

Report Project 2

Data Analysis and Statistical Modeling Prof Isabel Rodrigues



Grupo 1

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Introduction

For this project a datagram is given for us to analyse:

Data frame: Auto

Subset: observation 1 to 50 **Variables**: all except name:

- mpg miles per gallon
- cylinders number of cylinders between 4 and 8
- displacement engine displacement (cu. Inches)
- horsepower engine horsepower
- weight vehicle weight (lbs.)
- acceleration time to accelerate from 0 to 60 mph (sec.)
- year model year (modulo 100)
- origin (origin of the car (1. American, 2. European, 3. Japanese)

<u>1</u>

Summary statistics

> # Summary statistics

> summary(auto_subset)

| mpg | cylinders | displacement | horsepower | weight | acceleration | year | origin |
|---------------|--------------|---------------|----------------|--------------|---------------|---------------|--------------|
| Min. : 9.00 | Min. :4.00 | Min. : 97.0 | Min. : 46.00 | Min. :1835 | Min. : 8.00 | Min. :70.00 | Min. :1.00 |
| 1st Qu.:14.00 | 1st Qu.:4.50 | 1st Qu.:154.5 | 1st Qu.: 91.25 | 1st Qu.:2599 | 1st Qu.:11.50 | 1st Qu.:70.00 | 1st Qu.:1.00 |
| Median :17.50 | Median :7.00 | Median :280.0 | Median :121.50 | Median :3381 | Median :13.75 | Median :70.00 | Median :1.00 |
| Mean :18.08 | Mean :6.48 | Mean :268.8 | Mean :135.34 | Mean :3366 | Mean :13.40 | Mean :70.42 | Mean :1.28 |
| 3rd Qu.:22.00 | 3rd Qu.:8.00 | 3rd Qu.:357.8 | 3rd Qu.:173.75 | 3rd Qu.:4195 | 3rd Qu.:15.38 | 3rd Qu.:71.00 | 3rd Qu.:1.00 |
| Max. :28.00 | Max. :8.00 | Max. :455.0 | Max. :225.00 | Max. :5140 | Max. :20.50 | Max. :71.00 | Max. :3.00 |

| | vars | n | sd | trimmed | mad | min | max | range | skew | kurtosis | se | Winsorized_Mean | Variance |
|--------------|------|----|-------------|-----------|------------|------|--------|--------|-------------|------------|--------------|-----------------|-------------|
| mpg | 1 5 | 50 | 5.2092539 | 17.9000 | 5.18910 | 9 | 28.0 | 19.0 | 0.37391779 | -0.9913305 | 0.73669976 | 18.06 | 27.1363 |
| cylinders | 2 5 | 50 | 1.6932037 | 6.6000 | 1.48260 | 4 | 8.0 | 4.0 | -0.46070716 | -1.4771470 | 0.23945516 | 6.48 | 2.8669 |
| displacement | 3 5 | 50 | 115.7538839 | 267.5750 | 137.14050 | 97 | 455.0 | 358.0 | -0.07343823 | -1.3197659 | 16.37007125 | 263.80 | 13398.9616 |
| horsepower | 4 5 | 50 | 49.1945783 | 132.2750 | 49.66710 | 46 | 225.0 | 179.0 | 0.34493617 | -1.2440568 | 6.95716398 | 131.16 | 2420.1065 |
| weight | 5 5 | 50 | 899.0059865 | 3342.4250 | 1202.38860 | 1835 | 5140.0 | 3305.0 | 0.13682281 | -1.2067456 | 127.13864587 | 3354.26 | 808211.7637 |
| acceleration | 6 5 | 50 | 2.8193935 | 13.3375 | 2.59455 | 8 | 20.5 | 12.5 | 0.12596323 | -0.3767769 | 0.39872245 | 13.40 | 7.9490 |
| year | 7 5 | 50 | 0.4985694 | 70.4000 | 0.00000 | 70 | 71.0 | 1.0 | 0.31449986 | -1.9386713 | 0.07050836 | 6.48 | 0.2486 |
| origin | 8 5 | 50 | 0.6074369 | 1.1250 | 0.00000 | 1 | 3.0 | 2.0 | 1.93771682 | 2.4157790 | 0.08590455 | 1.00 | 0.3690 |

> #Covariance#

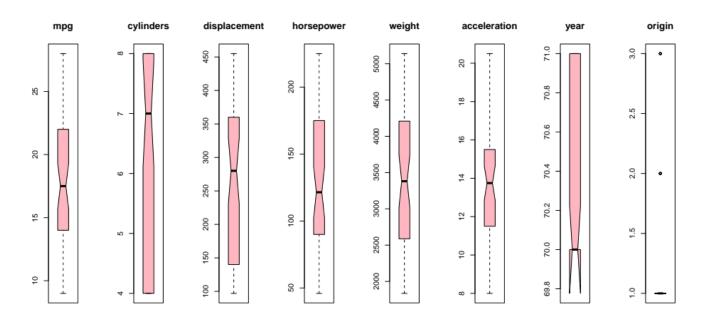
- > auto_cov = round(cov(auto_subset), digits = 4)
- > auto cov

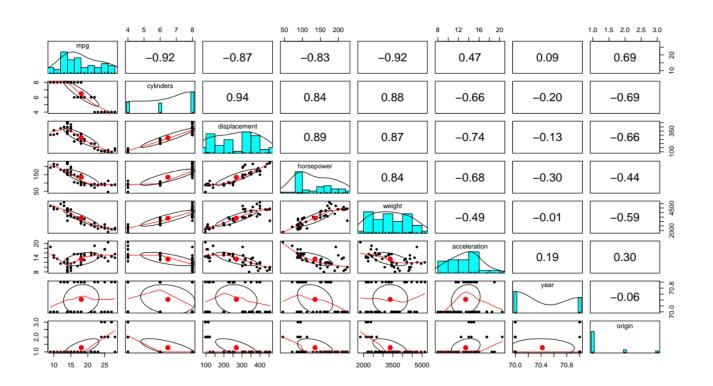
| | mpg | cylinders | displacement | horsepower | weight | acceleration | year | origin |
|--------------|------------|-----------|--------------|------------|-------------|--------------|---------|-----------|
| mpg | 27.1363 | -8.1208 | -527.3273 | -211.8033 | -4312.4865 | 6.8857 | 0.2310 | 2.1812 |
| cylinders | -8.1208 | 2.8669 | 184.3216 | 69.9967 | 1341.4890 | -3.1347 | -0.1649 | -0.7086 |
| displacement | -527.3273 | 184.3216 | 13398.9616 | 5050.3078 | 90877.8065 | -241.3816 | -7.4890 | -46.2784 |
| horsepower | -211.8033 | 69.9967 | 5050.3078 | 2420.1065 | 37211.8200 | -94.7204 | -7.3906 | -13.0971 |
| weight | -4312.4865 | 1341.4890 | 90877.8065 | 37211.8200 | 808211.7637 | -1253.5347 | -3.7482 | -321.2539 |
| acceleration | 6.8857 | -3.1347 | -241.3816 | -94.7204 | -1253.5347 | 7.9490 | 0.2673 | 0.5082 |
| year | 0.2310 | -0.1649 | -7.4890 | -7.3906 | -3.7482 | 0.2673 | 0.2486 | -0.0180 |
| origin | 2.1812 | -0.7086 | -46.2784 | -13.0971 | -321.2539 | 0.5082 | -0.0180 | 0.3690 |
| | | | | | | | | |

Total Variance



Summary Plots







2.A)

To find the best subset of regressors, we applied the regression model until we got the ones that we considered useful.

Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) | |
|--------------|------------|------------|---------|----------|-----|
| (Intercept) | 88.1914525 | 40.9568090 | 2.153 | 0.037085 | * |
| cylinders | -1.8554467 | 0.4601097 | -4.033 | 0.000228 | *** |
| displacement | 0.0036874 | 0.0079945 | 0.461 | 0.647005 | |
| horsepower | -0.0313082 | 0.0127249 | -2.460 | 0.018074 | * |
| weight | -0.0014804 | 0.0007306 | -2.026 | 0.049118 | * |
| acceleration | -0.3973985 | 0.1403159 | -2.832 | 0.007070 | ** |
| year | -0.6492297 | 0.5674529 | -1.144 | 0.259056 | |
| origin | 0.9263427 | 0.5777388 | 1.603 | 0.116343 | |

Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) | |
|--------------|------------|------------|---------|----------|-----|
| (Intercept) | 84.6660928 | 39.8672768 | 2.124 | 0.03949 | * |
| cylinders | -1.7606663 | 0.4078873 | -4.317 | 9.14e-05 | *** |
| horsepower | -0.0287331 | 0.0113296 | -2.536 | 0.01492 | * |
| weight | -0.0014294 | 0.0007155 | -1.998 | 0.05211 | |
| acceleration | -0.4288316 | 0.1215273 | -3.529 | 0.00101 | ** |
| year | -0.5934321 | 0.5493096 | -1.080 | 0.28602 | |
| origin | 0.8277284 | 0.5317864 | 1.557 | 0.12692 | |

Coefficients:

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|-----------------|------------|------------|---------|----------|-----|
| | Estimate | Std. Error | t value | Pr(> t) | |
| (Intercept) | 41.7214469 | 3.0398687 | 13.725 | < 2e-16 | *** |
| cylinders | -1.5852955 | 0.3749030 | -4.229 | 0.000117 | *** |
| horsepower | -0.0229062 | 0.0099822 | -2.295 | 0.026579 | * |
| weight | -0.0018702 | 0.0005889 | -3.176 | 0.002729 | ** |
| acceleration | -0.3882040 | 0.1157813 | -3.353 | 0.001652 | ** |
| origin | 0.9604299 | 0.5183869 | 1.853 | 0.070636 | |

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 45.3408068 2.3911834 18.962 < 2e-16 ***
cylinders -1.9702777 0.3203725 -6.150 1.87e-07 ***
horsepower -0.0179892 0.0098797 -1.821 0.075285 .
weight -0.0018947 0.0006044 -3.135 0.003026 **
acceleration -0.4238977 0.1172125 -3.616 0.000752 ***
```



Coefficients:

| | Estimate | Std. Error | t value | Pr(>ltl) | |
|--------------|------------|------------|---------|----------|-----|
| (Intercept) | 43.9154963 | 2.3155947 | 18.965 | < 2e-16 | *** |
| cylinders | -2.0388707 | 0.3260589 | -6.253 | 1.21e-07 | *** |
| weight | -0.0024559 | 0.0005329 | -4.609 | 3.23e-05 | *** |
| acceleration | -0.3250775 | 0.1064735 | -3.053 | 0.00376 | ** |

In the end, cylinders, weight, and acceleration are the selected ones. We chose these because it would allow us to work with less predictors. The adjusted \mathbf{r}^2 value of the last two iterations is similar and lower in the last iteration.

After fitting a regression model to explain the mpg variable using the predictors we just selected we get the values:

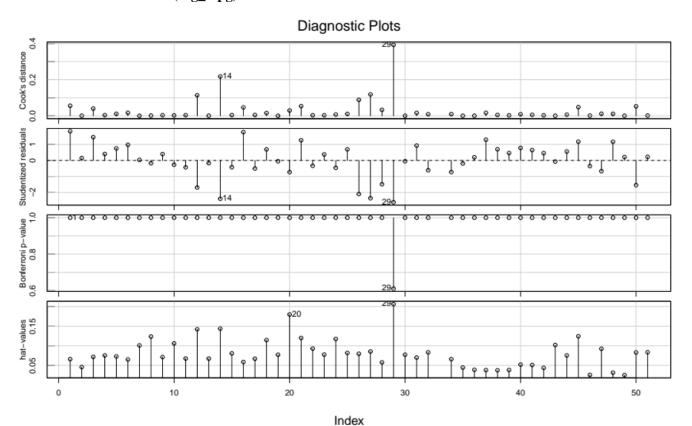
```
\mathbf{r}^2 = 0.891092607413735
\mathbf{r}^2 \mathbf{adj} = 0.8839899513755
```

Given that our \mathbf{r}^2 and \mathbf{r}^2 adj values are relatively high (>0.8), it suggests that the current model explains a significant portion of the variability in the response variable.

2.B)

For this regression we are using p = 3 predictors for n = 50 observations Searching for possible influential/leverage observations we get this:

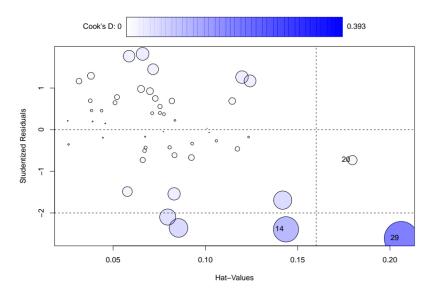
influenceIndexPlot(reg_mpg)





influencePlot(reg_mpg)

```
StudRes Hat CookD
14 -2.3937542 0.1436755 0.2179395
20 -0.7317671 0.1796745 0.0296206
29 -2.6115400 0.2060838 0.3928817
```



For mpg, the possible leverage observations are 29, 20 and 14. The two observations with highest cook's distance are 14 and 29, so the more possible influential observations are 29 and 14.

2.C)

Calculating the 97.5% Confidence Interval and Prediction Interval for the expected values of the responses for observations 14 and 31 we get:

```
      Obs_14
      Obs_31

      CI ] 2.77279693700092 , 2.92437757683037 [ ] 3.19053386221619 , 3.29633578732302 [ PI ] 2.63475473062577 , 3.06241978320552 [ ] 3.03660472892808 , 3.45026492061112 [
```

The prediction interval (PI) for Obs_14 is noticeably wider than the confidence interval (CI). This wider width in the prediction interval reflects the additional uncertainty associated with predicting individual observations, considering both the uncertainty in estimating the mean and the variability of individual observations.

Similar to Obs_14, the prediction interval (PI) for Obs_31 is wider than the confidence interval (CI). This wider width suggests a higher level of uncertainty when predicting individual observations, considering both the variability in estimating the mean and the variability of individual data points.



In both cases, the prediction intervals are wider than the corresponding confidence intervals. This is a common characteristic, as prediction intervals need to account for the variability in individual observations, making them more conservative and wider. The confidence intervals, on the other hand, primarily focus on the uncertainty around estimating the mean.

In summary, the widths of the prediction intervals highlight the increased uncertainty when making predictions for individual observations compared to estimating the mean.

Conclusion

To finish, this analysis provided a comprehensive understanding of the relationships within the Auto dataset and helped us learn more about regression models and their uses.