

Highlights

Iron's impact on silicon solar cell execution: comprehensive modeling across diverse scenarios

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- The iron defect transformation effect on Si solar cells' performance was studied using SCAPS simulation
- Short-circuit current changes are most suitable for estimating iron impurity concentration.
- Open-circuit voltage changes are a non-monotonic function of iron concentration at low doping levels.
- Monochromatic illumination is more effective than AM1.5 for accurate iron concentration estimation.

Iron's impact on silicon solar cell execution: comprehensive modeling across diverse scenarios

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ABSTRACT

Transitioning to renewable energy sources is paramount for humanity's sustainable development, and silicon solar cells are at the forefront of solar energy conversion. Iron in these structures is a primary one of the most detrimental metallic impurities. This study examines the impact of iron defect variability on silicon solar cell performance across various scenarios. We have simulated solar cells using SCAPS software across a range of temperatures (290 – 340) K, base thicknesses (180 – 380) μm , doping levels (10^{15} – 10^{17}) cm^{-3} , with iron concentrations varying from 10^{10} to 10^{14} cm^{-3} under AM1.5 and monochromatic (940 nm) illumination. Analyzed across all cases were the effects of iron–boron pair dissociation on short-circuit current, open-circuit voltage, fill factor, and efficiency. The experimental measurements validated the simulation results, demonstrating good agreement for all photovoltaic parameters. This study investigates the potential of using photovoltaic parameter changes induced by iron-related defect restructuring to estimate iron concentration. It is shown that changes in short-circuit current obtained under monochromatic illumination are the most reliable, while the fill factor is the least effective. The study examined the correlation between changes in photovoltaic parameters caused by pair dissociation while establishing the expedience of applying principal component analysis in impurity concentration evaluation with the help of multiple parameters.

1. Introduction

The necessity for renewable energy sources to meet the growing global demand for sustainable and environmentally friendly energy alternatives has become evident. Among the wide range of renewable energy sources, sunlight is the cleanest, safest, and most abundant source for use in sustainable energy to support economic growth [1]. The utilization of solar energy heavily depends on the use of photovoltaic cells. The development of next-generation solar cells is primarily driven by the search for novel materials suitable for their fabrication. Particular attention is given to exploring the potential use of composites and nanoparticles (e.g., Cu-La-based systems [2], cerium oxide, and copper indium sulfate [3]), MAX phases [4, 5], and chalcogenides (such as GeSe, MoSe₂, Sb₂Se₃, and SnSe as hole transport materials [6] or SnS₂ and WS₂ as electron transport materials [7]), as well as metal silicides (e.g., FeSi₂ as an absorber layer [8]). These studies cover a broad range of materials [9], with the primary goal of developing highly efficient and cost-effective photovoltaic devices. Frequently, these novel materials are integrated with silicon in solar cells [8, 10]. However, it is worth noting that traditional silicon-based devices continue to play a dominant role in the photovoltaic market [11, 12].

The issue of semiconductor purity has become increasingly significant since the advent of the transistor in 1947 [13]. The 1960 study by Shockley and Queisser [14] demonstrated that the electrical properties of $n^+ - p$ silicon diodes deteriorate when impurity atoms of metals such as Cu, Fe, Mn, Au, Zn, and Ni are present. This study prompted investigations focused on preventing contaminating metals from entering semiconductors during manufacturing. In particular, metallic impurities are known to reduce the efficiency of silicon-based devices through direct shunting [15], increased leakage current [16], or bulk recombination [17]. Despite extensive study of metallic impurities in silicon over the past fifty years [13, 18], the problem continues to attract significant attention [19, 20, 21, 22, 23].

Iron is prominent among metallic contaminants, with its atoms being among the most prevalent and detrimental impurities in silicon solar cells (SSCs) [24]. Even in small concentrations (about 10^{10} cm^{-3}), point defects related to Fe can significantly influence the performance of SSCs [25, 26]. Therefore, it is of critical importance to assess the concentration of iron impurities. In response to this challenge, various methodologies have been put forward,

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often based on the property of iron atoms to form pairs with acceptors. In particular, iron atoms are predominantly located in interstitial positions in silicon, forming the Fe_i defect. In p -type crystals, without external illumination, iron atoms carry positive charges and tend to bond with negatively charged doping atoms (boron, aluminum, gallium, or indium), forming $\text{Fe}_i\text{B}_{\text{Si}}$ pairs [27]. However, these pairs can destabilize by intense illumination, electron injection, or heating up to 200 °C [28]. The recombination properties of iron-related defects Fe_i and Fe_iB_s differ significantly, which profoundly affects the overall characteristics of the crystal. This fact formed the basis for the first method of assessing iron concentration [29], which relied on measuring the diffusion length of minority carriers using the surface photovoltaic method [30]. Many other methods involve measurements of carrier lifetime [31, 32], Quasi-Steady-State Photoconductance [33], or the study of kinetic dependencies of short-circuit current [34] or photoluminescence intensity [35] during the reaction $\text{Fe}_i\text{B}_{\text{Si}} \rightleftharpoons \text{Fe}_i + \text{B}_{\text{Si}}$.

Notably, the presence of Fe-related defects affects the dynamics of electron and hole movement within the solar cell, which is reflected in changes to the appearance of the current–voltage (I – V) characteristics of SSCs overall, as well as modifications to the main photoelectric parameters (short-circuit current I_{SC} , open-circuit voltage V_{OC} , efficiency η , and fill factor FF) in particular. These findings create fundamental possibilities to advance methods for estimating iron concentration by I – V curves measuring before and after pair dissolution. The advantages of such an approach are associated with the possibility of directly characterizing finished solar cells, as well as the absence of the need for additional equipment other than that required for I – V measurements, which is extremely common. Efforts have been made initially in developing such methods. For instance, it was proposed to estimate the concentration of iron in SSCs based on changes in the ideality factor [36, 37] or open-circuit voltage [26]. However, developing such approaches requires evaluating how a particular parameter changes when iron-containing pairs dissolve and determining whether it can estimate the iron concentration N_{Fe} . For example, the most evident conditions for utilizing a specific parameter include its change due to the transformation $\text{Fe}_i\text{B}_{\text{Si}} \rightarrow \text{Fe}_i + \text{B}_{\text{Si}}$, at least by 10 %, along with a monotonic dependence of these changes on N_{Fe} .

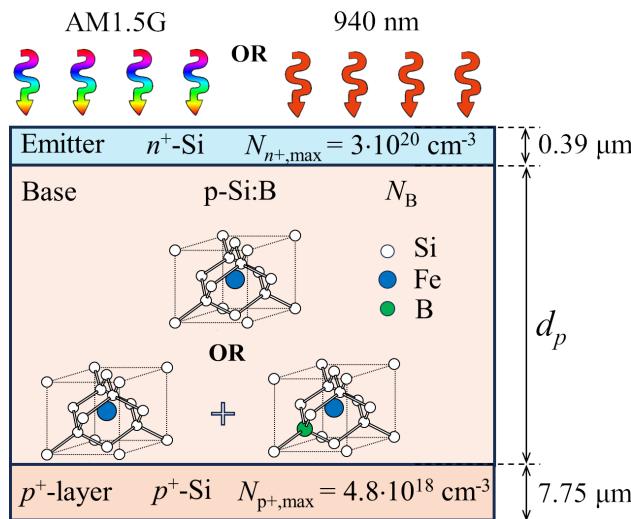
This paper intends to determine the variations of I_{SC} , V_{OC} , η , and FF resulting from the decay of iron-containing pairs in boron-doped silicon solar cells. Previous similar calculations have been conducted [38, 25, 19], but the results presented typically pertain only to certain temperatures, illumination levels (often AM1.5), and solar cells with specific parameters. In this study, we performed calculations over a sufficiently wide temperature range (290–340 K) and for solar cells with varying base thickness (180–380 μm) and doping levels (boron concentration in the base ranging from 10^{15} to 10^{17} cm^{-3}). The results obtained allow us to assess the feasibility and potential of using the main photovoltaic parameters of specific solar cells to estimate the N_{Fe} value across a range of temperatures, including conditions similar to those encountered in typical SSC applications. Furthermore, investigations have explored changes in photoelectric performance under not only solar illumination (AM1.5G) but also low-intensity monochromatic light (wavelength of 940 nm, intensities of 5 W/m^2 and 10 W/m^2). In the first case, while it is customary to adhere to standard conditions, it's essential to consider that illumination at 1000 W/m^2 can lead to the decay of Fe_iB_s complexes [39]. Therefore, measurements for cases requiring the presence of undissociated pairs in silicon must meet specific constraints. On the other hand, intentionally chosen monochromatic illumination penetrates the emitter with negligible losses and does not reach the rear side. In this context, the photoelectric parameters show remarkable sensitivity to recombination processes occurring within the solar cell base and to iron concentration in this region. Finally, in our calculations, we attempted to use the latest literature data concerning the exact values of silicon parameters, including light absorption values [40] and coefficients characterizing intrinsic recombination [41, 42].

2. Research Methodology

2.1. Simulation Details

The study involved simulation I – V curves of SSCs with an $n^+ - p - p^+$ structure, as illustrated in Fig. 1. A back surface field (p^+ -layer) is a notable feature observed in both Al-BSF cells (full area), which are gradually losing relevance, and PERC cells (locally), which are the most widely used in mass production. The structures with a base uniformly doped with boron were under consideration. The doping concentration N_B , and the base thickness d_p were varied during the modeling process, as detailed in Table 1. The emitter and p^+ -layer were considered to be unevenly doped. The concentration profiles of the dopants, their maximum values ($N_{p^+, \text{max}}$ and $N_{n^+, \text{max}}$), and layer thicknesses (see Fig. 1) were selected according to Fell et al. [43].

The simulation was conducted using the SCAPS 3.3.11 code [44]. SCAPS-1D software, developed by the University of Gent, is founded on theoretical computations that involve solving Poisson's equation, continuity equations

**Figure 1:** Schematic diagram of analyzed solar cells.**Table 1**

Parameters varied during the simulation

Parameter	Range of values
d_p (μm)	180 – 380
N_B (cm^{-3})	$10^{15} – 10^{17}$
N_{Fe} (cm^{-3})	$10^{10} – 10^{14}$
T (K)	290 – 340
Illumination	AM1.5G, 1000 W/m^2 ; 940 nm, 5 W/m^2 ; 940 nm, 10 W/m^2

for holes and electrons, and drift-diffusion at each position within the solar cell, considering the boundary conditions. Despite its one-dimensional modeling approach, SCAPS is extensively used for modeling various types of solar cells [6, 7, 8, 45, 46, 47, 48] in general and for investigating the effects of defects on their performance [6, 8, 49, 50, 51] in particular.

As can be seen from Table 1, calculations spanned a broad range of temperatures and base doping levels. Therefore, to improve the accuracy of the calculations when inputting the initial parameters into SCAPS, temperature and concentration (where applicable) dependencies of the following silicon parameters were taken into account:

- bandgap according to Passler [52];
- doping induced bandgap narrowing according to Yan & Cuevas [53];
- effective density of states at conduction and valence band and intrinsic carrier concentration according to Couderc et al. [54];
- thermal carrier velocities according to Green [55];
- free carrier effective masses according to O'Mara et al. [56];
- carrier mobilities according to Klaassen's theory [57];

The values of surface recombination coefficients were considered equal to the thermal velocities of carriers [43]. The calculations addressed recombination processes within the structural volume, incorporating both intrinsic recombination and Shockley-Read-Hall (SRH) recombination at iron-related defects. In the first case, processes of band-to-band radiation recombination were considered (where the calculation of the corresponding coefficient included

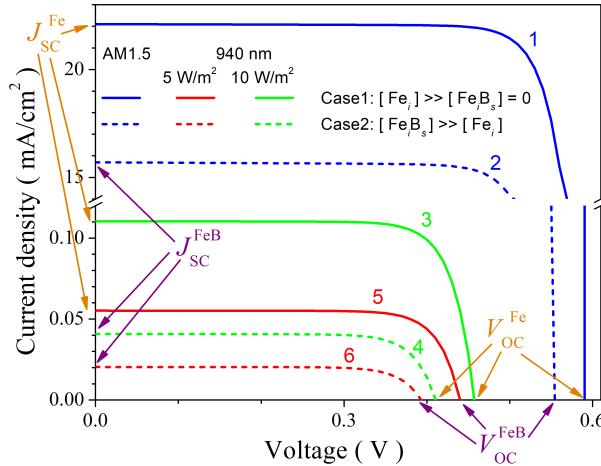


Figure 2: Typical IV characteristics, calculated for structure with $d_p = 180 \mu\text{m}$, $N_B = 10^{17} \text{ cm}^{-3}$, $N_{\text{Fe}} = 10^{14} \text{ cm}^{-3}$ at $T = 290 \text{ K}$. Illumination: AM1.5 (curves 1, 2), 940 nm 10 W/m^2 (3, 4) and 940 nm 5 W/m^2 (5, 6). Solid and dotted lines correspond to Case 1 and Case 2, respectively.

the fraction of radiatively emitted photons reabsorbed via band-to-band processes according to Niewelt et al.[41]) and Auger recombination (where the coefficients considered the effect of Coulomb enhancement [42] and temperature dependence [58]).

When accounting for the influence of iron impurities, we considered that Fe atoms were uniformly distributed within the base and p^+ -layer with a total concentration of N_{Fe} (see Table 1). Two cases were under consideration:

Case 1. The concentration of interstitial iron defects $[\text{Fe}_i] = N_{\text{Fe}}$ at each position throughout the solar cell, with no pairs present $[\text{Fe}_i\text{B}_s] = 0$. This case corresponds to the state of the structure immediately after intense illumination, for example.

Case 2. Iron atoms predominantly form pairs with acceptors, $[\text{Fe}_i\text{B}_s] \gg [\text{Fe}_i]$, but the exact concentration ratio depends on the position of the Fermi level and temperature [59, 60] and varies from point to point within the solar cell. Further details about calculation of the concentration profiles of Fe_iB_s and Fe_i are provided in [37, 36]. This case corresponds to prolonged storage of the structure in darkness or under conditions of low-intensity ($< 0.01 \text{ J cm}^{-2}$ [39]) illumination.

During the calculations, it was assumed that Fe_i forms a single donor level, while the Fe_iB_s pair has a trigonal configuration and acts as an amphoteric defect. We obtained defect parameters (including level positions within the bandgap and electron and hole capture cross-sections) from relevant studies [61, 62, 63].

As previously mentioned, the solar cell behavior was simulated under different illumination conditions, including solar light (AM1.5G) and monochromatic light (wavelength 940 nm, intensity of $W_{\text{ill}} = 5 \text{ W/m}^2$ or 10 W/m^2) — see Table 1. The calculations incorporated the light absorption values in silicon based on Green's study [40].

The I - V characteristics were simulated for both Case 1 and Case 2 (see Fig. 2), and from each curve, the short-circuit current, open-circuit voltage, efficiency, and fill factor were determined. Assessing the influence of iron defect variability relied on the relative changes in each photovoltaic conversion parameter:

$$\epsilon A = \frac{A^{\text{FeB}} - A^{\text{Fe}}}{A^{\text{FeB}}} \times 100\%, \quad (1)$$

where A represents one of the parameters (I_{SC} , V_{OC} , η , and FF), superscript “FeB” corresponds to the parameter value for coexistence of Fe_i and Fe_iB_s (Case 2), superscript “Fe” is related to the decay of all pairs (Case 1).

Impact of change of iron defects was investigated as a function of temperature from 290 K to 340 K, base depth from $180 \mu\text{m}$ to $380 \mu\text{m}$, base doping level from 10^{15} cm^{-3} to 10^{17} cm^{-3} , and total impurity iron atom concentration from 10^{10} cm^{-3} to 10^{14} cm^{-3} . It is worth noting that investigating the effects of doping density, defect density, temperature, and active layer thickness on photovoltaic parameters is a well-established practice [6, 7, 8]. For each illumination scenario, calculations were carried out with 11 different temperature values and 5 base depth values, evenly distributed

within the specified ranges. The concentration values were distributed equally on a logarithmic scale with 4 (N_B case) and 6 (N_{Fe} case) steps per decade. As a result, for the AM1.5 illumination scenario, for instance, 24750 I - V characteristics were simulated. An exception occurred with monochromatic illumination at $W_{ill} = 10 \text{ W/m}^2$, where we used only two d_p values.

2.2. Experimental Details

To evaluate the validity of the simulated results, we also conducted experimental studies on the effect of changing the state of iron-related defects on the photoelectric parameters of silicon solar cells.

The $n^+ - p - p^+$ -Si samples were used in the experiment. The structure was fabricated from a 380 μm thick p -type boron-doped Czochralski silicon (100) wafer with doping level $N_B = 1.36 \times 10^{15} \text{ cm}^{-3}$. The n^+ emitter with a sheet resistance of about 20–30 Ω/\square and thickness of 0.7 μm was formed by phosphorus diffusion. The anti-recombination isotype barrier was created by using a p^+ layer (10–20 Ω/\square) formed by boron diffusion. On the front surface, SiO_2 (40 nm) and Si_3N_4 (30 nm) films were formed as antireflective and passivating layers, respectively. The solid and grid Al contacts were formed by magnetron sputtering on the back and front surfaces, respectively.

The I - V characteristics were measured using a Keithley 2450 source meter and low-intensity monochromatic light source (light-emitting diode SN-HPIR940nm-1W with light wavelength 940 nm and intensity of about $W_{ill} = 5 \text{ W/m}^2$).

For different samples, the iron concentration ranged from 2×10^{11} to $4 \times 10^{13} \text{ cm}^{-3}$. The values of N_{Fe} were determined using a methodology [64, 34], based on fitting the kinetics of short-circuit current. The decay of Fe_iB_s pairs was realized using intensive (7000 W/m^2) halogen lamp illumination.

The measurements were carried over the temperature range of 300–340 K. The sample temperature was driven by a thermoelectric cooler controlled by an STS-21 sensor and maintained constant by a PID algorithm embedded in the software that serves the experimental setup.

3. Results and Discussion

3.1. Short-circuit current

Figure 3 illustrates the characteristic dependencies of short-circuit current variations resulting from the reconfiguration of iron-containing defects, as obtained from the simulations. We present a more comprehensive set of figures that depict the detailed dependencies of εI_{SC} on all parameters varied during the calculations in the Supplementary Material (Figs. S1–S6). It is important to note that the qualitative nature of the short-circuit current variations remains practically identical under both solar and monochromatic illumination, with the quantitative parameters of εI_{SC} differing: at 940 nm, the absolute values of εI_{SC} are approximately 3–4 times greater than those observed under AM1.5 conditions, assuming other parameters are constant. Among other features of εI_{SC} changes, we can highlight the following:

- The module εI_{SC} increases monotonically with increasing iron concentration, but the sign of this value depends on the doping level. At low boron concentrations ($N_B = 10^{15} \text{ cm}^{-3}$) $\varepsilon I_{SC} > 0$, whereas at high concentrations ($N_B = 10^{17} \text{ cm}^{-3}$) $\varepsilon I_{SC} < 0$ — see Figs. 3a, 3c, S3–S6;
- Increasing the acceptor concentration causes a monotonic decrease in εI_{SC} (Figs. 3b, 3d); the N_B value at which the sign of εI_{SC} changes depends on the temperature (decreases with decreasing in T value) and the type of illumination (is generally higher in the case of monochromatic light) — see Fig. S2;
- In the case where $\varepsilon I_{SC} < 0$, an temperature increase causes a decrease in the absolute magnitude of the relative changes in short-circuit current, with the dependence being nearly linear and the slope increasing with higher doping levels and iron concentration (Figs. 3a, 3c, S4). In the case where $\varepsilon I_{SC} > 0$, a T changing results in minor non-monotonic variations of the short-circuit current after the dissociation of Fe_iB_s pairs (Fig. S3);
- The influence of base thickness on εI_{SC} increases with increasing N_B and decreasing N_{Fe} (Figs. S5, S3), but it is minimal overall. As calculations have shown, increasing d_p by more than twice causes changes in εI_{SC} that do not exceed 0.5 %;
- Changing the intensity of the monochromatic illumination (from 5 W/m^2 to 10 W/m^2) does not practically change the value of εI_{SC} ;
- The absolute values of εI_{SC} can reach relatively high values (more than 100 % for 940 nm illumination); however, in cases where $N_{Fe} < 10^{11} \text{ cm}^{-3}$ and around $N_B = 10^{16} \text{ cm}^{-3}$, the changes in short-circuit current do not exceed a few percent.

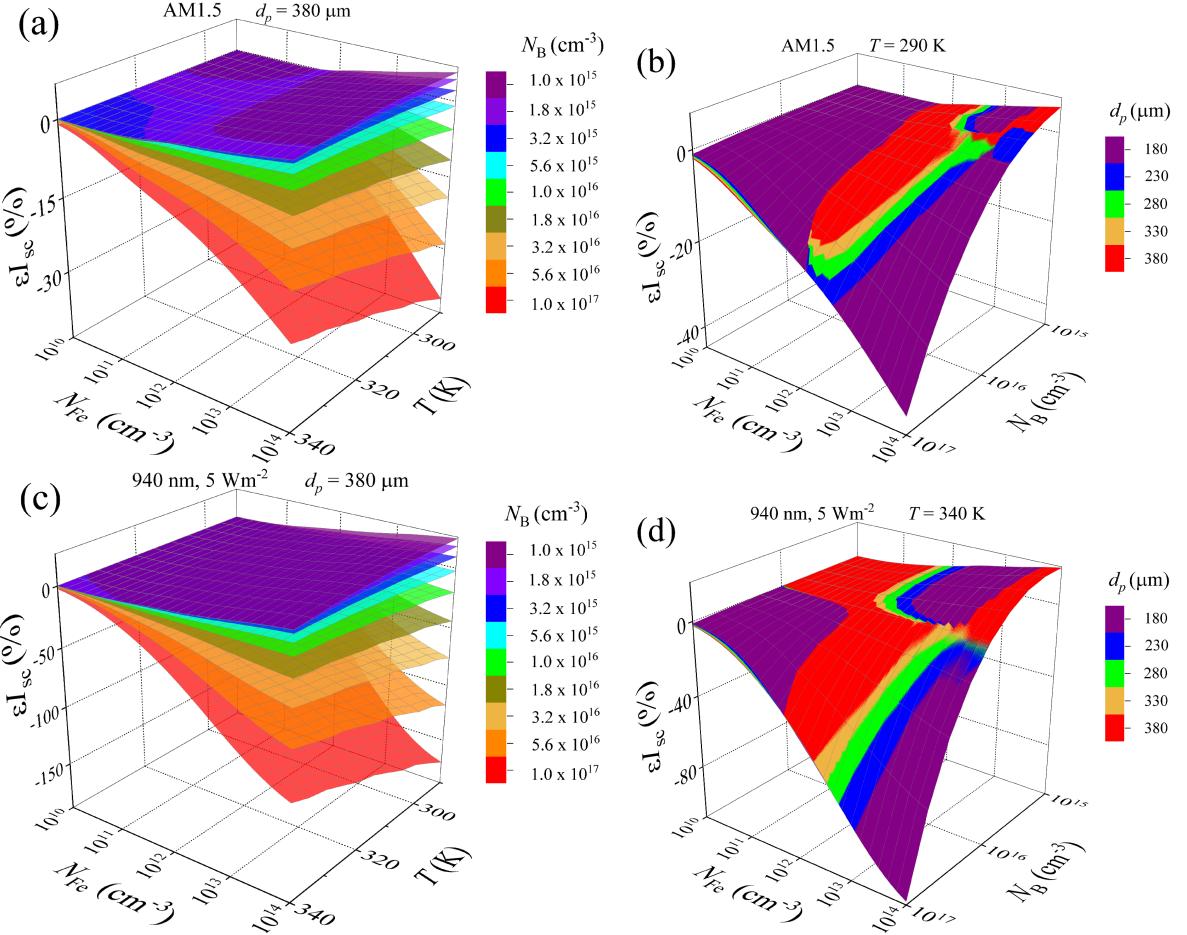


Figure 3: Relative changes in short-circuit current caused by a complete dissociation of Fe_iB_s pairs as a function of iron concentration and temperature (panels a and c) or doping level (b, d). Illumination: AM1.5 (a, b), 940 nm 5 W m^{-2} (c, d). $T, \text{ K}$: 290 (b), 340 (d). Different surfaces correspond to different doping levels (a, c) and base depths (b, d).

The identified features of the ϵI_{SC} changes can be explained by considering the main reasons for the influence of factors, which varied during simulation, on the photovoltaic conversion. It is known [65] that the main influence of metal impurities on solar cell performance is caused by their effect on the collection efficiency (CE, portion of excess carriers that reach the depletion region of $p-n$ junction). Neglecting the influence of series and shunt resistances, the short-circuit current coincides with the photocurrent I_{ph} , which equals the CE multiplied by the number of light-induced excess carriers. In turn, the CE can be calculated as a convolution of generation function, which is proportional to $\exp(-\alpha z)$ (where α is the absorption coefficient and z is the coordinate along the axis directed perpendicular to the $p-n$ junction from the emitter) and the collection probability, which can be obtained as a solution of homogeneous diffusion equation.

The photogenerated current for the cell can be obtained by adding the relevant quantities for the base $I_{\text{ph},b}$ and the emitter $I_{\text{ph},e}$ [66]:

$$I_{\text{SC}} \approx I_{\text{ph}} = I_{\text{ph},e} + I_{\text{ph},b}. \quad (2)$$

However, considering the location of the impurity iron, it can be assumed that during the $\text{Fe}_i\text{B}_{\text{Si}} \rightleftharpoons \text{Fe}_i + \text{B}_{\text{Si}}$ reconfiguration, the first term on the right-hand side of Eq. (2) remains unchanged ($I_{\text{ph},e}^{\text{FeB}} = I_{\text{ph},e}^{\text{Fe}} = I_{\text{ph},e}$), and therefore,

considering Eq. (1):

$$\varepsilon I_{SC} = \frac{I_{ph,b}^{FeB} - I_{ph,b}^{Fe}}{I_{ph,e} + I_{ph,b}^{FeB}} \times 100\%. \quad (3)$$

In turn, the base photocurrent the under monochromatic illumination can be expressed as follows [67]:

$$I_{ph,b} = \frac{qF(1-R)\alpha L_n}{\alpha^2 L_n^2 - 1} \left(\alpha L_n - \frac{\frac{SL_n}{D_n} \left[\cosh\left(\frac{d^*}{L_n}\right) - \exp(-\alpha d^*) \right] + \sinh\left(\frac{d^*}{L_n}\right) + \alpha L_n \exp(-\alpha d^*)}{\frac{SL_n}{D_n} \sinh\left(\frac{d^*}{L_n}\right) + \cosh\left(\frac{d^*}{L_n}\right)} \right), \quad (4)$$

where F is the photon flux, R is the reflection coefficient, S is the surface recombination velocity, L_n is the minority carrier (electron) diffusion length, D_n is the electron diffusion coefficient, d^* is the thickness of the quasi-neutral region base, since the space charge region (SCR) width for the modeled structures did not exceed $1 \mu m$, it follows that $d^* \simeq d_p$.

The recombination rate affects the value of L_n and, according to the SRH model, depends on trap concentrations, capture cross-sections of electrons and holes, temperature, the Fermi level E_F location, and defect levels. Temperature also affects the values of α and D_n . In turn, the position of E_F within the band gap depends on temperature and doping level. Fig. 4 shows the calculated by using SCAPS temperature and concentration dependence of the Fermi level in the base of the investigated structure. In addition, this figure shows the positions of the levels associated with interstitial iron and the FeB pair. It is worth noting that Fe_i acts as a deep center; the donor state of the Fe_iB_s pair shows only negligible recombination activity, while the presence of the acceptor state Fe_iB_s causes the carrier lifetime to be doping-dependent under low injection conditions [38].

The relationship between N_B and E_F is the key factor in the influence of doping level on the sensitivity of photovoltaic parameters to iron presence. Specifically, the rate of SRH recombination — and consequently, variations in photovoltaic parameters due to iron impurities — depends on the relative positioning of E_F concerning the Fe_iB_s and Fe_i levels. Additionally, the equilibrium ratio of Fe_iB_s and Fe_i concentrations is also determined by the Fermi level position [59, 60]. Therefore, N_B affects the number of defects that change their state due to the complete dissociation of Fe_iB_s pairs, leading to corresponding relative changes in photovoltaic parameters analyzed in this study. Besides, the N_B concentration also affects the SCR depth (see Fig. 4). The ratio of different charge states for both interstitial iron atoms and iron-boron pairs differs between the SCR and the bulk of the base, leading to distinct SRH recombination rates and variations in photovoltaic conversion efficiency for structures with different doping levels. Furthermore, according to Klaassen's model [57], the concentration of ionized impurities influences charge carrier mobility and, consequently, the diffusion coefficient D_n , diffusion length L_n , and photoelectric conversion efficiency (see Eq. (4)). However, the effect of N_B via D_n and L_n is significantly weaker than its influence through E_F and SCR depth variations. Minor effects are expected as well due to both bandgap narrowing and changes in light absorption by free carriers with varying doping levels. The impact of doping level on photovoltaic parameters has been studied in heterojunction [8], thin-film [10], and perovskite [6] solar cells. Moreover, it has been shown [10] that doping concentration variations affect other barrier structure parameters, such as saturation current and ideality factor.

In our opinion, the change in sign and the monotonic decrease of εI_{SC} with increase in doping level value reflect the change in recombination activity caused by the Fermi level shift. It should be noted that at low boron concentrations, E_F in all points of the base is located below the donor level of Fe_i , while at $N_B > 10^{16} \text{ cm}^{-3}$, they intersect in the vicinity of the $p-n$ junction — see Fig. 4. The weak dependence on base thickness indicates that the second term in parentheses in Eq. (4) is significantly smaller than the first. In addition, when comparing monochromatic and solar illumination, the latter generates a significantly larger number of non-equilibrium carriers in the emitter due to shorter-wavelength photons. As a result, the emitter current under AM1.5 illumination increases, which, as shown in Eq. (3), leads to a decrease in εI_{SC} value.

Fig. 5 illustrates the alterations in the short-circuit current, both observed in experimental studies and calculated for structures with identical base parameters. It should be noted that the figure shows simulation results obtained at various levels of illumination, confirming that εI_{SC} is independent of W_{ill} .

One can see that the theoretical dependencies of εI_{SC} on iron concentration and temperature qualitatively agree with the experimental results. To achieve quantitative agreement, a correction factor of $C_{cor} = 1.4$ must be applied: the experimentally obtained value $\varepsilon I_{SC,exp}$ should be replaced by $\varepsilon I_{SC,exp}/C_{cor}$ — as illustrated in Fig. 5. This

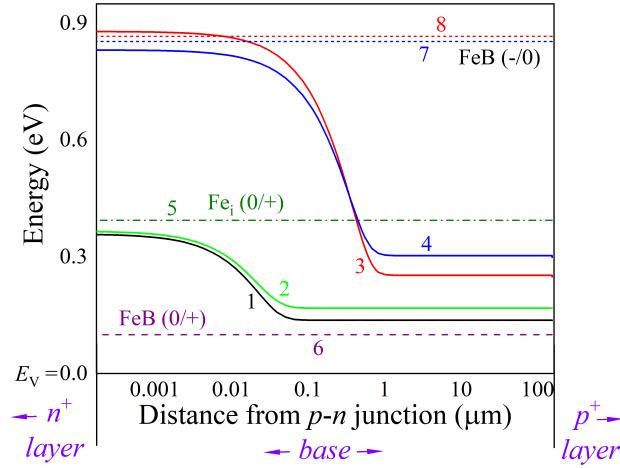


Figure 4: The location of the Fermi level (curves 1–4) in the base of the n^+ - p - p^+ structure as a function of distance from p - n junction. The zero energy value corresponds to the top of the valence band. Also shown are the locations of the donor ($0/+$) levels for the interstitial iron atom Fe_i (5) and the FeB pair (6) and the acceptor ($-/0$) level for the FeB pair (7, 8). T , K: 290 (1, 3, 8), 340 (2, 4, 7). N_B , cm^{-3} : 10^{17} (1, 2), 10^{15} (3, 4, 7, 8).

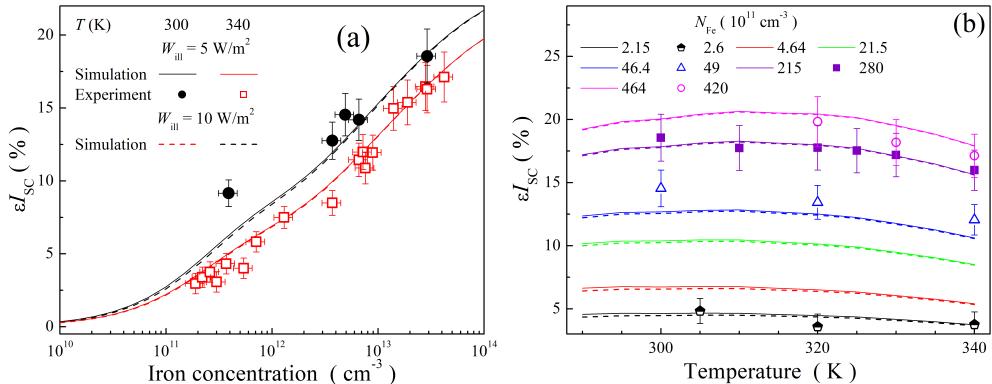


Figure 5: Relative changes in short-circuit current caused by a complete dissociation of Fe_iB_s pairs as a function of iron concentration (a) and temperature (b) for SSC with $d_p = 380 \mu m$ and $N_B = 1.36 \times 10^{15} cm^{-3}$ in the case of monochromatic (940 nm) illumination. The marks are the experimental results (divided by factor $C_{cor} = 1.4$), the lines are the simulation results. W_{ill} , W/m^2 : 5 (marks and solid lines), 10 (dotted lines). Different lines and marks correspond to different temperatures (a) or N_{Fe} values (b) — see legends.

methodology is frequently cited in the literature [25] and is associated with correcting specific systematic errors in simulations.

As mentioned above, one of the primary objectives of this study is to assess the feasibility of utilizing changes in photoelectric parameters resulting from the dissociation of FeB pairs to estimate iron concentration. One of the most promising approaches in this regard is the application of machine learning algorithms. In this context, ϵI_{SC} is expected to serve as one of the features. It is worth noting that a popular preprocessing technique involves standardizing feature values, where the distribution of each feature is transformed to have a mean of zero and a standard deviation of one. This approach ensures that multiplying the entire array of ϵI_{SC} values by a constant does not affect the resulting normalized values.

In our case, simulation errors may arise because certain factors present in actual SSCs were not accounted for in the calculations, specifically:

- the possible influence of series and shunt resistances;

- the antireflective SiO_2 and passivating Si_3N_4 layers on the front surface induce a spectral dependence in reflectance, corresponding calculations necessitating the consideration of multiple reflections [68];
- the shading caused by electrodes;
- the presence of defects unrelated to iron.

Overall, the results indicate that relative changes in short-circuit current following the complete dissociation of FeB pairs can be used to estimate iron concentration: $\varepsilon I_{\text{SC}}$ depends monotonically on N_{Fe} , and its values can be pretty significant. In this context, determining the amount of impurity atoms is more appropriately conducted using photovoltaic parameters obtained under monochromatic illumination, as this method offers greater sensitivity (response amplitude of $\varepsilon I_{\text{SC}}$). However, it should be noted that for low iron concentrations ($N_{\text{Fe}} < 10^{11} \text{ cm}^{-3}$) and solar cells with boron concentrations in the base around 10^{16} cm^{-3} , this approach appears to be unproductive. At these levels, there are blind spots in determining impurity metal concentrations.

3.2. Open-circuit voltage

Figure 7 presents the characteristic simulation results of open-circuit voltage changes due to the dissociation of FeB pairs. Figures S7–S12 in the Supplementary Material show additional $\varepsilon V_{\text{OC}}$ dependencies. Notably, the changes in V_{OC} value are almost an order of magnitude smaller than the values observed for I_{SC} . Moreover, differences in the behavior of open-circuit voltage changes as a function of iron concentration at low ($N_{\text{B}} < 2 \times 10^{16} \text{ cm}^{-3}$) base doping levels in the cases of monochromatic and AM1.5 illumination are noteworthy. Under solar illumination, $\varepsilon V_{\text{OC}}$ values are negative, and the $\varepsilon V_{\text{OC}}(N_{\text{Fe}})$ dependency is non-monotonic — see figs. 6a, 6b. Additionally, the base thickness significantly impacts the iron concentration, which correlates with the minimum $\varepsilon V_{\text{OC}}$ value (Fig. 6a). When illuminated by photons with a wavelength of 940 nm, $\varepsilon V_{\text{OC}}$ values are positive and increase monotonically with iron concentration. As boron concentration increases, the behavior of $\varepsilon V_{\text{OC}}(N_{\text{Fe}})$ becomes similar, regardless of the type of illumination: the relative changes in open-circuit voltage during the rebuilding of iron-containing defects are negative and increase monotonically in absolute value with increasing both N_{Fe} and N_{B} . Furthermore, changes in V_{OC} are more significant under monochromatic illumination, similar to the case of the short-circuit current.

The effect of temperature on $\varepsilon V_{\text{OC}}$ also depends on the base doping level: as N_{B} increases, the temperature coefficient of $\varepsilon V_{\text{OC}}$ gradually shifts from positive to negative. This trend is observed for both AM1.5 and 940nm illumination, as shown in Figs. S9, 6a, and 6b. The impact of d_p on changes in open-circuit voltage is more significant than the effect observed for $\varepsilon I_{\text{SC}}$. However, base thickness is not a determining factor for $\varepsilon V_{\text{OC}}$; it mainly affects low doping levels and temperatures, as shown in Figs. S9, S11, and S12. Another difference between the behavior of $\varepsilon V_{\text{OC}}$ and $\varepsilon I_{\text{SC}}$ is the former dependence on monochromatic illumination intensity. At $W_{\text{ill}} = 10 \text{ W/m}^2$, changes in open-circuit voltage are less significant, with differences increasing as iron concentration decreases and showing weak temperature dependence.

Understanding the features of $\varepsilon V_{\text{OC}}$ requires recalling that the open-circuit voltage depends not only on the photocurrent but also on the saturation current I_0 and the ideality factor, which in turn are determined by the state of the defect subsystem and other parameters that varied in simulation [36, 65]. In the case of simplified single-diode model [65]:

$$V_{\text{OC}} = nkT \left[\ln \left(\frac{I_{\text{ph}}}{I_0} \right) + 1 \right]. \quad (5)$$

Similar to the photocurrent, we can express I_0 as the sum of the currents from the base and the emitter [66]:

$$I_0 = I_{0,\text{e}} + I_{0,\text{b}}, \quad (6)$$

and the second term can be expressed as follows [67]:

$$I_{0,\text{b}} = \frac{qn_i D_n}{N_{\text{B}} L_n} \cdot \frac{\frac{D_n}{SL_n} \sinh \left(\frac{d_p}{L_n} \right) + \cosh \left(\frac{d_p}{L_n} \right)}{\sinh \left(\frac{d_p}{L_n} \right) + \frac{D_n}{SL_n} \cosh \left(\frac{d_p}{L_n} \right)}, \quad (7)$$

where n_i is the intrinsic carrier concentration. The last equation explains the observed dependence of $\varepsilon V_{\text{OC}}$ on the base thickness.

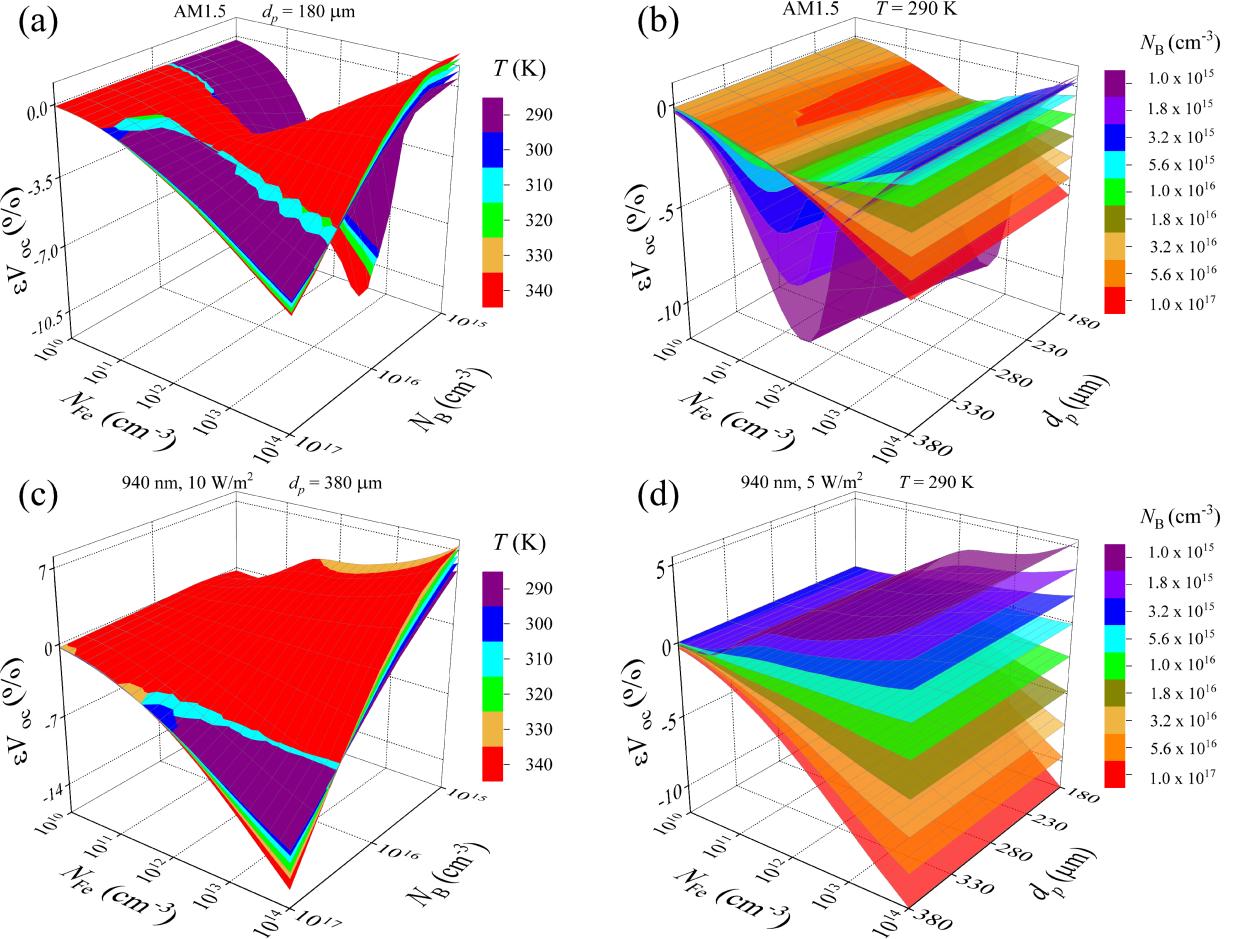


Figure 6: Relative changes in open-circuit voltage caused by a complete dissociation of Fe_iB_s pairs as a function of iron concentration and doping level (panels a and c) or base depth (b, d). Illumination: AM1.5 (a, b), 940 nm 10 W/m^2 (c), 940 nm 5 W/m^2 (d). T, K : 290 (b, d). Different surfaces correspond to different temperatures (a, c) and doping levels (b, d).

It was shown [37, 36] previously that changes in the ideality factor during restructuring $\text{Fe}_i\text{B}_{\text{Si}} \rightleftharpoons \text{Fe}_i + \text{B}_{\text{Si}}$ do not exceed a few percent. This slight variation, combined with the logarithmic dependence of V_{OC} on I_{ph} as shown in Eq. (5), explains the small absolute values of ϵV_{OC} .

Schmidt [38] attributes the non-monotonic dependence of ϵV_{OC} (N_{Fe}) (Fig. 6b) to the significantly higher injection level in the cell base under open-circuit conditions compared to short-circuit conditions. Overall, the results support this hypothesis. In fact, for monochromatic illumination with significantly lower intensity, the injection level remains below the crossover point [38] throughout the I - V curve, which results in the absence of a minimum in the ϵV_{OC} (N_{Fe}) dependence.

The data presented in Fig. 7 compare the experimental and simulation results. Overall, the results in both cases are qualitatively consistent. However, to ensure that the absolute values are consistent, a correction factor dependent on iron concentration must be used. According to the data, C_{cor} is less than 1 for low values of N_{Fe} and greater than 1 for high values. By the way, Schubert et al. [25] also observed such dependence of the correction factor.

It is believed [65] that the main effect of metals on the V_{OC} values can be determined by shunt formation. However, SCAPS does not account for the effect of shunt resistance, which we believe is the primary reason for the discrepancies between experimental and simulated values.

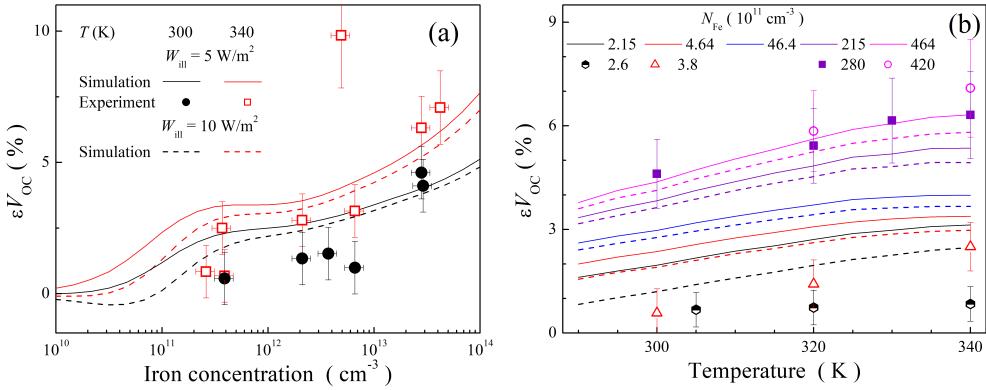


Figure 7: Relative changes in open-circuit voltage caused by a complete dissociation of Fe_iB_s pairs as a function of iron concentration (a) and temperature (b) for SSC with $d_p = 380 \mu\text{m}$ and $N_B = 1.36 \times 10^{15} \text{ cm}^{-3}$ in the case of monochromatic (940 nm) illumination. The marks are the experimental results, the lines are the simulation results. W_{ill} , W/m^2 : 5 (marks and solid lines), 10 (dotted lines). Different lines and marks correspond to different temperatures (a) or N_{Fe} values (b) — see legends.

In summary, using relative changes in open-circuit voltage due to FeB pair dissociation is less convenient for estimating iron concentration compared to ϵI_{SC} . It is because of the smaller absolute values of ϵV_{OC} , the non-monotonic dependence of ϵV_{OC} on N_{Fe} under certain conditions, and the need for precise control over the intensity of monochromatic illumination. However, using ϵV_{OC} as an additional parameter alongside ϵI_{SC} can significantly enhance the accuracy of iron concentration measurements for $N_{\text{Fe}} < 10^{11} \text{ cm}^{-3}$ and $N_B = (1 - 5) \times 10^{15} \text{ cm}^{-3}$ under AM1.5 illumination. In this case, the dependence of ϵV_{OC} on N_{Fe} is sufficiently sharp (Fig. 6b), and ambiguity in associating specific ϵV_{OC} values with iron concentration can be resolved by the monotonic behavior of ϵV_{OC} in this range. Notably, these boron concentrations are most relevant to typical real SSCs.

3.3. Fill factor

The fill factor is another defining term in the overall behavior of a solar cell. FF is the ratio of the maximum obtainable power to the product of short circuit current and open-circuit voltage. In general, FF depends on both I_{SC} and V_{OC} . However, it can be shown that it is mainly determined by the V_{OC} value. Indeed, it is shown [65] within the single-diode model

$$FF \approx \frac{v_{\text{OC}} - \ln(1 + v_{\text{OC}})}{v_{\text{OC}} + 1}, \quad (8)$$

with v_{OC} being the normalized open-circuit voltage $v_{\text{OC}} = qV_{\text{OC}}/nkT$. Another well-known empirical relation for the maximum achievable fill factor of a solar cell is proposed by Green [69, 70]:

$$FF \approx \frac{v_{\text{OC}} - \ln(0.72 + v_{\text{OC}})}{v_{\text{OC}} + 1}. \quad (9)$$

Thus, any factors that affect V_{OC} also impact the FF . However, since V_{OC} appears in both the numerator and denominator of Eqs. (8)-(9), the resulting changes in the fill factor are expected to be smaller than those in the open-circuit voltage.

Recently, Bothe et al. [71] proposed explicit expressions for the FF in terms of other key solar cell parameters. Specifically, for p -type SSCs and intrinsic limits, the parameterization can be expressed as follows:

$$FF = \frac{90.4924}{d_p^{0.00220}} \left[0.9478 + \frac{0.0519}{1 + \left(\frac{\log N_B}{17.3739 d_p^{-0.0093}} \right)^{76.3}} \right], \quad (10)$$

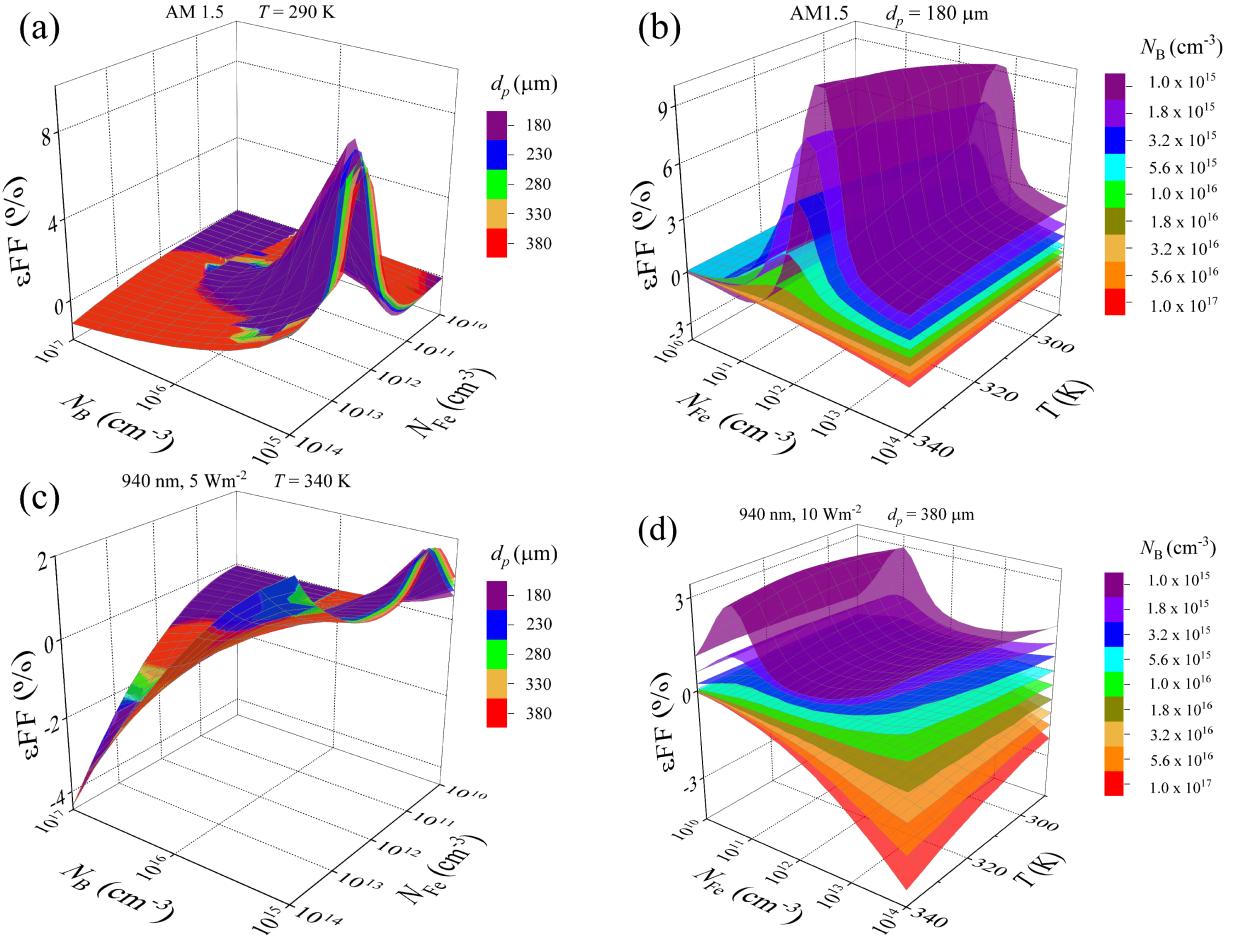


Figure 8: Relative changes in fill factor caused by a complete dissociation of Fe_xB_y pairs as a function of iron concentration and doping level (panels a and c) or temperature (b, d). Illumination: AM1.5 (a, b), 940 nm 5 W/m^2 (c), 940 nm 10 W/m^2 (d). T, K : 290 (a), 340 (c). $d_p, \mu\text{m}$: 180 (b), 380 (d). Different surfaces correspond to different base depths (a, c) and doping levels (b, d).

where d_p is expected to be in micrometers. Additional recombination (e.g., Shockley–Read–Hall) leads to a decrease in FF value [71].

Figs. S13–S16 in the Supplementary Material, along with Fig. 8, illustrate how the fill factor varies with iron defect variability. The following features of ϵFF can be identified from the presented data:

- The changes in the fill factor are the smallest among the parameters considered, with maximum ϵFF values not exceeding 10%;
- At low boron concentrations ($N_B < 10^{16} \text{ cm}^{-3}$), the dependence of ϵFF on N_{Fe} is notably non-linear. Within the used concentration range, two regions of decrease and two regions of increase in ϵFF are observed. A similar relationship between the fill factor and defect concentration was observed in BaZrSe_3 -based perovskite solar cells [6];
- At low boron concentrations, the change in fill factor value is positive and, in contrast to ϵV_{OC} and ϵI_{SC} , AM1.5 illumination causes more significant changes in ϵFF than monochromatic illumination. At high boron concentrations, the ϵFF is negative and does not exceed 4%;
- The absolute value of ϵFF increases, regardless of the value sign, with temperature increases;
- Increasing the base thickness leads to a decrease in ϵFF (a reduction in the fill factor with increasing d_p is expected according to (10)). Additionally, this results in a shift of the ϵFF (N_{Fe}) dependence towards lower iron concentrations. The impact of d_p is more pronounced at low boron concentrations and in the case of AM1.5 illumination;

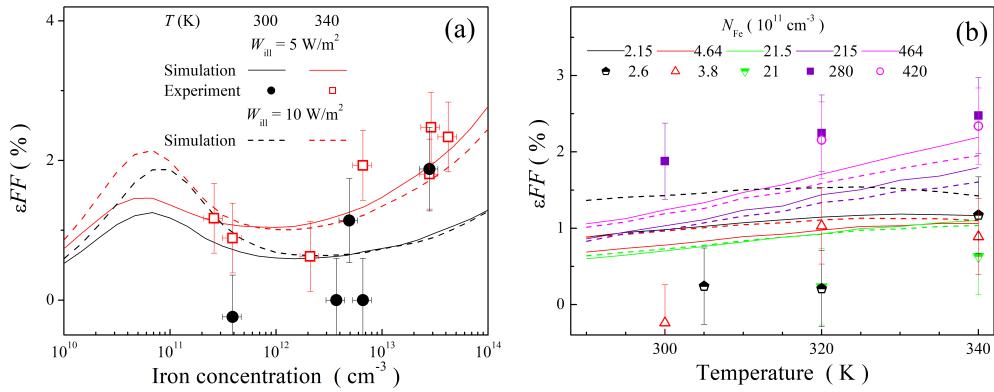


Figure 9: Relative changes in fill factor caused by a complete dissociation of Fe_3B_2 pairs as a function of iron concentration (a) and temperature (b) for SSC with $d_p = 380 \mu\text{m}$ and $N_B = 1.36 \times 10^{15} \text{ cm}^{-3}$ in the case of monochromatic (940 nm) illumination. The marks are the experimental results, the lines are the simulation results. W_{ill} , W/m^2 : 5 (marks and solid lines), 10 (dotted lines). Different lines and marks correspond to different temperatures (a) or N_{Fe} values (b) — see legends.

- In the case of monochromatic illumination, the light intensity significantly affects the relative changes in the fill factor (ϵFF can vary by a factor of 2 when W_{ill} changes from 5 to 10 W/m^2). This impact is influenced by both iron concentration (which can even change the sign of the effect) and temperature.

Fig. 9 shows that the experimental dependencies of $\epsilon FF(N_{\text{Fe}})$ and $\epsilon FF(T)$ align well with the calculated values.

Figure 9 shows that the experimental dependencies $\epsilon FF(N_{\text{Fe}})$ and $\epsilon FF(T)$ are in good agreement with the calculated values. In our opinion, the quantitative agreement is limited by the relatively low accuracy of ϵFF measurements and the dependence of fill factor on series and shunt resistances [69, 70], which were not considered in the simulation.

The observed characteristics of ϵFF suggest that the fill factor is considerably less suitable for estimating iron concentration in SSCs than the short-circuit current and open-circuit voltage. ϵFF can serve as an auxiliary parameter to refine N_{Fe} ; however, if monochromatic illumination is used, light intensity must be controlled with high precision.

3.4. Solar cell efficiency

Solar cell efficiency depends on all the photovoltaic conversion parameters previously discussed:

$$\eta = \frac{I_{\text{SC}} V_{\text{OC}} \text{FF}}{W_{\text{ill}} A}, \quad (11)$$

where A is the illuminated area of the solar cell. Considering the differential of Eq. (11), a cumulative effect on the relative changes in efficiency can be anticipated.

Considering the differential of formula (11):

$$d\eta = \frac{dI_{\text{SC}}}{I_{\text{SC}}} + \frac{dV_{\text{OC}}}{V_{\text{OC}}} + \frac{d\text{FF}}{\text{FF}}, \quad (12)$$

a cumulative effect on the relative changes in efficiency can be anticipated. Fig. 10 illustrates the simulation results for the solar cell efficiency, while Figs. S17–S20 offer additional details in the Supplementary Material.

The data indicate that the primary features of the $\epsilon\eta$ dependencies on solar cell parameters and temperature align with those observed for ϵI_{SC} . However, a few differences are evident: 1) the amplitude of $\epsilon\eta$ is enhanced, reaching up to 50% for AM1.5 and 200% for 940 nm; these results align with the expectations from Eq. (12) and make SC efficiency more convenient for iron concentration estimating; 2) for AM1.5, in the region $N_B < 5 \times 10^{15} \text{ cm}^{-3}$, a non-monotonic dependence of $\epsilon\eta(N_{\text{Fe}})$ is observed, rendering it impossible to use relative changes in efficiency as the sole parameter for iron concentration estimating under specified conditions; 3) the existing dependence of $\epsilon\eta$ on the intensity of the monochromatic illumination is weak, which does not prevent the use of $\epsilon\eta$ for determining N_{Fe} , even with not very precise W_{ill} measurements; 4) the temperature dependence of $\epsilon\eta$ is weaker than that of ϵI_{SC} .

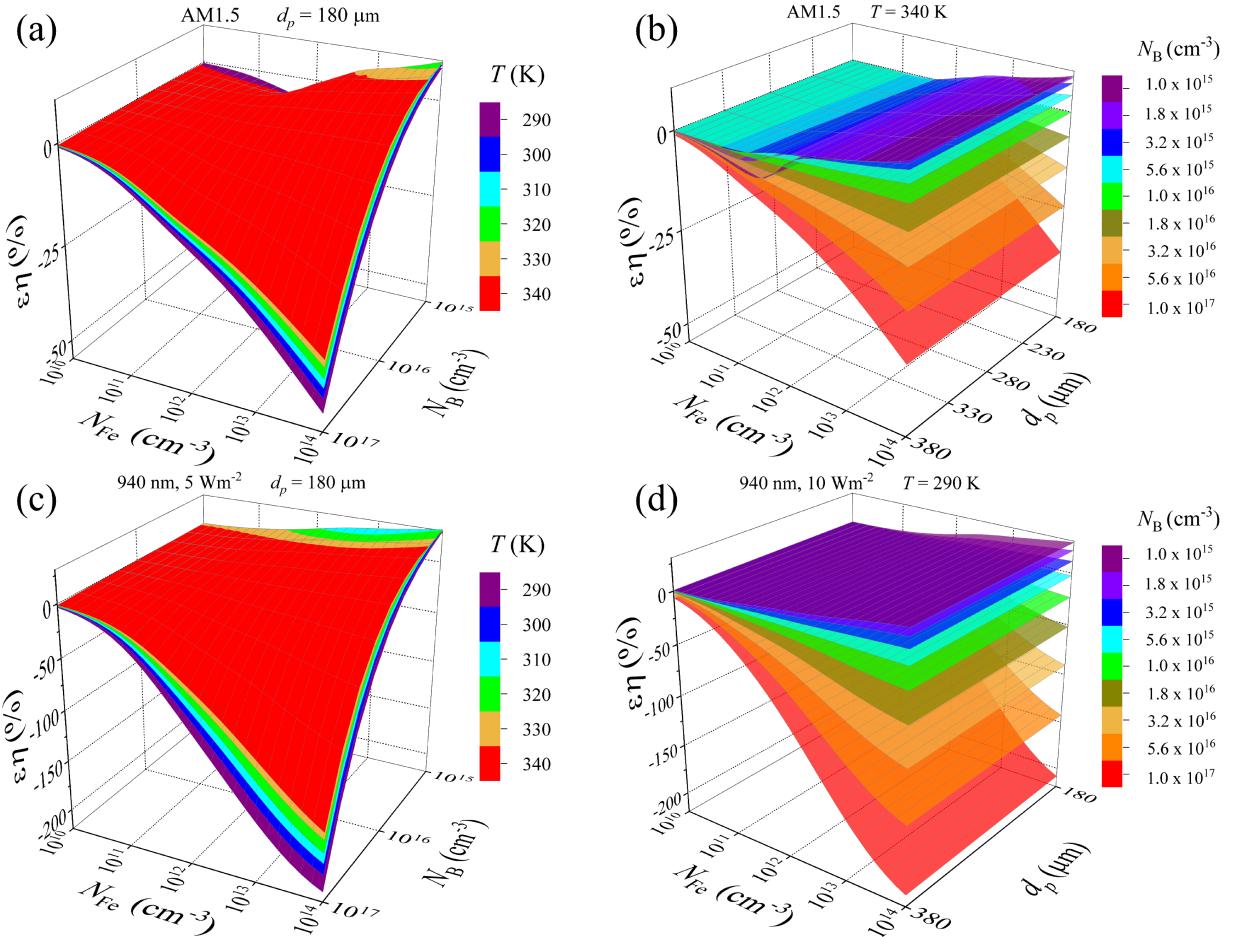


Figure 10: Relative changes in SSC efficiency caused by a complete dissociation of Fe_iB_s pairs as a function of iron concentration and doping level (panels a and c) or base depth (b, d). Illumination: AM1.5 (a, b), 940 nm 5 W/m^2 (c), 940 nm 10 W/m^2 (d). T, K : 290 (d), 340 (b). $d_p, \mu\text{m}$: 180 (a, c). Different surfaces correspond to different temperatures (a, c) and doping levels (b, d).

Fig. 11 shows the experimental and simulated values of changes in the efficiency of the solar cell with a $380 \mu\text{m}$ base thickness and a doping concentration of $1.36 \times 10^{15} \text{ cm}^{-3}$. When presenting the experimental data, the same correction factor, $C_{\text{cor}} = 1.4$, was applied as in the case of the short-circuit current. The data align closely, indicating that the inaccuracies typical for V_{OC} and FF do not significantly contribute.

The revealed characteristics of $\epsilon\eta$ indicate that this photoelectric parameter is entirely suitable for estimating iron concentration.

3.5. Photoelectric parameters correlation

The previous subsections demonstrated that by using the relative changes in photovoltaic energy conversion parameters following the dissociation of FeB pairs (e.g., changes in short-circuit current), along with considering solar cell parameters (such as base depth and doping level) and measurement conditions (such as temperature and illumination type), it is possible to predict iron concentration. One approach to evaluating the value of N_{Fe} is to apply a machine learning algorithm (random forest, gradient booster, or artificial neural network etc.). If we assume that training process is conducted separately for each illumination variant, the input set of descriptors could be $(T, d_p, N_B, \epsilon I_{\text{SC}})$. Obviously, the $\epsilon\eta$ value can be used simultaneously with ϵI_{SC} for a more accurate determination of iron concentration. Indeed, expanding the set of descriptors allows the incorporation of additional information, thereby improving prediction precision. However, when comparing Fig. 3 and Fig. 10, it is clear that ϵI_{SC} and $\epsilon\eta$ are not

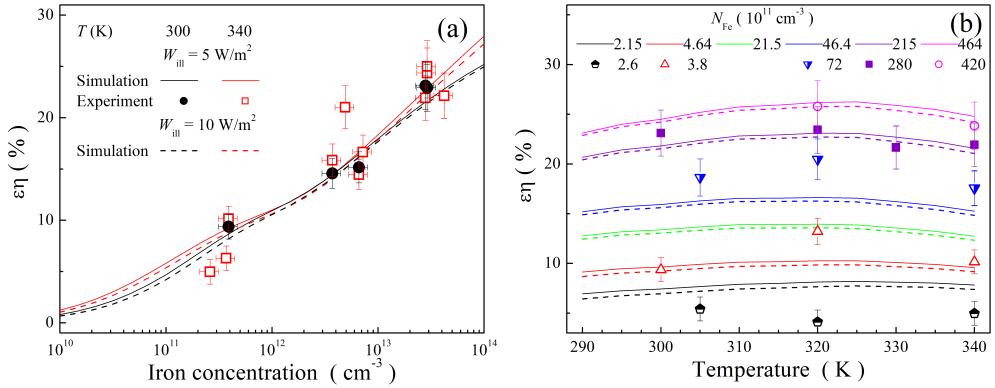


Figure 11: Relative changes in SSC efficiency caused by a complete dissociation of Fe_iB_s pairs as a function of iron concentration (a) and temperature (b) for SSC with $d_p = 380 \mu\text{m}$ and $N_B = 1.36 \times 10^{15} \text{ cm}^{-3}$ in the case of monochromatic (940 nm) illumination. The marks are the experimental results (divided by factor $C_{\text{cor}} = 1.4$), the lines are the simulation results. W_{ill} , W/m^2 : 5 (marks and solid lines), 10 (dotted lines). Different lines and marks correspond to different temperatures (a) or N_{Fe} values (b) — see legends.



Figure 12: Correlation plot of photoelectric conversion parameters and solar cell characteristics. Data above and below the main diagonal correspond to AM1.5 and 940 nm (5 W/m^2) illumination, respectively.

entirely independent. Therefore, with an input parameter set ($T, d_p, N_B, \varepsilon I_{\text{SC}}, \varepsilon\eta$), we may be processing redundant data that offer no new or additional information regarding iron concentration.

Analyzing their correlations can help evaluate the independence of the parameters. Fig. 12 presents the Pearson correlation coefficients calculated for all parameter sets. Additionally, it shows the correlation between iron concentration and each input parameter. It's worth noting that the N_{Fe} and N_B values in the logarithmic scale were used in calculations. It is a common approach for quantities that span several orders of magnitude [72].

Firstly, it is noteworthy that, as indicated by the obtained data, the value of N_{Fe} exhibits a weak correlation with each descriptor. Consequently, using any parameter in isolation from others is not feasible for precise iron concentration estimation. Regarding the descriptors associated with photovoltaic energy conversion, all of these parameters correlate strongly with the base doping level, except for open-circuit voltage under AM1.5 illumination. In addition, these parameters are substantially correlated with each other, which is particularly noticeable when using

Table 2

PSA results for sets of variables that serve to estimate the iron concentration in SSC. The numbers represent the ratio of information variance associated with each principal component when using AM1.5 illumination / 940 nm illumination.

set of descriptors	Explained Variance Ratio (%)						
	PC0	PC1	PC2	PC3	PC4	PC5	PC6
(T , d_p , N_B , ϵI_{SC})	43.23/42.80	25.00/25.00	25.00/25.00	6.70/7.20	—	—	—
(T , d_p , N_B , ϵI_{SC} , $\epsilon\eta$)	52.39/52.46	20.00/20.00	20.00/20.00	7.48/7.51	0.13/0.03	—	—
(T , d_p , N_B , ϵI_{SC} , $\epsilon\eta$, ϵV_{OC})	44.40/59.02	18.78/16.73	16.67/16.67	16.46/6.28	3.61/1.29	0.08/0.01	—
(T , d_p , N_B , ϵI_{SC} , $\epsilon\eta$, ϵV_{OC} , ϵFF)	43.29/63.24	22.59/14.41	14.29/14.29	14.19/5.65	4.29/1.95	1.35/0.46	0.002/0.01

monochromatic illumination. Thus, augmenting the descriptor set by incorporating relative changes in additional photoelectric parameters introduces substantial redundancy in the input data.

To assess the redundancy of information, we can use principal component analysis (PCA), widely used in solving various problems, including identifying defects in solar cells [73]. PCA uses a linear combination of the original variables to build the new variables (principal component, PC) while keeping maximum variance information. PCs are not correlating with each other and in the case of some particular principal component having a low information variance ratio, it can be discarded with little to no loss of useful information.

PCs were built for different combinations of photovoltaic parameters and solar cell characteristics for the full set of simulated data, and the results are listed in Table 2. As evident, when only changes in short-circuit current are considered along with the solar cell's base parameters and temperature, there is no excessive information present. Adding $\epsilon\eta$ to the set of descriptors practically does not change the number of independent variables. With the additional use of ϵV_{OC} values obtained under AM1.5 illumination, it is advisable to consider five independent variables. For the same set of descriptors in a monochromatic illumination case, one can limit oneself to using only four independent components (cumulative variance ratio for PC4 and PC5 does not exceed 1.3%). When considering changes in all photoelectric parameters due to complete dissociation of Fe_iB_s pairs, the actual number of independent variables is six for AM1.5 illumination and five for 940 nm lighting.

4. Conclusion

We have provided the results of modeling the impact of variations in the state of iron impurities on the photovoltaic parameters of silicon solar cells with different base properties under various external conditions (temperature, intensity, and spectral composition of illumination). The simulation results have been compared with experimental data.

The feasibility of using relative changes in short-circuit current, open-circuit voltage, fill factor, and efficiency resulting from the dissociation of FeB pairs to estimate the concentration of iron impurities in a solar cell has been analyzed. It is shown that changes in short-circuit current are the most suitable parameter. It is more expedient to determine the photovoltaic parameters under monochromatic illumination with a wavelength matching the predominant absorption in the solar cell base rather than using AM1.5 illumination. Next in suitability are changes in efficiency and open-circuit voltage, although their use becomes restricted at low doping levels of the base ($< 10^{16} \text{ cm}^{-3}$). In our opinion, using the fill factor to estimate iron concentration is not practical.

It has been shown that the potential accuracy of estimating iron concentration depends on the doping level of the base: at a boron concentration around 10^{16} cm^{-3} , it is minimal, while decreasing or increasing this value enhances the response of I_{SC} to the presence of iron. Furthermore, the accuracy of N_{Fe} determination is significantly influenced by the availability of precise information on the doping level of the base, as well as the accuracy of estimating the intensity of monochromatic illumination, especially when using $\epsilon\eta$ and ϵV_{OC} .

At the same time, $\epsilon\eta$ and ϵV_{OC} can serve as additional parameters for refining the determination of iron concentration. In our opinion, for estimating iron concentration through changes in photovoltaic parameters due to variability in iron-related defects, it is advisable to use a set of (T , d_p , N_B , ϵI_{SC} , $\epsilon\eta$) or (T , d_p , N_B , ϵI_{SC} , $\epsilon\eta$, ϵV_{OC}). In these cases, to expedite calculations, it is advisable to use principal component analysis to reduce the number of variables while retaining the maximum variance information.

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Supplementary data

Supplementary data to this article can be found online at <http://surl.li/qneich>

Data availability

Data will be made available on request.

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