

# First-principles identification of deep energy levels of sulfur impurities in silicon and their carrier capture cross sections

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## Abstract

Studies of the deep energy levels and nonradiative carrier capture induced by sulfur doping in silicon were initiated 60 years ago; however, the defect configurations, their deep energy levels, and the carrier capture cross sections are still not well understood. In this study, we focus on  $S_{Si}$  substitution, and perform a first-principles study of its defect configurations and the deep energy levels using hybrid exchange-correlation functional. We discover a new distortive configuration for  $S_{Si}^+$  besides the previously obtained structure with higher symmetry. For both  $S_{Si}^+$  configurations, the deep transition levels  $\varepsilon(0/+)$  and  $\varepsilon(+/2+)$  are determined as 0.35 eV and 0.68 eV below the conduction band minimum, respectively. As a benchmark calculation, the hole-capture cross sections for neutral and +1 charged states are obtained based on the distortive structure. The cross section for  $S_{Si}^+$  agrees with the experiment, demonstrating the multi-phonon process for  $S_{Si}^+$  capturing a hole, whereas the cross section of  $S_{Si}^0$  is significantly lower than the experimental data because hole capture by  $S_{Si}^0$  is an Auger-type process. Our calculations provide a benchmark for the evaluation of the cross section of carrier capture in semiconductors using multi-phonon nonradiative recombination theory.

Supplementary material for this article is available [online](#)

Keywords: nonradiative carrier capture, sulfur doping, first-principles study

(Some figures may appear in colour only in the online journal)

## 1. Introduction

Sulfur doping in silicon has not only been used to elevate the sensitivity of the photodiodes that detect photons with energies below the band gap of silicon [1, 2], but also to enhance the absorption of photons and improve the photoelectric efficiency of solar cells because of the induced deep energy levels

[3, 4]. However, the conversion efficiency of sulfur-doped silicon solar cells is decided not only by the concentration of sulfur but also by the defect configurations [5], because deep energy levels in solar cells also induce the nonradiative carrier recombination via the Shockley–Read–Hall process, which in turn reduces the photogenerated carrier densities as well as the carrier lifetime, and thus reduces the performance of photovoltaic semiconductors [6–8]. Therefore, an in-depth understanding of the defect configurations and carrier

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recombination effects introduced by sulfur doping is of great importance to improve photovoltaic conversion efficiency.

Nevertheless, sulfurdoping in silicon has been under-researched both experimentally and theoretically. The earliest experimental studies of sulfurdoping in silicon include the work done by Carlson *et al* [9], who found that sulfur acted as a donor impurity, and donor levels were  $E_c - 0.18$  eV and  $E_c - 0.37$  eV, respectively, where  $E_c$  is the conduction band minimum (CBM). Krag and Zeiger [10] performed optical characterization at a low temperature and determined four ground-state energies: 0.109 eV, 0.187 eV, 0.368 eV, and 0.612 eV below  $E_c$ , respectively. Subsequent experiments have further determined that the four main energy levels generated from sulfurdoping are 0.188 eV, 0.318 eV, 0.371 eV, and 0.614 eV below  $E_c$ , respectively. In addition, they suggested that the energy levels are probably mainly caused by two defects: isolated substitutional sulfur ( $S_S$ ) and molecular substitutional sulfur ( $S_{2S}$ ) [11–21]. However, disagreement about the specific values of the defect energy levels still exists depending on different experiments. In terms of the nonradiative carrier recombination, Kleverman *et al* [17] employed a deep-level transient spectroscopy technique and a pulse-train method to measure the values of hole-capture cross section of single ionized  $S^+$ , and also assessed that the process of hole capture may be a multi-phonon nonradiative emission process or a combination of multi-phonon nonradiative emission and radiative capture process. From a theoretical perspective, Mo *et al* [22] found that, for an isolated S-atom in silicon, the lowest energy configuration is the substitution site by first-principles calculations. Based on the substitution defect type, Coutinho *et al* [23] calculated the transition energy levels of S-related defects in Si using a formation energy method and a marker method, but the results of these methods disagree. The formation energy method does not give transition energy levels that match the experiments for  $S_S$  and  $S_{2S}$ , whereas the marker method can only obtain the energy level of  $S_{2S}$  that matches the experiment using the measured  $S_S$  energy level as a reference. Although the defect configuration was investigated in these studies, theoretical understanding of the carrier capture cross section has not yet been reported.

Analytical models and computational approaches for capture cross sections were developed from the 1950s [24–28]; based on this, the multi-phonon nonradiative recombination process in semiconductors has been extensively studied. In recent years, theoretical studies based on multiple computational methods for a nonradiative recombination process have mainly focused on direct band gap semiconductors, such as GaN [29–33], GaP [26, 30], CdTe [34],  $Cu_2ZnSnS_4$  [35–37], and  $Cu_2ZnSnSe_4$  [38], while studies on indirect semiconductor materials such as Si have rarely been reported [39]. In particular, a combination of an electron–phonon coupling effect and static coupling formalism is used to calculate the carrier capture cross section, while the electron–phonon coupling matrix elements can be obtained using the conventional finite difference method. For large systems, the conventional finite difference method has been prohibitively time-consuming, until Shi and Wang [29] and Shi *et al* [30] developed the variational method, which has been successfully

utilized to study GaN and GaP. Subsequently, this has allowed quantitative evaluation of the capture cross section of deep energy levels in a large system [40].

In this paper, we conduct a first-principles study of the defect configurations and corresponding energy levels introduced by sulfur doping in Si, as well as the hole-capture cross sections of the deep energy levels. As a benchmark study for the indirect band gap materials, which is Si in our case, we utilize the static coupling theory and first-principles calculation of electron–phonon coupling matrix elements to calculate the hole-capture cross sections. Our main results mainly include the following three aspects. First, using the hybrid exchange–correlation functional, we determine the defect configurations of the  $S_{Si}$  substitution with different charged states, together with their corresponding deep energy levels. Other than the highly symmetric structure found in previous studies, a new distortive structure of  $S_{Si}$  substitution in a +1 charged state is discovered. Moreover, we obtain the hole-capture cross sections for a neutral and a +1 charged state, and the hole-capture cross section for  $S_{Si}^+$  to  $S_{Si}^{2+}$  agrees with the experiment. In addition, the highly symmetric structure of the  $S_{Si}^+$  gives negligibly low hole-capture cross sections, so there is a low possibility of it getting involved in the hole-capture process.

## 2. Computational methods

### 2.1. Defect calculations

Our first-principles defect calculations are performed based on density-functional theory (DFT) [41, 42] as implemented in the Vienna *Ab initio* Simulation Package (VASP) [43, 44]. The ion–electron interaction is modeled by the frozen-core projector augmented wave method [45]. The Heyd–Scuseria–Ernzerhof (HSE06) [46] hybrid functional and spin-polarization are employed for all calculations, in which 25% of the exact exchange is used. A 350 eV energy cutoff is adopted for the defect calculations. The defect is simulated using a 512-atom Si supercell with one Si atom substituted by a S atom. Only  $\Gamma$  point (0,0,0) is used to sample the first Brillouin zone. We test the defect formation energy depending on the size of the supercells, and find that a 512-atom Si supercell with  $\Gamma$  point is sufficient for the formation energy calculation. The lattice parameters are fixed and the internal coordinates are fully relaxed when the energy and force become smaller than  $1 \times 10^{-5}$  eV/atom and  $0.01$  eV  $\text{\AA}^{-1}$ , respectively.

To calculate the transition energy levels of a defect, the formation energy of a defect is given by [47–49]:

$$\Delta H(\alpha, q) = E(\alpha, q) - E(\text{host}) + \sum_i n_i (\mu_i + E_i) + q(E_F + E_{\text{VBM}}(\text{host}) + \Delta V) + \Delta E_{\text{MP}}, \quad (1)$$

where  $\mu_i$  is the chemical potential of element  $i$ , with reference to the total energy  $E_i$  of their elemental monomeric phases. The Fermi energy level  $E_F$  is referenced to the valence-band maximum (VBM) of the host of Si, so the value of  $E_F$  can vary between the VBM and the CBM.  $E(\alpha, q)$  is the total

energy of the supercell with a defect in charged state  $q$ .  $E$  (host) and  $E_{\text{VBM}}$  (host) are the total energy and the eigenvalue of the VBM of the perfect silicon supercell, respectively.  $n_i$  is the number of atoms exchanged with the external environment during the formation of defects.  $\Delta V$  is the potential alignment correction referenced to the core energy level of the atom far from the defect. Due to the periodic boundary conditions, the Coulomb interactions among the charged defects in repeating supercells are treated by the Makov–Payne correction  $\Delta E_{\text{MP}}$ , as proposed by Lany and Zunger [49].  $\Delta E_{\text{MP}}$  is given by:

$$\Delta E_{\text{MP}} = (1 + f) \frac{\alpha \times q^2}{2\epsilon L} \quad (2)$$

where  $\alpha = 1.4186$  is the Madelung constant and  $\epsilon = 11.9$  is the relative dielectric constant.  $L = 21.72 \text{ \AA}$  and  $1 + f \approx \frac{2}{3}$  are applied for all defect calculations.

The defect transition energy level  $\varepsilon(q/q')$  is defined as the Fermi energy level at which a defect transits from a  $q$ -charged state to a  $q'$ -charged state. The defect transition energy level relative to the VBM is given by:

$$\varepsilon(q/q') = \frac{\Delta H(\alpha, q) - \Delta H(\alpha, q')}{q - q'}. \quad (3)$$

## 2.2. Hole-capture cross section

The variational method proposed by Shi and Wang [29] is adopted to calculate the electron–phonon coupling matrix elements. This method only requires two self-consistent field calculations, which is significantly faster than the traditional finite-difference method. The form of electron–phonon coupling matrix elements is given by:

$$\langle \varphi_f | \frac{\partial H}{\partial Q_k} | \varphi_i \rangle = \sum_R \frac{\mu_k(R)}{\sqrt{M_R}} \langle \varphi_f | \frac{\partial H}{\partial R} | \varphi_i \rangle, \quad (4)$$

where  $f$  and  $i$  denote the final and initial states.  $M_R$  is the mass of the  $R$ th atom and  $\mu_k(R)$  is the  $R$ th component of the  $K$ th phonon eigenvector. Because of the large 512-atom supercell, the Perdew–Burke–Ernzerhof (PBE) [50] functional and spin-polarization are employed for the calculation of phonon modes using the finite displacement method, as implemented in the VASP code. The single-particle Hamiltonian  $H$  is given by:

$$H = -\frac{\hbar^2}{2} \sum_k \nabla^2 + V_{\text{tot}} + \sum_{L,R} |\phi_{L,R}\rangle \langle \phi_{L,R}|, \quad (5)$$

where  $V_{\text{tot}}$  is the total local potential for a given atomic configuration and  $|\phi_{L,R}\rangle$  is the non-local potential projector for atom  $R$  and angular momentum  $L$ . By plugging equations (5) to (4), the electron–phonon coupling constant is given by:

$$\begin{aligned} \langle \varphi_f | \frac{\partial H}{\partial R} | \varphi_i \rangle &= \langle \varphi_f | \frac{\partial V_{\text{tot}}}{\partial R} | \varphi_i \rangle \sum_{L,R} \\ &\times \langle \varphi_f | \frac{\partial}{\partial R} (|\phi_{L,R}\rangle \langle \phi_{L,R}|) | \varphi_i \rangle. \end{aligned} \quad (6)$$

The first term on the right-hand side is evaluated by  $\langle \varphi_f | \frac{\partial V_{\text{tot}}}{\partial R} | \varphi_i \rangle = \int \rho_{fi} \frac{\partial V_{\text{tot}}}{\partial R} d\mathbf{r} = \frac{dF_R}{d\lambda}$ , where  $\rho_{fi} = \text{Re} [\varphi_f^*(r) \varphi_i(r)]$  [29], and  $\frac{dF_R}{d\lambda}$  is the change of the atomic forces introduced by a small variation in the charge density based on  $\rho_{fi}$ , or  $\rho_\lambda(r) = \sum_k |\psi_k(r)|^2 + \lambda \rho_{fi}$ , where  $\lambda$  is chosen as 0.05 in our calculations. The second term is the non-local contribution, which can be calculated by the Hellman–Feynman theory in the conventional DFT calculations [51, 52]. For the spin-polarized case, when the defect captures a spin-up or spin-down electron, we add the variational charge density  $\lambda \rho_{fi}$  to the charge density of the corresponding spin state. Capturing a hole is treated in the same way as capturing an electron. The calculations of electron–phonon coupling matrix elements are implemented in Quantum Espresso code [51].

The probability of nonradiative decay between electron state  $i$  or  $f$  is given by the static coupling theory [30, 35, 53, 54] as:

$$\begin{aligned} W_{\text{if}} &= \frac{2\pi}{\hbar} \sum_n \sum_m \rho(i, n) \left| \sum \langle \psi_f | \frac{\partial H}{\partial Q_k} | \psi_i \rangle \langle \phi_{f,m} | Q_k | \phi_{i,n} \rangle \right|^2 \\ &\times \delta(\hbar\omega_{fm} - \hbar\omega_{in} + \Delta E_{\text{if}}), \end{aligned} \quad (7)$$

where  $n$ ,  $m$ , and  $k$  represent the initial phonon state, final phonon state, and phonon number, respectively.  $\psi_f | \frac{\partial H}{\partial Q_k} | \psi_i$ , also denoted as  $|C_{\text{if}}|$ , are the calculated electron–phonon coupling matrix elements.  $p(i, n)$  is the probability of the system being in the initial phonon state  $n$ .  $\phi_{f,m} | Q_k | \phi_{i,n}$  are the lattice transition matrix elements between the initial and final phonon states, and  $Q_k$  is the coordinate of the  $k$ th phonon.  $\hbar\omega_{fm}$  and  $\hbar\omega_{in}$  are the energy of the initial and final state phonons, respectively.  $\Delta E_{\text{if}}$  is the energy difference between the initial and final states. All parameters are obtained using spin-polarized calculations.

Based on the nonradiative decay probability  $W_{\text{if}}$ , the carrier capture rate  $B$  is calculated as  $B = S(T) \times V \times W_{\text{if}}$ , where  $S(T)$  is the Sommerfeld factor [36, 55, 56], which characterizes the Coulomb interaction between carriers and defects at temperature  $T$ .  $V$  is the volume of the supercell. In our work, we study the process of hole capture by the donor level, so the Sommerfeld factor  $S(T)$  denotes the repulsive interaction between a defect in charged state  $Q$  and a carrier with charge  $q$ , and is given by:

$$S(T) = \frac{8}{\sqrt{3}} \left( \frac{\pi^2 Q^2 m_h^* q^2}{2\hbar^2 \epsilon^2 k_B T} \right)^{\frac{2}{3}} \exp \left[ -3 \left( \frac{\pi^2 Q^2 m_h^* q^2}{2\hbar^2 \epsilon^2 k_B T} \right)^{\frac{1}{3}} \right], \quad (8)$$

where  $m_h^* = 0.7m_0$  is the effective mass of the hole and  $\epsilon$  is the dielectric constant of crystalline silicon.  $k_B$  is the Boltzmann constant. With the hole-capture rate  $B_h$  calculated, the corresponding hole-capture cross section is calculated as  $\sigma_h = \frac{B_h}{v_h}$ , where  $v_h = \sqrt{\frac{3k_B T}{m_h^*}}$  is the thermal velocity of the hole.

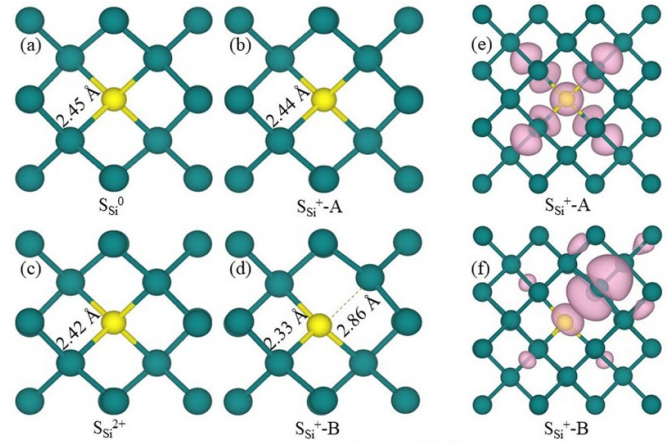
### 3. Results and discussion

The band gap of the 512-atom Si supercell at  $\Gamma$  point is calculated as 1.2 eV, which is almost identical to the result of the primitive cell, 1.15 eV. The detailed band structure of the 512-atom Si supercell is described in the supplementary information (available online at [stacks.iop.org/JPD/54/335103/mmedia](https://stacks.iop.org/JPD/54/335103/mmedia)). As mentioned above, the sulfur atom is found to prefer replacing the silicon atom when an isolated sulfur atom is doped into crystalline silicon [22]. Therefore, we focus on the  $S_{Si}$  substitution. Taking spin-polarization into consideration, we optimize the structures of the 0, +1, and +2 (three charged states of the  $S_{Si}$  substitution) separately and calculate their total energies. Based on our calculations, the  $S_{Si}$  substitution is revealed as a donor defect that can be stabilized at three charged states: 0, +1, and +2.

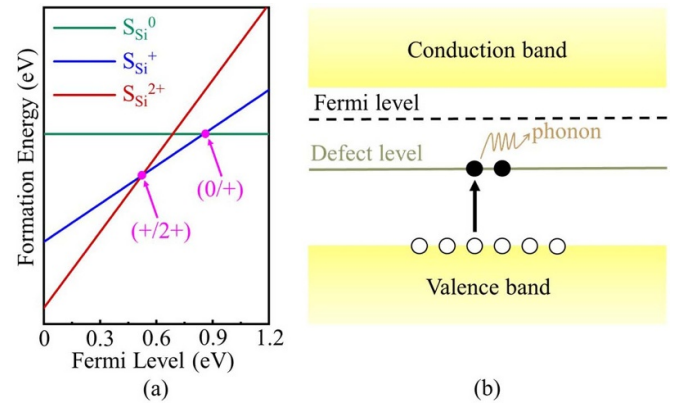
As shown in figures 1(a) and (c), the sulfur atom is found to be centrally located in the middle of four surrounding Si atoms in  $S_{Si}^0$  and  $S_{Si}^{2+}$  substitutions. The S–Si bond lengths in  $S_{Si}^0$  and  $S_{Si}^{2+}$  substitutions are 2.45 Å and 2.42 Å, respectively. The shortening of the S–Si bond length in  $S_{Si}^{2+}$  is mainly due to a stronger Coulomb interaction between the defect center  $S_{Si}^{2+}$  and the surrounding electrons. Interestingly, two distinct stable structures for  $S_{Si}^+$  substitution, denoted as  $S_{Si}^+-A$  and  $S_{Si}^+-B$  (figures 1(b) and (d)), are obtained after the structure optimization. Similar to the structure of  $S_{Si}^{2+}$  substitution, the  $S_{Si}^+-A$  has four equivalent S–Si bonds around the S atom, with the same bond lengths 2.44 Å, as shown in figure 1(b). Due to the weaker Coulomb interaction than  $S_{Si}^{2+}$  substitution, the S–Si bond length in  $S_{Si}^+-A$  is slightly longer.  $S_{Si}^+-B$  exhibits a much more distortive structure with symmetry breaking, which is similar to the distortive structure of the  $Mg_{Ga}$  defect found in GaN [57]. As shown in figure 1(d),  $S_{Si}^+-B$  has three short S–Si bonds (2.33 Å) and one long bond (2.86 Å). Such a distortive structure is not observed in either previous Perdew–Wang 91 (PW91) [23] or our PBE calculations. The total energy of the  $S_{Si}^+-B$  structure is calculated to be 0.003 eV lower than that of the  $S_{Si}^+-A$  structure.

In figures 1(e) and (f), we also plot the charge densities of the defect states of  $S_{Si}^+-A$  and  $S_{Si}^+-B$ . The defect states for  $S_{Si}^+-A$  and  $S_{Si}^+-B$  are both the antibonding states of s-p hybridization of the S–Si bonds; however, the defect state for  $S_{Si}^+-A$  is contributed to by all four S–Si bonds around S, while the defect state for  $S_{Si}^+-B$  is mainly localized on the longest S–Si bond. Using the climbing image nudged elastic band method [58], we find that the energy barrier for the structure transition from the  $S_{Si}^+-B$  to  $S_{Si}^+-A$  is 0.01 eV.

Figure 2(a) shows the relative formation energies of the three charged states of the  $S_{Si}$  substitution calculated using the method as described in equation (1). Although  $S_{Si}^+$  has two different structures, their total energies are almost the same and the calculated formation energies and transition energy levels are almost identical. Therefore, we only plot the result of the spin-polarization of a  $S_{Si}^+-B$  in figure 2(a). The calculated  $\epsilon(0/+)$  and  $\epsilon(+/2+)$  levels are 0.349 eV and 0.678 eV below the CBM, which are deep energy levels in the Si gap. Our results accurately agree with the experimental values; i.e.  $E_c - 0.32$  eV and  $E_c - 0.61$  eV, respectively [13–15, 17]. As



**Figure 1.** The atomic structures of  $S_{Si}$  substitution in three charged states: (a)  $S_{Si}^0$ , (b)  $S_{Si}^+-A$ , (c)  $S_{Si}^{2+}$ , and (d)  $S_{Si}^+-B$ . The charge densities of the defect states of (e)  $S_{Si}^+-A$  and (f)  $S_{Si}^+-B$ . S atom and Si atom are shown in yellow and green, respectively.



**Figure 2.** (a) HSE06 calculated the relative formation energies of the  $S_{Si}$  substitution at different charged states as functions of the Fermi level, using spin-polarized calculations. (b) Multi-phonon nonradiative recombination process in n-type Si.

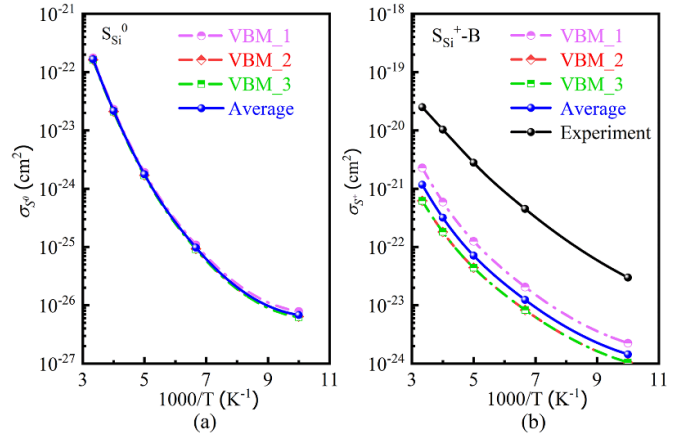
a comparison, the study by Coutinho *et al* [23] determines the transition energy levels at 0.78 eV and 1.25 eV below the CBM, respectively. Such a discrepancy is possibly due to the correction from the HSE06 hybrid functional. It is also essential to perform spin-polarized calculations, because non-spin-polarized calculations provide the wrong  $\epsilon(0/+)$  and  $\epsilon(+/2+)$  levels at 0.408 eV and 0.619 eV below the CBM. Therefore, it is also necessary to use spin-polarized calculations for the following study of the hole-capture cross section.

Experimentally, S can be doped into both n-type and p-type Si to form defects and generates deep energy levels that introduce the nonradiative recombination [2, 4, 19, 21]. Figure 2(b) shows a schematic diagram of the nonradiative recombination process for S doping in n-type silicon. In n-type Si samples, the Fermi energy level is close to the conduction band, and the deep energy level is usually occupied with electrons carriers. The deep energy level can capture a hole from the VBM, leading to a transition from the neutral state to the +1 charged



state, the cross section of which is denoted as  $\sigma_{S^0}$ . It is also possible that a second hole is captured from the VBM, leading to a transition from the  $+1$  charged state to the  $+2$  charged state, the cross section of which is denoted as  $\sigma_{S^+}$ . Due to the high concentration of electrons in n-type Si, the defect state easily captures an electron from the CBM when the deep energy level is half occupied by electrons or empty. As a result, the hole-capture cross section plays a decisive role in this recombination. Carrier capture processes in p-type Si can be understood similarly by replacing holes with electrons [40].

Following equation (7),  $\sigma_{S^0}$  and  $\sigma_{S^+}$  as functions of temperature are calculated, as shown in figure 3. For  $\sigma_{S^0}$ , the initial and final states are  $S_{Si}^0$  and  $S_{Si}^+$ , respectively, whereas for  $\sigma_{S^+}$ , the initial and final states are  $S_{Si}^+$  and  $S_{Si}^{2+}$ , respectively. The phonon modes of the initial states are used to calculate electron-phonon coupling matrices during both hole-capture processes. Only the ground state structure of the  $+1$  state  $S_{Si}^+-B$  is considered in the process of  $S_{Si}^0$  to  $S_{Si}^+-B$  and  $S_{Si}^+-B$  to  $S_{Si}^{2+}$ . Cross sections for the process of  $S_{Si}^0$  to  $S_{Si}^+-A$  and  $S_{Si}^+-A$  to  $S_{Si}^{2+}$  are ignored, which will be discussed later. Since VBM is triply degenerated, we denote the three degenerate states as VBM\_1, VBM\_2, and VBM\_3, separately from which  $S_{Si}^0$  and  $S_{Si}^+$  can possibly capture a hole. For all three degenerate VBM states,  $\sigma_{S^0}$  values are almost identical, and they increase as the temperature increases. The hole-capture cross sections of three VBM states are averaged following Matthiessen's rule, or  $\frac{1}{\tau} = \frac{1}{\tau_1} + \frac{1}{\tau_2} + \frac{1}{\tau_3}$ , and  $\frac{1}{\tau_h} = \sigma \times v_h \times N_D$ , where  $\tau_h$  is the maximum lifetime of a hole carrier,  $N_D$  is the defect concentration, and  $v_h$  is the thermal velocity of the hole. Based on the structures of  $S_{Si}^0$  to  $S_{Si}^+-B$  (figures 1(a) and (d)), the averaged  $\sigma_{S^0}$  is calculated to be within the range from  $6.84 \times 10^{-26} \text{ cm}^2$  to  $1.66 \times 10^{-22} \text{ cm}^2$  for the temperature range (100 K to 300 K). It is about six orders of magnitude lower than the experimental result [17] of  $10^{-16} \text{ cm}^2$  at a temperature of 300 K. Such a discrepancy is possibly because the hole capture measured in the experiment is an Auger-type capture process [17], whereas our simulation of the capture process is based on the multi-phonon non-radiative recombination model. Similar to  $\sigma_{S^0}$ , based on the structures of  $S_{Si}^+-B$  to  $S_{Si}^{2+}$  (figures 1(d) and (c)), the cross section  $\sigma_{S^+}$  also increases as the temperature increases; however, the VBM\_1 state exhibits around 3.7 times higher values than VBM\_2 and VBM\_3. The average cross section  $\sigma_{S^+}$  is determined to be within the range from  $1.44 \times 10^{-24} \text{ cm}^2$  to  $1.17 \times 10^{-21} \text{ cm}^2$ , which agrees well with the experimental result of about  $10^{-23}$ – $10^{-20} \text{ cm}^2$ , as shown in figure 3. The calculated hole-capture cross section being lower than the experimental value by about an order of magnitude is probably due to the error induced by other co-existing defects in experimental samples, such as  $V_{Si}$ ,  $i_S$ , etc. Although their concentration is low, they can still introduce errors in the hole-capture cross section. Another possible source of the difference is the approximations taken in our theory, such as the supercell approximation or static approximation [53, 54]. In fact, one order of magnitude difference is normally considered as reasonable agreement in calculations of carrier capture cross sections [33]. Therefore, such an agreement indicates that hole



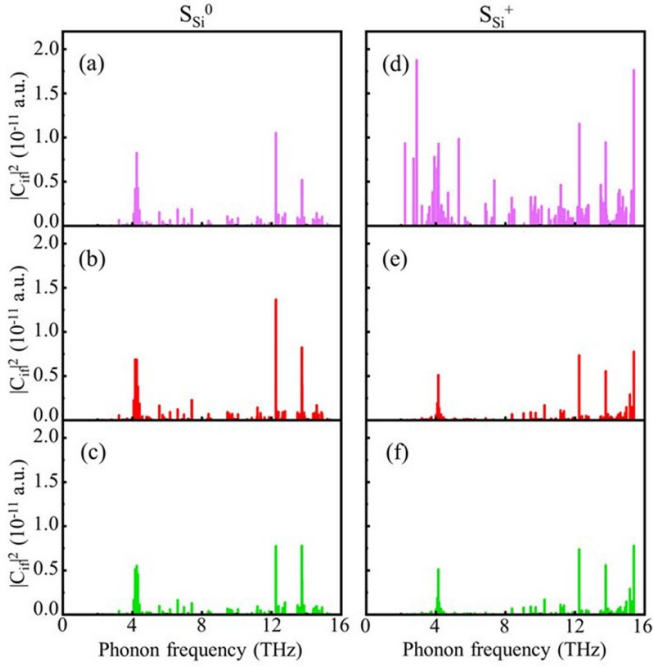
**Figure 3.** The hole-capture cross sections of the defect level which captures a hole from VBM\_1, VBM\_2, and VBM\_3 separately as functions of the temperature. The average hole-capture cross sections of (a)  $S_{Si}^0$  and (b)  $S_{Si}^+-B$  and the experimental values are shown in blue and black, respectively.

capture by  $S_{Si}^+-B$  is a multi-phonon nonradiative recombination process.

To reveal the contribution of the triplet states to the hole-capture cross section and the contribution of phonons in the hole-capture process, we plot the squared norms of electron-phonon coupling matrix elements  $|C_{if}|^2$  as functions of phonon frequency (as shown in figure 4) to quantitatively analyze the contribution from each phonon during the capture of a hole. Figures 4(a)–(c) are the electron-phonon coupling matrix elements for  $S_{Si}^0$  capturing a hole from VBM\_1, VBM\_2, and VBM\_3, respectively. The phonons with the greatest electron-phonon coupling strength, which are located at around 4.2, 12.2, and 13.7 THz, show a large portion of resemblance, leading to the almost identical  $\sigma_{S^0}$  curves for the three VBM degenerate states in figure 3(a). For  $S_{Si}^+$  capturing a hole, the coupling matrix elements of VBM\_1 are generally greater than those of VBM\_2 and VBM\_3, especially in the low-frequency phonon part (figures 4(d)–(f)). As a result,  $S_{Si}^+$  capturing a hole from VBM\_1 is expected to have a larger hole-capture cross section than the other two. Such behavior is also consistent with the observed phenomenon that higher hole capture tends to be accompanied by more low frequency phonons [34].

Both  $\sigma_{S^0}$  and  $\sigma_{S^+}$  are significantly lower than the hole-capture cross section in Au-doped in Si ( $1.0 \times 10^{-15} \text{ cm}^2$  at 300 K) measured by Bemski [59] and that of  $Pb_i$  antisite in  $CH_3NH_3PbI_3$  ( $1.8 \times 10^{-14} \text{ cm}^2$  at 300 K) predicted by Li *et al* [40]. Low  $\sigma_{S^0}$  is caused by the large energy difference between transition energy level  $\varepsilon(0/+)$  and the VBM, and capturing the hole is not inherently easy. Low  $\sigma_{S^+}$  can be understood by the Coulomb repulsion between the  $S_{Si}^+$  substitution and the already-existing hole in VBM.

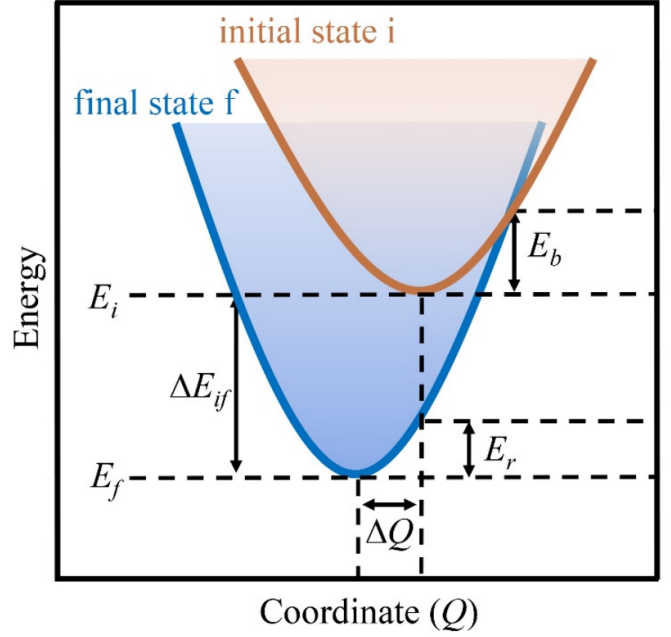
To further illustrate why  $\sigma_{S^0}$  and  $\sigma_{S^+}$  are low, we plot the schematic diagram of configuration coordinates for  $(0/+)$  and  $(+/2+)$  transitions, as shown in figure 5. During the hole-capture process, a transition in the electronic state leads to a change in the equilibrium structure, as presented by the initial



**Figure 4.** The squared norms of electron–phonon coupling matrix elements  $|C_{if}|^2$  as functions of phonon frequency between the triplet states and defect state.

and final state curves with different equilibrium positions. The probability of the electronic state transition in equation (7) can be fitted following  $W_{if} = C_1 + C_2 \exp\left[-\frac{E_b}{k_B T}\right]$  [31], where  $E_b$  is the energy barrier to be overcome when the initial state captures a hole and transforms to the final state. The energy barrier  $E_b$  can be calculated from  $E_b = \frac{(\Delta E_{if} - E_r)^2}{4E_r}$  [35, 60], where  $\Delta E_{if} = E_i - E_f$  is the transition energy level with  $E_i$  and  $E_f$  being the ground state energies of the initial and final states.  $E_r$  is the recombination energy produced during the structural relaxation from initial state towards the final state, and it can be calculated using  $E_r = \frac{1}{2} \sum_k \omega_k^2 \Delta Q_k^2$ , where  $\omega_k$  is the frequency of phonon modes and  $\Delta Q_k$  is the coordinate difference between the initial state and final state [26, 60]. As shown in table 1, the calculated recombination energy  $E_r$  for  $S_{Si}^0$  capturing a hole is 0.195 eV, and the transition energy level  $\Delta E_{if}$  is 0.851 eV above the VBM. The energy barrier  $E_b$  determined by  $E_r$  and  $\Delta E_{if}$  is 0.552 eV. The  $E_r$ ,  $\Delta E_{if}$ , and  $E_b$  for  $S_{Si}^+$  capturing a hole are 0.101 eV, 0.522 eV (above the VBM), and 0.439 eV, respectively. Compared to the 0.01 eV  $E_b$  and the corresponding  $1.8 \times 10^{-14} \text{ cm}^2$  hole-capture cross section of  $\text{Pb}_I$  antisite in  $\text{CH}_3\text{NH}_3\text{PbI}_3$  [40], our calculated energy level barriers are much higher and therefore the capture cross sections are much lower. The  $E_b$  for  $S_{Si}^+$  capturing a hole is lower by 0.114 eV than that for  $S_{Si}^0$  capturing a hole, which is consistent with the  $\sigma_{S^+}$  being larger than the  $\sigma_{S^0}$ .

We also consider the hole-capture cross sections for the  $S_{Si}^0$  to  $S_{Si}^+-A$  and  $S_{Si}^+-A$  to  $S_{Si}^{2+}$  processes. Although the calculated transition energy levels of  $S_{Si}^+-A$  are almost the same as those based on structure  $S_{Si}^+-B$ , the hole-capture cross sections of the hole-capture processes through  $S_{Si}^+-A$  are found to be too low and beyond the numerical accuracy



**Figure 5.** Schematic diagram of configuration coordinates for  $S_{Si}$  (i/f), such as (0/+) or (+/2+).  $Q$  is a relative configuration coordinate between the two charged states.

**Table 1.** Transition energy  $\Delta E_{if}$  (relative to the VBM level), reorganization energy  $E_r$ , and transition energy barriers  $E_b$  for the  $S_{Si}^0$  to  $S_{Si}^+-B$ ,  $S_{Si}^+-B$  to  $S_{Si}^{2+}$ ,  $S_{Si}^0$  to  $S_{Si}^+-A$ , and  $S_{Si}^+-A$  to  $S_{Si}^{2+}$  processes.

Structural transition	$\Delta E_{if}$ (eV)	$E_r$ (eV)	$E_b$ (eV)
$S_{Si}^0$ to $S_{Si}^+-B$	0.851	0.195	0.552
$S_{Si}^+-B$ to $S_{Si}^{2+}$	0.522	0.101	0.439
$S_{Si}^0$ to $S_{Si}^+-A$	0.847	0.015	11.537
$S_{Si}^+-A$ to $S_{Si}^{2+}$	0.526	0.024	2.625

of our method. As shown in table 1, the energy barrier  $E_b$  for  $S_{Si}^0$  to  $S_{Si}^+-A$  (11.537 eV) is much higher than  $S_{Si}^0$  to  $S_{Si}^+-B$  (0.552 eV). This is mainly because the calculated recombination energy  $E_r$  for  $S_{Si}^0$  to  $S_{Si}^+-A$  is 0.015 eV, which is an order of magnitude lower than that for  $S_{Si}^0$  to  $S_{Si}^+-B$  (0.195 eV). Similarly, the  $E_b$  for  $S_{Si}^+-A$  to  $S_{Si}^{2+}$  (2.625 eV) is much higher than that for  $S_{Si}^+-B$  to  $S_{Si}^{2+}$  (0.439 eV). This is also attributed to the fact that the  $E_r$  for  $S_{Si}^+-A$  to  $S_{Si}^{2+}$  (0.024 eV) is much lower than that for  $S_{Si}^+-A$  to  $S_{Si}^{2+}$  (0.101 eV). Therefore, if hole-capture processes happen through the  $S_{Si}^+-A$  structure, it has to overcome a significantly higher energy barrier than through  $S_{Si}^+-B$ , and the corresponding cross sections for  $S_{Si}^+-A$  should be negligibly low compared to  $S_{Si}^+-B$ . The much higher energy barrier for  $S_{Si}^+-A$  can be attributed to its much smaller  $\Delta Q$ , which is caused by the tiny structural differences between  $S_{Si}^+-A$  and  $S_{Si}^0/S_{Si}^{2+}$ . For a small  $\Delta Q$ , the minimum curves of initial and final states in figure 5 nearly coincide at the same coordinates, so the recombination energy  $E_r$  becomes low, and the energy barrier  $E_b$  becomes high.

## 4. Conclusion

In summary, using first-principles methods, we have studied the defect configurations and the transition energy levels for  $\text{S}_{\text{Si}}$  substitution defects with different charged states. Besides the defect configuration with high symmetry, we discovered a new distortive structure for  $\text{S}_{\text{Si}}^+$ , which does not appear in previous PW91 or our PBE calculations. For  $\text{S}_{\text{Si}}^+$ , the symmetric structure ( $\text{S}_{\text{Si}}^+$ -A) and distortive structure ( $\text{S}_{\text{Si}}^+$ -B), which have almost the same energy, are separated by a 0.01 eV energy barrier. The calculated transition energy levels  $\varepsilon(0/+)$  and  $\varepsilon(+/2+)$  are both consistent with the experimental values. Moreover, we obtained the hole-capture cross sections for both a neutral and a +1 charged state. The hole-capture cross section for  $\text{S}_{\text{Si}}^+$  to  $\text{S}_{\text{Si}}^{2+}$  through  $\text{S}_{\text{Si}}^+$ -B agrees with our experiment, but the  $\text{S}_{\text{Si}}^0$  to  $\text{S}_{\text{Si}}^+$  process shows a much lower cross section because it is an Auger process. Hole capture through  $\text{S}_{\text{Si}}^+$ -A has negligibly low cross sections, so it has a low possibility of getting involved in the hole-capture process. Our calculations provide not only a deeper understanding of the defect properties of the  $\text{S}_{\text{Si}}$  substitution, but also a benchmark for the computational study of the carrier capture cross section using multi-phonon nonradiative recombination theory.

## Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

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