

# A review of the top of the barrier nanotransistor models for semiconductor nanomaterials

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## ABSTRACT

The modelling and simulation of low-dimensional nanoelectronic devices is important, because the semiconductor industry has scaled transistors down to the sub-10 nm regime. The top of the barrier (ToB) transistor model has been developed and used to model transistors that are composed of various semiconducting materials. In this paper, a brief overview of the ToB transistor model is presented. The main objective of this paper is to provide a focused review on the device modelling milestones that have been achieved using the ToB transistor model. The accuracy of a few of these models is assessed by computing the normalised root mean square deviation. The ToB transistor model is widely used for computational studies on low-dimensional field-effect transistors with various channel materials, such as ultra-thin-bodies, two-dimensional materials and one-dimensional materials. The ToB transistor model is also useful for extensive research in circuit-level simulations. In summary, this nanoscale model helps researchers to identify and evaluate the potential nanomaterials for future nanoelectronic applications.

## 1. Introduction

Advances in the semiconductor industry are governed by Moore's Law, manifesting that the number of transistors per die is doubled at a regular interval (every two years) [1], as shown in Fig. 1. Various strategies for the further miniaturisation of transistors are outlined in the International Roadmap for Devices and Systems (IRDS) [2]. Meanwhile, the semiconductor industry based on silicon (Si) technology achieved the 7 nm technology node in 2018, and is expected to deliver 5 nm and 3 nm technology nodes in the near future [3]. Besides the continuous scaling of the Si-based metal-oxide-semiconductor field-effect-transistors (MOSFETs), "More than Moore" devices are rigorously being researched [2,4–6]. As a result, transistors based on other low-dimensional materials [7–9] have also been explored. These include, graphene [10–14], carbon nanotubes (CNTs) [15–20], phosphorene [21–24], silicene [25–28], transition metal dichalcogenides (TMDs) [29–35] and III-V semiconductors [36–41].

Velocity overshoot and ballistic transport have become dominant factors in nanoscale MOSFETs [42]. In this microscopic regime, conventional drift-diffusion transistor models are no longer suitable for describing the carrier transport properties within the channel regions, where the electric field is intensively high [43]. Modelling and simulation are important to provide guidance and theoretical explanations on the operation of nanoscale MOSFETs. Thus, a compact ballistic transistor model is required to describe the essential physics behind the nanoscale MOSFETs. The ballistic nanoscale transistor model [44] was developed by A. Rahman et al. in 2003,

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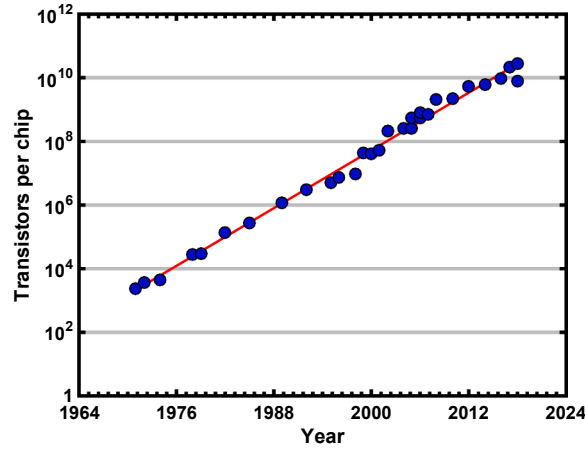


Fig. 1. The number of transistors in a microprocessor chip (or die) over the past five decades, adapted from Ref. [1].

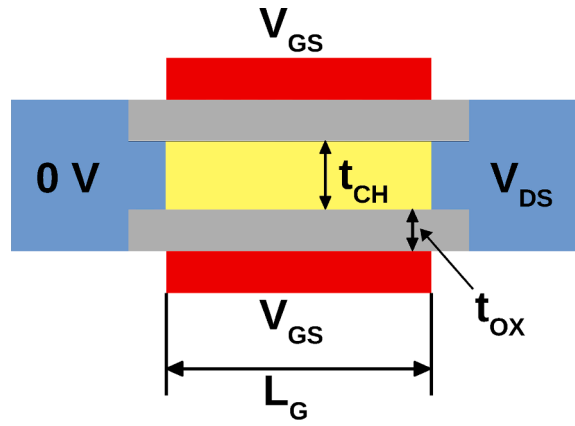


Fig. 2. Structural model of the double-gate MOSFET (n-channel), where  $V_{GS}$  is the gate voltage,  $V_{DS}$  is the drain bias,  $L_G$  is the gate length,  $t_{CH}$  is the channel thickness, and  $t_{OX}$  is the oxide thickness.

which is commonly known as the top of the barrier (ToB) transistor model in the literature. The ToB transistor model can be simply solved numerically using software such as MATLAB.

There are various conventional (e.g. Refs. [45–48]) and recent (e.g. Refs. [49–57]) theoretical transistor models in the literature. The relationship between the conventional and nanoscale theoretical models of the MOSFETs have been reviewed in Ref. [42]. However, the milestones achieved for a particular theoretical model are rarely discussed. The main objective of this paper is to provide a focused review of the transistor models (with various channel materials) based on the ToB transistor model. This paper presents a brief overview of the ToB transistor model in Section 2. In Section 3, the studies that have developed various transistor models based on the ToB transistor model are systematically reviewed. Subsequently, the model comparison and conclusion are clearly described in Sections 4 and 5 respectively.

## 2. Overview of the top-of-the-barrier transistor model

### 2.1. The ballistic MOSFETs

The ToB transistor model was developed based on the 10 nm double-gate MOSFET, as shown in Fig. 2. An n-channel MOSFET is a three terminal (source, drain, and gate) device where the drain bias lowers the Fermi level in the drain, and the gate voltage lowers the potential energy barrier in the channel. These conditions are achieved when the source is grounded. The energy band diagrams corresponding to variations in the drain bias and gate voltage are shown in Fig. 3.

The non-equilibrium Green's function (NEGF) simulation has largely contributed to the development of the ToB transistor model. The plot of the potential barrier potential versus position in the channel (Fig. 4) from the NEGF simulation under on-state conditions (high gate voltage and drain bias) shows that the ToB in the channel occurs closer to the source end (where the electric field is almost zero) of a ballistic MOSFET [58]. A. Rahman et al. showed that velocity saturation occurs in this particular region [44]. As current is

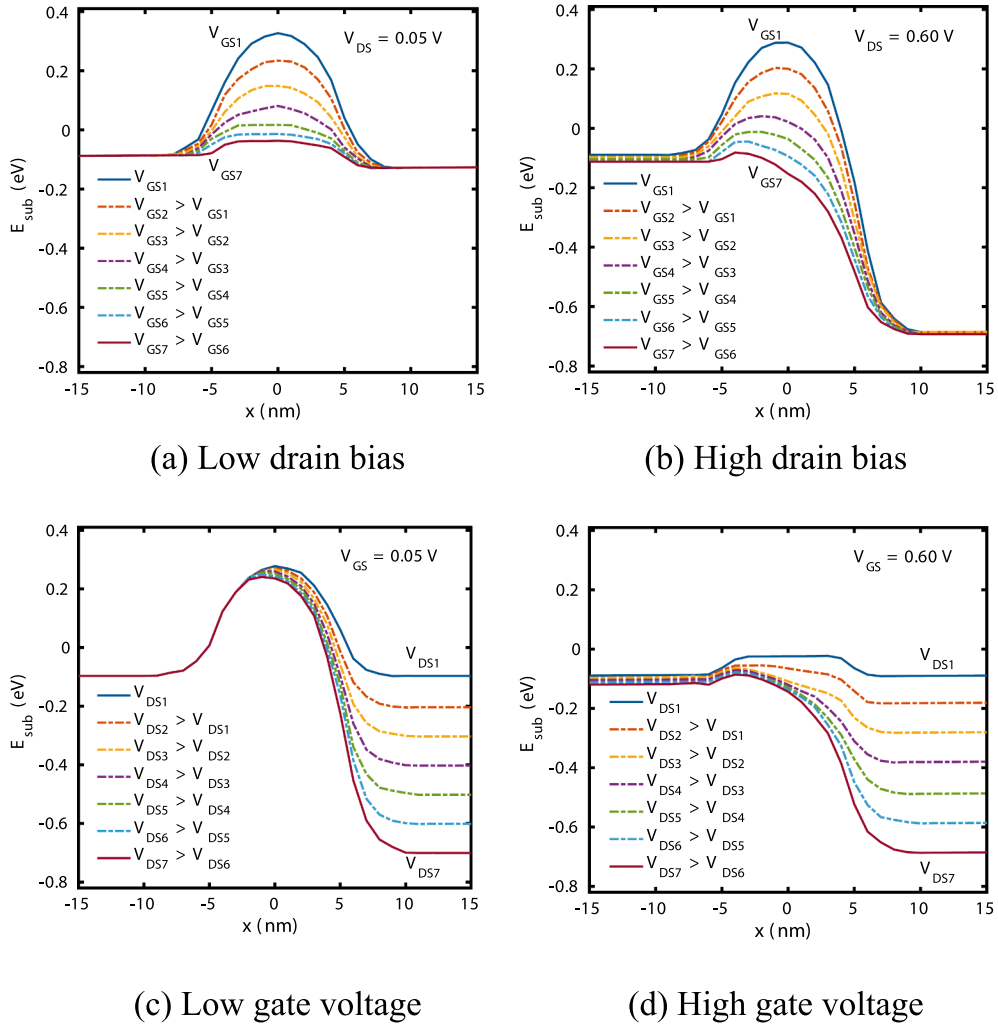


Fig. 3. Energy band diagram of a 10 nm double-gate MOSFET, adapted from Ref. [59].

the product of the charge and carrier velocity, the ToB is of great significance to the current-voltage (I-V) characteristics and device performance of a ballistic MOSFET.

## 2.2. The model and procedures

A simplified two-dimensional (2D) circuit model of a ballistic MOSFET is shown in Fig. 5(a). The gate voltage ( $V_{GS}$ ) and drain bias ( $V_{DS}$ ) are applied to the gate and drain terminals, respectively, while the source terminal is always grounded ( $V_s = 0$  V). The circuit model consists of three capacitors, the gate capacitor ( $C_G$ ), source capacitor ( $C_S$ ), and drain capacitor ( $C_D$ ). The mobile charge is placed at the ToB. The local density of states (LDOS), source Fermi energy level ( $E_{FS}$ ), drain Fermi energy level ( $E_{FD}$ ), and self-consistent potential at the ToB ( $U_{SCF}$ ) are used to determine the mobile charge. Fig. 5(b) depicts the filling of the electron states at the ToB by  $E_{FS}$  and  $E_{FD}$ .

The ToB includes the treatment of the quantum capacitance naturally through the self-consistent gate electrostatics (the quantum capacitance is the effective capacitance owing to the finite density of states, particularly in low-dimensional materials [60]). The equilibrium electron density at the ToB when no bias is applied is

$$N_0 = \int_{-\infty}^{+\infty} D(E)f(E - E_F) dE, \quad (1)$$

where  $D(E)$  is the LDOS and  $f(E - E_F)$  is the equilibrium Fermi-Dirac function. The Fermi-Dirac function describes the probability of occupancy of each states at a given temperature,  $T$  [61], and is given by

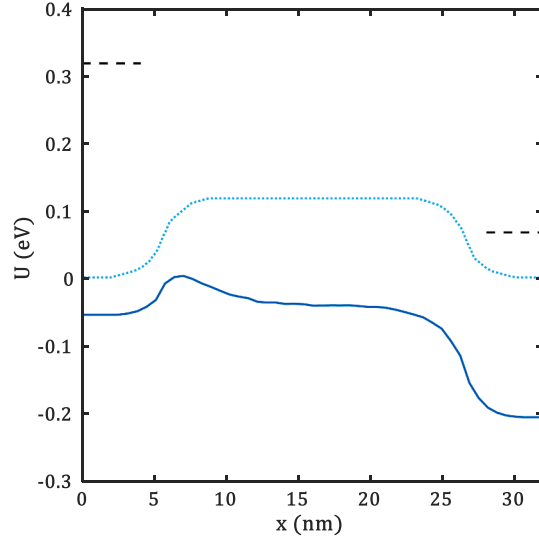


Fig. 4. The potential profile in a nanoscale device, adapted from Fig. 9A in Ref. [58].

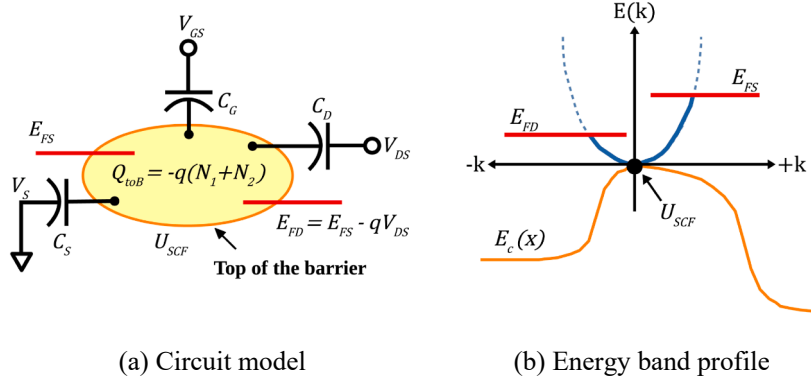


Fig. 5. Schematic diagram of the (a) circuit model of a ballistic transistor and (b) energy band profile, indicating how the states are filled at the ToB by the two Fermi levels.

$$f(E) = \left[ 1 + \exp\left(\frac{E - E_F}{k_B T}\right) \right]^{-1}, \quad (2)$$

where  $k_B$  is the Boltzmann constant.

When the gate voltage and drain bias are applied, the positive velocity states are filled by the source according to Eq. (3a) and the negative velocity states are filled by the drain according to Eq. (3b), creating a non-equilibrium condition. These conditions are described by

$$N_1 = \frac{1}{2} \int_{-\infty}^{+\infty} D(E - U_{SCF}) f(E - E_{FS}) dE, \quad (3a)$$

$$N_2 = \frac{1}{2} \int_{-\infty}^{+\infty} D(E - U_{SCF}) f(E - E_{FD}) dE, \quad (3b)$$

where  $E_{FS} = E_F$  and  $E_{FD} = E_F - qV_{DS}$ . To simplify the numerical procedures, changes in the variables are used (i.e. shifting the Fermi energy instead of shifting the energy levels in the LDOS) to re-express Eqs. (3a) and (3b) as

$$N_1 = \frac{1}{2} \int_{-\infty}^{+\infty} D(E) f_s(E_s) dE, \quad (4a)$$

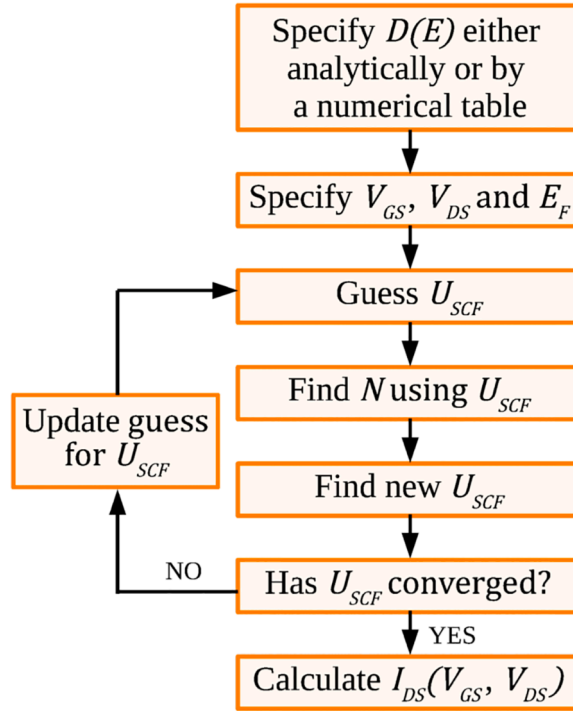


Fig. 6. The simulation flow chart for the ToB transistor model, adapted from Ref. [63].

$$N_2 = \frac{1}{2} \int_{-\infty}^{+\infty} D(E) f_D(E_D) dE, \quad (4b)$$

where the source and drain Fermi functions can now be defined as

$$f_S(E_S) \equiv f(E + U_{SCF} - E_{FS}), \quad (5a)$$

and

$$f_D(E_D) \equiv f(E + U_{SCF} - E_{FD}), \quad (5b)$$

respectively. The electron density at the ToB is evaluated as  $N_{ToB} = N_1 + N_2$ , provided that the LDOS,  $D(E)$ , locations of  $E_{FS}$  and  $E_{FD}$  are defined, and  $U_{SCF}$  is known. The bias induced charge,  $\Delta N$  is obtained by subtracting the equilibrium electron density,  $N_0$  from the non-equilibrium electron density filled by the source and drain,  $N_{ToB}$ , given by  $\Delta N = (N_1 + N_2) - N_0$ . The self-consistent potential is obtained by solving the Poisson equation involving the bias induced charge,  $\Delta N$  due to the terminal voltages

$$U_{SCF} = -\frac{q}{C_\Sigma} (Q_t - q\Delta N), \quad (6)$$

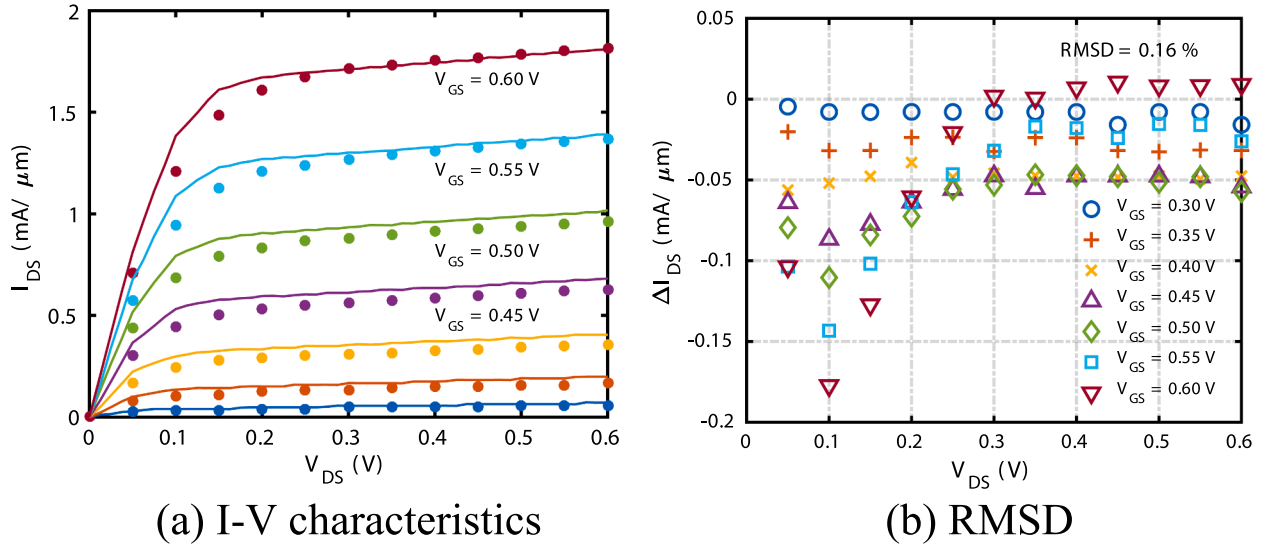
where  $q$  is the constant for electric charge and  $C_\Sigma = C_G + C_D + C_S$  is the total capacitance. The stored charge at the terminals [62],  $Q_t$  is defined as

$$Q_t \equiv V_G C_G + V_D C_D + V_S C_S, \quad (7)$$

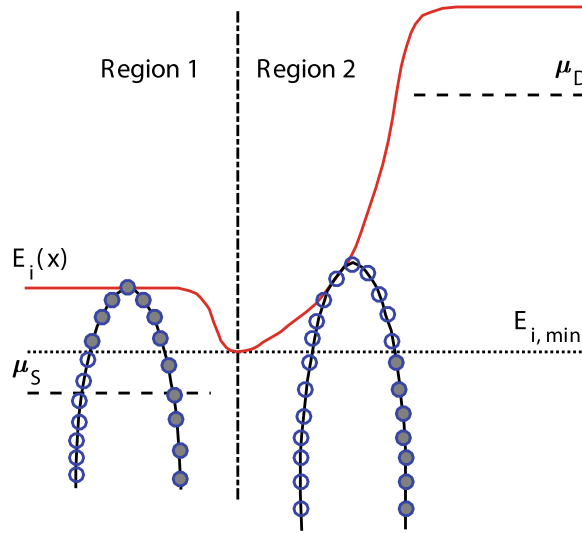
The two non-linear Eqs. (4) and (6) with two unknowns namely  $N$  and  $U_{SCF}$ , can be solved iteratively using numerical software such as MATLAB. After solving the unknown values, the drain current can be evaluated using Landauer-Büttiker ballistic current transport equation [44], given by

$$I_{DS} = \frac{q}{2} \int_{-\infty}^{+\infty} |v(E)| D(E) [f_S(E_S) - f_D(E_D)] dE, \quad (8)$$

where  $|v(E)|$  is the average velocity. The complete procedure for computing the particular value of  $I_{DS}$  at the selected values of  $V_{GS}$  and  $V_{DS}$  is summarised in the flow chart illustrated in Fig. 6.



**Fig. 7.** Comparison between the ToB transistor model [44] and nanoMOS simulator [72]. The solid lines in (a) represent results of the ToB transistor model, while the filled dots in (a) represent the results of the nanoMOS simulator.



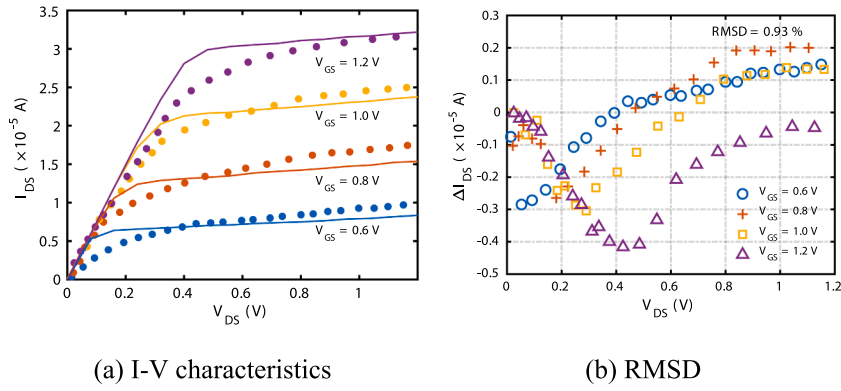
**Fig. 8.** The energy band profile for hole conduction (in p-channel MOSFETs) [68].

### 3. The transistor models

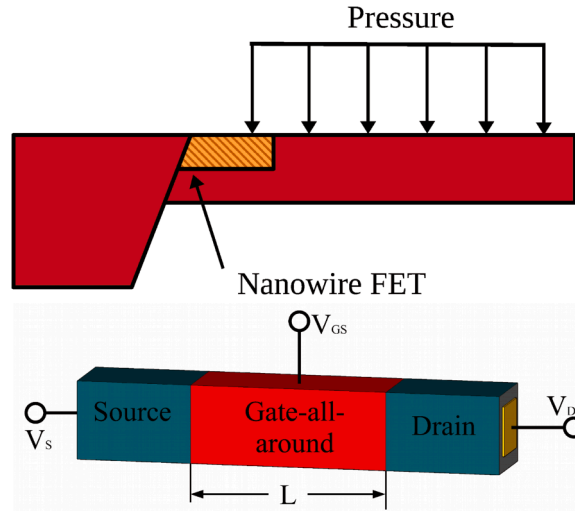
Theoretical studies are important for explaining the experimental results. In addition, they can provide a guideline and framework before the fabrication of expensive devices. In this section, previous theoretical works that have studied the ToB transistor model are reviewed. This section is divided into four subsections by classifying the type of materials, namely Si and germanium (Ge), carbon-based materials, graphene-like materials, and III-V compound semiconductors. The performance of the transistors is commonly measured using the device metrics [64] such as the threshold voltage ( $V_t$ ), drain-induced barrier lowering (DIBL), subthreshold swing (SS), and on-current to off-current ratio ( $I_{on}/I_{off}$ ). The performance of the published models (for a few selected works where the benchmarks of the results were available) is evaluated using the normalised root mean square deviation (RMSD) [65,66], given as

$$RMSD = \frac{\sqrt{(\sum_{i=1}^N (a_i - b_i)^2) / N}}{\max(a_i, b_i) - \min(a_i, b_i)} \times 100\%, \quad (9)$$

where  $N$  is the total number of data, and  $a_i$  and  $b_i$  are the values of the  $i^{th}$  data in the compared models.



**Fig. 9.** Comparison of the I-V characteristics of SiNWFET between the ToB model [69] and experimental measurement [74]. The solid lines in (a) represent the results of the ToB transistor model, while the filled dots in (a) represent the experimental measurement.



**Fig. 10.** Schematic diagram of the SiNWFET pressure sensor [70].

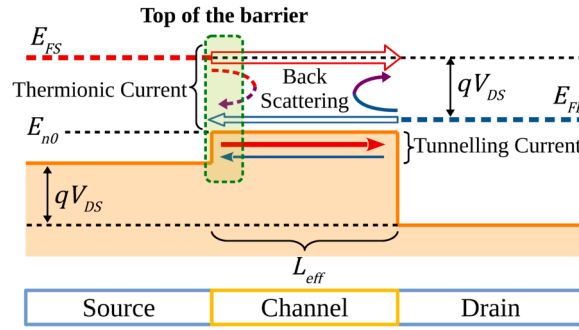
### 3.1. Silicon and germanium

Si and Ge are well-established semiconductors in the industry [67]. Several groups have employed the ToB transistor model to simulate Si-based [44,68–70] and Ge-based [71] MOSFETs within the ballistic limit. Rahman et al. [44] demonstrated that the ToB transistor model is accurate at both the low and high gate and drain biases by comparing their results with the nanoMOS numerical simulator [72]. Fig. 7(a) depicts a comparison between the results of the ToB transistor model and nanoMOS simulator with the same transistor parameters (Si body thickness of 1.5 nm, silicon dioxide thickness of 1.5 nm, doping concentration of the source and drain of  $10^{20} \text{ cm}^{-3}$ , and gate workfunction of 4.25 eV).

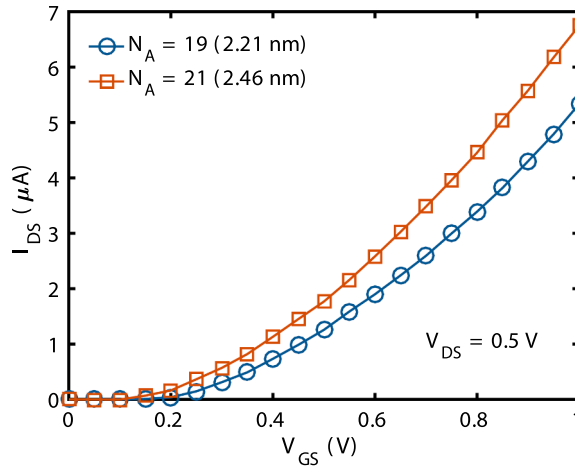
Complementary to the work of Rahman et al. [44] (which focused on the n-channel MOSFETs where electron conduction is the main concern), Ramesh et al. [68] discussed the application of the ToB transistor model to p-channel MOSFETs (where hole conduction is the main concern). In contrast to the energy band diagram based on the conduction band shown in Fig. 5(b), the ToB transistor model based on the valence band is illustrated in Fig. 8. Thus, the ToB transistor model is useful for simulating both the n-channel and p-channel MOSFETs and the results can be combined to form the complementary metal-oxide-semiconductor (CMOS) transistor technology [73].

The ToB model was employed by Chin et al. [69] to investigate the I-V characteristics of Si nanowire FET (SiNWFET) with a nanowire diameter of 16 nm and channel length of 10 nm. They showed that their simulation results were in agreement with the experimental results published by Li et al. [74], as shown in Fig. 9(a). The performance metrics of the simulated 10 nm SiNW indicated a DIBL of 88.66 mV/V, SS of 88.80 mV/dec, and  $I_{\text{on}}/I_{\text{off}}$  of  $10^4$ , which were all very close to the experimental measurement.

Besides gate-controlled FET devices, Zhang et al. [70] used the ToB transistor model to simulated p-channel pressure-controlled (pressure sensors) SiNWFETs with various channel orientations. They investigated the SiNW orientations in [100], [110], and [111] directions. They calculated the band structure of the SiNWs using  $k \cdot p$  theory. The structure of their model is shown in Fig. 10. Their



**Fig. 11.** Schematic diagram of the quasi-ballistic carrier transport in a GeNW p-channel MOSFET with the flat channel potential barrier approximation [71].



**Fig. 12.** Plots of the ballistic  $I_{DS} - V_{GS}$  characteristics of GNRFET with  $N_A = 19$  ( $3p + 1$  GNR family) and  $N_A = 21$  ( $3p$  GNR family) [77].

results showed that SiNWs with different orientations possessed different hole transport effective masses (the transport effective masses are parameters obtained from the parabolic band structure assumptions [25,67,75]). They concluded that the orientations of the channel materials played important roles with respect to the carrier density and injection velocity, which are both affected by the hole transport effective masses.

Tanaka et al. [71] modelled the p-channel Ge nanowire FET (GeNWFET) using the ToB transistor model. The model was modified to account for phonon and surface roughness scattering in the channel and source-to-drain direct tunnelling (quasi-ballistic hole transport regime) as shown in Fig. 11. In their work, the “backscattering rate” was taken into account by calculating the sum of scattering probability where the states move with negative velocity. Moreover, various orientations of GeNWs were also included in their studies. The valence band structures were calculated using  $sp^3d^5s^*$  tight-binding (TB) approach with spin-orbit coupling. They concluded that GeNW with  $[110]/(001)$  orientation exhibits a higher hole mobility as compared with the  $[110]/(1\bar{1}0)$  orientation in the quasi-ballistic transport regime, which is consistent with previous published results [76]. The results showed that the ToB transistor model could accurately describe the MOSFETs in both the ballistic and quasi-ballistic transport regimes.

### 3.2. Graphene and carbon nanotubes

Researchers have also used the ToB transistor model to perform simulations on two carbon-based materials that were awarded the Nobel Prize: graphene [77–82] and CNTs [66,83–87]. The success of graphene and CNTs is remarkable in the semiconductor industry. Interestingly, the CNT-based CMOS microprocessor (consisting of more than 14,000 CMOS CNTFETs) has also been successfully fabricated and programmed to run 32-bit instructions [88].

Zhao et al. [77] investigated the graphene nanoribbon FETs (GNRFETs) in the armchair orientations. They obtained the band structure profile using 3-nearest-neighbour TB approach. Fig. 12 shows a comparison of the performance of the armchair GNRFETs with a width,  $N_A$  of 19 (from  $N_A = 3p + 1$  GNR family) and 21 (from  $N_A = 3p$  family). These GNRFETs have silicon dioxide ( $\text{SiO}_2$ ) thickness of 10 nm. The results showed that GNRFET with  $N_A = 19$  (or width of 2.21 nm) exhibited a higher quantum capacitance and lower on-current than the GNRFET with  $N_A = 21$  (or width of 2.46 nm). Moreover, the GNRFET model was extended to include the edge scattering effect, which significantly reduced the on-current.



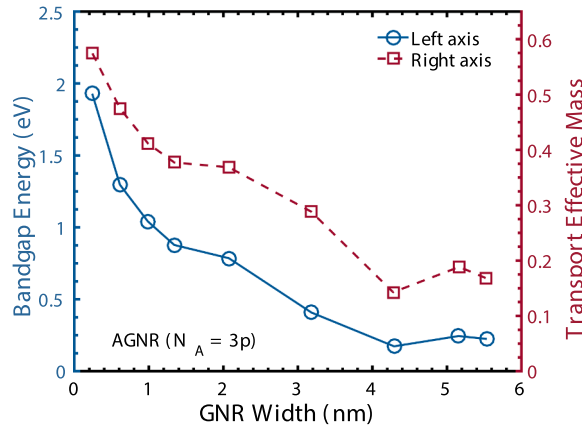


Fig. 13. Plots of the band gap and electron transport effective mass for  $N_A = 3p$  GNRs [78].

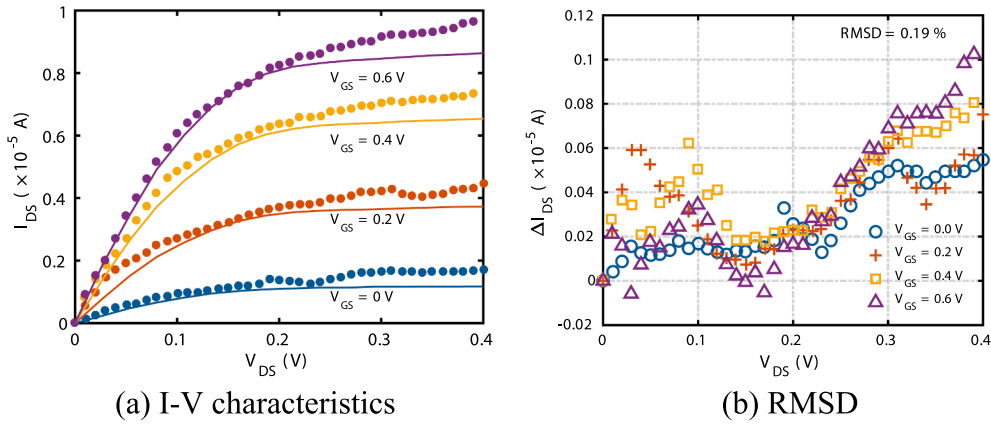


Fig. 14. Comparison between the simulation results [66] and experimental data [90] of a CNT transistor. The solid lines in (a) represent the results of the ToB transistor model, while the filled dots in (a) represent the experimental measurement.

Owing to the higher on-current of the  $3p$  GNR family, Tsuchiya et al. [78] performed simulations involving GNRFET with varying  $N_A = 3p$  widths. They extracted the values of the band gap and electron transport effective mass of the  $3p$  GNR family using first-principle band structure calculations based on density functional theory (DFT), as depicted in Fig. 13. They concluded that a proper selection of the GNR width is important to achieve a finite band gap and optimum switching delay. These results are consistent with the digital logic circuit level simulations of GNRFET using the combination of the ToB transistor model and spice simulation by Tan et al. [80], where it was found that the switching time of the GNRFET devices was lower when GNRFET widths were larger.

Besides investigations of the pristine monolayer GNRFETs, the ToB transistor model was also used to simulate the bilayer GNRFETs [79] and non-ideal monolayer GNRFET incorporating vacancy defects [82], where both group using the TB approach to compute the band structures. They found that the band gap of the bilayer GNR is larger but significantly degrades the I-V characteristics of the GNRFETs due to the deceleration of electrons [79]. Modelling of the vacancy defect is also important, as it is an unpreventable process during fabrication [89]. Nazari et al. [82] reported that the introduction of 3 single vacancy (3SVs) defects to the  $N_A = 12$  GNRFET improved the I-V characteristics in terms of the DIBL and SS. The improvement in DIBL ranged from 112 mV/V (pristine GNRFET) to 53 mV/V (3SVs GNRFET) and for SS is from 239 mV/decade (pristine GNRFET) to 147 mV/decade (3SVs GNRFET).

Kazmierski et al. [66] extended the ToB transistor model to reduce the computational cost, specifically for the CNT transistors. They compared their model with the experimental data from Ref. [90], as shown in Fig. 14(a). By improving the ToB transistor model, they reduced the CPU time by more than 40% for the simulation of an n-type CNT transistor at  $T = 300$  K (with a nanotube diameter of 1.6 nm and oxide thickness of 50 nm). In addition, this model can also be used to account for the strained CNTs, tunnelling effect, and phonon scattering.

### 3.3. Graphene-like two-dimensional materials

Catalysed by the rise of mechanically exfoliated graphene in 2004, many other graphene-like 2D materials (which means that the materials are in honeycomb lattice arrangements) have been rigorously explored. The 2D materials that have been commonly used as

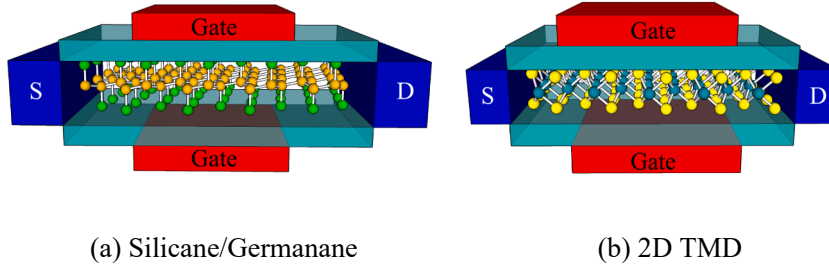


Fig. 15. Schematic structures of the double-gate graphene-like MOSFET devices (adapted from Ref. [93]).

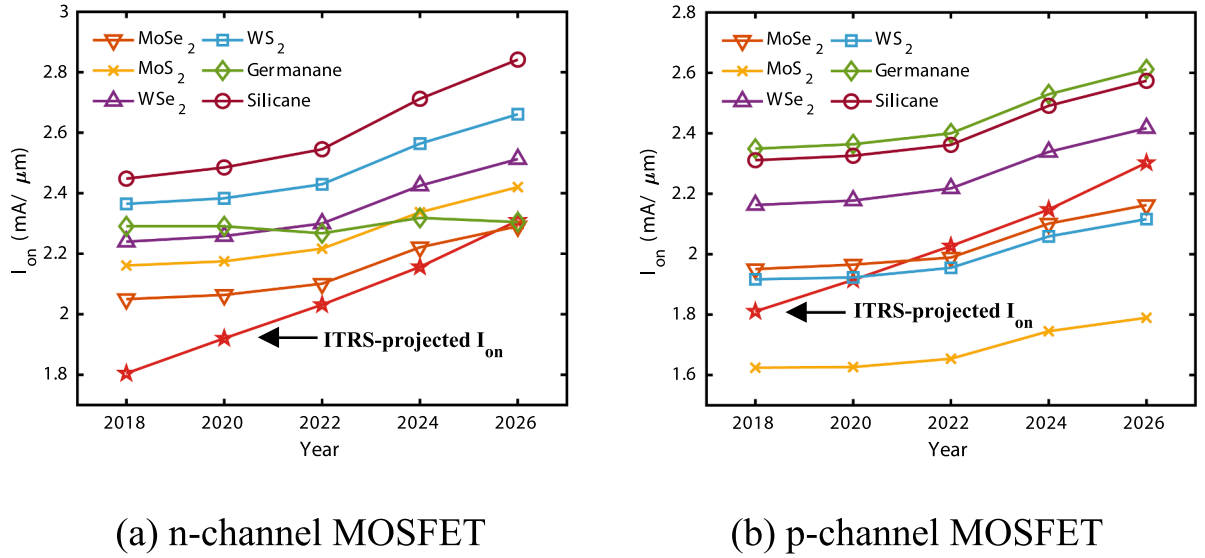


Fig. 16. Assessment of the on-currents in various MOSFETs using graphene-like 2D materials as the conducting channels [93].

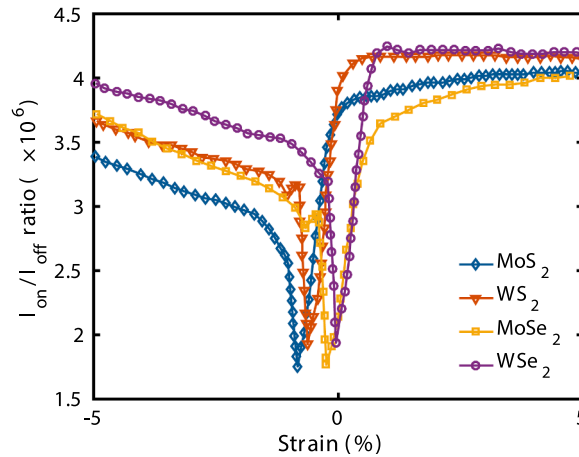


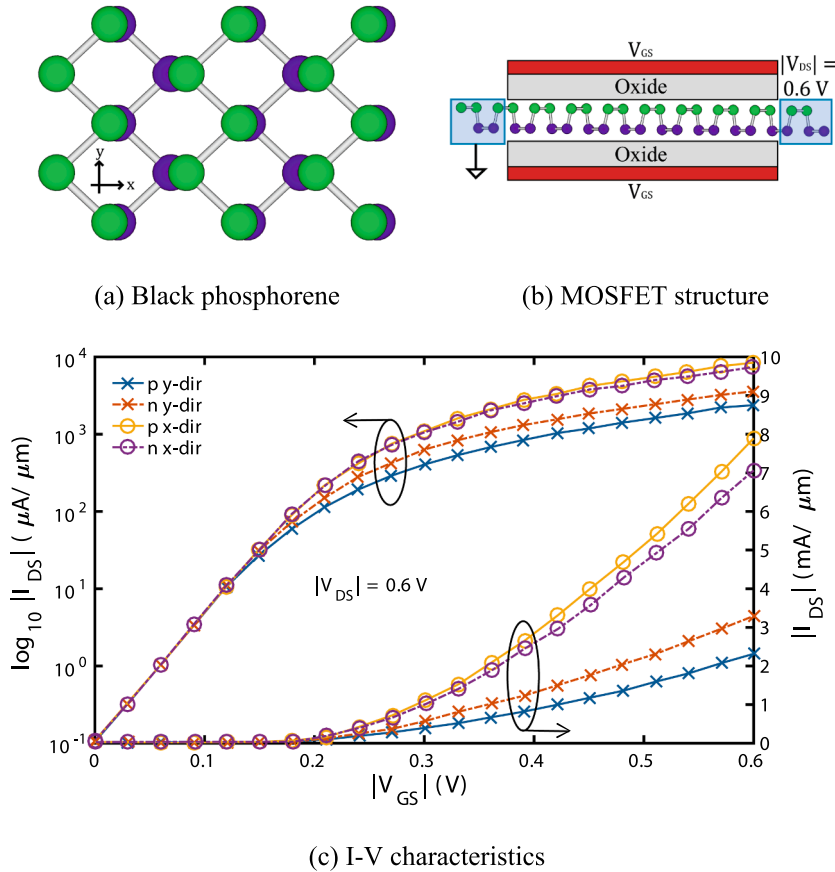
Fig. 17. The  $I_{on}/I_{off}$  ratio for various TMDs under biaxial strain at the supply voltage of 0.8 V [96].

channel materials for the ToB transistor models include phosphorene [91], germanene [92,93], silicene [92,93], and TMDs [94–96]. Phosphorene, germanene, and silicene are monolayers of honeycomb lattices that purely consist of phosphorus (P), Ge, and Si respectively. TMDs are also denoted as  $MX_2$ , where M is a transition metal atom such as molybdenum (Mo) or tungsten (W), and X is a chalcogen atom such as sulphur (S), selenium (Se), or Tellurium (Te) [97]. Fig. 15 illustrates examples of the double-gate MOSFETs with graphene-like materials as the conducting channels.

**Table 1**

Comparison between the results from the first-principle calculation [100] and ToB transistor model [96] for MoS<sub>2</sub> at various channel lengths. The applied voltages are  $V_{DS} = 0.5$  V,  $V_{GS}(off) = 0$  V and  $V_{GS}(on) = 0.8$  V.

Channel length (nm)	First-principle calculation [100]		ToB transistor model [96]	
	$I_{on}/I_{off}$ ratio	SS (mV/dec)	$I_{on}/I_{off}$ ratio	SS (mV/dec)
10	$2.3 \times 10^7$	65	$4.7 \times 10^7$	67
8	$9.3 \times 10^5$	75	$1.6 \times 10^6$	78
6	$1.8 \times 10^4$	98	$4 \times 10^{-2}$	102



**Fig. 18.** The I-V characteristics of the monolayer black phosphorene (BP) MOSFET shown using the linear and logarithmic scales on the same plot [91].

Low et al. [93] performed simulations for silicene and germanene (silicene and germanene are the hydrogenated versions of silicene and germanene, respectively [98]) using the ToB transistor model. They used DFT in the general gradient approximation with the Perdew-Burke-Ernzerhof exchange-correlation function to obtain the electronic band structures of silicene and germanene. Their on-current results were compared with that of the other TMDs, and the values projected by the International Technology Roadmap for Semiconductors (ITRS 2.0) [99] are plotted in Fig. 16(a) and (b) for the n-channel and p-channel MOSFETs, respectively. Silicene exhibits the highest on-current for the n-channel MOSFET, while germanene exhibits the highest on-current for the p-channel MOSFET. Their results showed the prospective applications of 2D materials in the future MOSFET devices.

Hosseini et al. [96] performed simulations on strained-TMD MOSFETs using the ToB transistor model. The electronic band structures of the channel materials was modelled using the DFT with the local density approximation. The relationship between the strain and  $I_{on}/I_{off}$  ratio of various TMD MOSFETs is shown in Fig. 17. The device metrics of the MoS<sub>2</sub> MOSFET models of various channel lengths are compared with the first-principle calculations from Ref. [100], as shown in Table 1. Although the device metrics do not fit exactly to the results from the first-principle calculations, the overall trends for the first-principle calculations and ToB transistor model data are consistent. This further confirms that TMDs offer great opportunities in further nanoelectronic applications. However, the fabrication of these devices is still in the infancy stage [33].

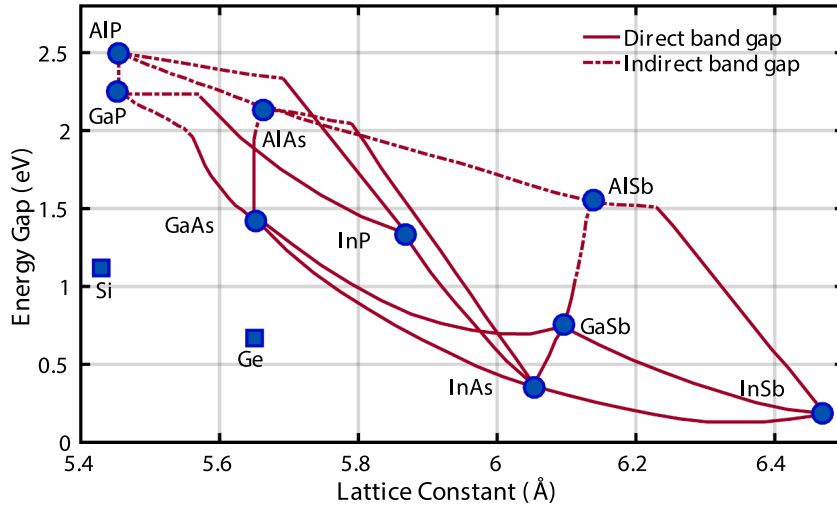


Fig. 19. The band gap and wavelength versus the lattice constant for common III-V compound semiconductors [101].

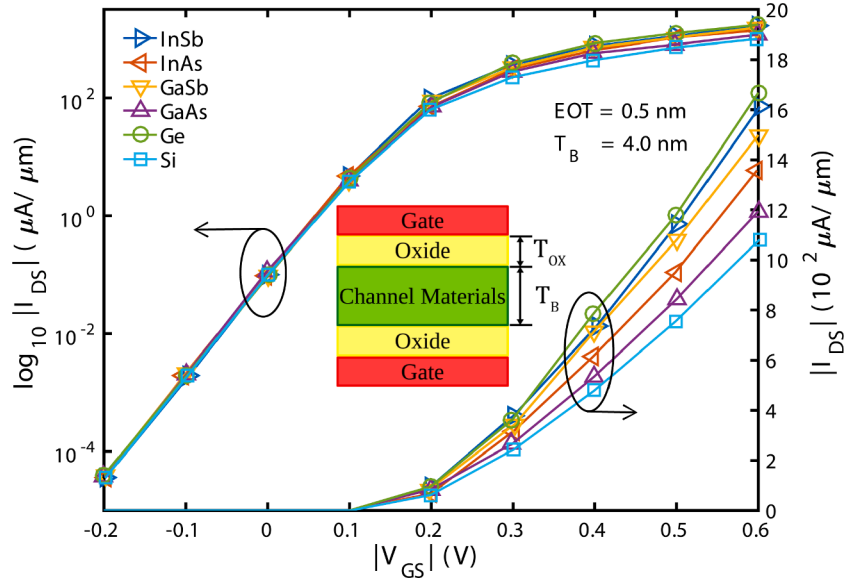


Fig. 20. The I-V transfer characteristics of ultra-thin-body (UTB) p-channel MOSFETs with various group IV and III-V conducting channels within the ballistic transport regime [108].

Lam et al. [91] investigated the n-channel and p-channel monolayer black phosphorene (BP) FETs in both the x- and y-directions, as shown in Fig. 18(a) and (b). The atomic structure of BP was modelled using DFT implemented in Vienna Ab initio Simulation Package (VASP). The results for the monolayer BP FET are plotted in Fig. 18(c). It can be observed that the monolayer BP in the x-direction (or “armchair” edge) exhibits a higher on-current than that in the y-direction (or “zigzag” edge) due to a higher DOS and higher injection velocity. Moreover, they concluded that the proposed BP FET models outperformed both the n-channel and p-channel FETs with MoS<sub>2</sub> and Si as the conducting channels.

### 3.4. III-V compound semiconductors

The III-V compound semiconductors have been applied in different devices according to their energy gap, as shown in Fig. 19. The compound semiconductors shown in Fig. 19 include aluminium phosphide (AlP), aluminium arsenide (AlAs), gallium phosphide (GaP), gallium arsenide (GaAs), indium gallium arsenide (InGaAs), indium phosphide (InP), aluminium antimonide (AlSb), gallium antimonide (GaSb), indium arsenide (InAs), and indium antimonide (InSb). The common types of transistors using these materials are high-electron-mobility transistors (HEMTs) and heterojunction bipolar transistors (HBTs) [101]. The ToB transistor model has also

**Table 2**

The benchmarks of the ToB transistor model based on the RMSD calculations.

Ref.	Research group	Benchmark	Material	RMSD
[44]	Rahman et al.	NanoMos Simulator [72]	Bulk Si	0.16 %
[69]	Chin et al.	Experiment [74]	SiNW	0.93 %
[66]	Kazmierski et al.	Experiment [90]	CNT	0.19 %

**Table 3**

Performance of the ToB transistor model for different materials.

Ref.	Device parameters (refer to Fig. 2)				Device metrics			
	Channel material	$t_{ox}(nm)$	$L_G(nm)$	$t_{CH}(nm)$	$V_i(V)$	SS (mV/dec)	DIBL (mV/V)	$I_{on}/I_{off}$ ratio
[69]	SiNW	2.5	10.0	16.0	–	88.8	88.7	$1.0 \times 10^4$
[78]	GNR	1.5	10.0	–	–	–	–	$\sim 3.0 \times 10^4$
[81]	GNR	1.5	10.0	–	0.40	$\sim 83.9$	$\sim 51.1$	$\sim 4.5 \times 10^4$
[82]	3SVs GNR	1.0	15.0	–	–	147.0	53.0	–
[87]	CNT	1.1	60.0	1.5	–	74.4	39.4	$9.2 \times 10^3$
[91]	Phosphorene	3.0	20.0	–	0.20	–	–	$\sim 1.0 \times 10^4$
[96]	MoS <sub>2</sub>	3.0	10.0	–	0.50	67.0	–	$4.7 \times 10^7$
[108]	GaAs	0.5	10.0	4.0	0.23	–	–	$\sim 9.0 \times 10^3$
[108]	GaSb	0.5	10.0	4.0	0.21	–	–	$\sim 11.0 \times 10^3$
[108]	InAs	0.5	10.0	4.0	0.24	–	–	$\sim 10.0 \times 10^3$
[108]	InSb	0.5	10.0	4.0	0.22	–	–	$\sim 12.0 \times 10^3$

been used to simulate various transistors [102–108] with III-V compound semiconductors as the conducting channels.

The ToB transistor model was applied to simulate ultra-thin-body (UTB) III-V p-channel MOSFETs by Chang et al. [108]. They obtained the valence band structures for all the materials using the  $k \cdot p$  method. They solved the eight-band strain-dependent  $k \cdot p$  Schrödinger and Poisson equations self-consistently. Via the simulation, they found that the effective oxide thickness (EOT) for the classical capacitance limits is 0.5 nm, and the I–V transfer characteristics are essentially affected by the transport effective masses of the conducting channels. The transport effective masses depend on several factors such as the type of materials, transport directions, and strain effects. Their results also showed that the on-current is enhanced by the lower transport effective mass. The I–V transfer characteristics within the ballistic transport regime of various p-channel MOSFETs with group IV and III-V conducting channels (with a body thickness of 4 nm, EOT of 0.5 nm, and drain bias of  $-0.5$  V) are shown in Fig. 20.

#### 4. Model comparison

We can observe from Section 3 that the ToB transistor model has been applied to simulate various low-dimensional materials at the device level including UTB bulk materials, 2D materials, and one-dimensional (1D) materials. Table 2 summarises the RMSD calculations from the simulation results obtained by Rahman et al. [44], Chin et al. [69], and Kazmierski et al. [66], as depicted in Figs. 7(b), 9(b) and 14(b), respectively. The ToB transistor models produce a higher normalised RMSD percentage when they are benchmarked with the experimental data. Overall, the RMSD percentage is close to zero. Thus, this indicates that the ToB transistor model can produce accurate results. In addition, this model is simple and easy to use because it requires the user to specify only the DOS of the semiconductor either analytically or by a numerical table. The DOS can be derived from the band structure of a semiconductor using various nanotechnology computational modelling approaches such as the ab initio, semi-empirical, and atomistic methods [109].

The device metrics of the ToB transistor models with various channel materials are summarised in Table 3. The  $t_{CH}$  parameter represents the channel thickness for the bulk materials and nanowire diameter of the nanowire materials. Furthermore,  $t_{CH}$  is not available for all monolayer 2D materials. The device metrics were extracted from the published models, and all unavailable data are marked with a dash (–). From Table 3, we can observe that most of the published works have computed the  $I_{on}/I_{off}$  ratio to evaluate the performance of the FET models. It is recommended that the other device metrics should also be extracted to obtain further insights on the performance of the FETs.

Among all the materials summarised in Table 3, MoS<sub>2</sub> with a gate length of 10 nm exhibits the highest  $I_{on}/I_{off}$  ratio up to the order of 7 (from Ref. [96]), while GaAs UTB with a gate length of 10 nm exhibits the lowest  $I_{on}/I_{off}$  ratio only up to  $9.0 \times 10^3$ . In contrast, opportunities remain for applying the ToB transistor model to other graphene-like 2D materials such as silicene [4] and boron nitride [110,111], because there is a minimal amount of similar work available in the literature. In term of the SS (the typical value is  $\geq 60$  mV/dec [112]), MoS<sub>2</sub> FET performs better than SiNW, GNR, and CNT FETs.

## 5. Conclusion

The demand for low-dimensional materials is rapidly growing, particularly in the semiconductor industry where transistor sizes are in the sub-10 nm regime. In summary, an overview of the ToB transistor model and its applications were reviewed in this paper. The ToB transistor model is simple and easy to use. We showed that the model is relatively accurate via RMSD calculations. In addition, the model shows good agreement with the data from the theoretical simulations and experimental measurements. The ToB transistor model, which incorporates various low-dimensional channel materials, was also summarised and discussed. The modelling and simulation of low-dimensional electronic devices for nanoelectronic applications is important to predict their performance and understand the essential physics behind the devices. The results from the device level models can be further explored and applied in circuit-level simulation.

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