

# Hydrogen-induced defects in ion-implanted Si

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(Received 4 July 2012; published 20 September 2012)

Single crystalline silicon implanted with  $^{28}\text{Si}$  ions and subsequently hydrogenated from an rf plasma at  $200^\circ\text{C}$  is studied by Raman and photoluminescence spectroscopy. A broad Raman band at  $3830\text{ cm}^{-1}$  previously assigned to the rovibrational transitions of hydrogen molecules trapped in Si multivacancies [Ishioka *et al.*, *Phys. Rev. B* **60**, 10852 (1999)] reveals a complex line shape at 60 K. In contrast, our study correlates the Raman band to three different localized traps for hydrogen molecules which are identified from the dependence on the ion dose and annealing behavior. Each of these traps, which is saturated with  $\text{H}_2$ , gives rise to three Raman transitions due to para- and ortho- $\text{H}_2$ . The  $\text{H}_2$  signals are shown to correlate with the Si-H vibrational modes at 1888, 1930, and  $1964\text{ cm}^{-1}$ . Ortho to para conversion rates of  $\text{H}_2$  at 77 K and room temperature were found to be  $62 \pm 15$  and  $8 \pm 2$  h, respectively.

DOI: 10.1103/PhysRevB.86.125205

PACS number(s): 78.30.Am, 61.72.jd, 61.72.uf, 61.80.Jh

## I. INTRODUCTION

Molecular hydrogen in silicon may occur at various places of the host lattice: (i) the interstitial  $T_d$  site<sup>1,2</sup>; (ii) in hydrogen-induced platelets<sup>3</sup>; (iii) bound to interstitial oxygen<sup>4-7</sup>; or (iv) trapped in multivacancies.<sup>8,9</sup>

Implantation of high energy ions results in the formation of different intrinsic defects, among others vacancy-related complexes. Raman spectra from samples subjected to a subsequent hydrogenation reveal a vibrational band of hydrogen molecules at  $3820\text{ cm}^{-1}$ .<sup>8,9</sup> The same signal also appears in the spectra of proton-implanted silicon<sup>10</sup>—a key part of the ion-cut technology developed to transfer and bond thin Si layers to a silicon substrate.<sup>11</sup>

It has been always assumed that the blistering of the surface layer in the ion-cut wafer occurs due to the pressurized  $\text{H}_2$  gas filling the blister cavities.<sup>12</sup> Thus, it seems to be natural to suggest that the  $3820\text{-cm}^{-1}$  band is due to molecules trapped in multivacancies which serve as precursors for the cavities.<sup>8,9</sup> The  $3820\text{-cm}^{-1}$  band, however, disappears from the Raman spectra after annealing the samples at around  $250^\circ\text{C}$ , which indicates that it cannot be directly related to  $\text{H}_2$  pressurizing the blisters that show up at higher temperatures.

The isolated vacancy and a number of complexes containing vacancies have been observed experimentally and discussed theoretically.<sup>13</sup> Theory predicts that the ring hexavacancy ( $V_6$ ) is a particularly stable defect<sup>14,15</sup> which in photoluminescence (PL) gives rise to the  $J$  lines ( $B_{80}^4$  center).<sup>16-18</sup> Hourahine *et al.* have found that if the material contains hydrogen molecules, these will be readily trapped by  $V_6$  where  $\text{H}_2$  dissociates with a barrier of less than 0.23 eV and forms Si-H complexes,<sup>16</sup> giving rise to the trigonal  $V_6\text{H}_2$  defects associated with the  $B_{41}$  and  $B_{71}^1$  PL centers.<sup>19,20</sup>

Saito *et al.*<sup>21</sup> and Akiyama and Oshiyama<sup>22</sup> theoretically investigated  $\text{H}_2$  trapped in hydrogen saturated vacancies  $\text{VH}_4$ ,  $\text{V}_2\text{H}_6$ ,  $\text{V}_6$ , and  $\text{V}_{10}$ . The vibrational modes of the molecules were found to be between those of the gas phase ( $4161\text{ cm}^{-1}$ ) and that of the interstitial  $T_d$  site ( $3627\text{ cm}^{-1}$ ). The frequency of  $\text{H}_2$  grows with the cluster size and reaches the vacuum value already for  $\text{V}_6\text{H}_{12}$ . The authors suggested that the  $3820\text{-cm}^{-1}$  band is associated with  $\text{H}_2$  at  $\text{V}_2\text{H}_6$ . No unambiguous experimental evidence, however, has been presented that hydrogen molecules exist in multivacancies.

Here we report the results of a combined Raman scattering and photoluminescence study performed at liquid helium temperatures. Single crystalline silicon samples were implanted with  $^{28}\text{Si}$  ions and subsequently hydrogenated from an rf plasma at  $200^\circ\text{C}$ . Earlier Raman investigations, carried out at room temperature, could not unveil the nature of the  $3820\text{-cm}^{-1}$  band, in particular, due to significant broadening of this vibrational mode.<sup>8-10,23</sup>

The total nuclear spin of  $\text{H}_2$  can be either 1 (ortho hydrogen,  $o\text{-H}_2$ ) or 0 (para hydrogen,  $p\text{-H}_2$ ). According to the Pauli principle the total wave function of any fermionic system has to be antisymmetric with respect to the permutation of the nuclei. Hence, only odd (even) values of the rotational quantum number  $J$  are allowed for  $o\text{-H}_2$  ( $p\text{-H}_2$ ).<sup>24</sup> The conversion between  $p$ - and  $o\text{-H}_2$  in silicon is remarkably slow because the nuclear spin of proton interacts only weakly with the lattice. Ortho-para conversion for interstitial  $\text{H}_2$ ,<sup>25,26</sup> the molecule bound to oxygen,<sup>27</sup> and in hydrogen-induced platelets<sup>28</sup> was investigated. The origin of a magnetic moment resulting in the nuclear spin flip of  $\text{H}_2$  is still not clear though a number of models were discussed.<sup>25,26,29</sup> Here the conversion rate of  $\text{H}_2$  giving rise to the  $3820\text{-cm}^{-1}$  band is studied to get further insight into the defect's structure.

## II. EXPERIMENTAL DETAILS

For this study,  $p$ -type float-zone silicon wafers with a resistivity of  $9.5\ \Omega\text{ cm}$  were implanted with  $200\text{ keV }^{28}\text{Si}$  ions to the doses of  $8 \times 10^{13}$ ,  $2 \times 10^{14}$ , and  $4 \times 10^{14}\text{ cm}^{-2}$ , respectively. According to SRIM simulations,<sup>30</sup> the penetration depth of Si ions at this energy is 450 nm. Subsequently, the samples were hydrogenated from a remote rf plasma (13.56 MHz, 40 W) at 200 or  $230^\circ\text{C}$  for 30 min.

Raman measurements were performed using the 532 nm Nd:YVO<sub>4</sub> laser line (1 W) for excitation. The samples were mounted in a coldfinger cryostat cooled with liquid He. The temperature of the sample during the measurements was controlled from the Stokes/anti-Stokes intensity ratio of the silicon optical phonon line at  $520\text{ cm}^{-1}$  and reached around 60 K. The spectral resolution was  $7\text{ cm}^{-1}$ , whereas the integration time varied between 1 and 4 h. Polarized Raman spectra were measured at room temperature. The polarization

geometry is defined with respect to the (100) surface of the sample: The  $x$ ,  $y$ , and  $z$  axis are parallel to the crystallographic axis  $[100]$ ,  $[010]$ , and  $[001]$ , whereas  $y'$  and  $z'$  are parallel to  $[01\bar{1}]$  and  $[011]$ , respectively. In the notation  $[a(b,c)d]$ ,  $a(d)$  refers to the propagation vector of the incident (scattered) light, while  $b(c)$  refers to the polarization vector of the incident (scattered) light. The polarized spectra were corrected with respect to the grating efficiency by calibration with a white light source.

Photoluminescence spectra were obtained with a 514 nm  $\text{Ar}^+$  laser (50 mW). During the measurements, the samples were immersed in a helium bath cryostat.

### III. RAMAN AND PHOTOLUMINESCENCE SPECTRA

#### A. General properties of the Raman lines

Figure 1 presents Raman spectra obtained for silicon samples implanted with  $^{28}\text{Si}$  ions and subsequently hydrogenated from an rf plasma. The left panel in the figure shows the optical lattice phonon signal at  $520\text{ cm}^{-1}$ . Its intensity decreases with the implantation dose, which is explained by the enhanced radiation damage of the sample caused by the  $^{28}\text{Si}$  ions.

The panel in the middle of the figure shows sections of the Raman spectra typical for the Si-H local vibrational modes (LVMs). The lines at  $2148$ ,  $2190$ , and  $2220\text{ cm}^{-1}$  originate from the vacancy-hydrogen complexes  $\text{VH}_2$ ,  $\text{V}_2\text{H}_6$ , and  $\text{VH}_4$ , respectively.<sup>31,32</sup> Two weak features at  $2025$  and  $2043\text{ cm}^{-1}$  were previously assigned to the LVMs of some unknown hydrogen-terminated Si dangling bonds.<sup>23</sup> The  $1964\text{ cm}^{-1}$  line was tentatively attributed to hydrogen saturated multivacancies.<sup>8</sup> The nature of the  $1888$ - and  $1930\text{ cm}^{-1}$  lines is unknown.

The right panel in the figure presents LVMs of  $\text{H}_2$  at around  $3830\text{ cm}^{-1}$ . Similar to the  $520\text{ cm}^{-1}$  phonon line, the integrated intensity of this band decreases with the implantation dose. The  $3830\text{ cm}^{-1}$  feature reveals a substructure, which, due to the thermal broadening of the Raman signals at elevated temperatures, can be detected only for temperatures

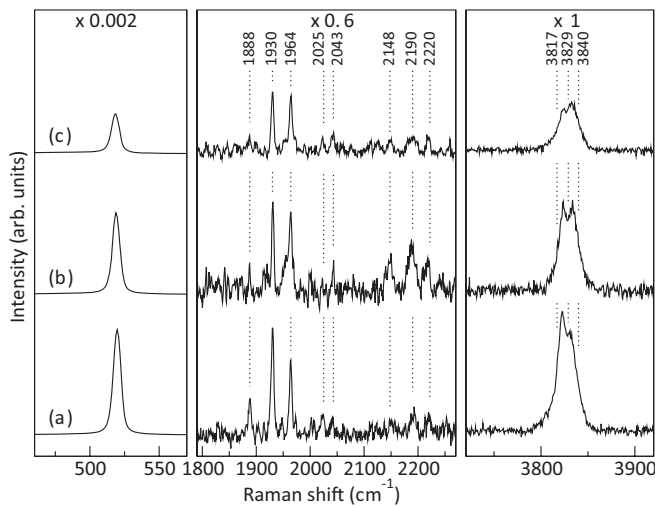


FIG. 1. Raman spectra of an as-prepared Si sample obtained at 60 K. The Si ion implantation doses are (a)  $8 \times 10^{13}$ , (b)  $2 \times 10^{14}$ , and (c)  $4 \times 10^{14}\text{ cm}^{-2}$ . The spectra are vertically offset for clarity.

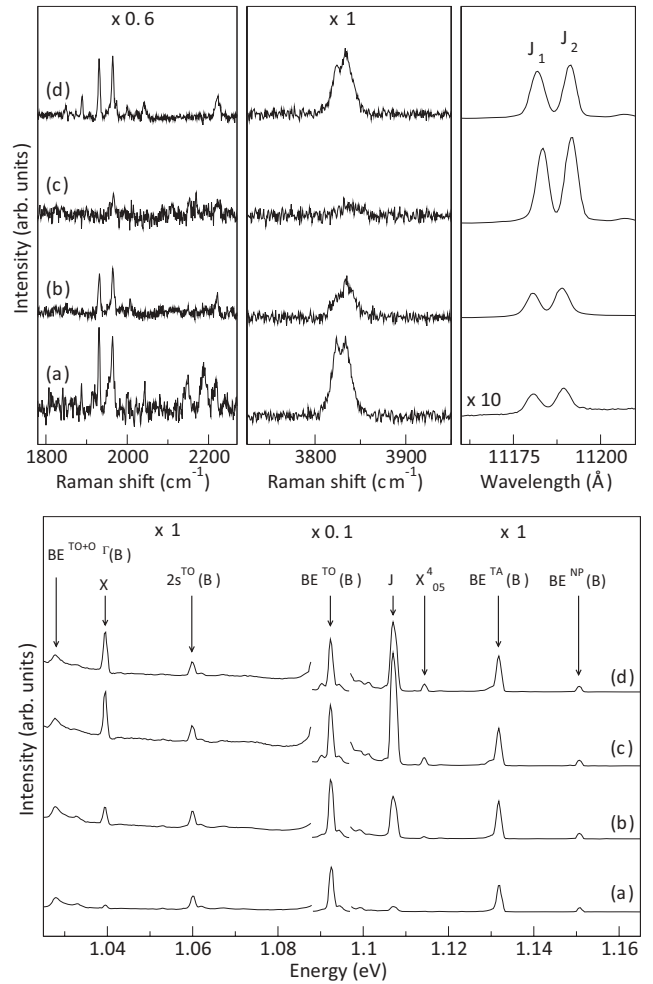


FIG. 2. Top: Raman (left and mid) and PL (right) spectra recorded for (a) an as-prepared Si sample; (b) after annealing at 250 and (c) 300 °C; and (d) after subsequent rehydrogenation at 200 °C. The Raman and PL measurements were performed at 60 and 4.2 K, respectively. The Si ion implantation dose is  $2 \times 10^{14}\text{ cm}^{-2}$ . The spectra are vertically offset for clarity. Bottom: PL spectra of the whole spectral range taken under same conditions like the upper spectra.

below 100 K. The shape of the  $3830\text{ cm}^{-1}$  band also depends on the implantation dose, which suggests that there are at least two different binding centers for the molecule. We will show in the next section that this band is composed of three complexes containing hydrogen molecules which give rise to  $Q(0)$  transitions at  $3840$ ,  $3829$ , and  $3817\text{ cm}^{-1}$ . We will label these complexes as  $K^{(1)}$ ,  $K^{(2)}$ , and  $K^{(3)}$ , respectively.

Ishioka *et al.* associated the  $3830\text{ cm}^{-1}$  band with  $\text{H}_2$  trapped in multivacancies formed by the ion implantation.<sup>9</sup> In order to get a deeper insight into the nature of the  $K^{(1)}$ ,  $K^{(2)}$ , and  $K^{(3)}$  complexes, an annealing series up to 300 °C followed by a rehydrogenation was performed. After each processing step, Raman and photoluminescence spectra were obtained. The results are presented in Fig. 2.

In accordance with previous studies, we find that the  $\text{VH}_2$  and  $\text{V}_2\text{H}_6$  complexes are unstable against annealing at 300 °C, whereas  $\text{VH}_4$  can be destroyed only at temperatures above 500 °C.<sup>31,32</sup> The results presented in the figure are

also consistent with the assignment of the 3817-, 3829-, and 3840- $\text{cm}^{-1}$  modes of  $\text{H}_2$  to different complexes since the relative intensities of these lines depend on the details of the sample treatment. We also conclude that the  $K^{(1)}$  complex is thermally more stable than  $K^{(2)}$  and  $K^{(3)}$ .

The  $\text{H}_2$  vibrational modes practically disappear from the spectra after annealing at 300 °C together with the LVMs of Si-H at 1888, 1930, and 1964  $\text{cm}^{-1}$ . Interestingly, these signals are recovered after an additional hydrogenation at 200 °C, which suggests that the binding centers for hydrogen are stable up to 300 °C.

As mentioned above, hydrogen-saturated hexavacancies were discussed as possible traps for  $\text{H}_2$  giving rise to the 3830- $\text{cm}^{-1}$  band. Previously, it was shown that the photoluminescence signal at around 1.107 eV ( $J$  lines or  $B_{80}^4$  centers)<sup>17,18,33</sup> originates from  $V_6$ .<sup>16</sup> In order to find out if there is a connection between the 3830- $\text{cm}^{-1}$  band and the  $J$  lines, PL spectra were recorded after each annealing step and an additional rehydrogenation (right panel in upper spectrum of Fig. 2). The photoluminescence spectra of the whole spectral range (bottom of Fig. 2) show mostly boron-related excitonic signals. Three radiation-induced peaks at 1.0398 eV ( $X$  center<sup>34</sup>), 1.1075 eV ( $J$  lines or  $B_{80}^4$  center), and 1.1144 eV ( $X_{05}^4$  center<sup>35</sup>) are present in all spectra and show similar annealing behavior. It is expected that the intensities of the  $J$  lines after rehydrogenation [Fig. 2(d), top spectra] are close to those (a factor of 30 weaker) obtained for the as-prepared samples [Fig. 2(a), top spectra] if the 3830- $\text{cm}^{-1}$  line originates from the  $V_6\text{H}_2$  complex. However, no unambiguous anticorrelation between  $V_6$  and the 3830  $\text{cm}^{-1}$  is seen, which leads us to the conclusion that the hexavacancy is not responsible for the 3830- $\text{cm}^{-1}$  band.

It follows from Fig. 2 that only Si-H modes at 1888, 1930, and 1964  $\text{cm}^{-1}$  seem to correlate with the 3830- $\text{cm}^{-1}$  band. First-principles calculations by Akiyama and Oshiyama have found that of all hydrogen-saturated vacancies  $V_n\text{H}_m$  only the  $V_6\text{H}_{12}$  complex and those with  $n > 6$  reveal Si-H modes in the spectroscopic region below 2000  $\text{cm}^{-1}$ .<sup>22</sup> On the other hand, vibrational frequencies of  $\text{H}_2$  trapped in these structures are close to that of the gaseous state (4161  $\text{cm}^{-1}$ ). Therefore it seems unlikely that  $V_n\text{H}_m$  complexes can trap  $\text{H}_2$  resulting in the 3830  $\text{cm}^{-1}$  band.

## B. ISOTOPE SUBSTITUTION

Figure 3 presents Raman spectra taken after ion implantation at a dose of  $8 \times 10^{13} \text{ cm}^{-2}$  and subsequent rf-plasma treatment with hydrogen, deuterium, and a mixture of both gases, respectively. The modes at 1888, 1930, and 1964  $\text{cm}^{-1}$  redshift to 1375, 1405, and 1430  $\text{cm}^{-1}$  after substitution of hydrogen by deuterium. Note that the broad band at 1450  $\text{cm}^{-1}$  originates from the second overtone of the silicon lattice phonon. No additional lines appear in the spectra if a sample is treated simultaneously with both isotopes. Such a behavior indicates that each defect responsible for these modes comprises a single Si-H bond. A substructure of the hydrogen modes at 1888, 1930, and 1964  $\text{cm}^{-1}$  cannot be resolved in our spectra due to the maximum resolution of our Raman setup which is 3  $\text{cm}^{-1}$ .

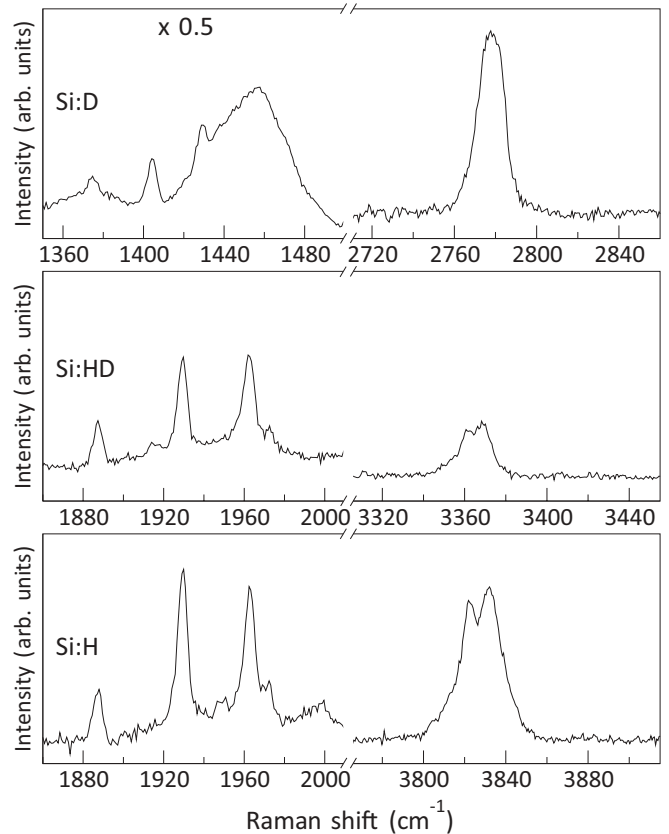


FIG. 3. Raman spectra of Si samples treated in a  $\text{H}_2$  (bottom),  $\text{H}_2 + \text{D}_2$  (middle), and  $\text{D}_2$  plasma (top) at 230 °C, respectively, after ion implantation with a dose of  $8 \times 10^{13} \text{ cm}^{-2}$ .

Isotope substitution experiments reveal the correlation between the 1888-, 1930-, and 1964- $\text{cm}^{-1}$  modes and the 3817-, 3829-, and 3840- $\text{cm}^{-1}$  lines comprising the 3830- $\text{cm}^{-1}$  band. We will show below that it takes days to convert ortho molecules to the ground para state at 77 K. This implies that each  $\text{H}_2$  Raman signal taken at helium temperatures consists of at least two lines due to the ortho and para species. Altogether, this should result in six lines comprising the 3830- $\text{cm}^{-1}$  band, which significantly complicates an analysis of the experimental data. The line shape of the  $\text{D}_2$  band at 2780  $\text{cm}^{-1}$  differs from that one of the 3830- $\text{cm}^{-1}$  band. The absence of a splitting is explained with the smaller ortho-para splitting of  $\text{D}_2$  ( $\sim 3 \text{ cm}^{-1}$ ) in comparison to  $\text{H}_2$  ( $\sim 9 \text{ cm}^{-1}$ ) which follows from the Morse potential.<sup>36</sup> This makes the quantitative analysis of the  $\text{D}_2$  LVMs even more difficult.

The situation is different for HD where all  $J$  states are in thermal equilibrium. At helium temperatures only the ground  $J = 0$  state of HD is populated. Figure 4 shows Raman spectra of a Si sample implanted with Si ions to the dose of  $8 \times 10^{13} \text{ cm}^{-2}$  and subsequently treated in the  $\text{H}_2 + \text{D}_2$  plasma at 230 °C. The spectra were taken directly after the treatment and after annealing at 240 °C. Relative intensities of the Si-H modes at 1888, 1930, and 1964  $\text{cm}^{-1}$  depend on the sample history and are 17:35:48 and 6:35:58 for the as-treated and annealed sample, respectively.

Spectra of the HD band at about 3360  $\text{cm}^{-1}$  are given in the right panel of the figure. The 3360- $\text{cm}^{-1}$  band was

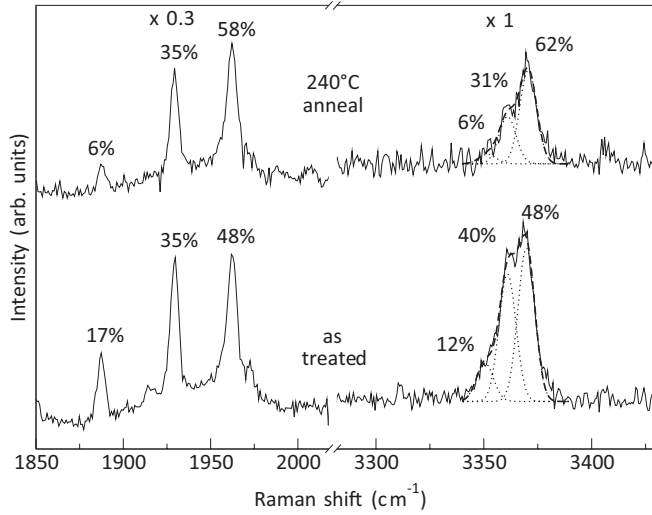


FIG. 4. Raman spectra of a Si sample treated in a  $\text{H}_2 + \text{D}_2$  plasma at  $230^\circ\text{C}$  (bottom) and after subsequent annealing at  $240^\circ\text{C}$  (top) obtained at  $60\text{ K}$ . The Si ion implantation dose was  $8 \times 10^{13}\text{ cm}^{-2}$ . For details of the fit (dashed lines) see text. The integrated intensities of the peaks normalized on the entire Si-H and HD intensities, respectively, are also given. Spectra are offset vertically for clarity.

fitted with three Gaussian functions of equal linewidth (dashed lines). Relative intensities of the fitting lines at  $3351$ ,  $3360$ , and  $3370\text{ cm}^{-1}$  were found to be  $12:40:48$  and  $6:31:62$  for the as-treated and annealed sample, respectively. This coincides within error bars with the relative intensities of the Si-H modes and gives us further support for the same origin of the  $1888$ -,  $1930$ -, and  $1964\text{-cm}^{-1}$  lines and those comprising the  $3830\text{-cm}^{-1}$  band.

### C. Thermal stability

Figure 5 presents relative intensities of the Si-H and  $\text{H}_2$  modes as a function of the annealing temperature. In agreement with the results presented in Figs. 1, 2, and 4 the intensities of the  $1888$ -,  $1930$ -, and  $1964\text{-cm}^{-1}$  lines correlate with those of the  $K$  complexes, which confirms the same origin of the LVMs due to Si-H and  $\text{H}_2$ . It also follows from the figure that thermal stability of the species grows in with the LVM frequency of the complex: The  $K^{(1)}$  complex is detected at about  $290^\circ\text{C}$ , whereas  $K^{(3)}$  disappears from the spectra after anneal at about  $260^\circ\text{C}$ .

Our results are supported by the work of Mori *et al.* who found that the  $3820\text{-cm}^{-1}$  band (RT value) consists of two lines with different thermal stabilities.<sup>37</sup> In this study, the low frequency line anneals out at  $200^\circ\text{C}$ , whereas the high frequency one disappears from the spectra after anneal at  $240^\circ\text{C}$ . The quantitative difference between our results and those reported by Mori *et al.* can be explained by different experimental conditions (starting material, implantation doses, parameters of hydrogenation, etc.).

### D. Polarized Raman spectra

Figure 6 presents polarized Raman spectra obtained at room temperature in four different scattering geometries labeled in the left panel of the figure. The sample was hydrogenated at

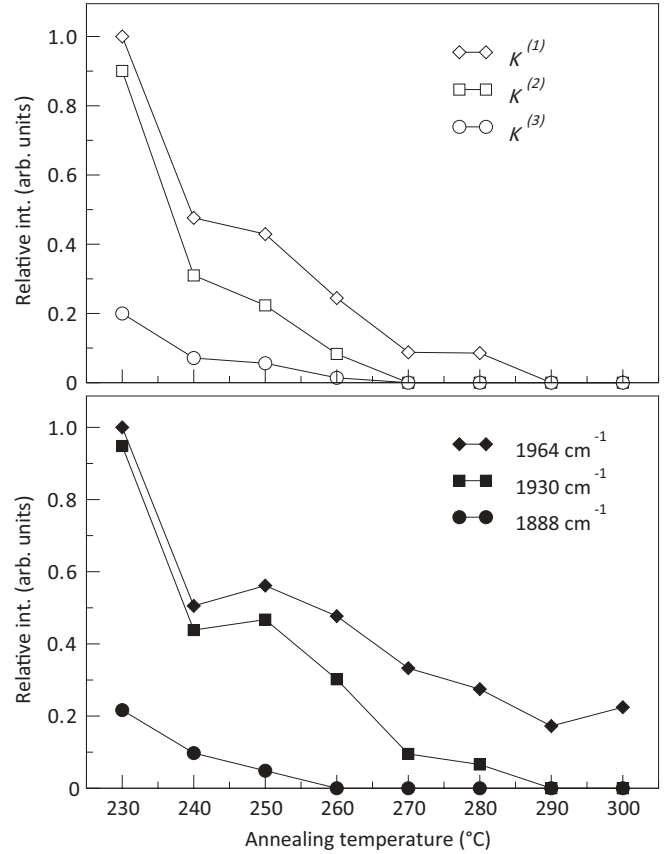


FIG. 5. Relative intensities of the  $\text{H}_2$  and Si-H LVMs taken at  $60\text{ K}$  after as a function of annealing temperature. The implantation dose was  $8 \times 10^{13}\text{ cm}^{-2}$ . Hydrogenation was done at  $230^\circ\text{C}$ .

$230^\circ\text{C}$ . The  $\text{H}_2$  band is polarized with the excitation laser light independent of the measurement geometry. This is a typical behavior of interstitial  $\text{H}_2$  in Si which follows from the values of its Raman tensor resulting in the reduction of

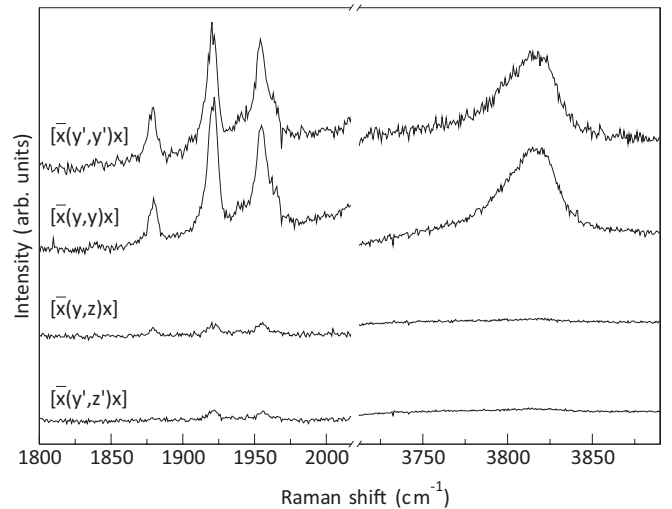


FIG. 6. Polarized Raman spectra of an as-treated sample taken at room temperature. For details of the geometry see Sec. II. Spectra are offset vertically for clarity.



the components obtained for the  $[\bar{x}(y',z')x]$  and  $[\bar{x}(y,z)x]$  geometries by around a factor of 50.<sup>7,38</sup>

The left panel in the figure shows the polarized Raman spectra of the Si-H modes at 1880, 1922, and 1956  $\text{cm}^{-1}$ . Note the redshift of these lines due to the temperature of about 300 K during the polarization dependent measurements. The 1880- $\text{cm}^{-1}$  line is most intense in the  $[\bar{x}(y',y')x]$  geometry and is basically zero in the  $[\bar{x}(y',z')x]$  geometry. This is a typical behavior of a defect with a trigonal symmetry (see Ref. 32) based on which the 1880- $\text{cm}^{-1}$  mode can be associated with a Si-H bond aligned in the  $\langle 111 \rangle$  direction of the crystal.

The polarization behavior of the 1922- and 1956- $\text{cm}^{-1}$  modes is different from that of the 1880- $\text{cm}^{-1}$  one. Both lines have maximum intensities in the  $[\bar{x}(y',y')x]$  and  $[\bar{x}(y,y)x]$  geometries, which are reduced by more than 90% in the  $[\bar{x}(y',z')x]$  and  $[\bar{x}(y,z)x]$  geometries. None of the lines disappear in the case of  $[\bar{x}(y',z')x]$  orientation, which indicates that the Si-H bonds comprising the defects are not aligned with the  $\langle 111 \rangle$  axis of the crystal. We take this as further indication that the defect complexes responsible for the 1922- and 1956- $\text{cm}^{-1}$  lines cannot be associated with the multivacancies saturated by hydrogen. Earlier, it was shown that Si-H bonds in such centers are basically aligned with the trigonal axes of the crystal.<sup>32</sup>

#### IV. QUANTITATIVE MODEL

Regardless of the nature of the  $K^{(1)}$ ,  $K^{(2)}$ , and  $K^{(3)}$  complexes, the vibrational spectrum of  $\text{H}_2$  at low temperatures should consist of transitions due to  $p$ - and  $o$ - $\text{H}_2$  in the  $J = 0$  and 1 states, respectively. In the next subsection we will show that at low temperatures the ortho-para conversion rate of  $\text{H}_2$  giving rise to the 3830- $\text{cm}^{-1}$  band is significantly slower compared to the measurement time. This implies that the ortho-to-para ratio in the spectra presented in Fig. 1 is equal to the room temperature value of 3:1.

The rotational  $J$  states of  $\text{H}_2$  are given by<sup>24</sup>

$$E(v, J) = B_v J(J + 1), \quad (1)$$

where

$$B_v = \frac{\hbar^2}{2\mu r_0^2} - \alpha_e \left( v + \frac{1}{2} \right). \quad (2)$$

Here  $v$  is the vibrational quantum number,  $\mu$  is the reduced mass of  $\text{H}_2$ , and  $r_0$  is the equilibrium distance between the hydrogen atoms in the molecule. Energetic and vibrational frequencies of  $\text{H}_2$  in different semiconductors were considered theoretically in Ref. 39. The force constant was found to be a linear function of  $r_0$ . From there we obtain that the interatomic distance for  $\text{H}_2$  giving rise to the 3830- $\text{cm}^{-1}$  band is 0.77 Å, which is between the values found for interstitial  $\text{H}_2$  in Si (0.788 Å) and that of the free molecule (0.751 Å).<sup>40,41</sup>

Assuming that  $\text{H}_2$  is trapped by a spherically symmetric potential, each  $K$  complex would result in two lines due to the  $Q(1)$  and  $Q(0)$  transitions with the relative intensities of 3:1, respectively. The frequency difference between the  $Q(1)$  and  $Q(0)$  modes is determined by the anharmonic part of the vibrational potential  $\alpha_e$  [see Eq. (2)], which, in turn, can be estimated from the frequency of the  $\text{D}_2$  counterpart of the 3830- $\text{cm}^{-1}$  band. Employing the Morse function to

model the vibrational potential<sup>24,42</sup> we get that each of the  $K$  signals should comprise a pair of lines split by about 8  $\text{cm}^{-1}$  with relative intensities of 3:1.

The model of freely rotating  $\text{H}_2$ , however, does not result in a reasonable fit of the 3830- $\text{cm}^{-1}$  band. This leads us to the conclusion that the threefold degeneracy of the  $J = 1$  state is lifted by the binding potential. Similar situation takes place for  $\text{H}_2$  bound to interstitial oxygen in Si where the  $Q(1)$  transition of  $o$ - $\text{H}_2$  splits into two states corresponding to the  $m = \pm 1$  and 0 projections of the angular momentum.<sup>6,7</sup>

In order to analyze the structure of the 3830- $\text{cm}^{-1}$  band quantitatively, we employ the simplest binding potential, whose spherical part with the  $z$  axis passing through the trap and the center of  $\text{H}_2$  is given by (a more sophisticated treatment can be found in Ref. 43)

$$V(\theta) = V_0 \cos^2 \theta. \quad (3)$$

The eigenvalues of the perturbed system are found by diagonalization of the corresponding Hamiltonian matrix  $\langle Y_J^{m_J} | V(\theta) | Y_L^{m_L} \rangle$ . Here the spherical harmonics  $Y_J^{m_J}$  form the basis set of the unperturbed system. Altogether, the 3830- $\text{cm}^{-1}$  band should comprise three groups of the  $Q(0)$ ,  $Q_0(1)$ , and  $Q_{\pm 1}(1)$  lines each of which is due to the  $K^{(1)}$ ,  $K^{(2)}$ , and  $K^{(3)}$  complexes. Note that the intensity ratio of the  $Q_0(1)$  and  $Q_{\pm 1}(1)$  transitions is now a function of temperature proportional to the Boltzmann factor  $\exp(-\Delta E/kT)$ , where  $\Delta E$  is the energy difference between the  $m = \pm 1$  and 0 states of  $o$ - $\text{H}_2$ .

Figure 7 presents a spectrum of the 3830- $\text{cm}^{-1}$  band recorded at 60 K together with the best-fit spectrum obtained according to the procedure described above. Note that only six fitting parameters were employed to simulate this spectrum. These are the value of the perturbation potential  $V_0$ , the relative concentrations of the  $K^{(1)}$ ,  $K^{(2)}$ , and  $K^{(3)}$  complexes, and the frequencies of the  $Q(0)$  modes. As seen from the figure, the simulated spectrum can adequately account for the shape of the

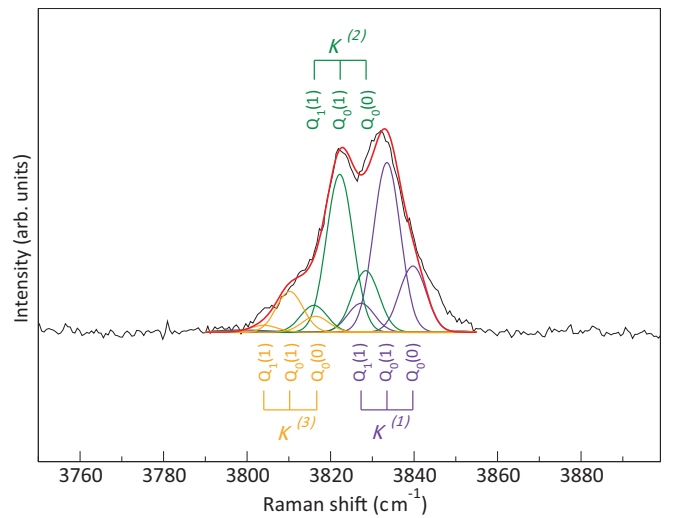


FIG. 7. (Color online) Experimental (black) and simulated (red) Raman spectra of  $\text{H}_2$  in the  $K$  defects. The experimental spectrum was obtained at 60 K for an as-prepared Si sample. The implantation dose was  $8 \times 10^{13} \text{ cm}^{-2}$ ; the temperature during hydrogenation was 230 °C. The ortho/para ratio is 3:1. For details of the fit see text.

TABLE I. Intensity ratios of the  $H_2$  signals comprising the  $3830\text{ cm}^{-1}$  band ( $K^{(2)}/K^{(1)}$  and  $K^{(3)}/K^{(1)}$ ) and the Si-H modes at 1888, 1930, and  $1964\text{ cm}^{-1}$  as a function of the implantation dose.

Dose ( $\text{cm}^{-2}$ )	$K^{(2)}/K^{(1)}$	$I_{1930}/I_{1964}$	$K^{(3)}/K^{(1)}$	$I_{1888}/I_{1964}$
$8 \times 10^{13}$	1.44	1.17	0.28	0.27
$2 \times 10^{14}$	1.06	0.92	0.20	0.17
$4 \times 10^{14}$	0.94	0.91	0.26	0.26

$3830\text{-cm}^{-1}$  band. The fit was also successfully employed to all those spectra recorded at different temperatures, for different implantation doses, and ortho-to-para ratios.

The simulations performed for different samples lead us to the energy-level diagrams of  $H_2$  in the  $K$  complexes presented in Fig. 8. Note that the  $J = 1$  state is split by  $88\text{ cm}^{-1}$ , which is comparable to the value of  $60\text{ cm}^{-1}$  found for hydrogen bound to the interstitial oxygen in Si.<sup>6,7</sup>

The relative occurrences of the three  $H_2$  signals comprising the  $3830\text{-cm}^{-1}$  band,  $K^{(2)}/K^{(1)}$  and  $K^{(3)}/K^{(1)}$ , determined from the simulated spectra are listed in Table I together with the intensity ratios  $I_{1930}/I_{1964}$  and  $I_{1888}/I_{1964}$  of the Si-H LVMs at 1888, 1930, and  $1964\text{ cm}^{-1}$ . As pointed out before, the  $K$  complexes correlate with the 1888-, 1930-, and  $1964\text{-cm}^{-1}$  lines.

Known hydrogen-related defects with frequencies of the Si-H vibrational modes below  $2000\text{ cm}^{-1}$  are the hydrogen saturated self-interstitial  $IH_2$  (1989.4, 1986.5, 748.0, and  $743.1\text{ cm}^{-1}$ ) and the hydrogen dimer  $H_2^*$  (2061.5, 1838.3, 1599.1, and  $817.2\text{ cm}^{-1}$ ).<sup>44,45</sup> The  $H_2^*$  dimer consists of one hydrogen atom located at the bond-centered site, whereas the second one occupies the antibonding position of the Si lattice. It is unlikely that the  $H_2^*$  complex acts as a binding center for hydrogen molecules, because it anneals out at  $200^\circ\text{C}$ .<sup>44</sup> This is in contradiction to the annealing behavior shown in Fig. 2, where the Si-H and  $H_2$  LVMs are recovered after annealing at  $300^\circ\text{C}$  and an additional hydrogenation. The  $IH_2$  defect, which originates from an intrinsic point defect, seems to be a more reasonable candidate for a binding center of hydrogen

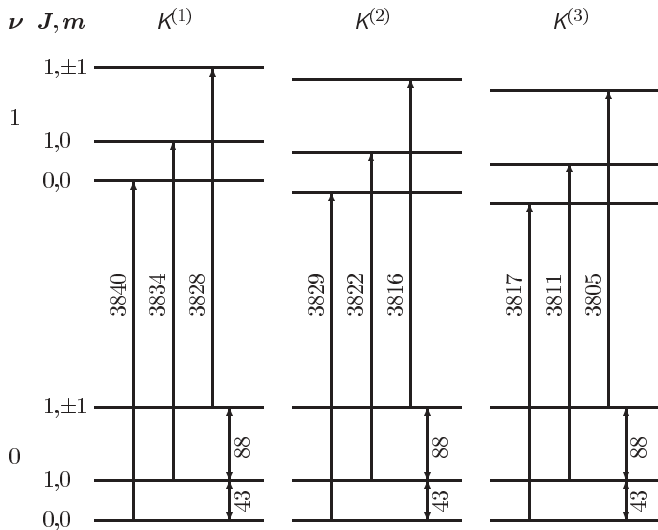


FIG. 8. Energy-level diagram of the first three rovibrational transitions of  $H_2$  in  $K^{(1)}$ ,  $K^{(2)}$ , and  $K^{(3)}$ . All values are given in  $\text{cm}^{-1}$ .

TABLE II. Ortho-para conversion rates (h) of  $H_2$  trapped at different sites of Si lattice determined at 77 and 300 K.

Trap	77 K	300 K	Ref.
$T_d$ interstitial	$229 \pm 14$	$8.1 \pm 0.5$	26
$O_i$	$140 \pm 50$	—	27
$\{111\}$ platelets	$9 \pm 4$	$6 \pm 4$	28
$K$ complexes	$62 \pm 15$	$8 \pm 2$	this work

molecules. We speculate, therefore, that the  $3830\text{-cm}^{-1}$  band is associated with the molecule trapped at interstitial-like defects rather than multivacancies. LVMs of the trapping centers deviate from the unperturbed values due to the interaction with the nearby  $H_2$ . Note that similar situation takes place in the case of the molecule trapped at the interstitial oxygen, where the LVM of oxygen in the presence of  $H_2$  shifts downwards in frequency to  $1075\text{ cm}^{-1}$  from the unperturbed value of  $1136\text{ cm}^{-1}$ .<sup>4</sup> We emphasize, however, that our suggestion about the nature of the trapping centers for hydrogen needs support from theoretical calculations.

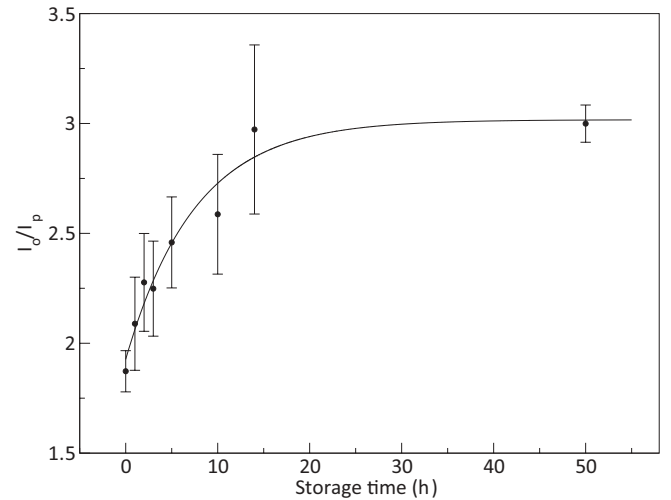
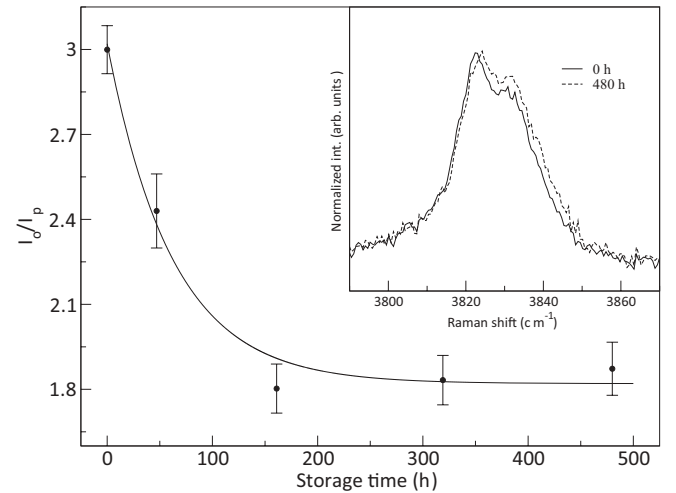


FIG. 9. Ortho-to-para ratio ( $I_o/I_p$ ) as a function of storage time at 77 (top) and 300 K (bottom). Solid lines—exponential fit with the conversion rates of 62 and 8 h, respectively. The inset shows the normalized Raman spectra obtained at 0 and 480 h.

## V. ORTHO-PARA CONVERSION

Energy-level diagrams of  $H_2$  in the  $K$  complexes presented in Fig. 8 allow us to probe the ortho-para conversion rate. Because the rovibrational properties of the hydrogen molecules in the three defects seem to be very similar, we assume that the conversion dynamic is almost the same.

Rotational levels of  $H_2$  with  $J > 1$  are practically not populated at the temperatures employed in our study and can be disregarded. Because of this, the equilibrium ortho-para ratio is determined by the lowest three levels of the molecule

$$\frac{I_o}{I_p} = 3 \frac{e^{-E_o(1)/kT} + 2e^{-E_{\pm 1}(1)/kT}}{e^{-E(0)/kT}}. \quad (4)$$

Here  $E_m(J)$  is the energy of the rotational state with a total angular momentum  $J$  and its projection  $m$ . The prefactor 3 comes from the different nuclear spin state degeneracies of the two hydrogen species. From Eq. (4) and the energy-level diagram presented in Fig. 8 we obtain that at 77 K the ortho-para ratio should be 1.8:1, which significantly differs from the cases of free and interstitial  $H_2$  resulting in equal number of each species ( $I_o/I_p = 1$ ).<sup>25</sup>

In order to determine the ortho-para conversion rate at 77 K, the samples were stored in  $LN_2$  for nearly 500 h. During the storage Raman measurements at 60 K were performed and the spectra were analyzed according to the procedure described in the previous subsection. The results are presented in Fig. 9. The solid line is the best-fit curve to the experimental data under assumption of a single exponential decay. As follows from the figure, the equilibrium value of  $I_o/I_p \approx 1.8$  agrees with the one estimated above from Eq. (4) on the basis of the energy-level diagram of  $H_2$ . From the fitting procedure we obtain that the ortho-para conversion rate is  $62 \pm 15$  h.

The ortho-para conversion at 300 K (see bottom panel of Fig. 9) was also investigated. As expected, the back conversion is a faster process yielding the rate of  $8 \pm 2$  h.

These values should be compared to those obtained for interstitial molecules,<sup>25,26</sup>  $H_2$  bound to the interstitial oxygen,<sup>27</sup>

and hydrogen trapped in platelets,<sup>28</sup> which are gathered in Table II. We see that the conversion rate of  $H_2$  bound to the  $K$  complexes is between the value found for interstitial molecule and those trapped in the  $\{111\}$  platelets. The latter system represents a two-dimensional gas under high pressure, so that the main mechanism resulting in nuclear spin flip is expected to be interaction between the neighboring molecules.<sup>28</sup>

The ortho-para conversion mechanism for interstitial  $H_2$  is still not clear.<sup>25,26,29</sup> The conversion rate of  $H_2$  giving rise to the  $3830\text{-cm}^{-1}$  band indicates that the nature of the nuclear spin flip is closer to that of interstitial molecules and molecules bound to interstitial oxygen rather than those trapped in platelets.

## VI. SUMMARY

Raman and photoluminescence spectra of  $^{28}\text{Si}$ -ion implanted and subsequently hydrogenated single crystalline silicon were presented. Such samples reveal a broad Raman line at  $3830\text{ cm}^{-1}$  (60 K) due to the rovibrational transitions of  $H_2$ . The  $3830\text{-cm}^{-1}$  band reveals a complex structure, which is assigned to three different traps for hydrogen occurring in concentrations which depend on the sample history. The  $H_2$  signals comprising the band are shown to correlate with the Si-H vibrational modes at 1888, 1930, and  $1964\text{ cm}^{-1}$ . Based on this correlation it is concluded that multivacancies cannot be the trapping centers for  $H_2$ . Ortho to para conversion rates of  $H_2$  at 77 and 300 K found to be  $62 \pm 15$  and  $8 \pm 2$  h, respectively.

## ACKNOWLEDGMENTS

This work was supported by the Deutsche Forschungsgemeinschaft (Grant No. LA 1397/3-1). S. Eisenwinder (Helmholtz-Zentrum Dresden-Rossendorf) is acknowledged for performing the ion implantation of our samples. The authors thank M. Allardt for the help with the photoluminescence measurements.

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