

APPLIED PHYSICS REVIEWS

Oxygen defect processes in silicon and silicon germanium

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Silicon and silicon germanium are the archetypical elemental and alloy semiconductor materials for nanoelectronic, sensor, and photovoltaic applications. The investigation of radiation induced defects involving oxygen, carbon, and intrinsic defects is important for the improvement of devices as these defects can have a deleterious impact on the properties of silicon and silicon germanium. In the present review, we mainly focus on oxygen-related defects and the impact of isovalent doping on their properties in silicon and silicon germanium. The efficacy of the isovalent doping strategies to constrain the oxygen-related defects is discussed in view of recent infrared spectroscopy and density functional theory studies. © 2015 AIP Publishing LLC.

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I. INTRODUCTION

Silicon (Si) has been the dominant microelectronic material for decades aided by the advantageous properties of its native oxide (SiO₂). In the past few years, the introduction of high-*k* gate dielectric materials has eliminated the requirement of a good quality native oxide.^{1–3} This has regenerated the interest to use alternative semiconductor materials such as silicon germanium (Si_{1–x}Ge_x) and germanium (Ge). These are appropriate candidate materials for the use in advanced nanoelectronic devices as they have a number of advantages over Si including their superior carrier mobilities, smaller band-gap, and low dopant activation temperatures.^{4–6} Considering Si_{1–x}Ge_x, another advantage is its compatibility to Si-processes and therefore existing Si process equipment has been/and may be used or adapted for Si_{1–x}Ge_x device fabrication.

Defects can be introduced in Si and Si_{1–x}Ge_x during the Czochralski crystal growth (from the graphite and SiO₂ components), device processing (e.g., implantation), during operation (for instance, by radiation in space or radiation damage in accelerators), and by contamination with impurities. Controlling defects can be important during wafer fabrication and device processing in order to prevent device degradation.^{7–15}

O-related defects have been investigated systematically in Si and to a lesser degree in Ge or Si_{1–x}Ge_x for over five

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decades. This is because O, which is introduced in the lattice mainly due to the growth or processing stages, impacts the properties of Si and $\text{Si}_{1-x}\text{Ge}_x$. Defects, such as the vacancy-oxygen pair (known as the A-center), have been studied since the early seminal investigations of Watkins (refer to Ref. 16 for an overview) but there is still a need to limit their deleterious impact. For example, A-centers in Si impact the operation of Charge-Coupled Devices (CCDs) in space. In particular, they interfere with the readout process and transfer signal by one or more pixels against the direction of transfer through the device.¹⁷ This impacts the picture quality from space missions and is a unique demonstration of how atomic scale defects can constrict our understanding of extremely large objects in space.¹⁷

The understanding of defect processes in materials has been aided by the ever increasing computational power, availability of resources, and advances in computational techniques.^{18–25} These have allowed the fundamental understanding of the structure and electronic properties of defects and their clusters at an atomistic scale providing exciting insights. In essence, they do not provide only information complementary to experiment but can be employed in conjunction with experiment to design defect engineering strategies to limit the impact of the O-related defects.

The present review is mainly focused on the O-related defects and processes in Si and Ge. In the first part, we discuss O, C, intrinsic defects, and their respective clusters. Important defects, such as the A-center, are discussed extensively from both an experimental and density functional theory (DFT) perspective. This is followed by an assessment of point defect engineering strategies using oversized isovalent atoms, which aim to control the O-related defects. Finally, to conclude a brief summary and outlook for future directions is given.

II. OXYGEN, CARBON, AND INTRINSIC DEFECTS IN SI

A. Intrinsic defects

Vacancies (V) and self-interstitials (Si_i) are intrinsic point defects that have an important role in many defect processes including self- or dopant diffusion, strain release in the lattice, and radiation defects. The formation of radiation defects is the result of direct or indirect participation of intrinsic defect and various impurities or dopants in the host material. A common way to study radiation defects in a controlled and systematic manner is by irradiation with electrons, neutrons, protons, or gamma rays. In these irradiated materials, vacancies and interstitials form at non-equilibrium concentrations.²⁶ These V and self-interstitials can form pairs and/or complexes with other intrinsic defects or dopant atoms present in the lattice. Vacancies typically form divacancies (V_2), or they are captured by O to form VO pairs. The Si_i 's can associate directly or indirectly with C and O impurities to form many complexes, including the C_iO_i , the C_iC_s , and the $\text{C}_i\text{O}_i(\text{Si}_i)$.¹⁵

1. Prior to irradiation

A way to investigate the temperature evolution of defects in irradiated Si is infrared spectroscopy. Previous

studies reported the sequential appearance upon annealing of defects in irradiated Cz-Si containing C as detected by infrared spectroscopy.^{27–29} Prior to irradiation, the O interstitials give rise to a number of IR bands in the spectra in the frequency range of 25–1835 cm^{-1} (refer to Fig. 1(a) and Ref. 30). The most important band is that being at 1106 cm^{-1} , from which the O concentration of the material is calculated using a calibration coefficient of $3.14 \times 10^{17} \text{ cm}^{-2}$. The C substitutionals give rise to an IR band at 605 cm^{-1} from which the C concentration of the material is calculated using a calibration coefficient of $1.0 \times 10^{17} \text{ cm}^{-2}$. The C substitutional-O interstitial pairs (C_sO_i) give rise to IR bands at 585, 637, 684, and 1004 cm^{-1} . The latter band may not be seen as it is masked by the much stronger band of O_i at 1006 cm^{-1} in this spectra range.

2. After irradiation

As it can be observed from Fig. 1(b) after irradiation, there are more and more complicated defects in Si. The O-vacancy (VO) pair gives rise to two IR bands, one at 830 cm^{-1} (neutral charge state) (refer to Fig. 1(b)) and one at 885 cm^{-1} (negative charge state).³¹ At $\sim 300^\circ\text{C}$, the defect becomes unstable and an important percentage of it is converted to the VO_2 defect.

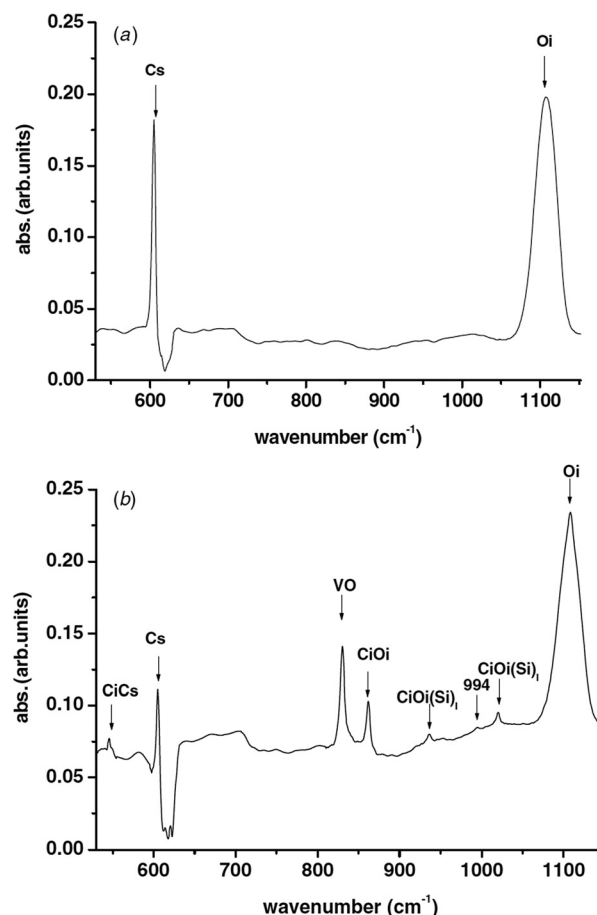


FIG. 1. Typical IR spectrum of the sample (a) prior and (b) after irradiation. Reprinted with permission from Londos *et al.*, Semicond. Sci. Technol. **24**, 075 002 (2009). Copyright 2009 Institute of Physics.

The C interstitial-O interstitial pair gives rise³² to a number IR bands the most important being that at $\sim 862\text{ cm}^{-1}$ depicted in the spectra (refer to Fig. 1(b)). At $\sim 300^\circ\text{C}$, the defect becomes unstable and dissociates although a small part of it is converted to the C_5O_{2i} defect, by pairing with the VO defect which anneals out at the same temperature.³²

The C interstitial-C substitutional pair gives rise to a number IR bands.^{33,34} These bands are very weak detected mainly at cryogenic temperatures. The most important is that at $\sim 546\text{ cm}^{-1}$ detected also at room temperatures and depicted in our spectra (refer to Fig. 1(b)). In essence, the latter band has the contribution of another band³⁵ in the same region from the C_iO_i defect. The defect anneals out by dissociation $\sim 250^\circ\text{C}$ following a complicated reaction kinetics which is not completely investigated so far.³²

The $\text{C}_i\text{O}_i\text{Si}_i$ defect gives rise²⁷ to two bands at 936 and 1020 cm^{-1} depicted in the spectra (refer to Fig. 1(b)). In room temperature measurements, the two bands are stable up to $\sim 150^\circ\text{C}$ and then disappear without being followed by the emergence of other bands in the spectra. Notably, in low temperature measurements,³⁶ the above two bands detected at 940 and 1024 cm^{-1} , respectively, begin to decay in the spectra at $\sim 150^\circ\text{C}$ followed by the emergence of three bands at 724 , 952 , and 973 cm^{-1} which at $\sim 250^\circ\text{C}$ begin to decay followed by three other bands at 959 , 969 and 977 cm^{-1} . The latter two sets of bands were attributed³⁶ to metastable configurations of the $\text{C}_i\text{O}_i\text{Si}_i$ complex. However, theoretical studies^{37,38} do not confirm these assignments. The issue has not been finally resolved so far pending further investigation.

3. Impact of isochronal annealing

The isochronal annealing of irradiated Si leads to the evolution and production of the defects. The isochronal annealing in the temperature range between 100 and 300°C leads to the formation of the V_2O and V_3O defects mainly due to the reactions $\text{VO} + \text{V} \rightarrow \text{V}_2\text{O}$ and $\text{VO} + \text{V}_2 \rightarrow \text{V}_3\text{O}$, respectively. The two defects give rise to IR bands in the spectral range of the VO defect, and their contribution is found by Lorentzian profile. In particular, V_2O defect gives rise to an IR band at $\sim 826\text{ cm}^{-1}$ and V_3O defect to an IR band at $\sim 839\text{ cm}^{-1}$.²⁹

Upon isochronal annealing at $\sim 300^\circ\text{C}$, the vacancy-dioxygen (VO_2) and the C substitutional-dioxygen interstitial (C_5O_{2i}) give rise to IR bands at $\sim 885\text{ cm}^{-1}$ and 1048 cm^{-1} , respectively (refer to Fig. 1(c) of Ref. 39). The formation of the VO_2 and C_5O_{2i} defects is mainly due to the reactions $\text{VO} + \text{O}_i \rightarrow \text{VO}_2$ and $\text{C}_i\text{O}_i + \text{VO}_i \rightarrow \text{C}_5\text{O}_{2i}$. The VO_2 defect is stable up to $\sim 450^\circ\text{C}$, where it begins to anneal out converting to the VO_3 defect. The signal from C_5O_{2i} defect begins to decay from the spectra just above 400°C and disappears around 550°C without giving rise to any other peaks in the spectra.

Upon isochronal annealing at $\sim 500^\circ\text{C}$ the vacancy-trioxygen (VO_3) defect gives rise (Refs. 27 and 28 and references therein) to three IR bands at ~ 904 , 968 , and 1000 cm^{-1} . The defect is stable up to $\sim 550^\circ\text{C}$, where it

converts to VO_4 defect (refer to Fig. 2). Thereafter, at $\sim 580^\circ\text{C}$, the vacancy-tetraoxygen (VO_4) defect gives rise (Refs. 27 and 28 and references therein) to two IR bands at ~ 985 and 1010 cm^{-1} . The defect is stable up to $\sim 650^\circ\text{C}$ where it converts to vacancy-pentaoxygen defect (VO_5) defect. Also at about this temperature signals from $\text{V}_m\text{O}_n/\text{VO}_n\text{C}_s$ defects appear in the spectra. In particular, the VO_5 gives rise to IR bands at ~ 1037 and 1051 cm^{-1} , whereas three other bands at ~ 762 , 967 , and 1005 cm^{-1} have been associated either with V_mO_n complexes or with the VO_nC_s defect (Refs. 27 and 28 and references therein).

B. Oxygen

Oxygen impurities, which are electrically neutral, occupy interstitial sites (O_i) within the Si. In the infrared spectra of Si, there are a number of localized vibrational modes associated⁴⁰⁻⁴³ with O in the frequency range of 25 – 1835 cm^{-1} . These bands with the associated normal modes responsible for them are at: 29 cm^{-1} , at LHe T (ascribed to a low frequency vibration of the O atom in the (111) plane perpendicular to the Si...Si broken bond), 1136 cm^{-1} , at LHe T (ascribed to the ν_3 antisymmetric mode of the Si-O-Si pseudo-molecule), two bands at 515 and 1205 cm^{-1} , at LHe T (ascribed, respectively, to the symmetric modes ν_2 and ν_1 of the Si-O-Si pseudo-molecule), 1749 cm^{-1} (attributed to a combination band involving O_i), as well as some weak bands as the 560 cm^{-1} band appearing only at room temperature, another one at 648 cm^{-1} , at LHe T, and two others at 1819.5 cm^{-1} and 1831.3 cm^{-1} . The most important band is at 1106 cm^{-1} , from which the O concentration in Si is calculated using a calibration coefficient of $3.14 \times 10^{17}\text{ cm}^{-2}$.

For completeness, considering Ge which is the end member of $\text{Si}_{1-x}\text{Ge}_x$ and isostructural to Si, O can also contribute in defect processes, however, its impact is less significant than in Si. This is because in Czochralski-grown Ge the concentration of O is not as high as in Si.⁴ At any rate, the experimental solubility of O in Ge is high (around 10^{18} cm^{-3}) and O can also be introduced in Ge when H_2O vapour or oxygen gas is present in the growth atmosphere or through diffusion at the Ge/oxide interfaces in devices.⁴ O_i are electrically inactive in Ge, but they may bind with V to form A-centers.

1. The A-center

Considering Si upon irradiation at room temperature, the vacancies and self-interstitials which form are very mobile and most of them are destroyed via the reaction $\text{V} + \text{Si}_i \rightarrow 0$. The surviving vacancies form either V_2 or if they are captured by O_i they form VO. The VO defect has a C_{2v} symmetry with the O atom being attached to the dangling bonds across the V. In essence, the O atom forms a Si-O-Si molecule. The other two Si atoms form a weak Si-Si molecular bond (refer to Fig. 3 and Ref. 14) that has the capacity of trapping an electron and is responsible for the electrical activity of the defect. This is the negative charge state of the defect structure that was proposed by EPR measurements more than five decades ago.⁴⁴ These EPR measurements⁴⁴

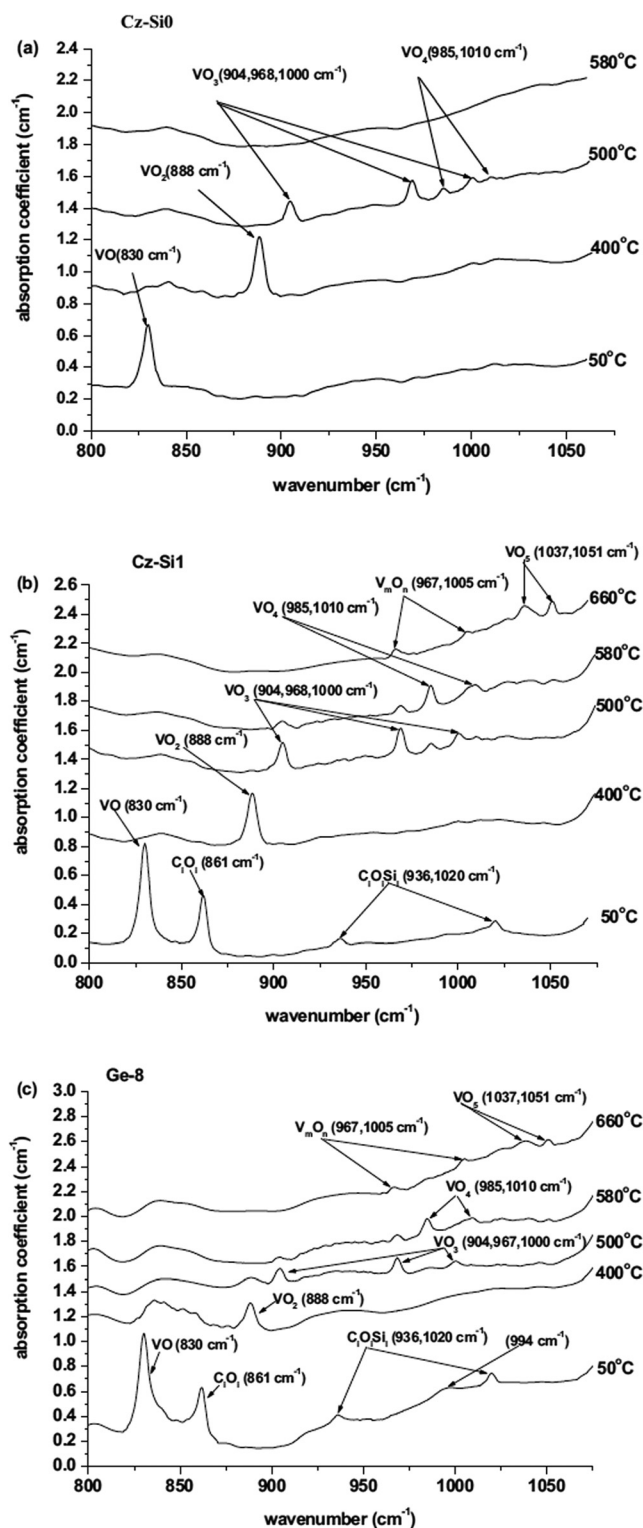


FIG. 2. IR spectra of Si samples with (a) C after irradiation ($[C_s]_{af.ir}$) below the detection limit (b) $[C_s]_{af.ir} = 9.92 \times 10^{16} \text{ cm}^{-3}$ and (c) $[C_s]_{af.ir} = 10^{17} \text{ cm}^{-3}$ and $[Ge] = 2 \times 10^{20} \text{ cm}^{-3}$. The IR spectra were recorded after irradiation and at various selective temperatures. Reprinted with permission from J. Appl. Phys. 109, 033508 (2011). Copyright 2011 AIP Publishing LLC.

determined that the wavefunction of the unpaired electron is highly localized, ($\sim 70\%$ on the Si-Si bond) leading to an acceptor level at $E_c - 0.17 \text{ eV}$ in the band gap in agreement with electrical studies.⁴⁴ Uniaxial stress studies determined⁴¹ that the VO defect has a neutral charge state with a similar

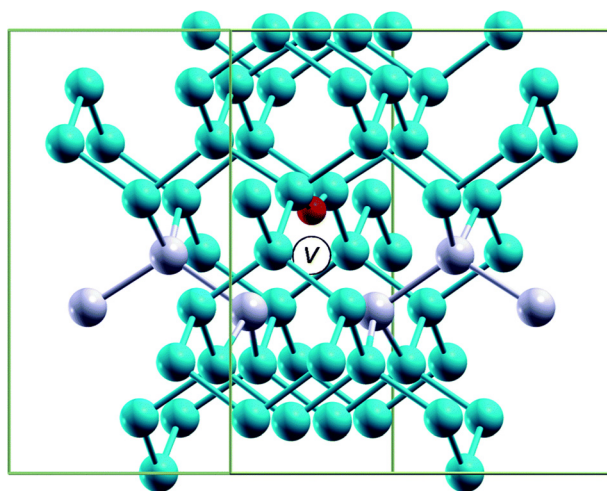


FIG. 3. A schematic of the VO defect. Medium blue spheres are the Si atoms, and the small red sphere is the O atom. Si atoms along the (10-1) direction are highlighted. Reproduced with permission from Wang *et al.*, Phys. Chem. Chem. Phys. 16, 8487 (2014). Copyright 2014 Royal Society of Chemistry.

structure. Interestingly, recent hybrid functional DFT calculations⁴⁵ showed that the A-center can form in the double negative charge state (refer to Sec. VIB). In the A-center, the O atom is not at a substitutional site but is slightly away ($\sim 0.9 \text{ \AA}$) from the vacancy site along the $\langle 100 \rangle$ direction.⁴⁶ DFT calculations by Coutinho *et al.*⁴⁷ calculated that in the negative charge state the O atom is displaced away from the reconstructed bond. This is consistent with the picture that the additional electron is trapped in this bond and repels the negatively polarized O atom. The higher Local Vibration Mode (LVM) frequency in comparison to that of the neutral charge state can be traced to the compression of the bonds around the O_i atom. Finally, the two bands at 1370 and 1430 cm^{-1} were assigned⁴⁸ to a combination of the antisymmetric B_1 stretching mode and the symmetric stretching mode A_1 in the two charge states, respectively, of the A-center.

Again for completeness, considering Ge the A-centers have been studied experimentally⁸⁻¹⁰ and theoretically.^{7,47} In previous DFT work, the A-center was calculated to have a binding energy of -0.36 to -0.45 eV (Refs. 7 and 47), and this small energy difference is justifiable by the different methods used in these DFT studies. What is important is that the A-center in Ge has a far small binding energy (as compared to Si), and this will imply that its concentration and impact will be smaller. This will in turn impact the defect processes of A-centers in Ge-rich $\text{Si}_{1-x}\text{Ge}_x$ alloys.

2. The VO_2 defect

In irradiated Si the VO_2 defect is formed at temperatures $\sim 300^\circ\text{C}$ as the VO centre migrates and is trapped by an O atom via the reaction ($\text{VO} + \text{O}_i \rightarrow \text{VO}_2$). VO_2 structure has D_{2d} symmetry and the two O_i share equivalently the vacant site. Every O_i is bonded with two Si atoms and the O-V distance increases in the VO_2 defect as compared to the A-center. Additionally, as two O atoms are accommodated in a vacancy, the lengths of the Si-O bonds become shorter in

VO_2 as compared to the VO defect. The consequence is the higher vibrating frequency (LVM frequency for VO_2 is $\sim 888 \text{ cm}^{-1}$ which is higher than that of $\sim 830 \text{ cm}^{-1}$ of the VO defect). Finally, as the two O_i in VO_2 saturate all four dangling bonds of the vacancy the defect is electrically inactive.

3. The V_mO_n defects

Upon thermal annealing, vacancies and O interstitial associate with VO converting it to V_mO_n defects. These are important as V_mO_n defects cause leakage currents in p - n junctions.^{49–51} Additionally, the V_2O and V_3O defects have been determined to be recombination centers contributing in the reduction of the minority carriers lifetime induced by irradiation.⁵² Large VO_n ($n = 4, 5, 6$) clusters may act as heterogeneous nuclei enhance oxygen precipitation in irradiated Si.^{53–56}

C. Carbon

C is introduced in the Si lattice during crystal growth. In particular, it is incorporated from the polycrystalline starting material, gaseous contaminants during the growth process and graphitic components in the equipment.^{57–60} The introduction of C leads to local strain due to its small size as compared to Si. It should be noted that when C occupies substitutional sites (C_s), it is electrically neutral as it is isovalent with Si (or Ge). C in infrared spectra is observed by a localized vibrational mode at 607 cm^{-1} in Si. C and O are highly electronegative and are chemically very reactive. Consequently, they form bonds with Si atoms, other defects, and dopants.

Upon irradiation, vacancies and Si interstitial (Si_i) atoms are formed at non-equilibrium concentrations. Most of these Si_i are trapped by C_s , which are pushed to interstitial sites according to $\text{C}_s + \text{Si}_i \rightarrow \text{C}_i$ (known as the Watkins displacement reaction).^{61,62} C_i has been related to the two localized vibrational modes at 922 and 932 cm^{-1} with this defect in low temperature irradiated Si,⁶³ whereas it is established it introduces in-gap states.⁶⁴ C_i is unstable at room temperature as it migrates and interacts with O_i and C_s to form C_iO_i and C_iC_s defects, respectively. Regarding the C_iO_i defect, it has been correlated with at least six localized vibrational modes with the most significant one appearing at 865 cm^{-1} .^{27,65} Considering C_iC_s defect, it is considered to be bistable with at least eleven localized vibrational modes being correlated with it mainly by low temperature measurements (exception being the one at 544 cm^{-1} that can be also observed at room temperatures).^{33,34} A third C_iC_s configuration, the $\langle 100 \rangle$ C-C dumbbell, was proposed by Liu *et al.*⁶⁶ using both theoretical and experimental investigations. Liu *et al.*⁶⁶ calculated that this configuration is energetically favourable as compared to the two bistable structures. The structure and properties of these three configurations in Si were recently studied by Wang *et al.*⁶⁷ using hybrid functional DFT and the conclusions were consistent with Liu *et al.*^{33,34,66} (refer also to Sec. VIC) for more information and comparison between the three C_iC_s configurations). The community is interested in the C_iO_i and C_iC_s defects as they introduce states in the Si

band gap and are affecting the operation of devices.⁶⁸ Thus, numerous experimental and theoretical studies were performed to investigate their structure, properties and applications (for example, C_iC_s is used to improve Si optical emitters).^{69–74}

From a fundamental viewpoint and under the course of irradiation C-related defects such as C_i , C_iO_i , and C_iC_s , defects can act as nucleation centers for Si_i to form complexes such as $\text{C}_i(\text{Si}_i)$ (IR bands at 953 cm^{-1} and 966 cm^{-1}), $\text{C}_i\text{O}_i(\text{Si}_i)$ (IR bands at 940 cm^{-1} and 1024 cm^{-1}), and $\text{C}_i\text{C}_s(\text{Si}_i)$ (IR bands at 987 and 993 cm^{-1}), respectively.^{35,37,38,75,76} These complexes can be very important as, for example, the $\text{C}_i(\text{Si}_i)$ can impact the transient enhanced diffusion of boron.⁷⁵

III. OXYGEN DIFFUSION PROCESSES IN SI

O in Si can be considered as both beneficial and deleterious as it can form electrically active defect centers, O precipitates act as gettering centers for metallic impurities, and can immobilize dislocations improving the mechanical strength of wafers.^{77–81} Understanding O diffusion is fundamentally important to control defect processes in Czochralski Si and Ge.

Numerous O-related species have been previously considered to be the diffusing species (including O_i trimmers, long O_i chains, and molecular oxygen),^{82–85} however, it is now established that their contribution to the O diffusion processes is insignificant.^{86–89} The diffusion of oxygen is mainly via O_i and O_{2i} species as described in a recent DFT study by Timerkaeva *et al.*⁸⁸ Regarding the O_i at the ground state configuration, the O atom is bonded to two neighbouring Si atoms (Si^1 and Si^2 , refer to Fig. 4(a)) and the remaining valence electrons form two lone pairs on the O atom.⁸⁸ At the saddle configuration, the O atom is bonded to three Si atoms (Si^1 , Si^2 , and Si^3 , refer to Fig. 4(b)) and the remaining valence electrons form a lone pair on the O, whereas the last electron is localized in a lone pair near the Si^2 atom (denoted by an arrow in Fig. 4(b)).⁸⁸ Figs. 4(c) and 4(d) refer to the O_2 diffusion ground state and saddle point. The important feature is that both O atoms diffuse in the same (110) plane, where they are bonded to Si atoms.⁸⁸ In the ground state configuration, each O atom has a couple of lone pairs.⁸⁸

Regarding the vacancy-O defects, VO has been proposed to act as a species enhancing O diffusion.^{90,91} Previous studies have inferred that the formation and rapid dissociation of VO defects may account for the enhanced O diffusion in annealed Si by reducing the barrier of O diffusion jumps in the Si lattice. Monte Carlo simulations⁹² show that O can impact the aggregation of vacancies during crystal growth through the formation of O-vacancy defects.⁹³

IV. POINT DEFECT ENGINEERING STRATEGIES TO RESTRAIN OXYGEN DIFFUSION IN SI

A. Background

Many defect engineering strategies have been proposed to eliminate the deleterious impact of defects, dopants, or their respective clusters in Si and related materials such as

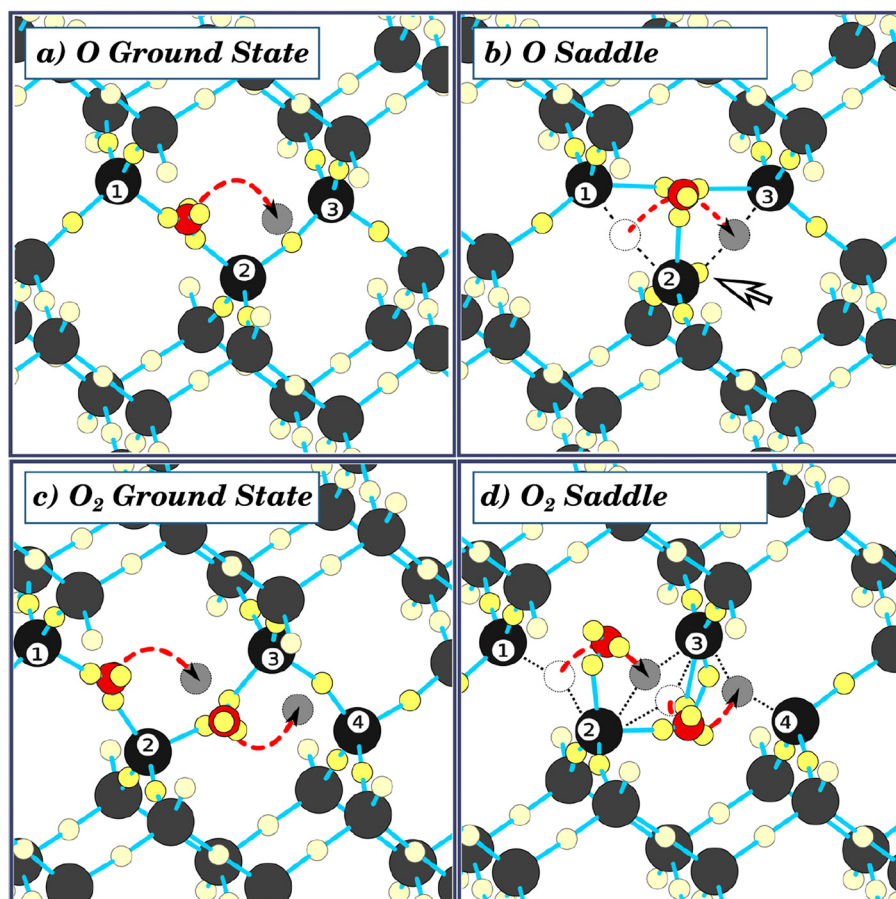


FIG. 4. (a) and (b) The O diffusion ground state and saddle point, and (c) and (d) the O₂ diffusion ground state and saddle point. Black and red balls represent Si and O atoms, respectively. The paths used by O are represented by a dashed arrow pointing to the final position (gray balls). Reprinted with permission from Appl. Phys. Lett. **103**, 251909 (2013). Copyright 2013 AIP Publishing LLC.

Ge. Commonly, the motivation behind these strategies is to introduce other dopants or competing native defects at a sufficient concentration to cancel or control the defect, dopants and their clusters. Interestingly, in a recent study, Bracht *et al.*⁹⁴ used proton irradiation to generate a supersaturation of Ge self-interstitials to annihilate the vacancies in Ge. Under equilibrium conditions, vacancies in Ge are the dominant native point defects that mediate the fast diffusion of *n*-type dopants (P, As, or Sb) and the formation of large dopant-vacancy clusters.^{95–97} The latter clusters lead to a deactivation of a significant proportion of the dopant profile.

A more common way to control the defect processes in Si and Ge is via the introduction of codopants in the lattice. In the example mentioned above, previous studies report the codoping of *n*-type doped Ge with isovalent atoms (C or isovalent atoms including Sn) or aliovalent dopants (for example, fluorine) or a second *n*-type dopant. Both DFT and experimental work on isovalent codoping in Ge are consistent revealing that although the transport of *n*-type dopants is constrained the formation of complex dopant-vacancy clusters is not hindered.^{98,99}

Previous experimental and DFT studies investigated the impact of F doping in Si^{100–102} and Ge.^{103–105} In both materials, doping with F is an effective way to immobilize the *V* as F atoms saturate their dangling bonds (F has a very high electronegativity). In essence, this limits the diffusion and association of *V* with donor atoms, which in turns constrains their diffusion. Additionally, it impacts the formation of extended donor-vacancy clusters.¹⁰³ The recent study of

Jung *et al.*¹⁰⁵ concluded that implanted F atoms passivate the *V* (at around 500 °C) and can lead to an enhancement in Ge-MOSFET performance.¹⁰⁵ This is an example of how the synergetic use of experiment and DFT can lead to a better understanding and the formulation of a defect engineering strategy in group IV semiconductors. At this point, we should consider the defect engineering strategies applied to limit the formation of the A-center in Si that is doping with large isovalent atoms.

B. Doping with large isovalent atoms

Of all the possible applications of isovalent doping in Si, none is expected to be more technologically important than its use in photovoltaics. For this reason, the elucidation of the effects of isovalent doping on improving the radiation hardness of Si continues today to be an exciting area of research. It has been demonstrated that **isovalent doping suppresses the formation of O-related and C-related radiation defects in Si**, allowing for its application in PV industry.

The community employs similar tactics that is the immobilization of the vacancies. This is because *V* is the native defect in the A-center and the elimination of the O concentration is very difficult to achieve in Czochralski grown Si. As in Czochralski grown Si, there is C that forms clusters that can impact properties, most studies concern oversized isovalent atoms. The introduction of a large isovalent atom in the diamond lattice results in elastic strains in the lattice. This is because of their larger tetrahedral covalent

radii, compared to that of the host atom. Consider, for example, the introduction of a Pb atom in the Si lattice and let the Δr being the difference of the tetrahedral radius between the Pb and Si atom ($\Delta r = r_{\text{Pb}} - r_{\text{Si}}$). It is expected¹⁰⁶ that the larger Pb substitutional atom pushes the first and the second nearest neighbours (NNs) to move radially outwards by Δr_1 and Δr_2 , respectively (and Δr_i for the i th NN). Reasonably, $\Delta r > \Delta r_1 > \Delta r_2 > \dots > \Delta r_i > \dots$ as a result of the compression of the Pb-Si bonds. For simplicity, the atomistic nature of the displacements beyond the nearest neighbour is neglected, and the Si lattice is described as a continuous medium. In this framework, Hooke's law can be applied to calculate the strain energy stored in the NN of the dopant atoms. This is expressed as¹⁰⁶

$$E^{\text{st}} = 4 \times \frac{1}{2} g K_c (\Delta r - \Delta r_1)^2 + 8 \pi G r_0 (\Delta r_1)^2, \quad (1)$$

where $g K_c$ is the stiffness constant of the dopant of the first nearest neighbour bonds, K_c is the force constant, and g is a dimensionless parameter of order unity. The second term of Eq. (1) represents the energy stored in the surrounding lattice atoms by the expansion of a cavity of radius r_0 by Δr_1 . r_0 is the Si interatomic distance and G is the Si shear modulus of elasticity. Equation (1) can be written as¹⁰⁶

$$E^{\text{st}} = \text{const} \times (\Delta r)^2. \quad (2)$$

For Si, *const* has a value of 15×10^4 ergs/atom.¹⁰⁶

The increase of the tetrahedral radius is calculated by the expression $r = r_d - r_{\text{Si}}$, where r_d is the covalent radius of the impurity atom and r_{Si} is this of a Si atom ($r_{\text{Si}} = 1.17 \text{ \AA}$). Thus, for Pb ($r_{\text{Pb}} = 1.44 \text{ \AA}$), Sn ($r_{\text{Sn}} = 1.41 \text{ \AA}$), and Ge ($r_{\text{Ge}} = 1.22 \text{ \AA}$), the corresponding differences are $\Delta r_{\text{Pb}} = 0.27 \text{ \AA}$, $\Delta r_{\text{Sn}} = 0.24 \text{ \AA}$, and $\Delta r_{\text{Ge}} = 0.05 \text{ \AA}$. Apparently, from Eq. (2), the larger the isovalent dopant, the larger the strain energy.

These strains can be relieved by the association of the dopant with a vacancy. This leads to the dopant vacancy pairs, which are competitive species to the A-centers. Previous studies have discussed how oversized isovalent atoms such as Sn or Pb can impact the defect processes in group IV semiconductors.^{107,108}

1. Ge doping in Si

Ge is only slightly larger than Si, however, it can be an effective trap for vacancies (GeV pairs) below room temperature (RT). At around 180 K, GeV defects become unstable and dissociate.¹⁰⁷ Typically, Ge suppresses the formation and thermal stability of VO, whereas it suppresses the formation but enhances the thermal stability of V_2 defects.^{109–111} Considering the case of high Ge content Si, Ge traps self-interstitials and in essence enhances the A-center concentration.¹¹² Importantly, Ge doping has been determined to retard and suppress thermal donor formation^{112,113} stabilizing the electrical properties of Si. Conversely, Ge enhances^{113,114} the generation of O precipitates, and this can be employed to increase the gettering capability of the material for metallic contaminants. This is important when considering Si for photovoltaic applications. Additionally, Ge doping

can improve the mechanical strength of Si by retarding dislocation movement and precipitation.^{115,116}

Ge codoping *p*-type or *n*-type dopants affect the photovoltaic properties of Si.^{117–124} Considering B codoping Ge improves segregation redistribution of boron during the thermal oxidation of Si and importantly limits the formation of boron-O defects.^{118,119} Notably, boron-O defects in solar cells can induce significant degradation of carrier lifetime, leading to a reduction of the energy conversion efficiency of the cell.

Moreover, by Ge doping the mechanical strength of the Si wafer is enhanced. This allows a decrease in the thickness of the wafer which enables the fabrication of thinner Cz-Si solar cells, leading to a reduction of their cost. In parallel, the cell efficiency and the photovoltaic module output power under illumination are enhanced.^{124,125}

2. Sn doping in Si

Sn are larger isovalent dopants compared to Ge and can strongly associate with vacancies, impact the vacancy-related defects,^{126–128} and influence the generation rate of interstitial-related defects in Si.^{129–132} In recent studies, it was shown that Sn doping can impact the diffusion and formation of A-centers in Si.^{23,113} Critical in this aspect is the formation of SnVO clusters, which are very bound and less mobile than the VO.²³ Additionally, SnV pairs and SnC_i defects also form in irradiated Si. The latter defect is of importance in the case where C and Sn are introduced via codoping in Si to associate and trap with self-interstitials and vacancies, respectively (Sn suppresses both the formation of VO and VO₂ defects).¹³³ Sn atoms capture vacancies and improve the radiation hardness of Si for solar cells and detectors by suppression of the formation of vacancy-related defects and their transformation to larger complexes upon heat treatments. Defects such as VO, VO₂, and PV (in *n*-type doped Si) affect negatively the output and reliability of photovoltaics. Additionally, Sn doping has been investigated as a method to study the impact of vacancies on impurity diffusion and to test diffusion models¹³⁴ (for example, antimony diffusion in Si) without modifying the dopant density and hence avoiding considering Fermi level effects. On the other hand, since the interactions of Sn with Si_i's are small, Sn has been used to study^{132,135} the behavior of Si_i's produced by room temperature irradiation. In particular, the reactions Si_i's participate and how they affect the production of C-related defects. Furthermore, Sn due to its electrical neutrality and its larger covalent radius as compared to Si has been used^{136,137} to compensate the strain layers in Si doped with high concentrations of donors and acceptors (like B and P, respectively) of smaller covalent radii than that of Si.

Nevertheless, the formation of SnV defects can diminish the impact of Sn for Si hardening as these defects introduce electrical levels in the gap.^{138–140} Importantly, Sn can affect the generation and annealing of O thermal donors as well as on O aggregation and precipitation processes in Si.^{141–143}

3. Pb doping in Si

Pb is a large isovalent dopant, and it has the propensity to attract vacancies (affecting the production of vacancy-O defects) to relieve the strain resulting from its incorporation in the lattice. Interestingly, a signal from the PbV pair has not yet been detected. Pb is usually codoped with C to relieve the strains in the lattice and can suppress the formation of the VO defect, affecting its thermal stability and reducing its conversion to the VO₂ defect. Pb can also impact the lifetime of non-equilibrium current charge carrier, the formation of thermal donors and O precipitates.

In particular, Pb increases the carrier's lifetime, which improves the optoelectronic properties of Si, leading to an enhancement of the performance of polycrystalline Si solar cells.¹⁴⁴ It deserves noting that Pb in Si does not introduce, to the best of our knowledge, any levels from radiation-induced defects in the forbidden gap in comparison with Sn.^{129,133} These levels in Sn-doped Si may act as recombination centers deteriorating the performance of solar cells. In this respect, the absence of such levels in Pd-doped Si is an advantage in comparison to Sn-doped Si.

V. OXYGEN RELATED DEFECTS IN SiGe

A. Background

The investigation of the A-center and other O related defects in Si_{1-x}Ge_x is limited as compared to Si.¹⁴⁵⁻¹⁴⁷ The A-center is also electrically active in Si_{1-x}Ge_x, and therefore, it is technologically important to determine its properties.^{146,147} The complication in Si_{1-x}Ge_x is that there are two atom species (Si or Ge) that can occupy a lattice site and this will result in Si-rich and Ge-rich areas. These in turn can impact the formation of point defects. For example, previous experimental studies determined that O interstitial atoms preferentially bond with Si atoms rather than Ge atoms in Si_{1-x}Ge_x.^{148,149} At any rate, most previous studies were confined to very low Ge-content Si_{1-x}Ge_x. Concerning vacancies previous experimental and DFT studies indicated that it is more energetically favourable for the vacancy to form near at least one Ge atom.^{150,151} In particular, the positron annihilation spectroscopy (PAS) investigation of Sihto *et al.*¹⁵⁰ determined that there is energy gain when a Ge atom replaces a Si atom next to a vacancy in strained Si_{1-x}Ge_x and this was supported by consequent DFT calculations.¹⁵¹ Another important aspect is in Si_{1-x}Ge_x is that the Ge content impacts the diffusion of O and the conversion of the VO pairs to VO₂ clusters.¹⁵²⁻¹⁵⁴

B. Impact of Ge content

In the study of Sgourou *et al.*,¹⁵⁴ FTIR spectroscopy was employed to clarify the interactions and in particular, to investigate the production and evolution of A-centers in *n*-type Si_{1-x}Ge_x (where $x = 0, 0.025$, and 0.055). Figure 5 represents typical segments of the IR spectra of the *n*-type Si_{1-x}Ge_x (where $x = 0, 0.025$, and 0.055) crystals recorded after irradiation and at 350 °C in the course of the 20-min isochronal anneals sequence.¹⁵⁴ The two selected temperatures are typical

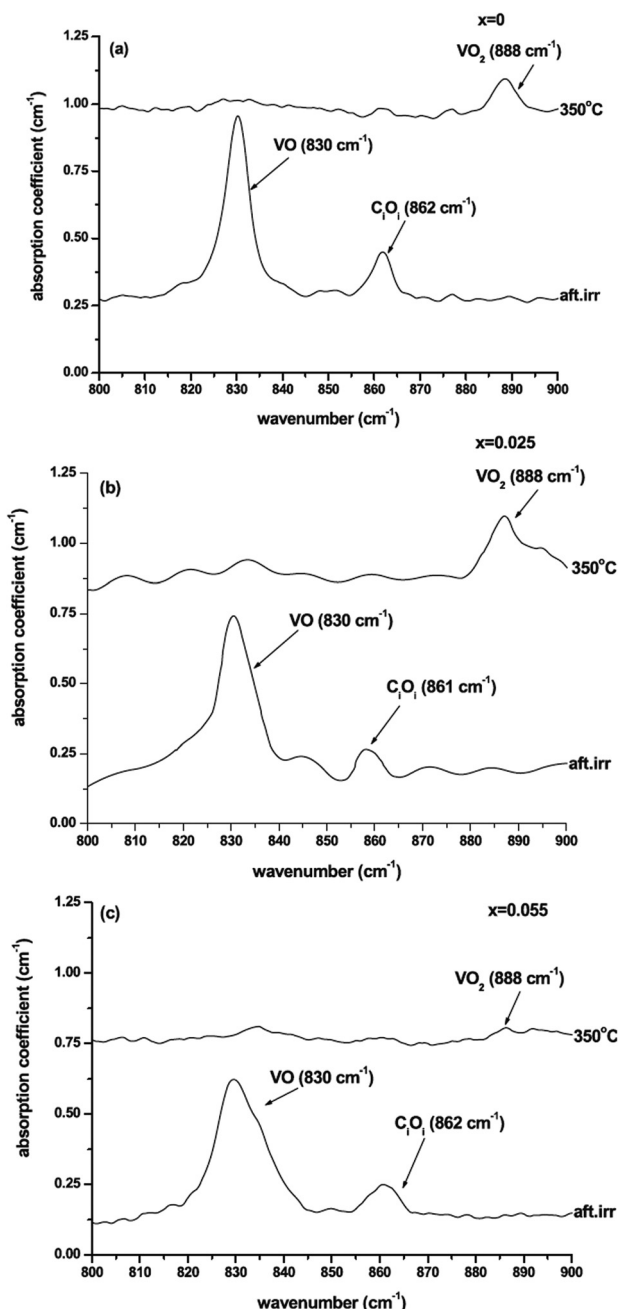


FIG. 5. Typical segments of the IR spectra of the *n*-type Si_{1-x}Ge_x crystals for (a) $x = 0$, (b) $x = 0.025$, and (c) $x = 0.055$ recorded after irradiation at 350 °C, in the course of the 20-min isochronal anneals sequence. Reprinted with permission from J. Appl. Phys. **113**, 113507 (2013). Copyright 2013 AIP Publishing LLC.

in exhibiting the evolution of the VO defect and its conversion to the VO₂ defect ($\text{VO} + \text{O}_i \rightarrow \text{VO}_2$). After irradiation only the VO is present in the spectra in full strength, although at 350 °C its signal has almost disappeared whereas the signal from the VO₂ defect appears quite strong.¹⁵⁴ The band at 862 cm⁻¹ arising from the C_iO_i defect being present after the irradiation also vanishes after the 350 °C isochronal anneal.¹⁵⁴ Regarding the VO defect, it is observed that the amplitude of the corresponding band at 830 cm⁻¹ decreases as x increases from 0 to 0.025 and then to 0.055, whereas the width of the band increases.¹⁵⁴ The band becomes wider and its shape distorted indicating the presence of more than one contributor in this spectral range.

Regarding VO_2 defect, it is observed that its amplitude increases at $x = 0.025$ in comparison with that at $x = 0$ and then decreases substantially for $x = 0.055$.¹⁵⁴

An important feature that was revealed by the FTIR studies is that VO defects have a lower concentration in $\text{Si}_{1-x}\text{Ge}_x$ and anneal at lower temperatures as compared to Si.¹⁵⁴ These have been linked to the weaker bonds (Si-Ge and Ge-Ge) that are also present in $\text{Si}_{1-x}\text{Ge}_x$. In a previous IR study,¹⁵⁴ Lorentzian analysis was employed to determine that the total VO signal in the spectra is composed by (a) VO surrounded by Si atoms up to the next nearest neighbour sites, (b) $(\text{VO-Ge})_1$ that is VO with Ge atom(s) only at the nearest neighbor site, and (c) $(\text{VO-Ge})_2$ that is VO with Ge atom(s) at the next nearest neighbor site. As the binding of O with Ge to form the $(\text{VO-Ge})_1$ and $(\text{VO-Ge})_2$ structures is strong, it results to higher annealing temperatures for these defects.¹⁵⁴ At 180°C , the A-centers migrate and associate with Ge atoms in the $\text{Si}_{1-x}\text{Ge}_x$ lattice.¹⁵⁴ This temperature is lower as compared to Si. The key to the association is the binding of the Ge atoms to the vacant site in the VO pair¹⁵⁴ as is illustrated by the increase of the $(\text{VO-Ge})_1$ and $(\text{VO-Ge})_2$ structures as the VO defects decrease (refer to Fig. 6).

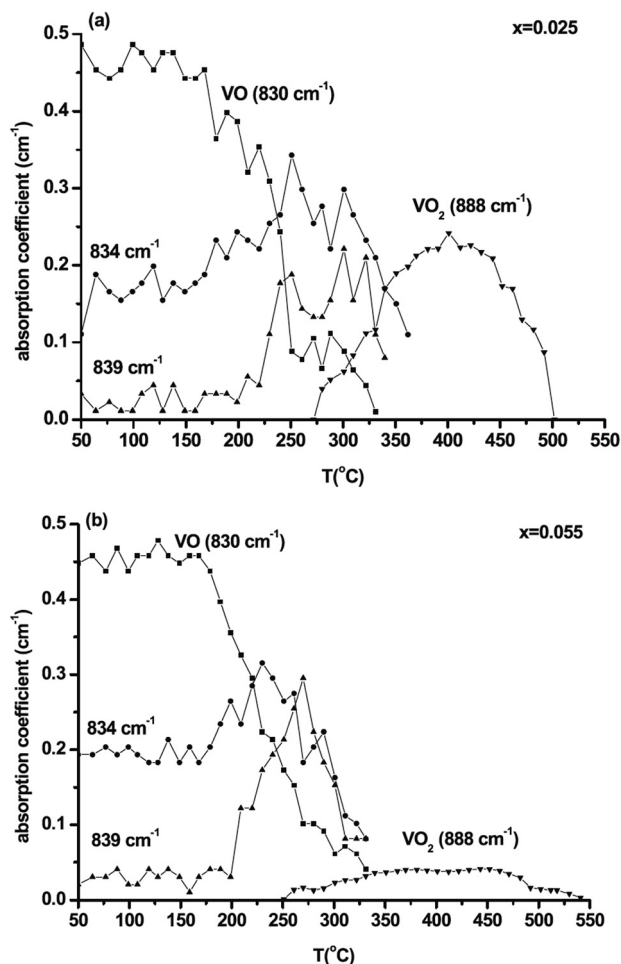


FIG. 6. FTIR results of the evolution of the VO, $(\text{VO-Ge})_1$ and $(\text{VO-Ge})_2$ bands in n -type $\text{Si}_{1-x}\text{Ge}_x$ crystals for (a) $x = 0.025$ and (b) $x = 0.055$ in the course of the 20 min isochronal anneals sequence. Reprinted with permission from J. Appl. Phys. **113**, 113507 (2013). Copyright 2013 AIP Publishing LLC.

At about 250°C , the VO, the $(\text{VO-Ge})_1$ and $(\text{VO-Ge})_2$ structures anneal out and form the VO_2 and $(\text{VO}_2\text{-Ge})$ defects.¹⁵⁴ Ge can impact the availability of self-interstitials thus impacting the processes related in the formation of the VO_2 defect. Studies of Ge-doped Si¹¹² have concluded that Ge atoms compete with C atoms in trapping Si_i mainly when the concentration of Ge is at least three orders of magnitude larger than that of C. This is the case for the $\text{Si}_{1-x}\text{Ge}_x$ material. Notably, the Ge atoms may act as centres of indirect recombination of vacancies and self-interstitials.^{109,155} Therefore, in $\text{Si}_{1-x}\text{Ge}_x$, the Ge concentration is expected to impact the formation of vacancy-related defects as, for instance, the VO_2 centre. It has also been reported¹¹⁰ that the Frenkel pair components may be trapped by the strain fields of the Ge atoms, thus affecting the formation of secondary defects. Additionally, Ge can lead to the formation of $(\text{VO}_2\text{-Ge})$ structures.¹⁵⁴ With the increase of the Ge content in $\text{Si}_{1-x}\text{Ge}_x$ material, the alternative reaction channels that may lead to the formation of VO_2 defects are substantially suppressed.¹⁵⁴ Further to this point, it should be added that additional formation of the VO_2 centre¹⁵⁶ through reaction paths as: $\text{V}_2 + \text{O}_2 \rightarrow \text{V}_2\text{O}_2 + \text{Si}_i \rightarrow \text{VO}_2$ and $\text{V}_2 + \text{Si}_i \rightarrow \text{V} + \text{O}_2 \rightarrow \text{VO}_2$ is expected to be largely restricted in $\text{Si}_{1-x}\text{Ge}_x$.

VI. INSIGHTS FROM ADVANCED COMPUTATIONAL TECHNIQUES

A. Background

Over the past few decades, the ever increasing computational power has allowed the widespread use of atomic scale modeling. The ever decreasing characteristic dimensions of devices and the high concentration of defects and dopants requires methods such as DFT to understand the materials properties. DFT has been employed to investigate O related defects in group IV semiconductors for a number of years, however, the first studies were plagued by the small number of atoms and the inappropriate description of the exchange-correlation functionals. Recent studies employ more advanced hybrid functionals (for example, the screened hybrid functionals due to Heyd, Scuseria, and Ernzerhof (HSE06)^{157,158}), which are deemed to be more appropriate in the description of the electronic structure of the material. Here, earlier DFT studies within the local density approximation (LDA) or the generalized gradient approximation (GGA) to calculate the relative energetics of defects will also be discussed.

B. A-centers revisited

Previous experimental studies determined that the A-center can form at different charge states depending upon the position of the Fermi level in the band gap.^{41,44} Recently, Wang *et al.*⁴⁵ used hybrid DFT calculations to study A-centers in Si. Fig. 7 reports the calculated formation energy of the A-center with respect to the Fermi energy for all possible charge states.⁴⁵ It can be deduced from this figure that only that only two charge states of the A-center are important. In particular, the VO^0 defect is energetically favourable

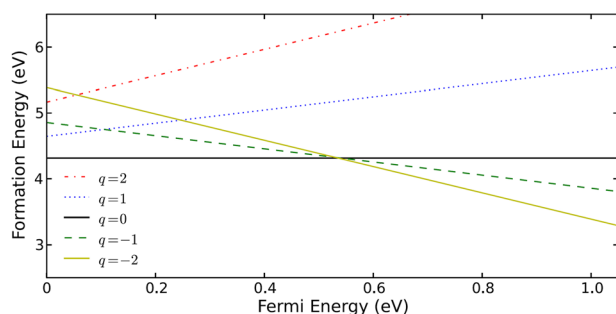


FIG. 7. Hybrid functional DFT formation energies of the A-center with respect to the Fermi energy. Reprinted with permission from Appl. Phys. Lett. **103**, 052101 (2013). Copyright 2013 AIP Publishing LLC.

up to a Fermi energy of 0.54 eV and then the VO^{-2} defect prevails.⁴⁵

How can this difference between experiment and hybrid DFT calculations be justified? Bean and Newman³¹ have determined that the increase of the temperature will lower the position of the Fermi level in the band gap and in effect reduce the VO^{-1} over VO^0 defect fraction. Additionally, it should be considered that DFT results correspond to 0 K, whereas experiment corresponds to far higher temperatures. Pesola *et al.*¹⁵⁹ used LDA/DFT and calculated that VO^{-2} is energetically favourable for Fermi energies above 0.53 eV. This is in agreement with the more recent hybrid DFT study of Wang *et al.*⁴⁵

Through DFT further insights on the A-center can be gained via considering its constituent elements (i.e., V and O_i). Fig. 8 reports the formation energies of the V and O_i defects with respect to the Fermi energy for various charge states. Concerning the V its formation energy is high at low Fermi energy (around 4.5 eV) and decreases to about 3 eV for the -2 charge state (Ref. 44 and Fig. 8(a)). The -2 charge state is favourable when the Fermi energy is above 0.27 eV.⁴⁵ This implies that under equilibrium conditions V is difficult

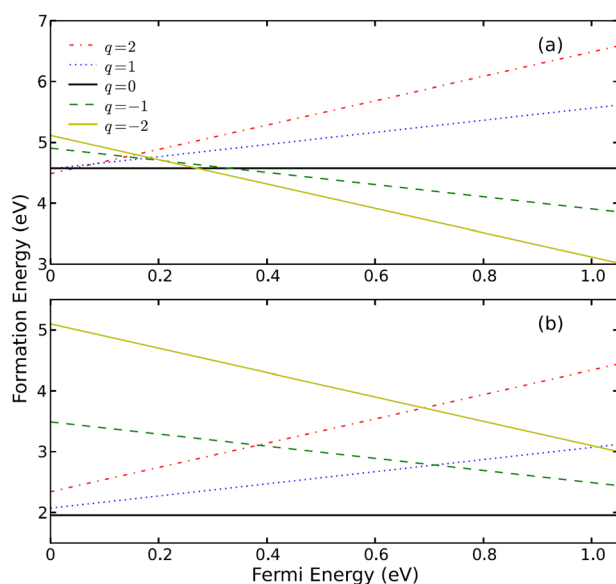


FIG. 8. Hybrid functional DFT formation energies of the (a) V and (b) O_i defects, with respect to the Fermi energy. Reprinted with permission from Appl. Phys. Lett. **103**, 052101 (2013). Copyright 2013 AIP Publishing LLC.

to form in the whole Fermi energy range. The high formation energy of Si vacancies is in agreement with experimental evidence from Si crystal growth, Si self-diffusion, high temperature wafer processing, and metal/dopant diffusion experiments.^{160,161} At any rate when considering an irradiation environment, there is a supersaturation of vacancies, which will lead to the formation of A-centers. Concerning the O_i defect the neutral charge state is dominant (formation energy of 1.95 eV) (Ref. 45 and Fig. 8(a)).

C. Carbon related defects

As in the case of the A-center (discussed above) hybrid DFT calculations were used to study the most important C related defects. In particular, Wang *et al.*⁶⁷ investigated the structure and energetics of defect pairs ($C_i(Si_i)$, C_iO_i , and C_iC_s) and defect clusters $C_iO_i(Si_i)$. Fig. 9 reports the structures derived by DFT of the most important C-related defects in Si. Considering the $C_i(Si_i)$ (refer to Fig. 9(a)), the Si-C dumbbell partially shares the interstitial site with the Si atoms surrounding the defect pair being slightly shifted away from their lattice sites.⁶⁷ In $C_i(Si_i)$, the C atom is threefold coordinated. Fig. 10(a) reports the formation energies for the $C_i(Si_i)$ defect indicating that the $+2$ state is prevalent up to high Fermi energy.

The structure of the C_iO_i defect given by the hybrid DFT calculations of Wang *et al.*⁶⁷ is consistent with the results of previous studies.^{70,162} In the C_iO_i defect, the C_i and O_i interstitials form with Si a ring (refer to Fig. 9(b)). Fig. 10(b) reports the formation energy of the C_iO_i defect as a function of the Fermi energy for different charge states.⁶⁷ It is calculated the lowest energy C_iO_i defect changes from the $+2$ to $+1$ and then to 0 charge state as the Fermi energy increases.⁶⁷

Figs. 9(e)–9(g) present the three stable configurations of the C_iC_s defect. The A- C_iC_s and B- C_iC_s were established decades ago,^{163,164} whereas the C- C_iC_s has been only demonstrated by DFT calculations to be the most stable configuration.¹⁶⁵ Figs. 10(e)–10(g) report the different charge states of the formation energy of the C_iC_s defect as a function of the Fermi energy. As it can be observed from this figure, the neutral charge state dominates the in between Fermi energy range.⁶⁷ At low Fermi energy, the positive charge states are dominant for both the A- and B-type configurations, however, the A- C_iC_s has a higher (1/0) transition level (refer to Figs. 10(e) and 10(f)). For the C- C_iC_s defect, the $+2$ and -2 charge states are favorable below Fermi energy 0.06 eV and above 0.91 eV, respectively.

Figs. 9(c) and 9(d) report the two configurations of $C_iO_i(Si_i)$, which were previously denoted $C_iO_i(Si_i)_a$ and $C_iO_i(Si_i)_b$.⁶⁷ They differ by the Si interstitial position relative to the C_iO_i pair⁶⁷ and are similar to the C4(a) and C4(c) configurations reported previously by Backlund and Estreicher.³⁸ The total energy of $C_iO_i(Si_i)_a$ is 0.28 eV lower than that of $C_iO_i(Si_i)_b$ for the 0, -1 , and -2 charge states but $C_iO_i(Si_i)_a$ is 0.45 eV and 1.51 eV higher in energy as compared to $C_iO_i(Si_i)_b$ for the $+1$ and $+2$ charge state, respectively.⁶⁷ Figs. 10(c) and 10(d) report the formation energy as a function of the Fermi energy for $C_iO_i(Si_i)_a$ and $C_iO_i(Si_i)_b$,

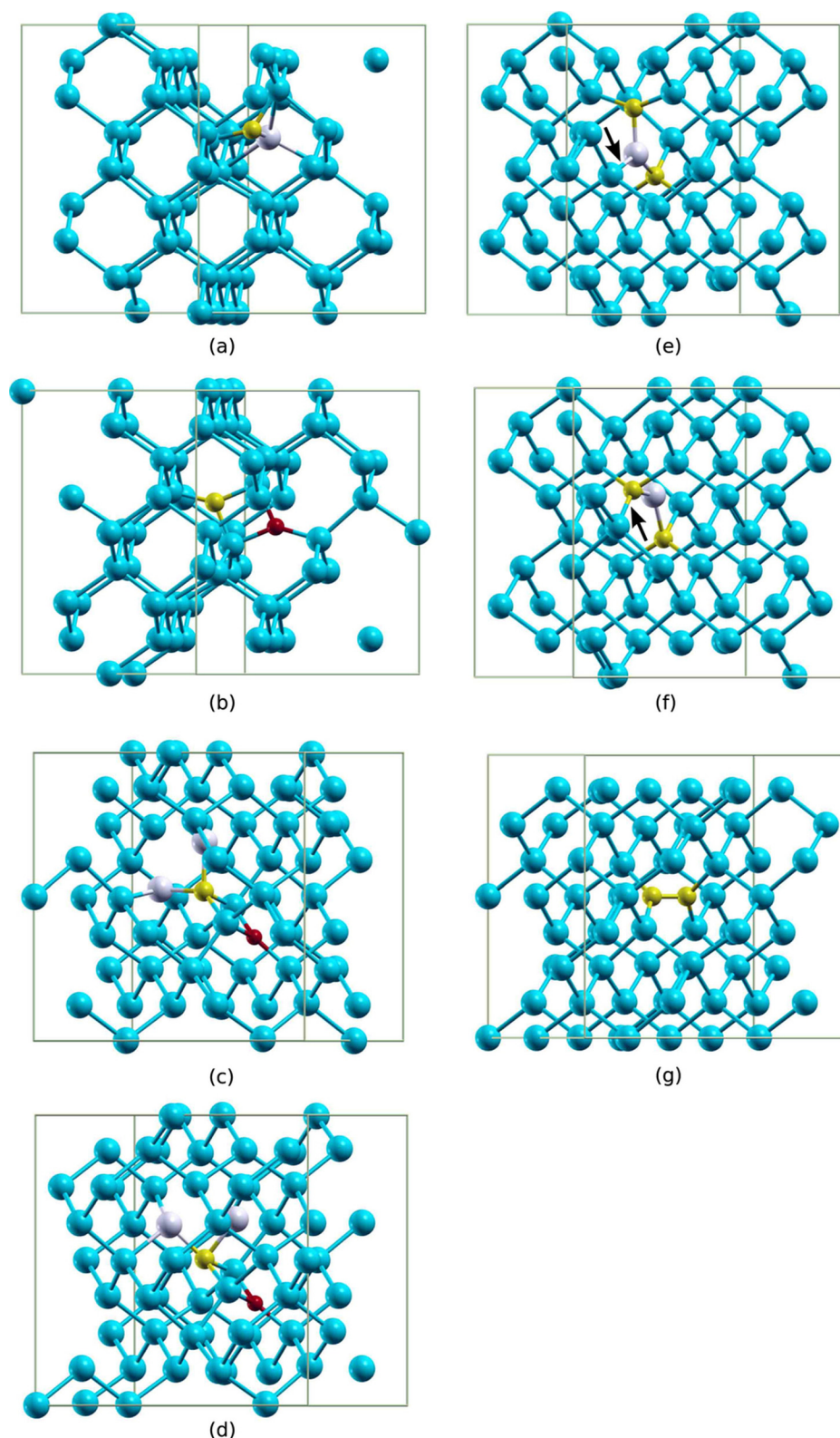


FIG. 9. The structures derived by DFT of the most important carbon-related defects in Si. (a) $C_i(Si_l)$, (b) C_iO_i , (c) $C_iO_i(Si_l)_a$, (d) $C_iO_i(Si_l)_b$, (e) A-type C_iC_s , (f) B-type C_iC_s , and (g) C-type C_iC_s . The big blue spheres represent the Si atoms, medium yellow spheres the C atoms, and small red spheres the O atoms. Grey represents the Si_l atom in $C_i(Si_l)$, the Si atom connecting two C atoms in A- C_iC_s and B- C_iC_s , and the two Si atoms that move significantly between the two $C_iO_i(Si_l)$ structures. Arrows point to the breaking and forming of bonds during the transition between A- C_iC_s and B- C_iC_s . Reprinted with permission from Wang *et al.*, Sci. Rep. 4, 4909 (2014).

respectively. The neutral charge state of the $C_iO_i(Si_l)_a$ has a lower formation energy than the neutral charge state of the $C_iO_i(Si_l)_b$ defect.⁶⁷ There is a transition from the +2 state into the neutral charge state for $C_iO_i(Si_l)_a$ as the Fermi energy increases.⁶⁷ Conversely, for the $C_iO_i(Si_l)_b$ defect the +2 dominates throughout the Fermi energy range.⁶⁷

D. Insights on isovalent doping

Previous computational studies have considered and compared the impact of isovalent doping on O-vacancy defects in Si. These studies were not confined to Ge, Sn, and Pb for which there was experimental evidence but were extended to large isovalent dopants such as hafnium (Hf).

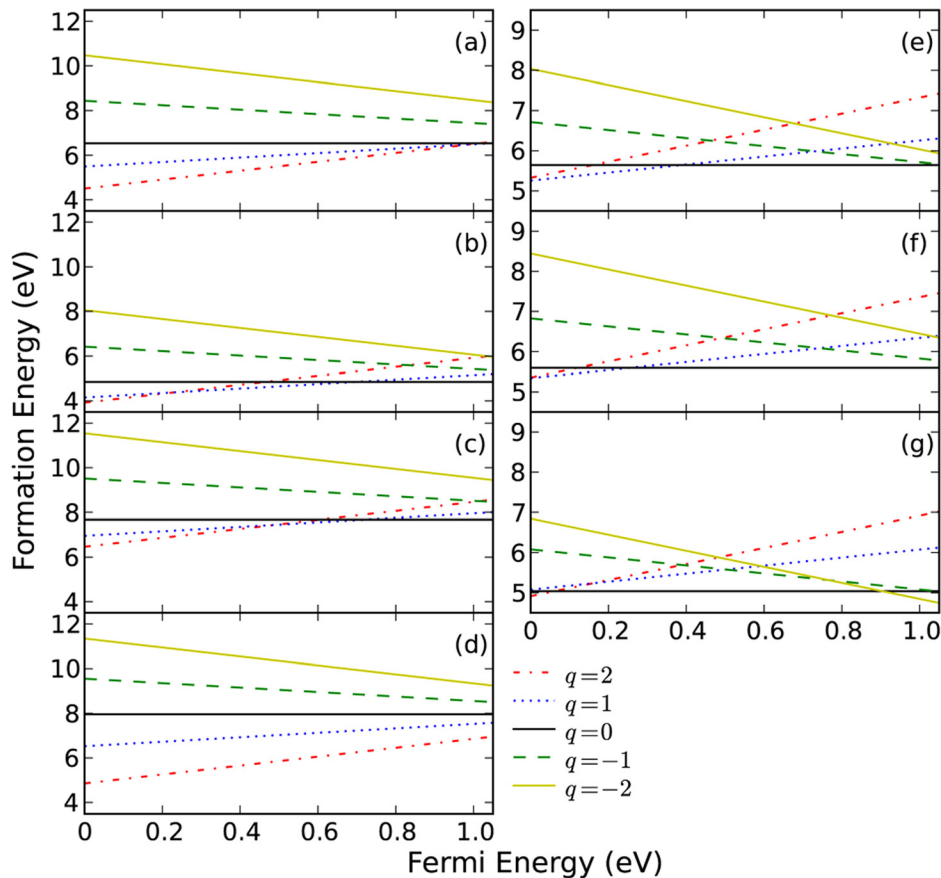


FIG. 10. Hybrid functional DFT formation energies of the (a) $C_i(Si_l)$, (b) C_iO_i , (c) $C_iO_i(Si_l)_a$, (d) $C_iO_i(Si_l)_b$, (e) A-type C_iC_s , (f) B-type C_iC_s , and (g) C-type C_iC_s defects with respect to the Fermi energy. Reprinted with permission from Wang *et al.*, Sci. Rep. 4, 4909 (2014).

Figure 11 represents the optimized structures of the DV and DVO defects ($D = \text{Ge, Sn, and Pb}$) in the atomic chain along the (10-1) direction (refer also to Fig. 3).¹⁴ In a Si perfect crystal, the calculated nearest neighbour distance is 2.35 Å, which increases to 2.40 Å by the vacancy in this chain in the DVO and DV defects.¹⁴ Being oversized the Sn and Pb dopants in a DV defects preferably occupy the space between two semi-vacant lattice sites in what is known as the split-vacancy configuration.¹⁶⁶ In the SnVO and PbVO structures, the O interstitial atom effectively prevents Sn and Pb to shift towards the vacancy.¹⁴ This in turn is reflected upon the distance between the two Si atoms next to the vacancy (in the (10-1)) chain, which reduce from 3.21 Å in the VO structure to 2.99 Å and 3.05 Å in SnVO and PbVO, respectively.¹⁴ The Ge-related defects are distinct as compared the Sn and Pb-related defects as the size of the Ge atom is close to that of the Si atom. Consequently, the GeV and GeVO almost maintain the geometries of the structures without the Ge dopant.¹⁴

Fig. 12 reports the formation energy with respect to the Fermi energy for different charge states of the DVO and DV defects.¹⁴ Interestingly, GeVO exhibits similar behaviour to VO as it transits from the charge neutral to charge -2 (at a Fermi energy of 0.47 eV).^{14,45} The SnVO and PbVO defects exhibit similar behaviour as the charge neutral state is favourable in a wide Fermi energy range. Consequently, these defects are not likely to accept electrons and impact the charge carrier concentration in n-type doped Si.¹⁴ The GeV defect has a single positive charge for low Fermi

energy and a doubly negative charge for all other conditions.¹⁴ For the SnV and PbV, the -2 charge state dominates at high Fermi energy, the +2 charge state in the low Fermi energy range (indicating that these defects can donate electrons), and there is also an intermediate region where the neutral, +1 and -1 charge states can become prevalent.¹⁴

The GeV defects are favourable to be charged and to trap charge carriers. The difference with the SnV and PbV defects is that for the latter states can appear in a wider energy range and this may be linked to the split-vacancy configuration resulting from the larger radii of the Sn and Pb atoms.¹⁴ The high binding energies for SnVO and PbVO illustrate that codoping with Sn and/or Pb is an efficient strategy to restrain the concentration of VO defects.

In essence, the hybrid DFT studies of Wang *et al.*¹⁴ extended previous investigations and highlighted that oversized isovalent atoms are an effective defect engineering strategy to control the concentration of vacancy-related defects in Si. Future studies should be focused on other oversized isovalent dopants such as hafnium and zirconium for which there is limited work on Si.

VII. SUMMARY AND FUTURE DIRECTIONS

In the present review, we identified the issues and recent progress associated with O related defects in Si and $Si_{1-x}Ge_x$. Experimental studies in conjunction with DFT calculations can provide more complete understanding of the defects processes and structure of these defects. The FTIR

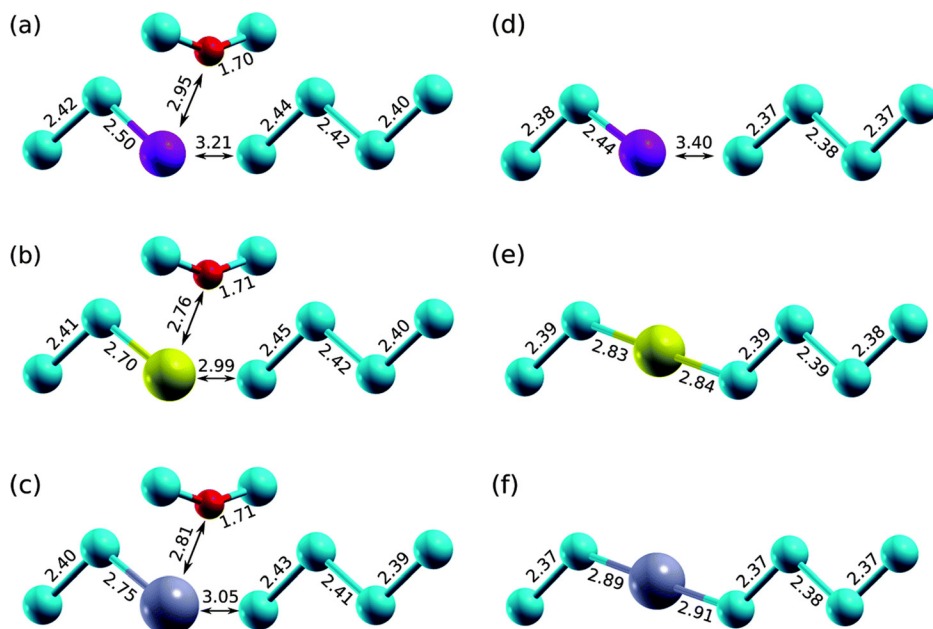


FIG. 11. Hybrid DFT calculations of the structure of the (a) GeVO, (b) SnVO, (c) PbVO, (d) GeV, (e) SnV, and (f) PbV. Only the chain along the (10-1) direction (also refer to Fig. 3) is shown. The big spheres represent the isovalent atoms, medium blue spheres the Si atoms, and small red spheres the O atoms. The distances are given in Å. Reproduced with permission from Wang *et al.*, Phys. Chem. Chem. Phys. **16**, 8487 (2014). Copyright 2014 Royal Society of Chemistry.

studies are consistent with the DFT and illustrate that large isovalent dopants, such as Sn or Pb, can contain the formation of A-centers as well as their conversion to VO_2 defects. DFT studies provide useful information on defects such as PbV which have not been observed experimentally. Additionally, they motivate the investigation of other potentially important oversized dopants such as Hf. In that respect, DFT can be utilized to design point defect engineering strategies. The present review highlights recent hybrid functional DFT results offering new evidence about the charge states of the A-center that will need to be verified by further experiments.

A fruitful and uncharted area of research will be the understanding of the impact of high concentration of Sn on the O related defects in $\text{Si}_{1-x}\text{Ge}_x$. At the extreme case, the formation of A-centers in $\text{Sn}_{1-x}\text{Ge}_x$ alloys will provide further evidence regarding the behavior of O in group IV semiconductors. $\text{Sn}_{1-x}\text{Ge}_x$ alloys are important as they offer a range of strain options enabling the lattice matching of Si or $\text{Si}_{1-x}\text{Ge}_x$ substrates with most III-V and II-VI compounds.^{167–170} The properties of O related defects in binary and ternary group IV alloys, such as $\text{Sn}_{1-x}\text{Ge}_x$ and $\text{Si}_{1-x-y}\text{Ge}_x\text{Sn}_y$, have not been investigated in detail.

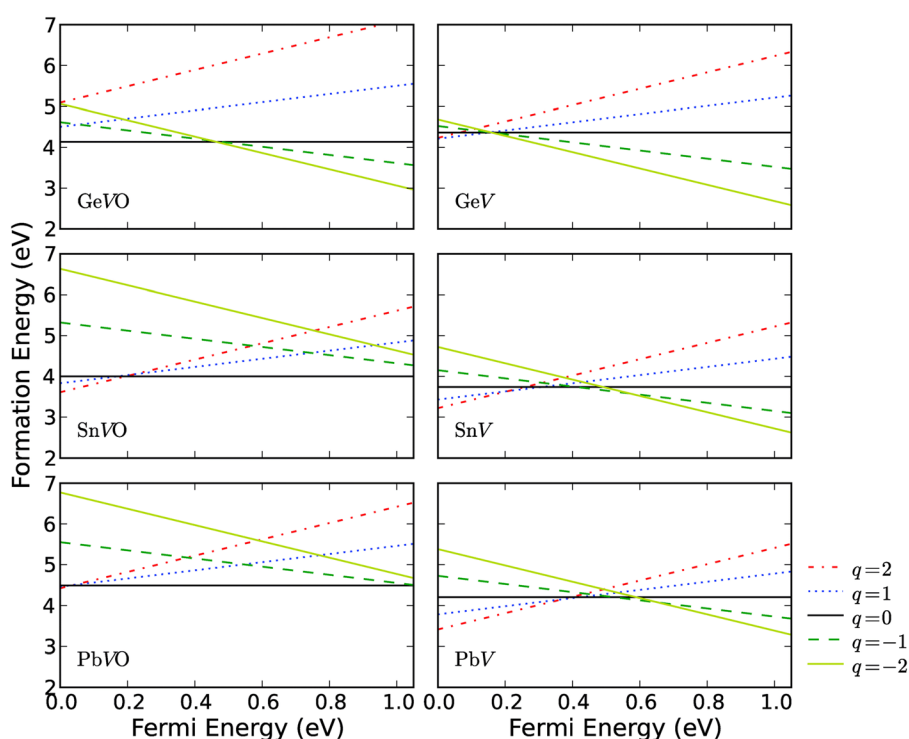


FIG. 12. Hybrid DFT calculations of the formation energies as a function of the Fermi energy for different charge states of DVO and DV (where D = Ge, Sn, and Pb) defects. Reproduced with permission from Wang *et al.*, Phys. Chem. Chem. Phys. **16**, 8487 (2014). Copyright 2014 Royal Society of Chemistry.

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