systems [109, 112]. These models eliminate the spatial dependence of the Boltzmann moments in favor of an assumed spatial distribution. This allowed the studies to consider a large number of species and reaction pathways. Following these examples, a decision was made to use a global model in the simulation of the RPND. The final model tracked a total of 32 different excited states of helium from before the pulse until the return of the first reflection. Between these possible states a total of 535 different reaction processes were incorporated including electron-related reactions, radiative processes, and inter-atomic interactions.

In order to compare the metastable measurements to the global results, it was necessary to convert the line-integrated densities from Chapter 4 to volumetric densities, along the path of the laser. It has been noted that a similar FIW [19] and the same RPND [120] exhibited radial variations in emission intensity, electron density, and metastable density. Unfortunately, the cause of these variations is not clearly understood. It has been suggested that high-energy electrons from the walls may be responsible [121]. However, lacking any empirical, theoretical, or numerical results with which describe the evolution of the radial profile during the discharge, the metastable distribution was simply assumed to be uniform. This assumption likely affects the inferred plasma parameters, however more accurate results are possible provided time-resolved measurements of the radial metastable density or an improved understanding of the RPND.

### 5.1.1 Continuity Equation

Equation 2.4, the continuity equation, forms the basis for tracking the populations of the excited states in the plasma. Eliminating the spatial gradients reduces this to,

$$\frac{dn_\alpha}{dt} = G_\alpha - L_\alpha, \quad (5.1)$$

where  $\alpha$  identifies the particle species,  $G$  is the gain term, and  $L$  is the loss term. The gain and loss terms represent all possible reactions which can alter the population of  $\alpha$ . The model presented incorporates helium states up to  $n = 4$ , helium ions, and electrons. It should be noted that helium dimers and impurities were also likely present in the experimental discharge. However, they were neglected in the case of this model. As observed in Chapter 4, the total e-folding time for the metastable decay was approximately  $25 \mu\text{s}$ . This indicates that the processes associated with the dimers and impurities are irrelevant on the sub-microsecond time scale.

There were several possible processes that were considered for inclusion in the model:

- electron impact ionization,
- electron impact (de)excitation,
- atomic impact (de)excitation,
- atomic excitation transfer,
- dielectronic recombination,
- three-body recombination,
- radiative decay, and
- diffusion.

As with the impurities and dimer formation, diffusion occurs on a much longer time scale, and was subsequently neglected. Three-body recombination in the volume of the discharge is not important at the estimated temperatures and densities [90], therefore this too was neglected. In general, dielectronic recombination is a rare process [122], however it was incorporated in early versions of the model and was subsequently retained. Inter-atomic excitation and de-excitation is not generally considered important given the low energies of the atoms in discharges.

The remaining processes were found to be the most important for the RPND. This included electron-impact ionization and excitation which dominated the short time-scale dynamics. In addition, excitation transfer between atoms was found to occur at rates relevant to the simulation period [90]. Likewise, radiative decay occurred fast enough relative to the simulation period to necessitate inclusion [102].

For these processes, equation 5.1 was rewritten as,

$$\frac{dN_i}{dt} = n_e \left[ \sum_{j \neq i} N_j K_{j,i}^e(T_e) - N_i \sum_{j \neq i} K_{i,j}^e(T_e) \right] + \left[ \sum_{j > i} N_j K_{j,i}^o - N_i \sum_{j < i} K_{i,j}^o \right] + N_g \left[ \sum_{j \neq i} N_j K_{j,i}^a - N_i \sum_{j \neq i} K_{i,j}^a \right]. \quad (5.2)$$

Here, the subscripts of  $i$  and  $j$  represent different states of helium,  $N$  is the state density,  $K$  is a rate coefficient,  $T_e$  is the electron temperature, and  $N_g$  is the neutral helium density. The first subscript of the rate coefficients represents the initial excited state while the second coefficient represents the final excited state. Therefore,  $K_{ij}$  is a rate coefficient for a process that transfers an atom from state  $i$  to state  $j$ .

The equation is split into three sets of processes, represented by the superscripts of the rate coefficients:  $e$  - electron impact processes,  $o$  - radiative decay, and  $a$  - atomic excitation transfer. Therefore, the first bracketed term on the right hand side contains all the rate coefficients for electron impact excitation and de-excitation (including ionization). The second bracketed term contains the rate coefficients for optical transitions in and out of the excited state. The final bracketed term contains the gains and losses as a result of excitation transfer caused by collisions with the ground state (collisions between excited states are relatively rare).

The rate coefficients in equation 5.2 are compiled from a number of different sources. The optical transition rates and the energies of each level were obtained from the NIST Atomic Spectra Database [102]. The excitation transfer rate coefficients came from the

studies of Catherinot and Dubreuil [123, 124]. Coefficients were only available for the transitions with  $\Delta n = 0$  and  $n = 3, 4$ . No constants were found for other excitation transfer reactions. The dielectronic recombination rates were adapted from the work of Nahar [122].

The semi-empirical relations derived by Ralchenko et al. [125] were used to calculate the electron (de)excitation and ionization cross sections for levels through  $n = 4$ . At the time of writing they were the most accurate set of cross sections available for neutral helium with a quoted accuracy of 10-30% for  $\Delta S = 0$ , and  $> 30\%$  for  $\Delta S \neq 0$ . Only reactions resulting in an energetically uphill reaction were tabulated. The inverse or superelastic cross sections were calculated using the principle of detailed balance [100],

$$\sigma_{ji}(\varepsilon) = \frac{\varepsilon}{\varepsilon - \Delta\varepsilon_{ij}} \frac{g_j^2}{g_i} \sigma_{ij}, \quad (5.3)$$

where  $\Delta\varepsilon$  is the threshold energy of the  $ij$  reaction and  $g$  is the statistical degeneracy of the corresponding state. These cross sections can be used to calculate the rate coefficients for each reaction using equation 2.5. However, this equation requires an appropriate EEDF and leads back to the topic of which one is appropriate for the RPND.

### 5.1.2 Distribution Effects

Per the discussion of the Boltzmann equation in Chapter 2, there are two analytic equilibrium solutions: the Maxwell-Boltzmann distribution, and the Druyvesteyn distribution. However, research by Starikovskaia and Starikovskii [24] has shown that the EEDF in a nitrogen FIW can deviate from both. This is not surprising given the non-equilibrium nature of the FIW discharge. Since the RPND shares many of its properties, there was the possibility that the equilibrium solutions would not apply to the RPND either.

In order to better understand the energy distributions in a RPND, a numerical study of the EEDF in a helium RPND was conducted. First, a particle-in-cell (PIC) code was used to simulate the effect of a voltage pulse on electrons in a quasi zero-dimensional geometry.

This generated an evolution of the EEDF in a helium plasma as a function of time. Then, the mean energy for the EEDF was calculated for a series of time steps. These values were then used to generate equivalent Maxwell-Boltzmann distributions and approximate solutions of the Boltzmann equation.

PIC simulations do not attempt to solve the Boltzmann equation directly. Instead, they simulate the behavior of many plasma particles in an experimental geometry using the basic laws of motion and electromagnetism [6]. A discrete EEDF can then be calculated from the particle population (or subset thereof). As the number of simulated particles increases the discrete EEDF will approach the continuous EEDF which would result from a solution of the Boltzmann equation. The relatively small number of assumptions used in PIC simulations suggest that its results will be the most accurate representation of the EEDF in a RPND.

Generally, PIC simulations do not use a one-to-one correspondence between computer particles and physical particles—most plasmas involve more particles than can be reasonably simulated. Instead, they treat a population of macro-particles, each of which possesses some statistical weight [6]. This allows the macro-particle to represent a group of physical particles. The macro-particles each possess velocities and positions which are continuous within the limits of floating point representation. However, the electromagnetic fields are spatially discretized. This necessitates a mapping of the particle-related fields to the discretized coordinates, and the force of the fields from the discretized coordinates to the particles.

Each PIC simulation begins with a definition of the system geometry and the external fields. Some specified number of macro-particles with a known distribution of velocities are then placed within this geometry. After these steps have been completed, the physics loop, illustrated in figure 5.1, begins. The equations in the loop reflect a one-dimensional system, thus each macro particle possesses only one spatial component,  $x$ . However, the simulation supposes the existence of a magnetic field which induces motion perpendicular to the simulation domain. Thus, each macro-particle possesses a velocity vector,  $\vec{v}$ , with three components.

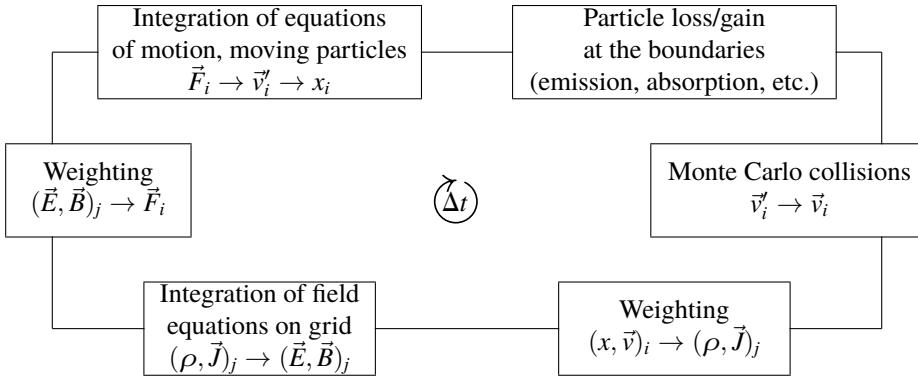


Figure 5.1: Schematic description of the PIC simulation process, adapted from [6].

The loop generally begins with an initial field calculation based on the external fields combined with that of the particles. This is followed by a particle “push” where the Lorentz equation,  $\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$ , is used to calculate a new position for a given time step,  $\Delta t$ . Afterward, particles which have moved out of the boundaries of the system are removed from the simulation. Next, collisions (including ionization and excitation) are modeled using Monte Carlo methods [6]. Finally, the fields of the macro-particles are mapped to the spatial grid, the total fields are recalculated, and the next time step begins.

The XDPD1 code, developed by Verboncoeur et al. [126], was used for the PIC simulations. The code was originally designed to simulate a one-dimensional discharge between two parallel electrodes. However, collection at these electrodes complicated the study of the EEDF and did not correspond well to the zero-dimensional nature of the global model. Charged particle collection near the boundaries induced spatial variations in the EEDF. Additionally, the high mobility of electrons often meant that they were preferentially collected on short time scales. This led to the formation of large regions of positive space charge which shielded the plasma from the applied electric field.

In order to address these issues, the code was modified to use periodic boundary conditions. Such conditions resulted in a quasi zero-dimensional simulation, equivalent to a plasma of infinite extent. This eliminated the issue of spatial variations in the EEDF and

was more consistent with the assumptions that led to the development of the global model.

Previous measurements of the electric field in a similar FIW found that the electric field values varied from 0-350 Td [87]. Based on these results, it was decided to examine the distribution characteristics over the range of 10-600 Td. In each case, the electric field was applied from the start of the simulation. Though the actual field in the RPND has a finite rise and fall, the use of an impulse field exacerbated non-equilibrium characteristics of the EEDF. Therefore, the results of these PIC simulations would overestimate deviations from equilibrium solutions of the Boltzmann equation.

Helium gas was used as the background gas and was kept at a pressure of 2.0 Torr for all simulations. An initial plasma was assumed to exist within the volume with a density of  $1.0 \times 10^8 \text{ cm}^{-3}$ . The plasma was considered quasineutral (equal numbers of ions and electrons), and was modeled with one computational particle for every  $10^6$  physical particles. Electrons were initialized with a thermal energy of 2.0 eV, and the helium ions were given an initial energy of 0.025 eV (equal to room temperature).

XPDPI's internal set of cross sections were used. These included: elastic scattering, atomic excitation, and charge exchange. The cross sections had a semi-empirical form which increased linearly with energy to a peak value. After the peak they declined as the logarithm of the energy, divided by the energy [126]. The time domain of the simulation was 10 ns. This period was long enough to observe fast EEDF dynamics associated with the impulse electric field. A time step of  $4 \times 10^{-13} \text{ s}$  was used to satisfy the Courant-Friedrich-Lowy stability condition. However, the EEDF was only sampled every 0.25 ns. The spatial domain of the code was 10 cm, discretized at  $1 \mu\text{m}$  intervals.

BOLSIG+ was used to obtain the approximate solutions of the Boltzmann equation [119]. This is a publicly available computer code which uses the two-term expansion of the Boltzmann equation to solve for the equilibrium EEDF in a given electric field. It uses Legendre polynomials to expand the EEDF into an unperturbed component with a small, superimposed, perturbation. This assumes that the distribution is accurately represented by

this type of superposition. In reality, this assumption does not hold for large electric field values. In the case of BOLSIG+, solutions for helium fail to converge for fields approaching 1000 Td.

The solver was initialized with the cross sections for helium generated by Alves and Ferreira [127]. The temporal growth model for electrons was used, and the electron-electron collisions were neglected as a result of the low ionization fraction in the RPND (about  $10^{-5}$ ). Solutions were calculated for the range of mean energies observed in the PIC (about 2-50 eV). A cubic, nearest-neighbor interpolation scheme was then used to generate an EEDF for the precise mean energies for each time step of the PIC simulations.

These same energies were used to determine equivalent Maxwell-Boltzmann distributions for comparison. The EEDFs generated by the PIC simulations, approximate Boltzmann solutions, and Maxwell-Boltzmann distributions can be seen in figure 5.2, as a series of contour plots on a logarithmic scale. The jaggedness of the PIC simulations results from the finite number of particles in the system and the low probability of high energy electrons. This problem is ameliorated at higher electric fields where the probability of high-energy electrons increases. It is also helped by the ionization processes which begin to occur after the first few nanoseconds.

At 10 Td, the EEDFs are relatively unchanged over the duration of the simulation. The subtle slopes of the contours suggest a small increase in the overall temperature and energy of the system as a function of time. This is more noticeable at 30 Td, where the contours have a more distinct slope. The spacing between the slopes is relatively constant for each case—equivalent to a Maxwell-Boltzmann distribution. However, there is some deviation at low energies in the case of the BOLSIG+ solutions.

At 60 and 100 Td, the PIC results begin to exhibit contour spacings which are consistent at low energies, but begin to grow at higher energies. This is evidence of a growing population of high-energy electrons, in excess of what is predicted by a Maxwell-Boltzmann distribution. Interestingly, the BOLSIG+ solutions exhibit unique contour shapes which are

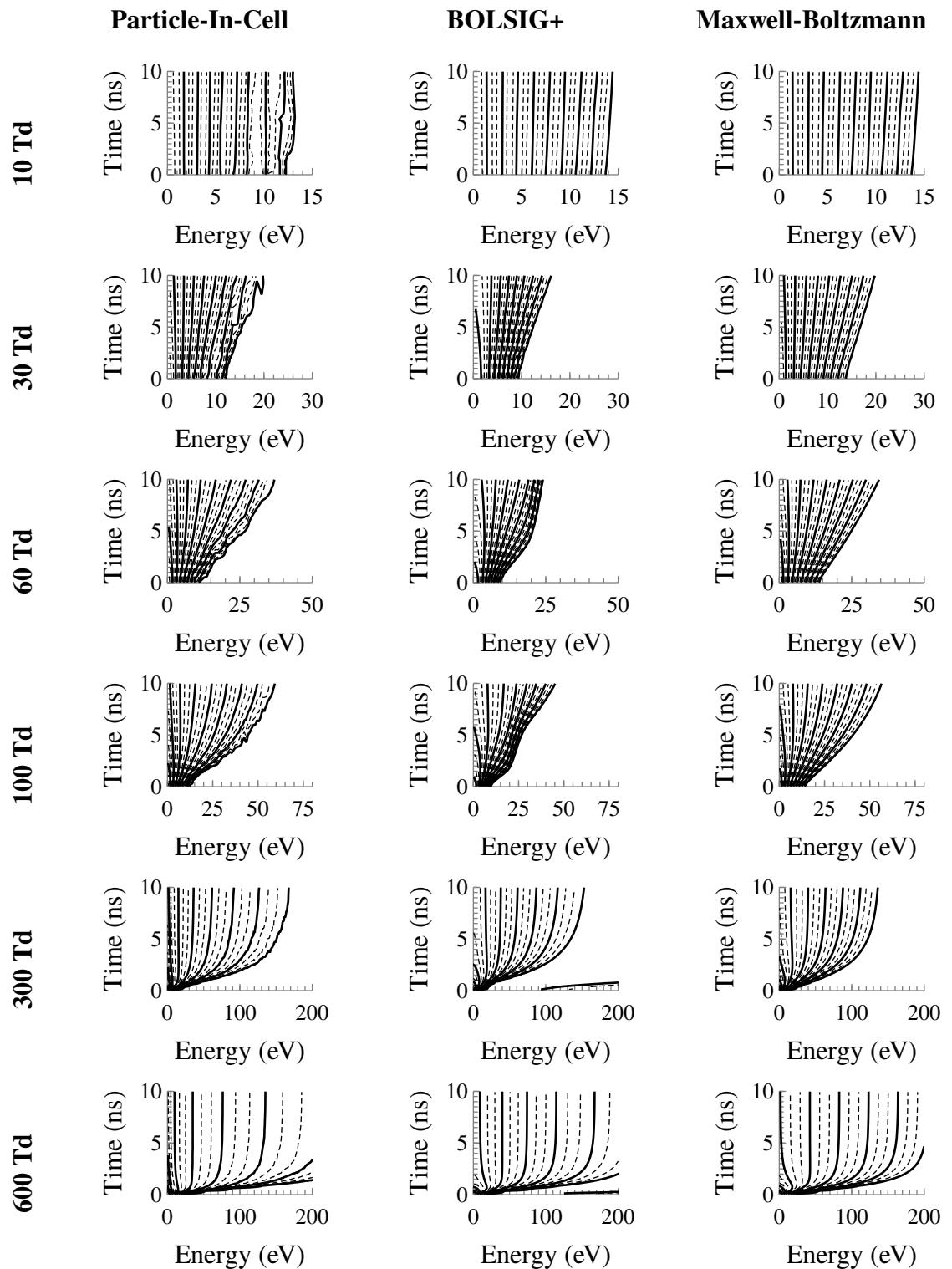


Figure 5.2: Contour plots of the EEDFs determined from PIC simulations, and the corresponding Maxwell-Boltzmann distributions for a range of electric fields.

inconsistent with the other cases. Additionally, the spacing of the contours is less consistent, with a dearth of high energy electrons.

By 300 and 600 Td this situation is reversed, as the Maxwell-Boltzmann distributions begin to underestimate the population of high energy electrons. Examination of the individual distributions shows that the PIC EEDFs have a larger population of low energy (less than 20 eV) and high energy (greater than 100 eV) electrons. This can be explained by the general shape of the cross sections. The only reactions available to electrons in the PIC simulations are elastic scattering, excitation (19.6 eV threshold), and ionization (24.6 eV threshold). As the inelastic processes turn on at energies in excess of the 20 eV, the electron population undergoes depletion. Likewise, the electron population begins to rebound at higher energies as the cross sections fall off.

Unlike Starikovskaia and Starikovskii's results [24] the various approaches produce comparable EEDFs. Generally, the Maxwell-Boltzmann results provide the best match to the PIC simulations at electric fields of 100 Td and below. Conversely, the BOLSIG+ results better represent the EEDF past 100 eV at the higher field values. That said, these electrons do not provide a large contribution to the excited states of the plasma. They are well past the excitation and ionization cross section peaks and are relatively few in number. Given the larger computational burden of the Boltzmann solver and the small perceived benefit, it was concluded that the that the Maxwell-Boltzmann distributions provided an adequate representation of the EEDF for the global model.

### 5.1.3 Energy Equation

With an EEDF the rate coefficients in equation 5.2 can be calculated. However, as was seen in figure 5.2, the distribution function changes over time. Previously, the PIC simulations were used to determine the time evolution of the mean electron energy, but an alternate approach was required for the global model.

With suitable assumptions, equation 2.7 (the second moment of the Boltzmann equation)

can provide the means by which the mean energy can be evolved with each time step. Given the assumptions underlying the global model, the spatial derivatives can be neglected such that

$$\frac{d}{dt} \left( \frac{3}{2} p_e \right) = \frac{d}{dt} \left( \frac{3}{2} p_e \right) \Big|_{\text{coll}}. \quad (5.4)$$

Using the isothermal equation of state [90],  $p = n k_B T$ , this can be rewritten as,

$$\frac{d}{dt} \left( \frac{3}{2} n_e k_B T_e \right) = \frac{d}{dt} \left( \frac{3}{2} n_e k_B T_e \right) \Big|_{\text{coll}}. \quad (5.5)$$

The term on the RHS is the collision operator which expresses energy gained or lost by electrons<sup>1</sup> in particle collisions.

Several different types of energy transfer were considered by the global model. The first was the heating caused by the electric field. This was followed by electron energy losses as a result of elastic scattering by the atoms. Finally, inelastic collisions with all helium states through  $n = 4$  were considered. Together, these phenomena replace the term on the RHS of equation 5.5 with,

$$\frac{e^2 n_e E(t)^2}{m_e k_m(T_e) N_g} - n_e k_m(T_e) N_g \left( \frac{3m_e}{M} \right) \frac{3}{2} k_B (T_e - T_g) - n_e \sum_i \sum_{j \neq i} K_{ij}^e N_i \Delta \varepsilon_{ij}, \quad (5.6)$$

where  $E(t)$  is the time-varying electric field,  $k_m$  is the electron momentum transfer frequency from Pack et al. [128], and  $\Delta \varepsilon_{ij}$  is the energy lost or gained by the electron in atomic (de)excitation reactions. The first term includes the DC conductivity [90] of the plasma, and accounts for the heating of the electrons by the electric field. The second term is the elastic cooling of the electrons by the neutral atoms, where the gas temperature. The third term is the energy gained or lost by the electrons in atomic (de)excitation reactions. The equations 5.6, 5.5 and 5.2 form the primary components of the global model. Together they can

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<sup>1</sup>In some plasmas, it is desirable to also treat gas heating with a similar equation as it can have an appreciable impact on certain rate constants. However, as noted in Chapter 4, the gas temperature of the **rpdn!** in question remains at room temperature.

be used to solve for the evolution of the electron temperatures, electron densities, excited state densities, and plasma emissions as functions of time.

### 5.1.4 Model Solutions

For the purposes of computation, equation 5.2 can be rewritten for each atomic state,  $i$ , resulting in a set of linear, first order differential equations,

$$\begin{aligned} \frac{d}{dt} \begin{pmatrix} N_1 \\ N_2 \\ \vdots \\ N_M \end{pmatrix} &= n_e \begin{pmatrix} -\sum_{j \neq 1} K_{1,j}^e & K_{2,1}^e & \dots & K_{M,1}^e \\ K_{1,2}^e & -\sum_{j \neq 2} K_{2,j}^e & \dots & K_{M,2}^e \\ \vdots & \vdots & \ddots & \vdots \\ K_{1,M}^e & K_{2,M}^e & \dots & -\sum_{j \neq M} K_{M,j}^e \end{pmatrix} \cdot \begin{pmatrix} N_1 \\ N_2 \\ \vdots \\ N_M \end{pmatrix} \\ &+ \begin{pmatrix} 0 & K_{2,1}^o & \dots & K_{M,1}^o \\ 0 & -\sum_{j < 2} K_{2,j}^e & \dots & K_{M,2}^o \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & -\sum_{j < M} K_{M,j}^e \end{pmatrix} \cdot \begin{pmatrix} N_1 \\ N_2 \\ \vdots \\ N_M \end{pmatrix} \\ &+ N_g \begin{pmatrix} -\sum_{j \neq 1} K_{1,j}^a & K_{2,1}^a & \dots & K_{M,1}^a \\ K_{1,2}^a & -\sum_{j \neq 2} K_{2,j}^a & \dots & K_{M,2}^a \\ \vdots & \vdots & \ddots & \vdots \\ K_{1,M}^a & K_{2,M}^a & \dots & -\sum_{j \neq M} K_{M,j}^a \end{pmatrix} \cdot \begin{pmatrix} N_1 \\ N_2 \\ \vdots \\ N_M \end{pmatrix}, \end{aligned} \tag{5.7}$$

where  $M$  is the total number of atomic states and  $\varepsilon_i < \varepsilon_{i+1}$ . An additional equation can be added to separately account for electrons as and electron-specific processes, however the global model used here assumed quasineutrality by enforcing the relation  $N_{\text{ion}} = n_e$ . Changes in the density of each atomic state were calculated by numerical integration of these equations. The range of time scales exhibited by the RPND made it desirable to implement adaptive control of the time step size. For this reason, the Runge-Kutta-Fehlberg method,

adapted from Bradie [129], was used as the integration scheme.

The initial metastable densities came from the LAS measurements while the initial electron densities were determined from LCIF measurements made by Weatherford [121]. Electron density measurements were only available for 1.0, 4.0, and 8.0 Torr therefore, the global model analyses only consider these conditions. Sensitivity to changes in the initial electron density will be addressed in the following section.

It was necessary to assume a pre-pulse electron temperatures as no such measurements were available. Given the relatively long period of time between pulses, an initial temperature of 0.2 eV was used. Exploratory simulations found that changes in the initial electron temperature had a negligible impact on the final distribution of excited states. Initial excited state densities (not including ions and metastables) were determined from the 0.2 eV equilibrium distribution of states. Per the results from Chapter 4, the neutral gas temperature was fixed at 300 K for the duration of the simulation.

Despite access to the waveform of the applied potential, the actual time-evolution of the electric field at the metastable measurement points is not well known. This is a result of the distinctly nonlinear impedance of the RPND plasma. Takashima et al. performed measurements of the electric field in a FIW using a capacitive probe and found it to be significantly different from the vacuum field. Separately, Ito et al. [79] and Müller et al. [80], measured the electric fields in a RPND with a 1.2 mm gap between parallel electrodes using a wave-mixing approach. They too found a large difference between the vacuum field and the actual field.

In all three cases, the evolution of the electric field could be best described by a Gaussian-like pulse, followed by a small, persistent electric field. This persistent field was on the order of 20-25% of the peak field value, and would remain for at least several tens of nanoseconds. The total duration and magnitude of the persistent field varied between studies and some, such as the work of Anikin et al. [130], did not find evidence of it. Given the uncertainty associated with the nature of this persistent field, the global model simulations only consid-

Table 5.1: Nominal simulation parameters for the 4.0 Torr operating condition.

Pressure (Torr)	Initial Electron Density ( $\text{m}^{-3}$ )	Pulse width (ns)	Peak Electric Field (Td)
4.0	$5.36 \times 10^{13}$	40	207

ered a single Gaussian pulse. The time domain of the simulations covered 190 ns with the peak of the pulse centered at 40 ns.

## 5.2 Perturbation Study

The input values for the initial metastable density, electron density, and pressure were fixed. However, the same could not be said for the peak electric field and the width of the pulse. It was initially expected that the pulse-width would be approximately equal to the width of the applied pulse, 25 ns. The global models were matched to the metastable measurements by iterative adjustment of the peak electric field and the pulse-width. However, there was no clear means by which to estimate the error in the global model calculations.

In order to provide a qualitative understanding of the possible error, a preliminary fit of the 4.0 Torr data was made and used as a benchmark. Subsequent simulations were run with small perturbations to the peak electric field, pressure, pulse-width, and initial electron density. In each case, the benchmark value was perturbed by  $\pm 10\%$ .

The nominal conditions of the simulation are recorded in table 5.1 and results of these simulations are shown in figure 5.3. The metastable trends suggest that the initial electron density has a relatively small impact on the metastable dynamics. Closer examination reveals that the final metastable densities change by approximately  $\pm 10\%$ , almost one-to-one with the initial electron density. In contrast, changes to the pulse-width produce much more significant changes in the metastable densities. As the pulse-width is increased, the metastable densities increase. As the electric field was fixed for these simulations, this change can be attributed to the increase in energy deposited in the electron population.

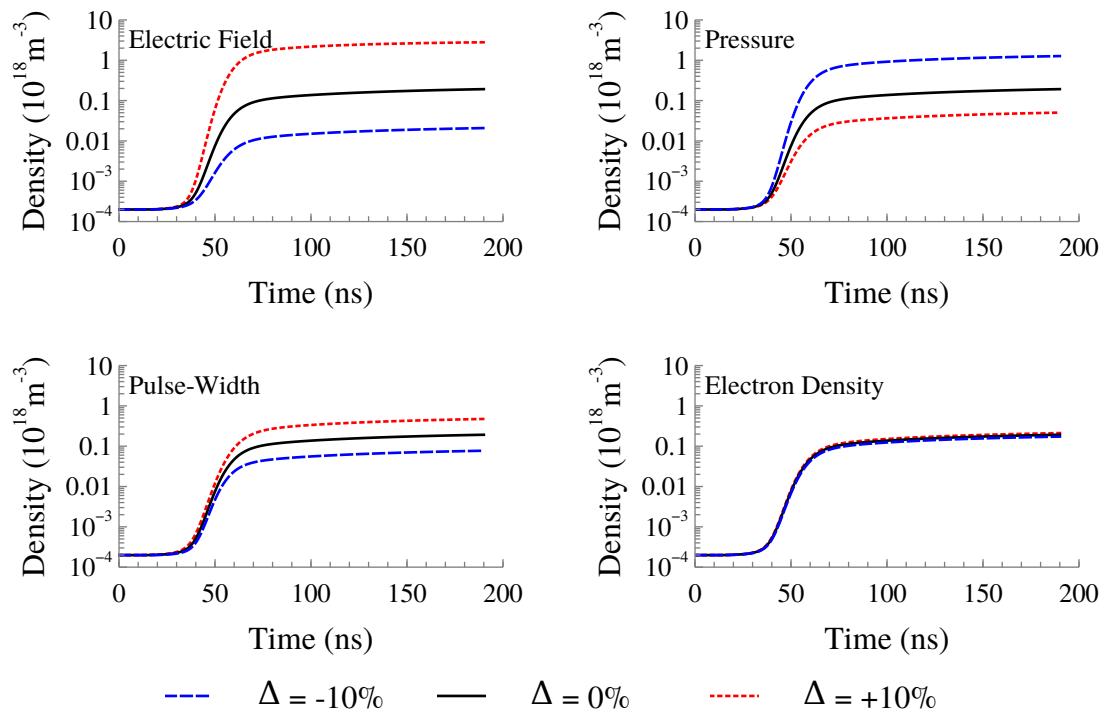


Figure 5.3: Simulations showing the effects of perturbations to the initial conditions on the metastable dynamics.

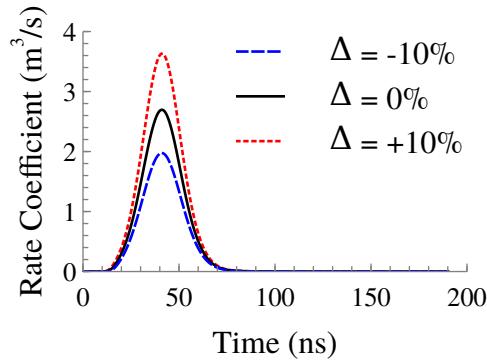


Figure 5.4: Ionization rates coefficients corresponding to the perturbed electric field simulations.

The two most influential factors in the determination of the metastable densities were the neutral gas pressure and the electric field. The perturbations to these quantities resulted in largest changes in the final metastable densities. As can be seen in figure 5.3, increases in pressure corresponded to a decrease in metastable densities. Changes to the neutral gas pressure tend to affect the system via several different mechanisms. As seen in equation 5.6, increases to the gas pressure tend to decrease the energy deposited in the electrons, and increases losses due to elastic scattering. This reduces the energy that can be deposited in excited states. However, the reduced electron energy density competes with the increased number of ground state atoms available for excitation. The perturbation results indicate that the reduced energy deposition in the electrons is more significant than the increased availability of neutral atoms.

The large influence of the electric field can be traced back to changes in the ionization rate for each condition. As seen in figure 5.4, the magnitude of the ionization rate coefficient corresponds to the magnitude of the electric field. While the changes are somewhat modest, as seen in Chapter 2, ionization processes exponentially with time. This means that small changes to the rate coefficient manifest as large differences in the final electron density. Since the rate of metastable generation is proportional to the electron density, large changes to the electron density equate to large changes in the metastable density.

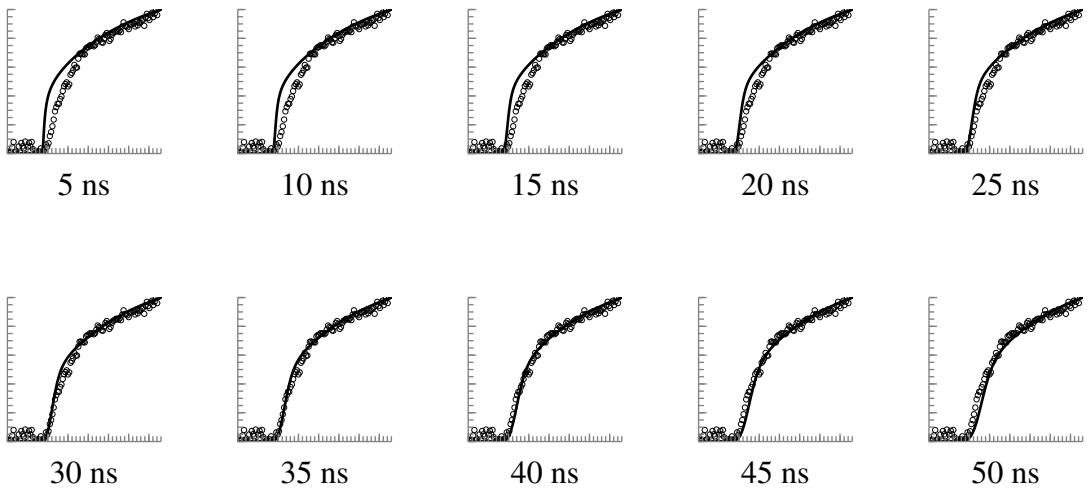


Figure 5.5: Comparison of measured metastable values (represented by open circles) to simulations with a range of pulse-widths.

### 5.3 Plasma Dynamics

The plasma dynamics for the 1.0, 4.0, and 8.0 Torr conditions were obtained by iteratively matching the pulse-width and peak electric field to the metastable density immediately before the arrival of the reflected pulse. The process was somewhat complicated by the fact that multiple combinations of the peak field and pulse-width could produce the same metastable density. Therefore, it was necessary to fix or otherwise predict one of the values.

Of the two, the pulse-width was the most promising to eliminate as a variable. The characteristics of the applied pulse already provided a bound on the possible widths. Therefore, the 4.0 Torr condition was simulated with a range of pulse-widths from 5-50 ns with the peak field selected to produce the same final metastable density in each case.

The metastable density trend for each pulse-width is compiled in figure 5.5. It is immediately apparent that the short pulse-widths do not provide an optimal description of the data. This includes the results for the 25 ns simulation which shows a much high production rate of metastables than was observed in the experiment. The time resolution of the experimental measurements was determined by the photodiode which had a response time of 5 ns.

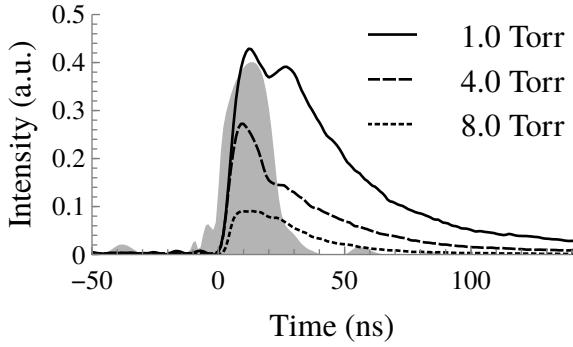


Figure 5.6: The emissions of the  $4^1\text{P}^{\circ}$ - $2^1\text{S}$  transition in the RPND, overlaid on top of the voltage pulse.

Therefore, the slowed change in metastable density appears to be a real phenomena. This suggested that the effective pulse-width in the RPND extended longer than the duration of the applied voltage. Indeed, the best match of the data for the illustrated simulations occurs for a pulse-width of 40 ns.

The results of the pulse-width comparison suggested that additional excitation was taking place beyond the applied pulse. In order to determine the origin of this excitation, a survey was made of the neutral emissions spectra. The details of these measurements will be discussed in more detail in Chapter 6. The strongest signal was observed at 396 nm, corresponding to the  $4^1\text{P}^{\circ}$ - $2^1\text{S}$  transition. The emissions from this transition were measured as a function of time, producing figure 5.6. Here the emissions for each operating condition have been overlaid on the applied voltage pulse for comparison. The voltage pulse clearly coincides with an initial increase in the number of helium atoms occupying the  $4^1\text{P}^{\circ}$  state. 15 ns later, another increase is visible, particularly at 1.0 and 4.0 Torr. This second transient is similar to the return strokes observed in streamer research [34, 36, 131]. The observation of return strokes in similar studies [19, 75, 132] suggests that this is a reasonable explanation for the double-peaked emissions. If the forward and return strokes possess durations equal to the applied voltage (25 ns), separated by 15 ns, then the excitation period would be approximately 40 ns. This is consistent with the pulse-width required to match the observed

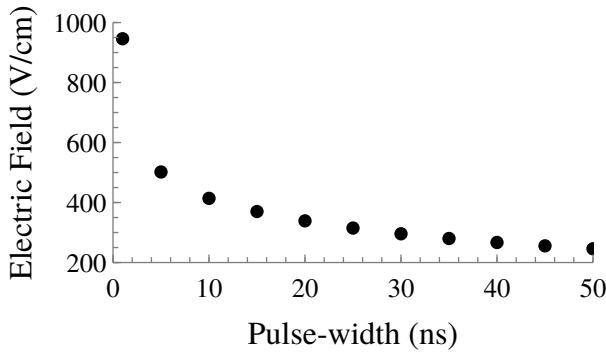


Figure 5.7: The electric fields necessary to generate the same metastable density at 4.0 Torr as a function of the pulse-width.

data. As a result, a pulse-width of 40 ns was used in all subsequent simulations.

Figure 5.7 is a scatter plot of the peak electric fields necessary to obtain the same final metastable density as a function of the pulse-width. Initially, as the pulse-width is decreased from 50 ns, only small increases of the electric field are required to obtain the same number of metastable atoms. However, as the pulse-width is decreased further, the rate at which the electric field must increased grows substantially.

Eventually, for short enough pulses, it is no longer possible to maintain the same metastable density, regardless of further increases in the electric field. This occurs for the same reason that the EEDF from the PIC simulations was depressed between 20 and 100 eV—eventually, the cross sections fall off with increasing electron energy. This places an upper limit on the rate coefficient as a function of electron temperature and a limit to the number of metastables which can be generated in a given period of time. Figure 5.8 shows the ionization and metastable rate coefficients as functions of the electron temperatures in the system. The ionization rate coefficient peaks at approximately 320 eV, while the metastable rate coefficient peaks much lower at around 23 eV. These rate coefficients, along with the general form of the cross sections for the reactions, show that there is an optimal field strength for ionization and excited state generation. Further increases in the electric field would only serve to reduce to reduce the final density of these particles. However, there may be additional

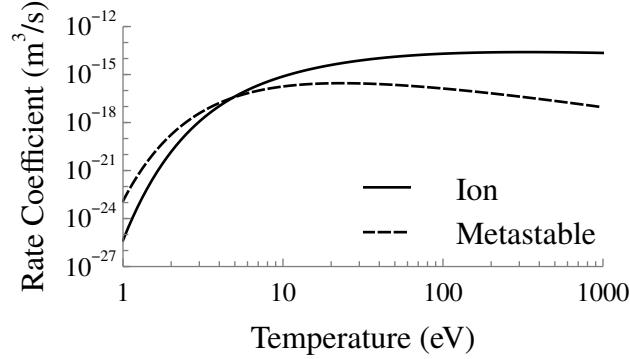


Figure 5.8: Ionization and metastable rate coefficients as functions of electron temperature.

benefits in the use of a higher electric field. The runaway electrons which can be generated at these field strengths, described by Vasilyak [19] among others, could help increase the discharge volume and homogeneity via nonlocal energy deposition.

Figure 5.9 shows the comparison of the measured metastable densities for 1.0, 4.0, and 8.0 Torr overlaid atop the applied voltage pulse<sup>2</sup>. As seen in chapter 4, there was little axial variation in the metastable measurements at 1.0 and 4.0 Torr. For this reason, simulations were conducted only for the measurements at the midstream positions. In contrast, the axial distribution of metastables showed noticeable variation at 8.0 Torr. Therefore, each location was considered independently in the simulations.

Despite the assumptions involved in the development of the global model, the simulation results show impressive agreement with the measurements. This includes the period of 0-40 ns when the metastable growth rate is the largest. The plasma behavior during this time is dominated by energetic electrons that have been accelerated by the large electric fields. Given the relatively short period, inter-atomic and radiative processes play a relatively unimportant role. The most significant discrepancies appear in the 1.0 Torr simulations where the global appears to overestimate the metastable density during the pulse.

The global model also performs well in the afterglow period, from 40 ns to the end

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<sup>2</sup>The relative timing of the metastable measurements and the voltage pulse are approximate. Corrections were made in post-processing to account for different cable lengths in the system.

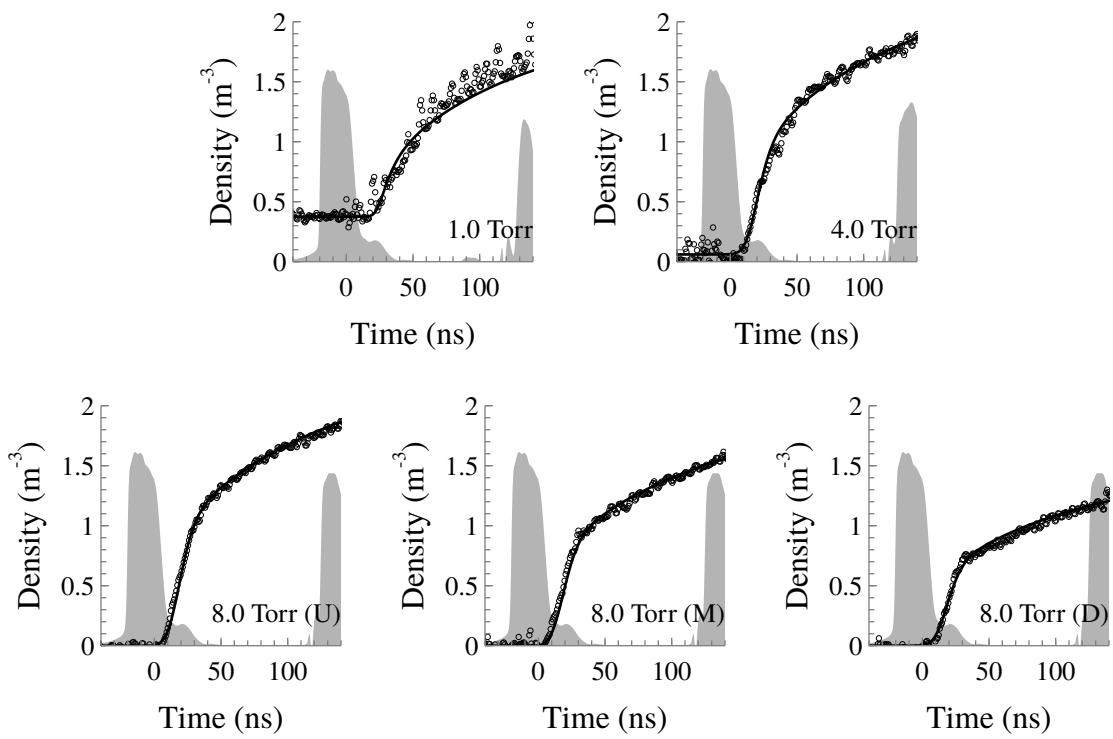


Figure 5.9: Comparison of the measured metastable densities (open circles) to the global model simulations. The shaded region illustrates the applied voltage pulse. The parentheses following the 8.0 Torr labels indicate the axial location of the measurement.

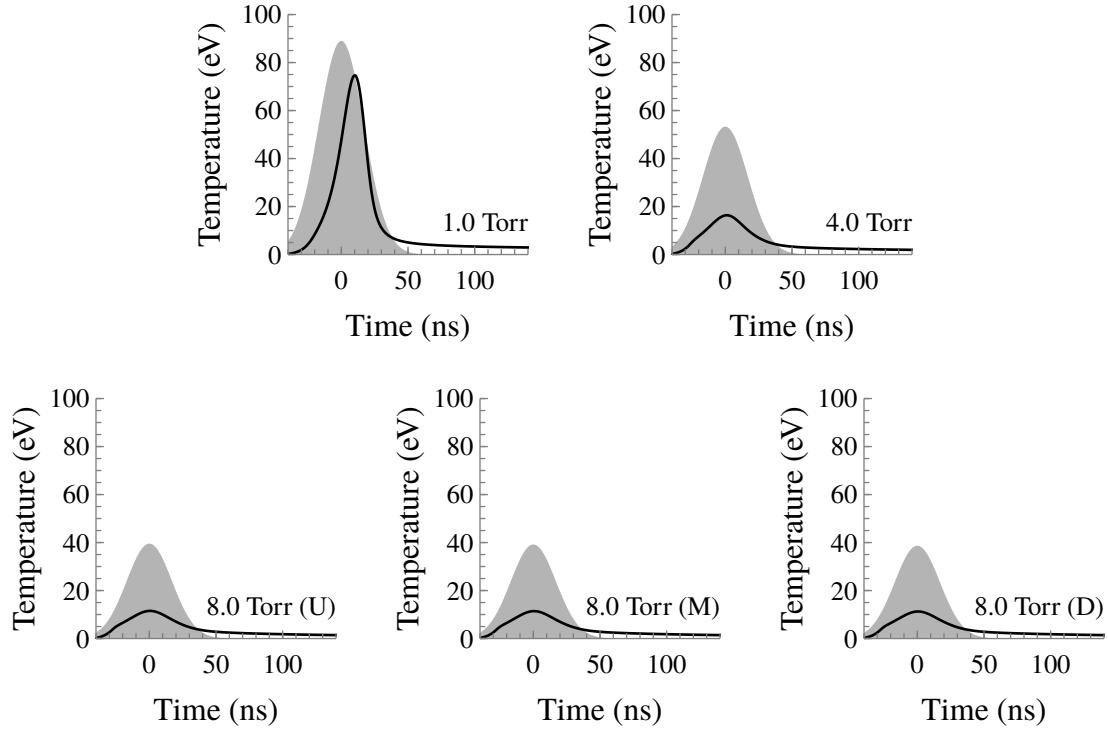


Figure 5.10: Global model predictions of the electron temperatures at the simulated conditions, overlaid on the corresponding electric field.

of the measurements. After the pulse, the electrons begin to undergo rapid cooling, as seen in figure 5.10. By 50 ns, the electron temperatures have fallen below 10 eV in all cases, and by the end of the simulation they are all below 3 eV. As a result of this rapid cooling, the rate of electron-induced reactions falls significantly. As was seen in figure 5.8, the rate for metastable and ion generation begin to undergo a fast decline at temperatures below 10 eV. This indicates that much of the metastable growth after 50 ns can be attributed to downward radiative transitions from upper excited states. Again, the most significant discrepancies appear for the measurements at 1.0 Torr. In this case, the simulations appear to underestimate the total metastable population.

The issues in accurately simulating the 1.0 Torr case may be a result of the large electric field present in the system. As can be observe in table 5.2 the electric field approaches 350 Td for the 1.0 Torr discharge. This corresponds to the regime in which the Maxwell-

Table 5.2: Summary of the peak values for several plasma parameters from the global model simulations.

Pressure (Torr)	E/N (Td)	T <sub>e</sub> (eV)	N <sub>m</sub> (m <sup>-3</sup> )	n <sub>e</sub> (m <sup>-3</sup> )
1.0	346	74.6	$1.62 \times 10^{17}$	$5.06 \times 10^{17}$
4.0	207	16.3	$1.87 \times 10^{17}$	$3.36 \times 10^{17}$
8.0 (Upstream)	154	11.5	$1.88 \times 10^{17}$	$2.57 \times 10^{17}$
8.0 (Midstream)	152	11.4	$1.57 \times 10^{17}$	$2.14 \times 10^{17}$
8.0 (Downstream)	150	11.3	$1.21 \times 10^{17}$	$1.65 \times 10^{17}$

Boltzmann distribution (as well as the BOLSIG+ results) begin to deviate from the PIC predictions. Specifically, the Maxwell-Boltzmann distribution tended to overestimate the number of electron in the range of 20-100 eV at high electric fields. These are precisely the electrons which are responsible for the generation of the metastable states. This suggests that the assumption of a Maxwell-Boltzmann distribution would tend to overestimate the metastable generation at large electric fields, consistent with what is observed in figure 5.9.

As the global model is applied to increasing pressures, the reduced electric field begins to fall. Likewise, the electron temperatures are also reduced, from about 75 eV down to 12 eV. Despite these changes, the final metastable densities remain approximately the same. Though the temperatures are lower, they still peak near the maximum in the metastable rate coefficient in figure 5.8. Additionally, the large number of neutral gas particles ensures that the total metastable production rate remains large.

Notably, the metastable densities and electron densities peak for different conditions. The electron density trends can be observed in figure 5.11 overlaid on the reduced electric fields. The electron density peaks at the lowest simulated pressure whereas the metastable density peaks at 4.0 Torr. Again, this can be seen as a result of the rate coefficients for the respective reactions. The ionization rate coefficient continues to increase well past 100 eV, whereas the metastable rate coefficient decreases after 23 eV. While the increase in electron density competes with the decline in the metastable rate coefficient, ultimately the rate

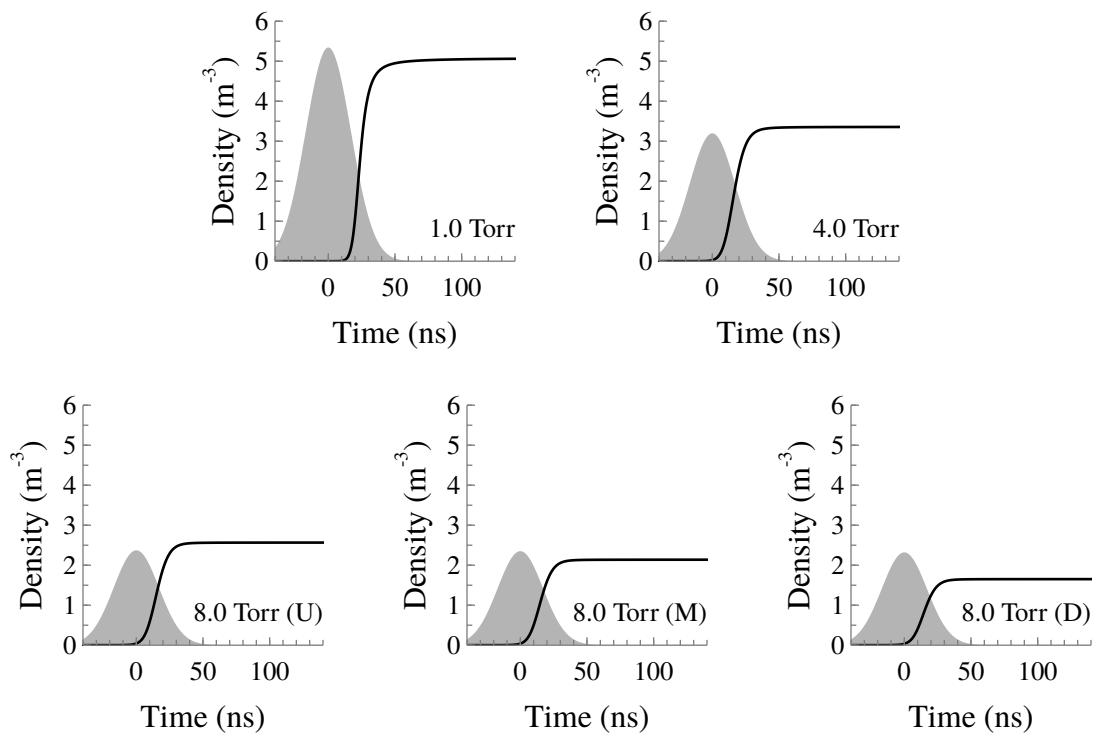


Figure 5.11: Global model predictions of the electrons densities at the simulated conditions overlaid on the reduced electric field.

coefficient falls too quickly.

Also observable in the evolution of the electron densities is a time-delay between the peak electric field and peak electron production rate for all conditions. For the cases under consideration the peak ionization rate occurs at about 23.5 ns at 1.0 Torr, 16.4 ns at 4.0 Torr, and 15.5 ns at 8.0 Torr. In contrast, the electron temperatures in figure 5.10 show little to no such delay. In part, this behavior reflects the need for a finite amount of time before the background electrons gain ionization-relevant energies. Additionally, the electron growth process is relatively slow at first given the low initial densities. This explanation is consistent with the initial electron densities measured by Weatherford [121] which showed the largest pre-pulse density at 8.0 Torr, and the smallest at 1.0 Torr.

Finally, the behavior axial behavior in the 8.0 Torr condition exhibits several interesting characteristics. At the position closest to the anode, the peak metastable density exceeds that of operation at 4.0 Torr. This contrasts with the position furthest from the anode which features the lowest measured metastable density for this range of conditions. However, the electric field and electron temperatures across all three locations only vary by about one percent. This recalls the electric field sensitivity that was noted in the earlier perturbation study and suggests that even small variations in the electric field of the RPND can have large implications on its homogeneity.

## 5.4 Summary

The metastable density measurements were only able to provide limited insight on the development of the RPND. However, production of the metastable atoms is determined by a number of other plasma quantities such as electron temperature, density, and electric field strength. Following a series of assumptions, a global model simulation was developed in order to infer the dynamics of these other quantities. The development of the model carefully considered the choice of distribution function and the sensitivity to various initial condi-

tions.

A comparison of several preliminary simulations to measured metastable data indicated the need for an electric field with a duration longer than applied voltage pulse. Examination of the plasma emissions showed that the extended excitation could be attributed to a return stroke in the system. Use of this extended excitation time yielded excellent agreement for all but the 1.0 Torr condition. In this case, what appeared to be mild deviations appeared with the model overestimating metastable production rate during the pulse, and underestimating it afterward. Given the large electric fields in this condition, these discrepancies can most likely be attributed to differences between the assumed EEDF and those in the actual device.

It was found that breakdown of the RPND was accompanied by a finite delay between the peak electric field value and the peak ionization rate. As the generation of electrons is essentially exponential, this appeared to be the result of the low pre-pulse electron densities and the finite heating time. Interestingly, the peak electron and metastable densities did not coincide. Instead, highest predicted electron density occurred at the same condition as optimal energy coupling to the plasma, as seen in Chapter 3. Simultaneously, as will be seen in Chapter 6, the peak metastable density is associated with the peak brightness of the plasma, the largest number of excited states, and the highest wave velocity. These contrasting results demonstrate that the RPND can be optimized for one of two conditions: production of excited atomic states, or ionization.

## **CHAPTER 6**

### **Population Kinetics**

## **CHAPTER 7**

### **Conclusions**

## **APPENDIX A**

### **Measurements in an Air RPND**

As early as 2001, researchers have proposed the use of a novel, hybrid engine design for use in supersonic and hypersonic flight [133]. In some ways similar to an earlier program [134], it suggested that magnetohydrodynamic (MHD) accelerators were an enabling technology for hypersonic transport. Briefly, a MHD accelerator could be used to simultaneously produce energy and slow the inlet airflow. This would allow the use of a conventional turbojet engine at speeds well above its normal operational range.

However, MHD accelerators require an ionized fluid flow. Even at the high altitudes associated with hypersonic flight, this is not easy to achieve. Originally, Macheret suggested the use of electron beams, carefully tuned to coincide with the peak in the ionization cross section in air. However, the use of electron beams in the ionization of high pressure gases is accompanied by a large number of technical issues, similar to those of some excimer lasers. Therefore, in 2002, Macheret et al. proposed the use of a RPND to produce an “electron beam” *in situ* [64] akin to the beams observed in certain FIW studies.

The use of a RPND is accompanied by a reduced ionization efficiency in comparison to an electron beam. However, it reduces the some of the implementation challenges and Macheret argued that it offered a more efficient and stable option than breakdown with DC electric fields. Though the densities of FIWs in several air-related chemistries have been measured on several occasions [63, 112, 130, 135], similar studies do not appear to exist for RPNDs in air. Therefore, there is a need for electron density measurements to confirm that

RPNDs are adequate for the MHD accelerator requirements and to quantify their ionization efficiency.

In addition, previous studies of FIWs in air have observed fast gas heating of molecular systems [109]. Up to 40% of the input energy can be converted into translational energy through dissociation of oxygen and quenching or electronically excited nitrogen states. As the RPND physics are very similar to that of the FIW, there is the possibility that it may also cause fast gas heating. In combustion, this can play an important role in the chemistry, flame holding, and ignition delay. More generally, gas heating can impact material processing and ionization efficiency. As such, it is important to develop reliable temperature diagnostics for RPNDs in molecular gases.

This appendix records the development of two diagnostics for an air RPND at NASA Glenn Research Center (GRC). Measurement of the electron density was accomplished using millimeter-wave interferometry. Plasma interferometry measures changes in the phase and amplitude of an electromagnetic wave which has passed through the plasma [90]. The phase shift is proportional to the density of electrons while the change in amplitude is related to the electron-neutral collision frequency. As with other wave-based techniques, the density resulting from this approach is line integrated. The translational temperature of the system was measured via

Translational temperatures were measured by analysis of the rotational spectra associate with the second positive system of nitrogen. Rotational spectra result from changes in the rotational quanta of a molecule. As the energy spacing of the rotational levels is generally quite small (often on the order of  $10^{-4}$  eV), inter-molecular collisions can easily redistribute them [136]. Provided enough collisions, the distribution of rotational states should reflect the distribution of translational energy for the molecules.



Figure A.1: Vacuum chamber used in RPND experiments at the NASA GRC along with an intensified CCD used for fast imaging.

## A.1 Discharge Apparatus

Experiments were conducted in a cylindrical vacuum chamber, reproduced in figure A.1, with a volume of approximately 30 L. The chamber was evacuated by a Varian TriScroll 300, scroll pump and the pressure was monitored by a capacitance manometer. Before each experiment the chamber pressure was reduced to below 100 mTorr, after which the chamber was sealed from the pump by a bellows valve. The chamber was then back-filled with ambient air until the pressure reached 20.0 Torr.

The discharge was sustained between two parallel cylindrical electrodes, 2.5 cm in diameter and 0.625 cm in length. In the interferometry experiment, the electrodes were mounted in a silicone-based dielectric epoxy, cast such that it was flush with the faces of the electrodes. Optical emission experiments eliminated the dielectric epoxy in favor of a machinable ceramic and slightly different geometry, seen in figure A.2. This choice was made as a result of damage observed to the epoxy molds. Plasma breakdown appeared to be occurring at the interface of the mold and the electrodes. The use of the Mykroy fitting allowed longer duration operation necessary for the optical emissions measurements.

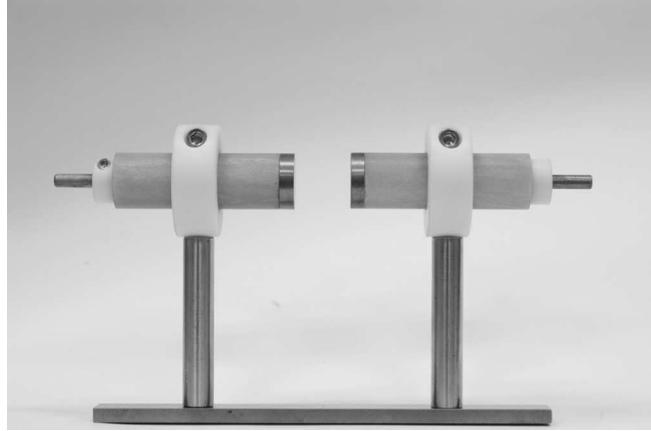


Figure A.2: The electrodes used in the RPND at NASA GRC. The electrodes are made of copper with a ceramic sheath made of Mykroy.

The power supply was built by FID (model FPG 60-100-MC4-S5) and supplied voltage pulses of up to 60 kV at repetition rates from 6-100 kHz with pulsewidths of 5 ns. Unless otherwise stated, all measurements were made with the power supply operating at 20 kHz using a Wavetek FG3C as the master clock.

Maintenance of the electrodes and other components of the discharge apparatus required that the chamber volume regularly be brought up to atmospheric pressure. When the discharge was initiated after the chamber was returned to the 20.0 Torr operating pressure, a pressure transient was observed. This transient caused the chamber pressure to rise by about 2.0 Torr after several minutes of operation, after which the pressure would remain relatively stable. This was believed to be caused by the outgassing of the discharge apparatus surfaces. Throughout operation, the pressure would continue to increase at a greatly reduced rate, on the order of several tenths of a Torr per minute.

## A.2 Millimeter-Wave Interferometry

Traditionally, plasma interferometry has been conducted with microwaves, as the electron densities in processing plasmas cause readily observable phase shifts at these wavelengths. However, results from similar RPNDs [24] suggested that the electron densities could ap-

proach  $10^{13}$  cm $^{-3}$ . Such densities exceed the cutoff wavelength of microwave interferometers [90]. As a result, it was necessary to use millimeter-wave (mmW) interferometry which uses much higher frequencies in order to avoid this issue.

### A.2.1 Theory

The theory underlying interferometry can be found in many plasma diagnostic textbooks, however the majority of the treatments only concern plasmas in which there are no neutral particles. In contrast, the work of Akhtar et al. [137] introduces a frictional force to the derivation which accounts for the effects of neutral particles. Following this approach, the theory below provides the necessary set of equations in order to determine the electron density and collision frequency provided measurements of the mmW phase shift and change in amplitude.

The derivation begins with the motion of electron in an oscillating electromagnetic field. The position of a charged particle in such a field can be found from the non-relativistic Lorentz equation,

$$F = q(E + v \times B), \quad (\text{A.1})$$

where  $F$  is the force on the particle,  $q$  is its charge,  $E$  is the electric field,  $v$  is the particle's velocity, and  $B$  is the magnetic field. In the case of a weak electromagnetic field (such as in interferometry) the magnetic field component can be assumed to be zero. Without loss of generality, the equation may be reduced to a single dimension. Afterward, the drag force which accounts for the neutral particle collisions can be introduced. The acceleration of the electron can then be written as

$$\ddot{r} = -\frac{eE}{m} - v_{\text{eff}} m_e \dot{r}, \quad (\text{A.2})$$

where  $r$  is the position of the electron,  $e$  is the elementary charge,  $v_{\text{eff}}$  is the effective rate of momentum transfer, and  $m_e$  is the mass of the electron.

The electric field of the incident mmW can be expressed as  $E_0 e^{i\omega t}$  where  $E_0$  represents the peak field strength and  $\omega$  is the angular frequency. The form of  $E$  suggests a sinusoidal solution such that  $r \propto e^{i\omega t}$ . Solving the differential equation for  $\dot{r}$  yields

$$\dot{r} = -\frac{eE}{m_e} \frac{v_{\text{eff}} + i\omega}{v_{\text{eff}}^2 + \omega^2}. \quad (\text{A.3})$$

This is the drift velocity of the electron. It can be used to solve for the complex plasma conductivity and, subsequently, the dielectric constant. This allows one to write the complex propagation coefficient for the mmW,

$$\gamma = \alpha + i\beta, \quad (\text{A.4})$$

where the real component,  $\alpha$ , results in a decay of the wave amplitude.  $\beta$  on the other hand, induces a phase shift in the wave. The full solution for the separate propagation components is given by Akhtar [137] as,

$$\beta = \frac{\omega}{c} \left\{ \frac{1}{2} \left( 1 - \frac{\omega_p^2}{\omega^2 + v_{\text{eff}}^2} \right) + \frac{1}{2} \left[ \left( 1 - \frac{\omega_p^2}{\omega^2 + v_{\text{eff}}^2} \right)^2 + \left( \frac{\omega_p^2}{\omega^2 + v_{\text{eff}}^2} \frac{v_{\text{eff}}}{\omega} \right)^2 \right]^{1/2} \right\}^{1/2}, \quad (\text{A.5})$$

$$\alpha = \frac{\omega}{c} \left\{ -\frac{1}{2} \left( 1 - \frac{\omega_p^2}{\omega^2 + v_{\text{eff}}^2} \right) + \frac{1}{2} \left[ \left( 1 - \frac{\omega_p^2}{\omega^2 + v_{\text{eff}}^2} \right)^2 + \left( \frac{\omega_p^2}{\omega^2 + v_{\text{eff}}^2} \frac{v_{\text{eff}}}{\omega} \right)^2 \right]^{1/2} \right\}^{1/2}. \quad (\text{A.6})$$

From these components, explicit solutions can be derived for the electron density and ef-

fective collision frequency,

$$\nu_{\text{eff}} = 2 \frac{c^2}{\omega} \frac{\alpha \beta}{\xi}, \quad (\text{A.7})$$

$$n_e = \frac{m_e \epsilon_0}{e^2} \xi (\omega^2 + \nu_{\text{eff}}^2), \quad (\text{A.8})$$

where  $\xi = 1 - (\beta^2 - \alpha^2)c^2/\omega^2$ . The values for  $\alpha$  and  $\beta$  come from the experimental measures of the phase shift and change in amplitude,

$$\Delta\varphi = \int_0^d (\beta_0 - \beta) dr, \quad \text{and} \quad (\text{A.9})$$

$$\Delta A = \int_0^d (\alpha_0 - \alpha) dr, \quad (\text{A.10})$$

where  $\Delta\varphi$  is the phase change,  $\Delta A$  is the amplitude change,  $d$  is the pathlength through the plasma, and  $\alpha_0$  and  $\beta_0$  are free space propagation values. As any measurements are integrated over the pathlength of the system, it is necessary to make some assumption about the variation of the density with respect to the path of the wave. In this case, the density will be assumed to be constant along the path of the wave.

## A.2.2 Experiment

The mmW interferometry was conducted using an HP 8510C network analyzer operating at 75 GHz. The network analyzer was controlled by a LabView script and had a maximum sample rate of 5 Hz. Each sample required approximately 100  $\mu$ s to complete.

The mmW signal was transmitted between two test sets which produced a variable frequency signal covering all of the V band (50-75 GHz). The output of each test set was connected to a high gain horn. The horns were aligned perpendicular to the axis of the discharge and transmitted through quartz windows on either side of the vacuum chamber. The horns were aligned by a maximization of the transmission through the chamber. During data analysis, the pathlength of the signal through the plasma was assumed to be 2.5

cm, however diffusion results in the transport of electrons outside of the discharge region, making this value an underestimate.

During operation, the actual pressures within the vacuum chamber varied from 19.9 to 22.6 Torr. The power supply was operated in a bipolar mode with one electrode pulsed to +9 kV and the other pulsed to -9 kV. Previous interest in the use of a DC sustainer discharge [65] prompted an investigation of the effects of the sustainer on the time-averaged electron density. The sustainer consisted of a pair of floating electrodes, perpendicular to the RPND. The sustainer electrodes were held at a potential difference that was slightly less than the DC breakdown voltage. The intended effect of the sustainer was to increase the time-averaged plasma density through additional ionization.

### A.2.3 Results

The original intent was to obtain a measurement of the electron density as it evolved during and after the pulse. However, the acquisition rate of 5 Hz prevented acquisition of the electron density evolution for a single pulse. Instead, it necessitated measurements spanning several minutes and many thousands of pulses. This made it necessary to determine the repeatability of the plasma produced by these pulses.

This is generally not an issue in systems which feature gas flows, such as those studied by Adamovich et al. [67]. However, in this case, the vacuum chamber was sealed. This mode of operation can cause a slow accumulation of chemical species, increases in gas temperature, deposits on electrode surfaces, and more. Each of these has the ability to slowly alter the nature of the discharge and can complicate analysis of data acquired after different pulses.

Measurements were made of the electron density for a period of 30 minutes at a rate of 5 Hz. A SRS DG535 was used to trigger the network analyzer at the same delay after each pulse. Acquisition for longer periods were prevented as a result of significant electromagnetic interference EMI. The master clock was particularly susceptible to this electrical noise. This would occasionally shut off the triggering signal or alter its frequency. Several

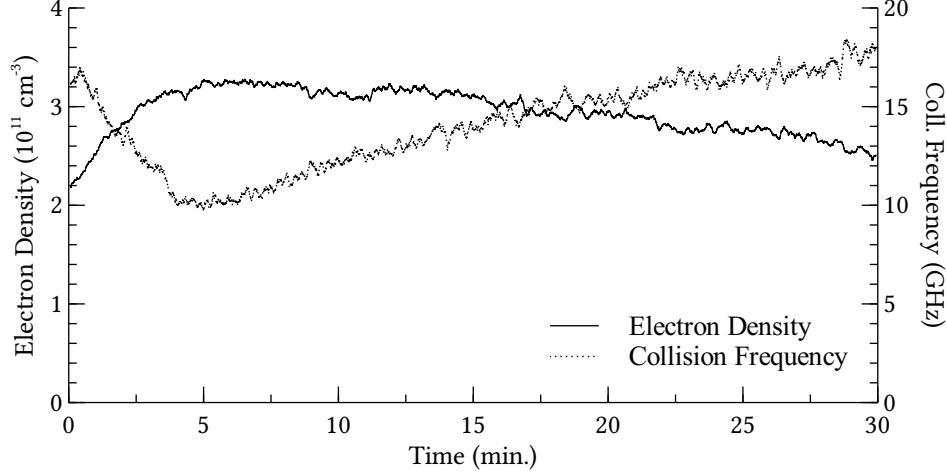


Figure A.3: The evolution of the density (—) and the collision frequency (··) in a RPND over a period of 30 minutes. These quantities reach their respective maximum and minimum after approximately five minutes, however these are not equilibrium values. The RPND continues to change over long durations.

attempts were made to limit the interference to the signal generator through shielding of the transmission cables and of the signal generator, however these attempts resulted in minimal benefit.

Figure A.3 shows the calculation of the electron densities and collision frequencies from the measured phase and amplitude changes. The data shown does not include the operation of the DC sustainer. The data appear to confirm the concern that the sealed vacuum chamber causes long-term variations in the plasma. The electron density changes by nearly 50% during the first five minutes of operation and is followed by a slow decline over the next 25 minutes. Simultaneously, the effective collisions frequency of the electrons ranges from 10-18 GHz. Overall, the electron density ranged from  $2.25-3.25 \times 10^{11} \text{ cm}^{-3}$ . This is somewhat less than the anticipated density. As previously noted, other studies in FIW discharges [81, 112, 138] measured densities well in excess of  $10^{12} \text{ cm}^{-3}$ .

$2.25 \times 10^{11} \text{ cm}^{-3}$  to  $3.25 \times 10^{11} \text{ cm}^{-3}$ . The magnitude of the electron density is somewhat less than anticipated; other papers such as [112], [138], and [81] state densities exceeding  $10^{12} \text{ cm}^{-3}$ . Separate experiments (not shown here) demonstrated similar electron densities

and collision frequencies. However, the time for the system to reach its quasi-equilibrium varied and, in some cases, required 10 minutes.

The observed increase in collision frequency was, perhaps, a result of increasing pressure and gas temperature in the chamber. Meanwhile, the change in electron density may be a result of a changing chemical composition. It is not immediately clear what mechanism is responsible for this, but it is well-known that electrons will readily attach to water molecules. As they are destroyed through dissociation, the attachment rate would decline and it would be reasonable to expect an increase in electron density.

#### A.2.4 DC Sustainer

Six separate experiments were run with the DC sustainer discharge on at approximately 750 V (current limited), and four experiments were run with the sustainer off (electrodes floating). Difficulties with EMI prevented a more complete evaluation of the sustainer's effect. Therefore, an absolute statement on the influence of the DC sustainer is not possible. However, experiments without the DC sustainer exhibited consistently higher, but variable, densities.

It is believed that the sustainer may have caused increased energy transfer to the excited states of atoms and molecules, but was ineffective at increasing the electron density. Indeed, the sustainer voltage was insufficient to produce a glow discharge independent of the high voltage pulses. As such, one may conclude that it will tend to extract more electrons than it produces. This being the case, a DC sustainer may be useful in situations requiring fast gas heating, but at the cost of a reduced ionization efficiency.

### A.3 Rotational Spectroscopy

The approach used measured the rotational spectra of a molecular system and used this information to infer the rotational temperature. As a result of the close energy-spacing of the

rotational levels, this temperature is usually a good measure of the translational temperature of the system [139]. This technique is limited by the ability to detect light from the transitions, and by the equilibration time of the translational and rotational temperatures.

The measurement of rotational transitions is a common diagnostic for the measurement of gas temperatures, particularly in the field of combustion. Matching of the rotational spectra is typically accomplished with a computer program such as Specair [140] and LIF-BASE [141]. However, a survey of the available programs revealed little documentation about the calculation methods and none which provided the necessary flexibility how the spectra were generated. This necessitated the development of a program to automate the generation and matching of rotational spectra.

## **APPENDIX B**

### **Laser-Absorption Analysis Code**

## **APPENDIX C**

### **Global Model Code**

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