# Application of Classification Models for Predicting Shooting Performance in the NBA

A Case Study of Kobe Bryant

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## Abstract

In a world with continuously increasing techological capabilities, the demand for answers increases alongside it. The domain of professional sports in particular is no exception to this trend. The very essence of competitive sports is rooted in a desire to optimize and gain every advantage over competitors. In this paper, we describe classification methodologies for predicting the performance of professional athletes through a scoped analysis of the long-time NBA allstar, Kobe Bryant. We detail three simulations modelling shooting accuracy over Bryant's 20 year career, using logistic regression and discriminant analyses to yield predictions about Bryant's theoretical future performance. We show that Bryant's potential to score is strongly dependent on his distance from the basket when shooting. We also show that Bryant's scoring performance in the post-season, as compared to that of the regular season, is consistent with his performance at any other point in the season.

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### 1 Introduction

With modern computers and the popularity of the budding disciple of data science, there are numerous predictive technologies readily available. In professionl sports alone, a host of disparate entities, players, ogranizations, and gamblers alike are hungry for new insights. Each bears an economic imperative to seek advantages and optimizations that will give them an edge over their peers. Technology, however, does not predicate useful and effective models. It is the rigorous application of sound statistical theory that yields actionable conclusions. Unfortunately, the appeal of novel algorithms and the sparkles of big data detract from the importance of a strong statistical foundation. Thus, we seek to right the ship of this rampant malpractice as it applies to this problem domain. In what follows, we explore insights we have garnered from the application of linear discriminant analysis and logistic regression, then leveraging those insights to appropriately tune the final predictive model.

Kobe Bryant marked his retirement from basketball by scoring 60 points in his final game as a member of the Los Angeles Lakers team on Wednesday, April 13, 2016. Starting to play professional basketball at the age of 17, Kobe earned the sport's highest accolades throughout his long career. Using 20 years of data on Kobe's shots made and shots missed, we wish to predict which shots will be successful.

## 2 Approach

#### 2.1 Problem Definition

Sports analytics is, as many previously low-tech markets are, poised to boom as sports organizations are increasingly able to generate more data. Recent research

"The Sports Analytics market is expected to grow from USD 123.7 Million in 2016 to USD 616.7 Million by 2021, at a Compound Annual Growth Rate (CAGR) of 37.9

The increasing volume of on-field and off-field data generated among various sports organizations has led to an increase in managing these data to analyze them. This need is driving the adoption of sports analytics solutions. Analytics and big data technologies have found huge potential in various industries, including sports. The increasing demand of coaches, mentors, and other management officials for real-time access to the insights of relevant information presents huge potential for sports analytics market. The demand for cloud-based sports analytics solutions is also expected to increase due to the lack of budget allocation for hiring technical skills and experts to analyze data for sports organization. These are some of the major factors expected to augment the growth of the market. Moreover, in order to remain competitive, organizations are adopting sports analytics solutions."

[1]

This study was birthed out of a need to reliably quantify three key metrics specifically, each used in assessing a professional basketball player's shooting ability. Those metris are:

- 1. Odds of making a shot as distance from the basket increases.
- 2. Linearity of the decline rate of the probability of making a shot with respect to the distance the shot was taken from the basket.

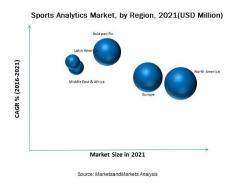


Figure 1: Market Analysis

3. The relationship between the distance from the shooter to the basket and the odds of the shot being made is different when in the regular season verses the post-season.

Rephrasing those metrics as questions helps clarify the focus of the analysis as it relates to Kobe Bryant. Those questions are as follows:

- 1. Do the odds of Kobe making a shot decrease with respect to distance he is from the hoop?
- 2. Does the probability of Kobe making a shot descrease linearly with respect to the distance he is from the hoop?
- 3. Is the relationship between the distance Kobe is from the basket and the odds of him making the shot different if they are in the playoffs.

To appropriately answer the questions of interest above, we must fit a series of classifier models to the training portion of our dataset, iteratively scoring and comparing the various models against one another so that we can tune their parameters and hone in on a final feature set.

The entirity of the analysis is implemented side-by-side in Python and SAS. Below, we set the stage for conducting our analysis through an exploratory analysis of the dataset.

#### 2.2 Exploratory Analysis

#### 2.2.1 Data Overview

The NBA has provided a comprehensive dataset of every shot Kobe Bryant took throughtout his career. Accompanying each shot record are a number of supplemen-

tary features that provide context to the positioning and environment in which a given shot was taken. Generally, the data was remarkably clean and readily manipulable. The majority of the wrangling effort was focused on synthesizing new predictors. A brief summary of the features is below.

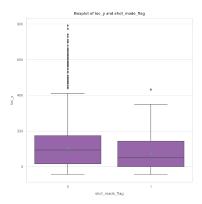
	count	mean	std	min	25%	50%	75%	max
game_event_id	25697	249	150	2	111	253	367	653
game_id	25697	24741091	7738108	20000012	20500064	20900337	29600270	49900088
lat	25697	34	0	33	34	34	34	34
loc_x	25697	7	110	-250	-67	0	94	248
$loc\_y$	25697	91	88	-44	4	74	160	791
lon	25697	-118	0	-119	-118	-118	-118	-118
minutes_remaining	25697	5	3	0	2	5	8	11
period	25697	3	1	1	1	3	3	7
playoffs	25697	0	0	0	0	0	0	1
seconds_remaining	25697	28	18	0	13	28	43	59
shot_distance	25697	13	9	0	5	15	21	79
$shot\_made\_flag$	25697	0	0	0	0	0	1	1
team_id	25697	1610612747	0	1610612747	1610612747	1610612747	1610612747	1610612747
$\operatorname{shot}_{\operatorname{\underline{\hspace{1pt}-id}}}\operatorname{id}$	25697	15328	8860	2	7646	15336	22976	30697
attendance	25697	15041	1076	11065	14314	15048	15738	20845
arena_temp	25697	70	2	64	69	70	71	79
avgnoisedb	25697	95	2	89	93	95	96	102

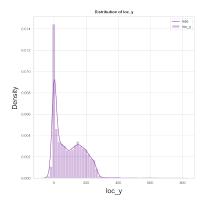
Table 1: Feature Summary

Table 2: Key Feature Descriptions

$Game\_event\_id$	Identification variable			
$Game\_id$	Identification variable			
Lat and loc y	Appear to be the same data (y-axis), based on location on the court.			
Lat and loc_y	The tall bar indicates the frequency of shots taken at the location near the basket			
Loc x and lon	Appear to be the same data (x-axis), based on location on the court.			
Loc_x and ion	The tall bar indicates the frequency of shots taken at the location near the basket			
Minutes remaining	Suggests that there is evidence that Kobe took more shots as the period			
Minutes_remaining	progressed (higher shot counts closer to the end of the period)			
Period	Indicates similar shot frequency across periods			
Playoffs	Playoffs were a rare event in the season, hence the lower shot frequency overall			
Season	Shot frequency was lower in 2 seasons			
	Suggests that there is evidence that Kobe took more shots in the final seconds			
Seconds_remaining	(higher shot counts closer to the end of the last minute in the period, correlates			
	with shot frequency in the minutes_remaining variable above)			
	High shot frequency at the basket, at the top of the key (field goals),			
Shot_distance	and the three-point line. Shot frequency was comparatively rarer			
	beyond the three-point line			

From the available features, the variable "shot\_made\_flag" indicates whether a particular shot was made (1) or missed (0), and is the feature that acts as our endogenous variable. The remainder of the features are the potential predictors, or





- (a) Boxplot of Shot Y Location
- (b) Distplot of Shot Y Location

Figure 2: Plots of y loc

exogenous variables. Since there are a managable number of them, we can simply generate descriptive plots for each exogenous feature. Univariate distribution or frequency plots are ideal for vizualizing the underlying distristribution of each variable. In addition, boxplots for each exogenous feature against each level of the endogenous variable allowed us to develop our intuition about the variance within each level of the target feature.

Most of the features show no signs of skewness or severe departures from normality, however, there are some exceptions.

It's clear that outliers are prevalent in some of the features, particularly those representing the distance to the hoop and the time remaining, as represented in figures 2b and 2a. Several solutions were explored to mitigate the potential impact of the outliers, none of which yielded a model with better results. Thus, all outliers were included in the final models on their original scale.

The exploratory boxplot of shot\_distance (figure 3) already hints at a potential relationship between a shot's likelyhood of being made verses the distance the shot was taken from the hoop.

#### 2.2.2 Multicollinearity

The base feature set was wrought with violations of independent variability. As noted in the table and it's accompanying correlation matrix, approximately half of the features showed a collinear relationship with other features in the data set. This caused our approach to feature selection vary from the normal methods. We chose to ignore the more nuanced stepwise / LASSO / LarsCV methods and

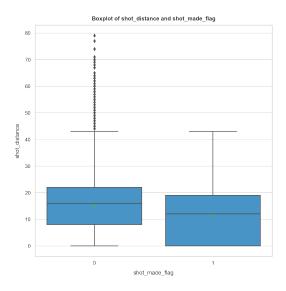


Figure 3: Boxplot of Shot Distance

instead implemented a procedure to recursively drop a feature with an exorbitant variance inflation factor on each iteration until reaching a feature set that showed no multicollinearity violations. We used an elimination cutoff of the initial median VIF + 2 standard deviations. Variance inflation factors for the original features can be seen in table 3. A correlation matrix of the same feature set is displayed in figure 4.

VIF Factor features 1  $35 \quad {\rm game\_event\_id}$ 2  $68 \quad {\rm game\_id}$ 3 inf lat 4  $\inf - loc\_x$ inf loc\_y 5 6 inf lon 7 inf minutes remaining 8 inf period 9 29 playoffs 10  $\inf \quad seconds\_remaining$ 11 3 shot\_distance 12 0 team id 14 shot\_id 13

**Table 3:** Variance Inflation Factors

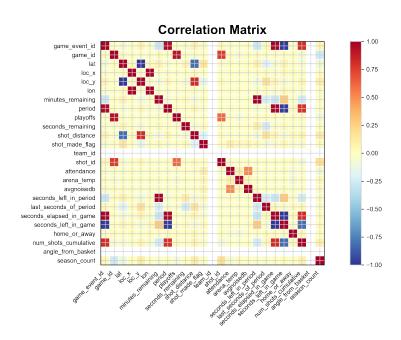


Figure 4: Correlation Matrix - All features

## 3 Methodoloy

#### 3.1 Feature Selection

As mentioned in the previous section, the feature selection process was dominated by the prevalent mulicollinearity between many of the features. As example, collinearity was reduced to a tolerable range in the featureset of one candidate model pictured in figure 5.

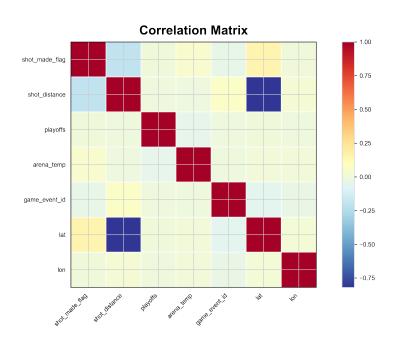


Figure 5: Correlation Matrix - Candidate Model

#### 3.2 Model Selection

Our key observation during model selection arose in differentiating the preformance of Fisher's linear discriminant and binary logistic regression. While both procedures are common choices for two-level classification, and often yield similar results, there as few critical assumptions that differ between them. The linear discriminant analysis (LDA) mandates the within-group covariance between each level of the endogenous variable be equal. Additionally, the LDA model is susceptible to the influence of extreme observations, and will potentially yield inconsistent results when outliers are not accounted for. Conversely, the logarithmic analysis has no exigence on the form of the model's predictors. The prevalence of outliers in the dataset, exposed during the exploratory analysis, was sufficient enough cause to move forward with the logistic regression as a conservative base on which we could build our predictions. Beta models using LDA can be found in the appendix (5.2).

Several iterations of model selection concluded on a final model that yielded a 0.615 AUC, with exceptional sensitivity (true positive rate) and moderate specificity (true negative rate). (table 4). Categorical predictors in the final model were substituted for dummied predictors for estimate. (See regression formula - 4)

#### Model 5 Log Loss 0.6664

AUC 0.6155 Sensitivity 0.744 Specificity 0.425

Table 4: Logistic Model Summary

$$Logit(\frac{\pi}{1-\pi}) = \beta_0 + \beta_1 \text{shot\_distance} + \beta_2 \text{playoffs}_0 + \beta_3 \text{playoffs}_1 + \beta_4 \text{arena\_temp} + \beta_5 \text{game\_event\_id} + \beta_6 \text{lat} + \beta_7 \text{lon}$$

$$\text{Regular Season (playoffs} = 0)$$

$$= \beta_0 + \beta_1 \text{shot\_distance} + \beta_2(1) + \beta_3(0) + \beta_4 \text{arena\_temp} + \beta_5 \text{game\_event\_id} + \beta_6 \text{lat} + \beta_7 \text{lon}$$

$$= \beta_0 + \beta_1 \text{shot\_distance} + \beta_2 + \beta_4 \text{arena\_temp} + \beta_5 \text{game\_event\_id} + \beta_6 \text{lat} + \beta_7 \text{lon}$$

$$Logit(\frac{\pi}{1-\pi}) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_4 x_4 + \beta_5 x_5 + \beta_6 x_6 + \beta_7 x_7$$

$$\text{Playoffs (playoffs} = 1)$$

$$= \beta_0 + \beta_1 \text{shot\_distance} + \beta_2(0) + \beta_3(1) + \beta_4 \text{arena\_temp} + \beta_5 \text{game\_event\_id} + \beta_6 \text{lat} + \beta_7 \text{lon}$$

$$= \beta_0 + \beta_1 \text{shot\_distance} + \beta_3 + \beta_4 \text{arena\_temp} + \beta_5 \text{game\_event\_id} + \beta_6 \text{lat} + \beta_7 \text{lon}$$

$$Logit(\frac{\pi}{1-\pi}) = \beta_0 + \beta_1 x_1 + \beta_3 x_3 + \beta_4 x_4 + \beta_5 x_5 + \beta_6 x_6 + \beta_7 x_7$$

$$Logit(\frac{\pi}{1-\pi}) = \beta_0 + \beta_1 x_1 + \beta_3 x_3 + \beta_4 x_4 + \beta_5 x_5 + \beta_6 x_6 + \beta_7 x_7$$

A model composition chart, displayed in figure 6 shows the features selected in the champion model, along with the model's confusion matrix.

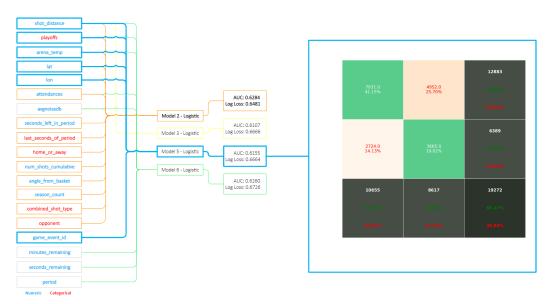


Figure 6: Model Composition Chart

[2]

A full listing of candidate models can be seen in the appendix (5.2).

#### 3.3 Evaluation

Goodness of fit measured by logarithmic loss function, where:

$$LogLoss = -(y log(p) + (1 - y) log(1 - p))$$

Logarithmic loss (related to cross-entropy) measures the performance of a classification model where the prediction input is a probability value between 0 and 1. Log Loss takes into account the uncertainty of a prediction based on how much it varies from the actual label, insead of simply counting if the predicted value exactly equals the true value, as is the case with accuracy. This gave us a more nuanced view into the performance of our model.

## 4 Conclusion

Finally, now that we've demonstrated the process of applying binary classification techniques to NBA shooting data, we can return to the original questions of interest. Our findings show a  $-1.87\%\pm0.85\%$  (-2.72%, -1.01%) step change in Kobe Bryant's shot making ability, measured with a p-value of < 0.001 at  $\alpha = 0.05$  (figure 7). That is to say, for every additional foot between Bryant and the basket, his accuracy is reduced by just under 2%. Another, perhaps more familiar way to put it is in terms of odds. Kobe's odds of making a basket are

$$0.9813 \pm 0.0084 \ (0.9728, 0.9899)$$

with respect to his distance from the basket.

Additionally, the model indicates a  $4.25\% \pm 9.9\% \ (-4.77\%, 14.15\%)$  increase in shooting ability

during the playoffs, however, the result was not statistically significant, with a p-value of 0.3671 at an  $\alpha of 0.05 on the \chi^2 distribution. There is not sufficient evidence to reject the null hypothesis. Figure tables of Log-odds, odds, and percentage change in shooting ability with respect to distance:$ 

		Coef.	Std.Err.	Z	P> z	[0.025	0.975]
	lat	0	0	-2	0	0	0
	lon	0	0	-0	1	0	153130194710622
	playoffs	71	0	1	0	0	1400174
	seconds_remaining	1	0	2	0	1	1
	shot_distance	0	0	-4	0	0	0
	attendance	1	0	10	0	1	1
Log-Odds:	arena_temp	28	0	4	0	6	133
	avgnoisedb	1	0	0	1	0	6
	$seconds\_left\_in\_period$	1	0	1	0	1	1
	$last\_seconds\_of\_period$	0	0	-7	0	0	0
	$seconds\_left\_in\_game$	1	0	2	0	1	1
	home_or_away	0	0	-1	0	0	32
	$num\_shots\_cumulative$	1	0	0	1	0	2
	$angle\_from\_basket$	1	0	0	1	1	1
	season_count	3	0	3	0	1	5

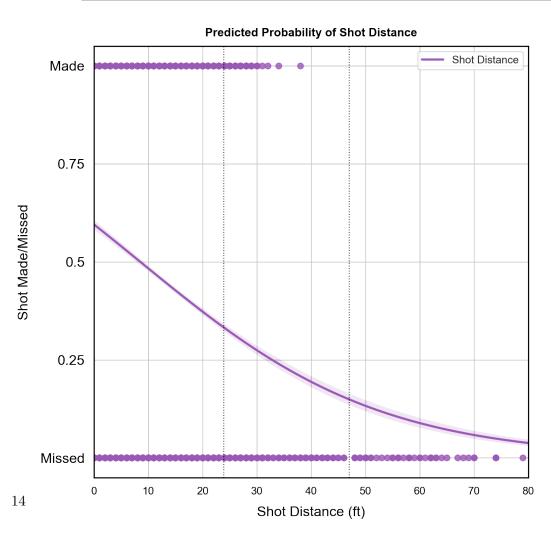


Figure 7: Predicted Shot Probability over Distance to Hoop

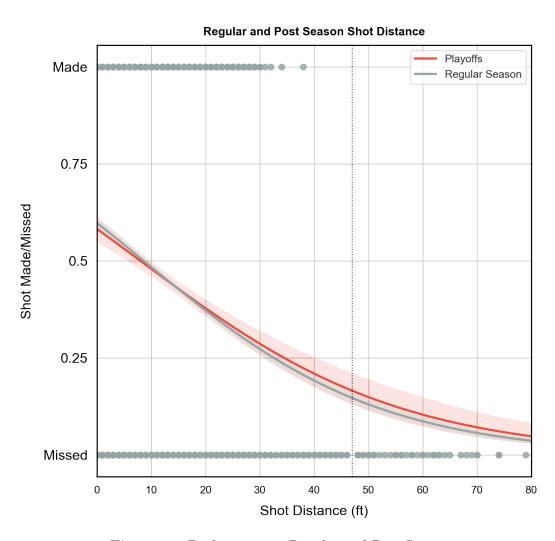


Figure 8: Performance in Regular and Post Season

·		Coef.	Std.Err.	$\mathbf{z}$	P> z	[0.025	0.975]
	lat	0	0	-2	0	0	0
	lon	0	0	-0	1	0	153130194710622
	playoffs	71	0	1	0	0	1400174
	seconds_remaining	1	0	2	0	1	1
	shot_distance	0	0	-4	0	0	0
	attendance	1	0	10	0	1	1
Odds:	arena_temp	28	0	4	0	6	133
	avgnoisedb	1	0	0	1	0	6
	$seconds\_left\_in\_period$	1	0	1	0	1	1
	$last\_seconds\_of\_period$	0	0	-7	0	0	0
	$seconds\_left\_in\_game$	1	0	2	0	1	1
	home_or_away	0	0	-1	0	0	32
	$num\_shots\_cumulative$	1	0	0	1	0	2
	$angle\_from\_basket$	1	0	0	1	1	1
	season_count	3	0	3	0	1	5

 Table 6: Odds with Respect to Distance

Percent Change:

	Coef.	[0.025	0.975]
lat	-100	-100	-99
lon	-99	-100	15313019471062054
playoffs	6978	-99	140017285
seconds_remaining	15	-3	37
shot_distance	-85	-93	-64
attendance	2	1	2
arena_temp	2699	505	13151
avgnoisedb	28	-72	499
$seconds\_left\_in\_period$	1	-1	2
last_seconds_of_period	-100	-100	-100
$seconds\_left\_in\_game$	1	0	1
home_or_away	-92	-100	3078
num_shots_cumulative	5	-53	140
$angle\_from\_basket$	2	-6	10
season_count	154	31	394

 ${\bf Table~7:~Percent~Change~over~Distance}$ 

# 5 Appendix

#### 5.1 Github Repository

We are on Github! (https://github.com/la-mar/Applied-Stats-Project-2)

#### 5.2 Appendix A

#### 5.2.1 Model Comparison - Continued

	Model 2	Model 3	Model 4A	Model 4B	Model 5	Model 6
	LOGIT w/PCA	LOGIT w/shot_distance	LOGIT w/shot_distance, (playoffs)	LOGIT w/shot_distance, (no playoffs)	LOGIT w/selected varsA	LOGIT w/selected varsB
R-Square	0.0498	0.0393	0.0328	0.0405	0.042	0.05
Max-rescaled R-Square	0.0666	0.0526	0.0439	0.0542	0.0562	0.0669
AIC	34035.67	34298.864	5042.4	29258.947	34237.279	34024.718
SC	34125.365	34315.172	5054.863	29274.939	34294.358	34098.106
-2 Log L	34013.67	34294.864	5038.4	29254.947	34223.279	34006.718
Area Under ROC Curve	0.6262	0.6107	0.6008	0.6124	0.6155	0.626
Log Loss		0.66666			0.6664	0.67267

#### 5.2.2 Data Dictionary

#### 5.3 SAS Code

```
9  delimiter=',';
10  getnames=yes;
11 n;
12
13  print data */
14 oc print data=train (obs=10);
```

	Model 1	
	GLM w/PCA	
Root MSE	0.48463	
Dependent Mean	0.44616	
R-Square	0.0498	
Adj R-Sq	0.0495	
AIC	-11521	
AICC	-11521	
SBC	-37155	
CV PRESS	6037.80515	

```
15 n;
17 investigate data for variable types*/
18 oc contents data=train;
19 n;
20
_{21} look for missing numeric data - may need to impute */
22 oc means data = train n nmiss;
23 var _numeric_;
24 n;
25
_{26} investigate means of training data and any missing values */
27 oc means data = train n nmiss;
29
30 univariate data analysis */
31 oc univariate data = train;
32 r season;
33 n;
35 note that certain "season" fields are missing */
36 ta _season;
  set train;
37
    where missing (season);
```

	Model 7
	LDA
Sensitivity (classified 1 when really 1)	0.4298
Specificity (classified 0 when really 0)	0.744
Type I Error (classified 1 when really 0)	0.256
Type II Error (classified 0 when really 1)	0.5702
Total Error	0.3962
Accuracy (1-Total Error)	0.6038

```
39 n;
_{41} print "season" data, where "season" is missing */
42 oc print data=_season (obs=200);
43 n;
44
45
46 more univariate data analysis */
47 s graphics on;
48 oc univariate data = train plot;
_{49} r recId
50 me_event_id
51 \text{ me\_id}
52 t
53 C_X
54 C_y
55 n
56 nutes_remaining
57 riod
58 ayoffs
59 ason
60 conds_remaining
61 ot_distance
62 ot_made_flag
63 am_id
64 me_date
65 ot_id
66 tendance
67 ena_temp
68 gnoisedb
69
70 n;
71 s graphics off;
72
```

```
73 create a time-based variable, concatenating Period, minutes
   → remaining, and seconds remaining, in descending order. This one
   → is for Periods remaining... */
74 ta train2;
75 set train;
      if period = 1 then periods_remaining2 = "14";
76
      else if period = 2 then periods_remaining2 = "28";
   else if period = 3 then periods_remaining2 = "42";
   else if period = 4 then periods_remaining2 = "57";
   else if period = 5 then periods_remaining2 = "71";
   else if period = 6 then periods_remaining2 = "85";
   else if period = 7 then periods_remaining2 = "99";
   else periods_remaining2 = period;
85
86 print data */
87 oc print data=train2 (obs=10);
88 n:
89
   Minutes remaining... */
91 ta train2;
92 set train2;
      if minutes_remaining = 11 then minutes_remaining2 = "99";
93
      else if minutes_remaining = 10 then minutes_remaining2 = "90";
   else if minutes_remaining = 9 then minutes_remaining2 = "81";
   else if minutes_remaining = 8 then minutes_remaining2 = "72";
   else if minutes_remaining = 7 then minutes_remaining2 = "63";
   else if minutes_remaining = 6 then minutes_remaining2 = "54";
   else if minutes_remaining = 5 then minutes_remaining2 = "45";
   else if minutes_remaining = 4 then minutes_remaining2 = "36";
100
   else if minutes_remaining = 3 then minutes_remaining2 = "27";
101
   else if minutes_remaining = 2 then minutes_remaining2 = "18";
102
   else if minutes_remaining = 1 then minutes_remaining2 = "09";
   else if minutes_remaining = 0 then minutes_remaining2 = "00";
   else minutes_remaining2 = minutes_remaining;
105
106 n:
```

```
107
   print data */
108
109 oc print data=train2 (obs=10);
110 n;
111
   Seconds remaining... */
112
113 ta train2;
114 set train2;
       if seconds_remaining = 59 then seconds_remaining2 = "99";
115
       else if seconds_remaining = 58 then seconds_remaining2 = "97.3";
116
    else if seconds_remaining = 57 then seconds_remaining2 = "95.6";
117
    else if seconds_remaining = 56 then seconds_remaining2 = "94";
118
    else if seconds_remaining = 55 then seconds_remaining2 = "92.3";
119
    else if seconds_remaining = 54 then seconds_remaining2 = "90.6";
120
    else if seconds_remaining = 53 then seconds_remaining2 = "88.9";
121
    else if seconds_remaining = 52 then seconds_remaining2 = "87.3";
122
    else if seconds_remaining = 51 then seconds_remaining2 = "85.6";
123
    else if seconds remaining = 50 then seconds remaining2 = "83.9";
124
    else if seconds_remaining = 49 then seconds_remaining2 = "82.2";
125
    else if seconds_remaining = 48 then seconds_remaining2 = "80.5";
126
       else if seconds_remaining = 47 then seconds_remaining2 = "78.9";
127
    else if seconds_remaining = 46 then seconds_remaining2 = "77.2";
128
    else if seconds_remaining = 45 then seconds_remaining2 = "75.5";
129
    else if seconds_remaining = 44 then seconds_remaining2 = "73.8";
130
    else if seconds_remaining = 43 then seconds_remaining2 = "72.2";
131
    else if seconds_remaining = 42 then seconds_remaining2 = "70.5";
132
    else if seconds_remaining = 41 then seconds_remaining2 = "68.8";
133
    else if seconds_remaining = 40 then seconds_remaining2 = "67.1";
134
    else if seconds_remaining = 39 then seconds_remaining2 = "65.4";
135
   else if seconds_remaining = 38 then seconds_remaining2 = "63.8";
136
    else if seconds_remaining = 37 then seconds_remaining2 = "62.1";
137
    else if seconds_remaining = 36 then seconds_remaining2 = "60.4";
138
    else if seconds_remaining = 35 then seconds_remaining2 = "58.7";
   else if seconds_remaining = 34 then seconds_remaining2 = "57.1";
140
    else if seconds_remaining = 33 then seconds_remaining2 = "55.4";
141
   else if seconds_remaining = 32 then seconds_remaining2 = "53.7";
```

```
else if seconds_remaining = 31 then seconds_remaining2 = "52";
143
    else if seconds remaining = 30 then seconds_remaining2 = "50.3";
144
    else if seconds_remaining = 29 then seconds_remaining2 = "48.7";
145
      else if seconds_remaining = 28 then seconds_remaining2 = "47";
146
   else if seconds_remaining = 27 then seconds_remaining2 = "45.3";
147
   else if seconds_remaining = 26 then seconds_remaining2 = "43.6";
148
    else if seconds_remaining = 25 then seconds_remaining2 = "41.9";
149
   else if seconds_remaining = 24 then seconds_remaining2 = "40.3";
150
    else if seconds_remaining = 23 then seconds_remaining2 = "38.6";
   else if seconds_remaining = 22 then seconds_remaining2 = "36.9";
152
   else if seconds_remaining = 21 then seconds_remaining2 = "35.2";
153
   else if seconds remaining = 20 then seconds remaining2 = "33.6";
154
   else if seconds_remaining = 19 then seconds_remaining2 = "31.9";
155
   else if seconds remaining = 18 then seconds remaining2 = "30.2";
156
    else if seconds_remaining = 17 then seconds_remaining2 = "28.5";
   else if seconds_remaining = 16 then seconds_remaining2 = "26.8";
158
   else if seconds_remaining = 15 then seconds_remaining2 = "25.2";
159
   else if seconds_remaining = 14 then seconds_remaining2 = "23.5";
160
   else if seconds_remaining = 13 then seconds_remaining2 = "21.8";
161
    else if seconds remaining = 12 then seconds_remaining2 = "20.1";
162
   else if seconds_remaining = 11 then seconds_remaining2 = "18.5";
163
   else if seconds_remaining = 10 then seconds_remaining2 = "16.8";
164
   else if seconds_remaining = 9 then seconds_remaining2 = "15.1";
165
      else if seconds_remaining = 8 then seconds_remaining2 = "13.4";
166
   else if seconds_remaining = 7 then seconds_remaining2 = "11.7";
167
   else if seconds_remaining = 6 then seconds_remaining2 = "10.1";
168
   else if seconds_remaining = 5 then seconds_remaining2 = "08.4";
   else if seconds_remaining = 4 then seconds_remaining2 = "06.7";
170
   else if seconds_remaining = 3 then seconds_remaining2 = "05";
171
   else if seconds_remaining = 2 then seconds_remaining2 = "03.4";
172
   else if seconds_remaining = 1 then seconds_remaining2 = "01.7";
173
   else if seconds_remaining = 0 then seconds_remaining2 = "00";
  se seconds_remaining2 = seconds_remaining;
176 n;
177
   print data */
178
```

```
179 oc print data=train2 (obs=10);
180 n;
181
182 concatenante data */
183 ta train2;
184 t train2;
185 s_remaining = cat(periods_remaining2, minutes_remaining2,

    seconds_remaining2);
186 n;
187
188 print data */
189 oc print data=train2 (obs=10);
190 n;
191
192 make field numeric (some components contained leading zeroes */
193 ta train2;
194 t train2;
195  n_pms_remaining = input(pms_remaining,8.);
196 n;
198 drop original non-numeric concetenanted data field */
199 ta train2;
200 t train2 (drop = pms_remaining);
201 n;
202 ta train2;
203
204 rename new numeric concatenated data field */
205 t train2 (rename=(
206 _pms_remaining'n='pms_remaining'n));
207 n;
208
209 print data */
210 oc print data=train2 (obs=10);
211 n;
212
213
```

```
214
215
216
217 check data - histogram */
218 s graphics on;
219 oc univariate data = train2;
220 r pms_remaining;
221 stogram;
222 n;
223 s graphics off;
224
   check data - scatter plot */
225
226 oc sgplot data=train2;
    scatter x=pms_remaining y=shot_made_flag / group=shot_made_flag;
228 n;
229
230
231
   transform data - log transformation on shot distance and time

→ remaining */

233 ta train3;
234 t train2;
235 shot_distance = log(shot_distance);
236 pms_remaining = log(pms_remaining);
237 n;
238
239
240 check data - scatter plot */
241 s graphics on;
242 oc univariate data = train3 plot;
243 r l_shot_distance l_pms_remaining;
245 s graphics off;
^{246}
247
248
```

```
249
250 correlation analysis */
251 s graphics on;
252 oc corr data=train2 plots=matrix(histogram);
_{253} r recId
254 me_event_id
_{255} me_id
256 t
257 C_X
258 C_y
259 n
_{260} nutes_remaining
_{261} riod
262 ayoffs
263 ason
264 conds_remaining
_{265} ot_distance
_{266} ot_made_flag
_{267} am_id
268 me_date
_{269} ot_id
270 tendance
271 ena_temp
272 gnoisedb;
273 n;
274 s graphics off;
275
276
277
278 principal component analysis */
279 s graphics on;
280 oc princomp plots=all data=train2 cov out=pca;
_{281} r recId
282 me_event_id
_{283} me_id
284 t
```

```
285 C_X
286 C_Y
287 n
288 nutes_remaining
289 riod
290 ayoffs
291 ason
292 conds_remaining
293 ot_distance
294 ot_made_flag
295 am_id
296 me_date
297 ot_id
298 tendance
299 ena_temp
300 gnoisedb;
301 n;
302 s graphics off;
303
304
   correlation analysis using train2 data vs shot made flag */
305
306 oc corr data=train2 plots=matrix(histogram);
      var shot_made_flag game_event_id lat loc_y minutes_remaining
307
       \rightarrow avgnoisedb;
      run;
308
309
310
    correlation analysis using pricipal components vs shot made flag */
311
312 oc corr data=pca plots=matrix(histogram);
      var shot_made_flag prin1 - prin10;
313
      run;
314
315
316
   model 1 - GLM select using PCA */
317
318 oc glmselect data=pca plots=all seed=3;
```

```
319 del shot_made_flag =prin1-prin10 / selection = stepwise(choose=CV

→ select=CV stop=CV);
320 n;
321
322
   model 2 - Logistic using PCA */
323
324 s graphics on;
325 oc logistic data=pca plots(only)=(roc(id=obs) effect);
326 model shot_made_flag (event='1') =prin1-prin10 / scale=none
                                               clparm=wald
327
                                                clodds=pl
328
                                               rsquare
329
                                                              lackfit
330
                                                               ctable;
331
332 output out = model_2_results p = Predict;
333 n;
334 s graphics off;
335
336
   model 3 - Logistic using train2 dataset (not PCA) only by distance
   → */
338 s graphics on;
339 oc logistic data=train2 plots(only)=(roc(id=obs) effect);
340 model shot_made_flag (event='1') = shot_distance / scale=none
                                                clparm=wald
341
                                                clodds=pl
342
                                                rsquare
343
                                                              lackfit
344
                                                               ctable;
345
346 output out = model_3_results p = Predict;
347 n;
348 s graphics off;
349
350
351 create data for model 4 - data sets for playoffs and not at playoffs
   → */
```

```
352
353 ta train2_playoffs;
354 t train2;
355 ere playoffs = 1;
356 n;
357
358 ta train2_no_playoffs;
359 t train2;
360 ere playoffs = 0;
361 n;
362
363
   model 4A - Logistic using train2 dataset (not PCA) during playoffs
364
   → */
365
366 s graphics on;
367 oc logistic data=train2_playoffs plots(only)=(roc(id=obs) effect);
368 model shot_made_flag (event='1') = shot_distance / scale=none
                                                clparm=wald
369
                                                clodds=pl
370
                                                rsquare
371
                                                               lackfit
372
                                                               ctable;
373
374 output out = model_4A_results p = Predict;
376 s graphics off;
377
378
   model 4B - Logistic using train2 dataset (not PCA) during playoffs
379
   → */
380
381 s graphics on;
382 oc logistic data=train2_no_playoffs plots(only)=(roc(id=obs) effect);
383 model shot_made_flag (event='1') = shot_distance / scale=none
                                                clparm=wald
384
                                                clodds=pl
385
```

```
rsquare
386
                                                               lackfit
387
                                                               ctable;
388
389 output out = model_4B_results p = Predict;
390 n;
391 s graphics off;
392
393
   model 5 - Logistic using train2 dataset (not PCA) during playoffs
394
   → */
395 s graphics on;
396 oc logistic data=train2 plots(only)=(roc(id=obs) effect);
397 model shot_made_flag (event='1') = shot_distance playoffs arena_temp
      game_event_id lat lon / scale=none
                                                clparm=wald
398
                                                clodds=pl
399
                                                rsquare
400
                                                               lackfit
401
                                                               ctable;
402
403 output out = model_5_results p = Predict;
404 n;
405 s graphics off;
406
407
   model 6 - Logistic using train2 dataset (not PCA) for all variables
408
   \rightarrow that had corr p < 0.0001 */
409 s graphics on;
410 oc logistic data=train2 plots(only)=(roc(id=obs) effect);
411 model shot_made_flag (event='1') = shot_distance playoffs period
     minutes_remaining seconds_remaining attendance arena_temp
       avgnoisedb / scale=none
                                                clparm=wald
412
                                                clodds=pl
413
                                                rsquare
414
                                                               lackfit
415
                                                               ctable;
416
```

```
417 output out = model_6_results p = Predict;
419 s graphics off;
420
421
    Model 7 - LDA Model */
422
423
424 oc discrim data=train2 outstat=LDAstat method=normal pool=yes
                  list crossvalidate;
425
       class shot_made_flag;
426
       priors prop;
427
       var shot_distance playoffs period minutes_remaining
428
           seconds_remaining attendance arena_temp avgnoisedb;
    run;
429
430
431
432
433
434
435
436
437
438
    Import test data for prediction model */
439
440
    import test data */
441
442 oc import datafile="c:\users\allen\documents\smu data science\MSDS
      6372 - Applied Statistics\project 2\project2pred.csv"
           dbms=dlm out=test replace;
443
      delimiter=',';
444
      getnames=yes;
445
446 n;
447
  print data */
448
449 oc print data=test (obs=10);
450 n;
```

```
451
   investigate data for variable types*/
453 oc contents data=test;
454 n;
455
   look for missing numeric data - may need to impute */
457 oc means data = test n nmiss;
458 var _numeric_;
459 n;
460
   investigate means of training data */
461
462 oc means data = test n nmiss;
463 n;
464
465 univariate data analysis */
466 oc univariate data = test;
467 r season;
468 n;
469
    note that certain "season" fields are missing */
471 ta _seasontest;
     set test;
472
     where missing (season);
473
474 n;
475
   print "season" data, where "season" is missing */
477 oc print data=_seasontest (obs=200);
478 n;
479
   add empty predicted response field */
481 ta test2;
482 t test;
483 ot_made_flag = .;
484
485
486 print data */
```

```
487 oc print data=test2 (obs=200);
488 n;
489
490
   Create TRAIN and TEST fields to distinguish test vs train data.
491
   → Combine data, predict missing values, create final data set */
492
493 ta train2b;
494 t train2;
495 le = "TRAIN";
496 n;
497
498 oc print data=train2b (obs=10);
500
501 ta test2b;
502 t test2;
503 le = "TEST";
504 n;
505
506 oc print data=test2b (obs=10);
507 n;
508
509
510
511
512 make a numeric shot_made_flag variable in test data */
513
514 ta test2c;
515 t test2b;
n_shot_made_flag = input(shot_made_flag,8.);
517 n;
518
519 drop original non-numeric shot_made_flag */
520 ta test2c;
521 t test2c (drop = shot_made_flag);
```

```
522 n;
523
524 rename numeric shot_made_flag */
525 ta test2c;
526 t test2c (rename=(
527 _shot_made_flag'n='shot_made_flag'n));
528 n;
529
   drop the n_shot_made_flag variable */
530
531 ta test2c;
532 t test2c (drop = shot_made_flag);
533 n;
534
535 rename rannum variable to recId */
536 ta test2c;
537 t test2c (rename=(
538 annum'n='recId'n));
539 n;
540
541
542
   combine data sets */
543
544
545 ta test3;
546 t train2b test2c;
547 n;
548
549 oc print data=test3 (obs=10);
550 n;
551
552 oc contents data=test3;
553 n;
554
555
556 predict response field (shot_made_flag) using desired method */
557 s graphics on;
```

```
558 oc logistic data=test3 plots(only)=(roc(id=obs) effect);
559 model shot_made_flag (event='1') = shot_distance playoffs period
   \hookrightarrow minutes_remaining seconds_remaining attendance arena_temp
       avgnoisedb / scale=none
                                                 clparm=wald
560
                                                 clodds=pl
561
                                                 rsquare
562
                                                                lackfit
563
                                                                ctable;
565 tput out = model_test_results p = Predict;
566 n;
567 s graphics off;
568
569
   check data for completeness */
571
572 oc means data = results n nmiss;
573 var _numeric_;
574 n;
576 oc print data=results (obs=10);
577 ere file = "TEST";
578 n;
579
580 oc contents data=results;
581 n;
582
583 oc means data=results
Mean Std Min Q1 Median Q3 Max;
585 n;
586
   This is the final step that maps the predicted value into the
   \rightarrow shot_made_flag variable
588 d then drops all variables except shot_id and shot_made_flag. */
589
590 ta results_final;
```

```
591 tain shot_id shot_made_flag;
592 t model_test_results;
shot_made_flag < 1 then shot_made_flag = predict;</pre>
594 ep shot_id shot_made_flag;
595 ere file = "TEST";
596 n;
597
598 oc print data=results_final (obs=100);
599 n;
600
601 oc contents data=results_final;
602 n;
603
604
605
606
607
608
609
610
611
612
613
614
615 s graphics on;
616 oc logistic data=test3 plots(only)=(roc(id=obs) effect);
617 model shot_made_flag (event='1') = shot_distance / scale=none
                                                  clparm=wald
618
                                                  clodds=pl
619
                                                  rsquare
620
                                                                 lackfit
621
                                                                 ctable;
623 output out = model_test3_results p = Predict;
624 n;
625 s graphics off;
626
```

```
627
628
   model 5 - Logistic using train2 dataset (not PCA) during playoffs
   → */
630 s graphics on;
631 oc logistic data=test3 plots(only)=(roc(id=obs) effect);
632 model shot_made_flag (event='1') = shot_distance playoffs arena_temp
       game_event_id lat lon / scale=none
                                                clparm=wald
633
                                                clodds=pl
634
                                                rsquare
635
                                                               lackfit
636
                                                               ctable;
637
638 output out = model_test5_results p = Predict;
639 n;
640 s graphics off;
641
642
  model 6 - Logistic using train2 dataset (not PCA) for all variables
   \rightarrow that had corr p < 0.0001 */
644 s graphics on;
645 oc logistic data=test3 plots(only)=(roc(id=obs) effect);
646 model shot_made_flag (event='1') = shot_distance playoffs period
   → minutes_remaining seconds_remaining attendance arena_temp
       avgnoisedb / scale=none
                                                clparm=wald
647
                                                clodds=pl
648
                                                rsquare
649
                                                               lackfit
650
                                                               ctable;
651
652 output out = model_test6_results p = Predict;
654 s graphics off;
655
656
657 ta results_final_6;
```

```
658 tain shot_id shot_made_flag;
659 t model_test6_results;
660 shot_made_flag < 1 then shot_made_flag = predict;
661 ep shot_id shot_made_flag;
662 ere file = "TEST";
663 n;</pre>
```

## 5.4 Python Code

```
# MSDS 6371 - Applied Statistics #
    # Allen Crane and Brock Friedrich #
    # Kobe Bryant Shot Selection
    # November 2018
7 port warnings
8 rnings.filterwarnings("ignore")
10 port os
11 port sys
12 port seaborn as sns
13 port matplotlib.pyplot as plt
14 port pandas as pd
15 port numpy as np
16 port statsmodels.api as sm
17 om statsmodels.stats.outliers_influence import

→ variance_inflation_factor

18 om sklearn.feature_selection import RFE
19 om sklearn.discriminant_analysis import LinearDiscriminantAnalysis
20 om sklearn.model_selection import train_test_split
21 om sklearn.metrics import confusion_matrix, log_loss, roc_auc_score
22 om sklearn.linear_model import LogisticRegression
24 port statsmodels.formula.api as smf
25 om scipy import stats
```

```
26 port matplotlib.pyplot as plt
27 port numpy as np
28 port pandas as pd
29 om pandas.plotting import (lag_plot,
                                             autocorrelation_plot,
30
                                             table, scatter_matrix,
31
                                             boxplot)
32
34 om patsy import dmatrices
35 om math import degrees, acos
36 om scipy.spatial import distance
37
39 os.chdir(os.path.dirname(__file__))
40 s.path.insert(0, os.getcwd()+'/src')
41 om eda import *
42 om confusion_matrix_pretty import *
43 from plotting import *
44 om logistic_regression import *
45 om linear_discriminant_analysis import *
47 f cols(df: pd.DataFrame) -> list:
    """Extract list of columns from input DataFrame and removing the
     \rightarrow dependent variable."""
49
    return [x for x in df.columns.tolist() if x not in [DEPENDENT]]
50
51
52 f get_dummies(df: pd.DataFrame, drop_first = False):
    """Replace catagorical variables with indicators"""
53
54
    df = pd.get_dummies(df, dtype = float)
    df.columns = df.columns \
56
                     .str.lower() \
                     .str.replace(" ", "_")
58
    return df
59
60
```

```
61 f LogRegModel(data: pd.DataFrame, add_constant = False):
    if add_constant:
        data = sm.add_constant(data)
63
    model = LogR(data, DEPENDENT)
64
    model.sm = model.statsmodel()
65
66
    model.yhat = model.sm.predict(model.test_x)
67
    print("\n Predicted Log Loss: {}\n".format(
68
        round(
69
             log_loss(model.test_y, model.yhat)
70
             , 4)))
71
    return model
72
73
74 f summarize_model(model: LogR):
    print(model.describe_features())
    print(model.sm.summary())
76
    print(model.sm.summary2())
77
    print(model.sm.wald_test_terms())
78
80 Import Data
81 TA = pd.read_excel('data/project2Data.xlsx', index_col = 'recId')
82 R_PREDICTION = pd.read_excel('data/project2Pred.xlsx', index_col =

    'rannum')

83 PENDENT = "shot_made_flag"
84
85 DUNDANT_FEATURES = [
86 'team_id', # constant term
87 'team_name', # constant term
88 'season',
89 'game_id', # violates independence
90 'matchup',
91 'shot_id',
92 'recId',
93 'shot_zone_area',
94 'shot_zone_basic',
95 'shot_zone_range',
```

```
96 'minutes_remaining',
97 'seconds_elapsed_in_game',
98 'game_event_id', # violates independence
99 'game_date', # violates independence
   'action_type',
         'loc_x', # collinear with lat
101
         'loc_y', # collinear with lon
102
103
104
105
106
107
108
109 f to_latex(df):
     pd.set_option('display.float_format', lambda x: '%.0f' % x)
     with open('temp.txt', 'w') as f:
111
         f.write(r'\resizebox{\textwidth}{!}{'+
112
             df.to_latex()
113
             + r'}\captionof{table}{Feature
114
              → Summary}\label{tbl:featuresummary}')
     pd.set_option('display.float_format', lambda x: '%.4f' % x)
115
116
117
118 f desc(df: pd.DataFrame):
119 ""Produces a summary of the input DataFrame
120
121 rguments:
122 df {pd.DataFrame} -- [description]
123
124 eturns:
125 pd.DataFrame -- DataFrame of summary statistics
126
127
128 esc = df.describe(percentiles = None).T
129 esc['missing'] = len(df.index) - desc['count']
130 desc = desc.astype('int')
```

```
131 esc['median'] = df.median()
132 esc['missing %'] = desc.missing / len(df.index) * 100
133 eturn desc.T
134
   "######### Model 0 - Predicted Log Loss: 0.6552 ##########"""
135
136
137
   "Dataset: d0 | Prediction set: d0_pred
     - Full Model
139
140 "
141
   = prepare_data(DATA.drop(columns = ['action_type']))
142
.game_date = d0.game_date.apply(lambda x: x.toordinal())
  = get_dummies(d0).fillna(0) # Get dummy variables for categoricals
__pred = wrangle_features(FOR_PREDICTION)
_pred.game_date = d0_pred.game_date.apply(lambda x: x.toordinal())
_pred = get_dummies(d0_pred).fillna(0) # Get dummy variables for
   \hookrightarrow categoricals
148 _pred = d0_pred[cols(d0)]
150 "Fit d2"""
151
152 del0 = LogRegModel(d0)
153 mmarize_model(model0)
154 del0.roc_plot()
155
   "######### Model 1 - Predicted Log Loss: 0.6652 ##########"""
157
158
   "Dataset: d1 | Prediction set: d1_pred
159
     - No categorical features
160
   = prepare_data(DATA, drop_categorical = True) # Wrangle Data
.game_date = d1.game_date.apply(lambda x: x.toordinal())
  = d1.fillna(0)
165 d1_pred = wrangle_features(FOR_PREDICTION)
```

```
166 \ d1\_pred.game\_date = d1\_pred.game\_date.apply(lambda \ x: \ x.toordinal())
  d1\_pred = d1\_pred[cols(d1)].fillna(0)
168
169 "Fit d1"""
170 del1 = LogRegModel(d1)
171 mmarize_model(model1)
172 del1.roc_plot()
173
   "######### Model 2 - Predicted Log Loss: 0.6479 ###########"""
175
   "Dataset: d2 | Prediction set: d2_pred
176
     - Categorical features as indicators
177
     - Drop redundant features
178
179
180
   = prepare_data(DATA, drop_columns= REDUNDANT_FEATURES)
182 \ d2. game\_date = d2. game\_date.apply(lambda \ x: \ x. toordinal())
183 d2.last_seconds_of_period = d2.last_seconds_of_period.astype(int)
  = get_dummies(d2).fillna(0) # Get dummy variables for categoricals
185 _pred = wrangle_features(FOR_PREDICTION)
_pred = get_dummies(d2_pred).fillna(0) # Get dummy variables for
   \hookrightarrow categoricals
187 _pred = d2_pred[cols(d2)]
188
  "Fit d2"""
190 del2 = LogRegModel(d2)
191 mmarize_model(model2)
192 del2.sm2 = model2.statsmodel ()
193 del2.sm2.fitted = model2.sm2.fit()
194 model2.sm.summary2()
195 del2.sm2.fitted.predict(model2.test_x)
196 pd. Series (model2. predict labels (d2 pred)).set index (d2 pred. sho)
197 model2.roc_plot()
198
199 f_train_x = model2.sm2.pdf(model2.train_x)
200 f_train_x = model2.sm2.cdf(model2.train_x)
```

```
201
202 sult = model2.sm.summary2()
203 godds = result.tables[1]
204 \text{ ds}[['Coef.','[0.025', '0.975]']] = np.exp(logodds[['Coef.','[0.025', '0.975]'])]
   → '0.975]']])
t_{change} = (odds[['Coef.','[0.025', '0.975]']] - 1) * 100
206
207
208 rr_matrix(wrangle_features(DATA.drop(columns = ['action_type'])))
209 ot_proba(model2)
210 ot_regular_vs_post_season(model2)
211 ot_confusion_matrix(model2)
212
213
214 "
215
216 logOdds
                                 Coef.
                                          Std.Err.
                                                             P > |z|
218
       [0.025
                   0.975]
219 t
                               -0.6565
                                          0.3081 -2.1307 0.0331
   → -1.2604
                    -0.0526
                               -0.0526
                                           0.1710 -0.3076 0.7584
220 n
   → -0.3879
                    0.2826
                                0.0417
221 ayoffs
                                             0.0462 0.9019 0.3671
   → -0.0489
                     0.1324
                                0.0014
                                             0.0009 1.5626 0.1182
222 conds_remaining
   → -0.0004
                     0.0031
223 ot_distance
                               -0.0189
                                             0.0044 -4.2505 0.0000
   → -0.0275
                    -0.0102
224 tendance
                                0.0002
                                             0.0000 10.3586 0.0000
   → 0.0001
                    0.0002
225 ena_temp
                                0.0328
                                             0.0076 4.3008 0.0000
   → 0.0178
                   0.0477
                                0.0025
                                             0.0078 0.3175 0.7509
226 gnoisedb
   → -0.0128
                    0.0177
```

```
0.0001 0.0001 0.7850 0.4325
227 conds_left_in_period
  → -0.0001
             0.0002
228 st\_seconds\_of\_period
                        -0.8629
                                  0.1282 -6.7335 0.0000
  \rightarrow -1.1141 -0.6117
229 conds_left_in_game
                        0.0001
                                  0.0000 2.2041 0.0275
           0.0001
  → 0.0000
                        -0.0259
                                   0.0305 -0.8465 0.3973
230 me_or_away
  → -0.0857
0.0340
231 m_shots_cumulative
                         0.0005
                                   0.0042 0.1257 0.9000
  → -0.0077
                0.0087
232 gle_from_basket
                        0.0002
                                   0.0004 0.3873 0.6985
  → -0.0006 0.0009
233 ason_count
                         0.0093
                                   0.0034 2.7567 0.0058

→ 0.0027 0.0159

234
235 Odds
236
                         Coef. Std.Err. z P>|z| [0.025
237
  → 0.975]
238
239 lat
                         → 0.2829 0.9467
                        240 n
  → 1.3251
241 ayoffs
                        1.0214
                                  0.0586 0.3602 0.7187 0.9105
  → 1.1458
242 conds_remaining
                       1.0014 0.0009 1.5652 0.1175 0.9996

→ 1.0031

243 shot_distance
                         0.9813
                                    0.0044 -4.2570 0.0000
  → 0.9728 0.9899
244 me_date
                        1.0002 0.0003 0.5708 0.5681 0.9995
  → 1.0008
                                    0.0000 10.3607 0.0000
245 attendance
                          1.0002
  0.0076 4.2622 0.0000
246 arena_temp
                         1.0331

→ 1.0177 1.0486
```

```
1.0025 0.0078 0.3238 0.7461 0.9873
247 gnoisedb
  → 1.0180
248 conds_left_in_period 1.0001
                                    0.0001 0.7873 0.4311 0.9999
  249 last_seconds_of_period
                          0.4220
                                     0.1282 -6.7317 0.0000

→ 0.3283 0.5425

                                     0.0000 2.2072 0.0273
250 seconds_left_in_game
                          1.0001
  251 me_or_away
                         0.9739
                                    0.0306 -0.8659 0.3865 0.9173
  252 m_shots_cumulative
                         1.0005
                                    0.0042 0.1242 0.9011 0.9923
  → 1.0088
253 gle_from_basket
                         1.0002
                                    0.0004 0.3880 0.6980 0.9994
  254 ason\_count
                        0.9419 0.1212 -0.4942 0.6212 0.7427

→ 1.1944

255
256 Percent Changes
                               Coef. Std.Err. z P > |z|
257
  \rightarrow [0.025 0.975]
258 lat
                              -48.1343 0.3081 -2.1307 0.0331
  → -71.6464 -5.1247
                             -5.1247 0.1710 -0.3076 0.7584
259 n
  → -32.1487 32.6623
260 ayoffs
                              4.2596 0.0462 0.9019 0.3671
  → -4.7756 14.1521
                              0.1395 0.0009 1.5626 0.1182
261 conds_remaining
  \rightarrow -0.0354 0.3147
262 shot_distance
                               -1.8678
                                           0.0044 -4.2505 0.0000
  → -2.7173 -1.0109
263 attendance
                                0.0173
                                           0.0000 10.3586 0.0000

→ 0.0141 0.0206

                                           0.0076 4.3008 0.0000
264 arena_temp
                                3.3317

→ 1.7998 4.8866

                              0.2476 0.0078 0.3175 0.7509
265 gnoisedb

→ -1.2714 1.7900
```

```
266 conds_left_in_period
                                0.0061
                                             0.0001 0.7850 0.4325
   → -0.0092 0.0215
last_seconds_of_period
                                -57.8070
                                              0.1282 -6.7335 0.0000
   → -67.1786 -45.7595
seconds_left_in_game
                                  0.0070
                                              0.0000 2.2041 0.0275
              0.0132
   → 0.0008
                                             0.0305 -0.8465 0.3973
269 me_or_away
                                -2.5519
   → -8.2134
               3.4588
_{270} m_shots_cumulative
                                0.0527
                                             0.0042 0.1257 0.9000
   → -0.7654
               0.8775
_{271} gle\_from\_basket
                                0.0150
                                             0.0004 0.3873 0.6985
   → -0.0610
               0.0911
272 ason_count
                                0.9308
                                             0.0034 2.7567 0.0058
   → 0.2681
              1.5979
273
  Significant features
274
                                                     [0.025 0.975]
                       Coef. Std.Err.
                                            z P>|z|
275
276 t
                      0.5175
                               0.3082 -2.1377 0.0325 0.2829 0.9467
277 ot_distance
                      0.9813
                               0.0044 -4.2570 0.0000
                                                     0.9728 0.9899
                             0.0000 10.3607 0.0000
278 tendance
                                                     1.0001 1.0002
                      1.0002
279 ena_temp
                      1.0331 0.0076 4.2622 0.0000 1.0177 1.0486
281 conds_left_in_game
                      1.0001 0.0000 2.2072 0.0273 1.0000 1.0001
282
283
284
285
286
287 " #! Interpretation
288 e p value is calculated based on the assumption that the null
   → hypothesis is true.
289
```

49

```
290 think about it this way: "assuming the null hypothesis is true, the
   → probability of the observed test statistic occurring is 0.02.
   \rightarrow That's not very probable. But the observed test statistic
   → definitely occurred, because it was observed. Therefore, it seems
   \rightarrow more likely that the null hypothesis is not true, i.e. It should
      be rejected."
291
292 suming the null hypothesis is true, the probability of measuring at
       least the observed test occurring is 0.02."
293
294 "
295
296 f_test_x = sm2.pdf(model2.test_x)
298 " Refine Model 2 """
299
300 ld = model2.sm.wald_test_terms()
301 ld.df = wald.summary_frame()
302 ld.significant = wald.df[wald.df['P>chi2'] < 0.1].index.tolist()
303
304 " Refined Fit - Predicted Log Loss: 0.6634 """
305
306 del2r = LogRegModel(d2[wald.significant + [DEPENDENT]])
307
308 "
309 t
                           -0.1393
310 ot_distance
                           -0.0447
311 tendance
                            0.0002
312 ena_temp
                            0.0337
313 conds_left_in_game
                           0.0001
314 st_seconds_of_period
                          -0.8275
315 "
316
317
318
319
```

```
Interpret: http://www-hsc.usc.edu/~eckel/biostat2/notes/notes14.pdf
320
321
   "######### Model 3 - Predicted Log Loss: 0.669 ##########"""
322
323
   "Dataset: d3 | Prediction set: d3_pred
324
     - Allen's Model
325
326
_{327} \text{ cols} = [
     'shot_distance',
328
     'playoffs',
329
     'arena_temp',
330
     'game_event_id',
331
     'lat',
332
     'lon',
333
     'shot_made_flag'
334
     1
335
    = DATA[d3cols]
  _pred = FOR_PREDICTION[d3cols].drop(columns = [DEPENDENT]).fillna(0)
338
  "Fit d3"""
340 del3 = LogRegModel(d3)
341 mmarize_model(model3)
342
343
344
   "########## Model 4 - LDA - Predicted Log Loss: 9.351
       #########"""
346
347 a = LinearDiscriminantAnalysis()
348 a = lda.fit(model2.train_x, model2.train_y)
349 a_x = lda.transform(model2.train_x)
350 = lda.transform(model2.test_x)
351 labels = lda.predict(model2.test_x)
352
353 g_loss(model2.test_y, z)
354
```

```
355
   "########## Model 5 #########"""
356
357
   "Dataset: d5 | Prediction set: d5_pred
358
     - shot_distance only predictor
359
360
361
   = DATA[[DEPENDENT, 'shot_distance']]
  d3_pred = FOR_PREDICTION[d3cols].drop(columns =
   → [DEPENDENT]).fillna(0)
364
  "Fit d5"""
365
   = sm.add_constant(d5)
366
367 del5 = LogR(d5, DEPENDENT)
368 del5.sm = model5.statsmodel()
369
370 del5.yhat = model5.sm.predict(model.test_x)
371
  del5 = LogRegModel(d5)
    = model5.sm.summary2()
373
374
    = np.exp(s5.tables[1]['Coef.'])
375
376
377
   "########## Model 6 - Log Loss: 0.669 ###########"""
378
379
   "Dataset: d6 | Prediction set: d6\_pred
380
     - Allen's model 5
381
382
383
    = DATA[[DEPENDENT, 'shot_distance', 'playoffs', 'arena_temp',
384
       'game_event_id', 'lat', 'lon']]
385
386 "Fit d6"""
387 	ext{ } d5 = sm.add\_constant(d5)
388 \mod el5 = LogR(d5, DEPENDENT)
```

```
389
390
391 del6 = LogRegModel(d6)
    = model6.sm.summary2()
393
394
    = np.exp(s6.tables[1]['Coef.'])
395
396
397 ot_confusion_matrix(model6)
398
399 del6.sensitivity()
400 del6.specificity()
401
402
   Data Overview
403
404
405 TODO: Add Univariate Plots
     # QQ
406
     # Hist
407
408
409
410
411
412 = d6 .select_dtypes(np.number)
413
414
415 cNoFocus = "red"
416
417
    Correlation Matrix
418
419
420
_{421} TA.shape
422
better model was at the cost of explainability and violation of
   → parsimony
```

```
424
425
426 The __odds of Kobe making a shot decrease with respect to the
   → distance he is from the hoop__. If there is evidence of this,
     quantify this relationship. (CIs, plots, etc.)
427
   Yes. His odds go down by -1.87\% + -.85\% (-2.72% -1.01%) for every
428
   → additional foot away from the basket.
429 "
430
431 "
432 The __probability of Kobe making a shot decreases linearly with
   → respect to the distance he is from the hoop__.
                                                            If there is
   \rightarrow evidence of this, quantify this relationship. (CIs, plots,
       etc.)
433
   It doesn't. Show pdf plot.
434
435
436 near up to 23ft, but is not at zero at 23ft, so probability curve
   \rightarrow must be curved.
437
438
439
440
441
442
443
444 The relationship between the __distance Kobe is from the basket and
   \rightarrow the odds of him making the shot is different if they are in the
   → playoffs__. Quantify your findings with statistical evidence one
      way or the other. (Tests, CIs, plots, etc.)
445
446
447
448 "
449
```

```
450
451 " Odds Ratios
452 ds ratios that are greater than 1 indicate that the event is more
       likely to occur as the predictor increases. Odds ratios that are
       less than 1 indicate that the event is less likely to occur as
       the predictor increases.
453
   tps://www.predictive analytics world.com/patimes/on-variable-importance-in-logistic-regress
455
    The model indicates a 4.25% increase in shooting ability during the
456
   \rightarrow playoffs, however, the result was not statistically significant.
457
   's overlap and contain zero. zome evidence but not enough to conclude
458
       there is a difference.
459
460
461 om sklearn.linear_model import LogisticRegression
  om sklearn.model_selection import train_test_split
  om sklearn.feature_selection import chi2
   om sklearn.metrics import (
464
         classification_report,
465
         roc_curve,
466
         auc
467
468
         )
469
470 port pandas as pd
471 om confusion_matrix_pretty import *
472 port statsmodels.api as sm
473 om sklearn.metrics import confusion_matrix
474
   ass LogR(LogisticRegression):
     """Sparse extension of sklearn.linear_model.LogisticRegression.
476
477
     11 11 11
478
479
     def __init__(self,
480
```

```
data: pd.DataFrame,
481
              dependent_name: None,
482
              store_covariance: bool = True,
483
              test\_size: float = 0.25,
484
              fit_intercept = False):
485
         super().__init__(solver = 'lbfgs',
486
                           fit_intercept = fit_intercept
487
488
         self.yhat = None
489
490
         self.train_x, self.test_x, self.train_y, self.test_y =
491
       train_test_split(data.drop(columns = [dependent_name]),
       data[dependent_name], test_size = test_size, random_state = 0)
492
     def __repr__(self):
493
         return super().__repr__()
494
495
     def __str__(self):
496
         return super().__str__()
497
498
     def describe_features(self):
499
500
         print(f"""
501
         X: features: {len(self.train_x)}
502
503
              dtypes:
504
              _____""")
505
506
         for k, v in self.train_x.dtypes.sort_index().items():
507
              print(f'''\t\t{k:<30}{v.name:} ''')</pre>
508
509
         print(f"""
510
         Y: {self.train_y.name}: {self.train_y.dtype}
511
         """)
512
513
     def confusion_matrix(self, test = False, plot = True):
514
```

```
"""Generate, and optionally plot, a confusion matrix for the
515
       test or train datasets
516
         Keyword Arguments:
517
             plot {bool} -- optionally plot the confusion matrix
518
              519
         Returns:
520
             pd.DataFrame -- confusion matrix
521
          11 11 11
522
         if test:
523
             x = self.test_x
524
             y = self.test_y
525
         else:
526
             x = self.train_x
527
             y = self.train_y
528
529
         # if y is not None and x is not None:
530
         self.cm = pd.DataFrame(confusion_matrix(y,
531
       self.sm2.fitted.predict(x)), index = [0, 1], columns = [0, 1])
         if plot:
532
             pretty_plot_confusion_matrix(self.cm, cmap='PuRd')
533
         return self.cm
534
         # else:
535
               print('X or Y is empty. Check parameters.')
536
                return None
537
538
     def score(self) -> float:
539
          """Wrapper for parent class method using xy's stored in child
540
       class object. Scores model fit using test data.
541
         Returns:
542
             float -- model score
543
544
         n n n
545
546
```

```
x = self.test_x
547
         y = self.test_y
548
549
         score = super().score(x, y)
550
         print(f'''
551
         Features:
552
              {' | '.join([x for x in x.columns])}
553
554
         Accuracy: {score:.2%}
556
         111)
557
         return score
558
559
     def plot_separability() -> None:
560
         """Plots a heatmap of fitted coefficients, highlighting
561
       features that are more likely seperable by a linear hyperplane.
         11 11 11
562
563
         x = self.train_x
564
         if len(x.columns.tolist()) == len(self.coef_[0]):
565
              fig, ax = plt.subplots(1, 1, <math>figsize=(12, 10))
566
              sns.heatmap(pd.DataFrame(self.coef_[0],
567
                                        columns=[1],
568
                                        index=x.columns.tolist()),
569
                           ax=ax, cmap='RdBu', annot=True)
570
571
             plt.title('LDA Feature Separability')
572
             plt.tight_layout()
573
         else:
574
              print('Length of input "x" does not match number of
575
       coefficients. Refit the model using the dependents in x.')
              return None
576
577
     def fit(self):
578
         """Wrapper for parent class method using xy's stored in child
579
       class object.
```

```
580
          Fit the model.
581
582
          Returns:
583
              pd.Series -- array of x values projected to maximize
584
               \hookrightarrow seperation
585
586
          super().fit(self.train_x, self.train_y)
587
588
     def predict(self, x):
589
590
          self.yhat = super().predict(x)
591
          return self.yhat
592
593
     def transform(self):
594
          """Wrapper for parent class method using xy's stored in child
595
       class object.
596
          Transform x to maximize seperation.
597
598
          Returns:
599
              pd.Series -- array of x values projected to maximize
600
               \hookrightarrow seperation
601
          11 11 11
602
          return super().transform(self.x)
603
604
     def log_loss(self, x = None):
605
606
          if self.yhat is not None:
607
               self.yhat = self.sm.predict(x or self.test_x)
608
609
          return round(log_loss(self.test_y, self.yhat), 2)
610
611
     def _decision_function(self):
612
```

```
#TODO: Implement, time permitting
613
          raise NotImplementedError()
614
615
     def classification_report(self):
616
          """Class wrapper for sklearn.metrics.classification_report
617
          11 11 11
618
619
          classification_report(
620
              self.test_y,
621
              self.yhat,
622
              target\_names = self.classes\_.astype(str).tolist())
623
624
     def statsmodel(self):
625
          """Model using statsmodels library.
626
627
         Returns:
628
              statsmodels result object
629
630
          11 11 11
631
632
          return sm.Logit(self.train_y, self.train_x).fit()
633
634
     def statsmodel_(self):
635
          """Model using statsmodels library.
636
637
          Returns:
638
              statsmodels result object
639
640
          n n n
641
642
          return sm.Logit(self.train_y, self.train_x)
643
644
645
     def roc_plot(self, sm = True):
646
647
          Referenced from:
648
```

```
649
             https://scikit-learn.org/stable/auto_examples/model_selection/plot_roc_crossval
          11 11 11
650
651
         y_score = self.predict_labels(self.test_x)
652
653
         fpr, tpr, _ = roc_curve(self.test_y, y_score)
654
655
         roc_auc = auc(fpr, tpr)
656
         plt.plot(fpr, tpr, lw=1, alpha=1,
657
                       label='ROC \ fold \ %d \ (AUC = \%0.2f)' \ % \ (1, \ roc\_auc))
658
659
         g = plt.plot([0, 1], [0, 1], linestyle='--', lw=2, color='r',
660
                  label='Chance', alpha=.8)
661
662
         plt.xlim([-0.05, 1.05])
663
         plt.ylim([-0.05, 1.05])
664
         plt.xlabel('False Positive Rate')
665
         plt.ylabel('True Positive Rate')
666
         plt.title('Receiver operating characteristic example')
667
         plt.legend(loc="lower right")
668
         g.set_title(f'Distribution of {y}', color = cNoFocus)
669
         g.set\_xlabel(f'\{y\}', size = 'xx-large', color = cNoFocus)
670
         q.set_ylabel(f'Density', size = 'xx-large', color = cNoFocus)
671
         q.set_xticklabels(q.qet_xticklabels(), size = 'xx-large')
672
         q.set_yticklabels(q.qet_yticklabels(), size = 'xx-large')
673
         g.tick_params(colors=cNoFocus)
674
         g.spines['bottom'].set_color(cNoFocus)
675
         g.spines['top'].set_color(cNoFocus)
676
         q.spines['left'].set_color(cNoFocus)
677
         q.spines['right'].set_color(cNoFocus)
678
         q.xaxis.label.set_color(cNoFocus)
679
         g.yaxis.label.set_color(cNoFocus)
         return
681
682
```

683

```
def predict_labels(self, x, thresh = 0.5):
684
          """Predict class labels"""
685
686
         self.yhat = self.sm.fitted.predict(x)
687
         pc = np.zeros(len(self.yhat))
688
         pc[self.yhat > thresh] = 1
689
         return pc
690
691
     def sensitivity(self):
692
         """Sensitivity - TP/(TP+FN)"""
693
694
         cm = self.sm.pred_table()
695
         sens = cm[0,0]/(cm[0,0]+cm[0,1])
696
         print('Sensitivity : ', sens )
697
         return sens
698
699
700
     def specificity(self):
701
          """Specificity = TN/(TN+FP)"""
702
703
         cm = self.sm.pred_table()
704
         spec = cm[1,1]/(cm[1,0]+cm[1,1])
705
         print('Specificity : ', spec)
706
         return spec
707
708
709
710
711
712 f RecursiveFeatureSelection(X, y):
     logreg = LogisticRegression()
713
     rfe = RFE(logreg, 20)
714
     rfe = rfe.fit(X.fillna(0), y.values.ravel())
715
     return rfe
716
717
718
719 Evaluate Model
```

```
720 https://www.r-bloggers.com/evaluating-logistic-regression-models/
722
723
   http://blog.yhat.com/posts/logistic-regression-and-python.html
724
725
   Dont use r-sq
726
727 https://stats.stackexchange.com/questions/3559/which-pseudo-r2-measure-is-the-one-to-repo
  TODO: Kobe last minute shots are outliers
729
730
731
732
733
734
735 X_train, X_test, y_train, y_test = train_test_split(
       d3.drop(columns=[DEPENDENT]),
736
        d3[DEPENDENT], test_size=0.3, random_state=0)
737
738 logreg = LogisticRegression(fit_intercept = True, C = 1e9)
739 logreg.fit(X_train, y_train)
740 y_pred = logreg.predict(X_test)
741 print('Accuracy of logistic regression classifier on test set:
   → {:.2f}'.format(logreg.score(X_test, y_test)))
742 log_loss(y_test, y_pred)
743 logreg.coef_
744
745 # SM
746 logit = sm.Logit(y_train, X_train)
747 logit.fit().params
748
749 port os
750 port sys
751 port seaborn as sns
752 port matplotlib.pyplot as plt
753 port pandas as pd
754 port numpy as np
```

```
755 port statsmodels.api as sm
756 om statsmodels.stats.outliers_influence import
   \rightarrow variance_inflation_factor
757 om sklearn.discriminant_analysis import LinearDiscriminantAnalysis
758 om sklearn.model_selection import train_test_split
759 om sklearn.metrics import confusion_matrix, log_loss
760 om sklearn.linear_model import LogisticRegression
761
762 port statsmodels.formula.api as smf
763 om scipy import stats
764 port matplotlib.pyplot as plt
765 port numpy as np
766 port pandas as pd
767 om pandas.plotting import (lag_plot,
                                              autocorrelation_plot,
768
                                              table, scatter_matrix,
769
                                              boxplot)
770
771
772 om patsy import dmatrices
773 om math import degrees, acos
774 om scipy.spatial import distance
775
776
777 os.chdir(os.path.dirname(__file__))
778 s.path.insert(0, os.getcwd()+'/src')
779 om eda import *
780 om confusion_matrix_pretty import *
781 from plotting import *
782
783 ass LDAB(LinearDiscriminantAnalysis):
    """Sparse extension of
784

→ sklearn.discriminant_analysis.LinearDiscriminantAnalysis for

      handling binary class cases.
785
     11 11 11
786
787
```

```
def __init__(self,
788
              data: pd.DataFrame,
789
              dependent_name: None,
790
              store_covariance: bool = True,
791
              solver = 'eigen',
792
              test\_size: float = 0.25):
793
         super().__init__(
794
                           \# n_{components} = 2,
795
                           solver = solver,
796
                           store_covariance = store_covariance
797
798
         self.yhat = None
799
800
         self.train_x, self.test_x, self.train_y, self.test_y =
801
       train_test_split(
                            data.drop(columns = [dependent_name]),
802
                           data[dependent_name],
803
                            test_size = test_size,
804
                           random_state = 0)
805
806
     def __repr__(self):
807
         return super().__repr__()
808
809
     def __str__(self):
810
         return super().__str__()
811
812
     def explained_variance(self) -> float:
813
          """Get variance explained per discriminant.
814
815
         Returns:
816
              float -- explained variance ratio
817
          11 11 11
818
819
         print(f'''Explained variance ratio:
820
         Discriminant 1: {self.explained_variance_ratio_[0]: .2f}''')
821
         # return self.explained_variance_ratio_[0]
822
```

```
823
     def describe_features(self):
824
825
         print(f"""
826
         X: features: {len(self.train_x)}
827
828
             dtypes:
829
             _____"")
830
831
         for k, v in self.train_x.dtypes.sort_index().items():
832
             print(f'''\t\t{k:<30}{v.name:} ''')</pre>
833
834
         print(f"""
835
         Y: {self.train_y.name}: {self.train_y.dtype}
836
         """)
837
838
     def confusion_matrix(self, test = False, plot = True):
839
         """Generate, and optionally plot, a confusion matrix for the
840
      test or train datasets
841
         Keyword Arguments:
842
             plot {bool} -- optionally plot the confusion matrix
843
              844
         Returns:
845
             pd.DataFrame -- confusion matrix
846
         11 11 11
847
         if test:
848
             x = self.test_x
849
             y = self.test_y
850
         else:
851
             x = self.train_x
852
             y = self.train_y
854
         \# if y is not None and x is not None:
855
```

```
self.cm = pd.DataFrame(confusion\_matrix(y, self.predict(x)),
856
       index = [0, 1], columns = [0, 1])
          if plot:
857
              pretty_plot_confusion_matrix(self.cm, cmap='PuRd')
858
          return self.cm
859
          # else:
860
                print('X or Y is empty. Check parameters.')
861
                return None
862
863
     def\ score(self,\ x,\ y)\ 	ext{->}\ float:
864
          """Wrapper for parent class method using xy's stored in child
865
       class object. Scores model fit using test data.
866
         Returns:
867
              float -- model score
869
          11 11 11
870
871
          \# x = self.test_x
872
          # y = self.test_y
873
874
         score = super().score(x, y)
875
         print(f'''
876
         Features:
877
              {' | '.join([x for x in x.columns])}
878
879
         Accuracy: {score:.2%}
880
881
          111)
882
          return score
883
884
     def plot_separability() -> None:
885
          """Plots a heatmap of fitted coefficients, highlighting
       features that are more likely seperable by a linear hyperplane.
          ,,,,,,
887
888
```

```
x = self.train_x
889
          if len(x.columns.tolist()) == len(self.coef_[0]):
890
              fig, ax = plt.subplots(1, 1, <math>figsize=(12, 10))
891
              sns.heatmap(pd.DataFrame(self.coef_[0],
892
                                         columns=[1],
893
                                         index=x.columns.tolist()),
894
                           ax=ax, cmap='RdBu', annot=True)
895
896
              plt.title('LDA Feature Separability')
897
              plt.tight_layout()
898
         else:
899
              print('Length of input "x" does not match number of
900
       coefficients. Refit the model using the dependents in x.')
              return None
901
902
     def fit(self):
903
          """Wrapper for parent class method using xy's stored in child
904
       class object.
905
         Fit the model.
906
907
         Returns:
908
              pd.Series -- array of x values projected to maximize
909
              \hookrightarrow seperation
910
          11 11 11
911
         super().fit(self.train_x, self.train_y)
912
913
     def predict(self, x):
914
915
         self.yhat = super().predict(x)
916
         return self.yhat
917
918
     def transform(self, x):
919
          """Wrapper for parent class method using xy's stored in child
920
      class object.
```

```
921
         Transform x to maximize seperation.
922
923
         Returns:
924
              pd.Series -- array of x values projected to maximize
925
                 seperation
926
927
         return super().transform(x)
928
929
     def log_loss(self, x = None):
930
931
          if self.yhat is not None:
932
              self.yhat = self.predict(x or self.test_x)
933
934
          return round(log_loss(self.test_y, self.yhat), 2)
935
936
     def _decision_function(self):
937
          #TODO: Implement, time permitting
938
          raise NotImplementedError()
939
940
     def classification_report(self):
941
          """Class wrapper for sklearn.metrics.classification_report
942
943
944
          classification_report(
945
              self.test_y,
946
              self.yhat,
947
              target\_names = self.classes\_.astype(str).tolist())
948
949
     def roc_plot(self):
950
          11 II II
951
         Referenced from:
952
953
              https://scikit-learn.org/stable/auto_examples/model_selection/plot_roc_crossval
          11 11 11
954
```

```
955
         y_score = self.decision_function(self.test_x)
956
957
         fpr, tpr, _ = roc_curve(self.test_y, y_score)
958
959
         roc_auc = auc(fpr, tpr)
960
         plt.plot(fpr, tpr, lw=1, alpha=1,
961
                       label='ROC\ fold\ \%d\ (AUC=\%0.2f)'\ \%\ (1,\ roc\_auc))
962
963
         plt.plot([0, 1], [0, 1], linestyle='--', lw=2, color='r',
964
                   label='Chance', alpha=.8)
965
966
         plt.xlim([-0.05, 1.05])
967
         plt.ylim([-0.05, 1.05])
968
         plt.xlabel('False Positive Rate')
969
         plt.ylabel('True Positive Rate')
970
         plt.title('Receiver operating characteristic example')
971
         plt.legend(loc="lower right")
972
         plt.show()
973
974
975
976
977
978
979 sumptions:
     - Each class must be:
980
         - normally distributed
981
         - identical cov matrices
982
         - independent
983
984
985
986
    __name__ == "__main__":
988
989
     #! Try full model
990
```

```
model = LDAB(data.fillna(0), DEPENDENT)
991
      model.fit()
992
      model.explained_variance()
993
      model.score()
994
      model.get_confusion_matrix()
995
      model.plot_separability()
996
      model_fi = model.feature_importance()
997
      model.log_loss()
998
999
      #! Try reduced model
1000
      data_reduced = data[model_fi.index]
1001
1002
      ldab_reduced = LDAB(data_reduced, DEPENDENT)
1003
      ldab_reduced.fit()
1004
      ldab_reduced.explained_variance()
1005
      ldab_reduced.score_()
1006
      ldab\_reduced.get\_confusion\_matrix()
1007
      ldab_reduced.plot_separability()
1008
      ldab_reduced.log_loss()
1009
1010
      disc1 = ldab_reduced.fit_transform(train_x_reduced, train_y)
1011
1012
1013
      # Plot single discriminant
1014
      sns.distplot(disc1)
1015
1016
      # TODO: Add plots
1017
1018
      #! Yes! Shows no seperation
1019
1020
      sns.pairplot(temp_x,
1021
              hue="shot_made_flag",
1022
              palette="husl",
1023
              markers = ['<', '>'],
1024
              plot_kws = {
1025
                   'alpha': 0.5,
1026
```

```
},
1027
               diaq_kws = {
1028
1029
               },
1030
1031
1032
      11 11 11
1033
      Conclusion:
1034
1035
      Reduced model, with only 2 features, yields results effectively
1036
          equivalent to those of the full model that uses 13 features.
1037
1038
      import os
1039
      import seaborn as sns
1040
      import matplotlib.pyplot as plt
1041
      import pandas as pd
1042
      import numpy as np
1043
      import statsmodels.api as sm
1044
      from statsmodels.stats.outliers_influence import
1045
    → variance_inflation_factor
      from sklearn.discriminant_analysis import
1046
    \rightarrow LinearDiscriminantAnalysis
      from sklearn import linear_model
1047
      import statsmodels.formula.api as smf
1048
      from scipy import stats
1049
      import matplotlib.pyplot as plt
1050
      import numpy as np
1051
      import pandas as pd
1052
      from pandas.plotting import (lag_plot,
1053
                                     autocorrelation_plot,
1054
                                     table, scatter_matrix,
1055
                                     boxplot)
1056
1057
      from patsy import dmatrices
1058
      from math import degrees, acos
1059
```

```
from scipy.spatial import distance
1060
1061
1062
1063
      pd.options.display.max_rows = None
1064
      pd.set\_option('display.float\_format', lambda x: '\%.3f' \% x)
1065
      pd.set_option('large_repr', 'truncate')
1066
      pd.set_option('precision',2)
1067
1068
      # Matplotlib global config
1069
      plt.rcParams.update({'legend.fontsize': 'x-large',
1070
                 'figure.figsize': (10, 6),
1071
                'axes.labelsize': 'large',
1072
                'axes.titlesize':'xx-large',
1073
                'xtick.labelsize':'small',
1074
                'ytick.labelsize':'small',
1075
                'savefig.dpi': 300,
1076
                'savefig.format' : 'png',
1077
                'savefig.transparent' : True,
1078
                'axes.labelpad' : 10,
1079
                'axes.titlepad' : 10,
1080
                'axes.titleweight': 'bold'
1081
               })
1082
1083
      # plt.style.use('seaborn-deep')
1084
1085
1086
      # Define Contants
1087
1088
      DEPENDENT = "shot_made_flaq"
1089
      PERIODS_IN_GAME = 4
1090
      MIN_IN_PERIOD = 12
1091
      MIN_IN_GAME = MIN_IN_PERIOD * PERIODS_IN_GAME
1092
      SECONDS_IN_PERIOD = MIN_IN_PERIOD * 60
1093
      SECONDS_IN_GAME = MIN_IN_GAME * 60
1094
1095
```

```
1096
       n n n
1097
      LOGISTIC MODEL:
1098
1099
      - Dependent: shot_made: bool
1100
1101
      11 11 11
1102
1103
       n n n
1104
      LDA MODEL:
1105
1106
      - Dependent: shot_made: bool
1107
1108
       11 11 11
1109
1110
1111
1112
      n n n
1113
1114
      EDA:
1115
1116
      - Potential Mulicolinearity:
           - Court Position: lat/log
1117
                               x/y
1118
                               shot_zone_area (cat)
1119
                               shot_zone_basic (cat)
1120
                               shot_zone_range (cat)
1121
1122
           - (maybe) game_date:
1123
1124
1125
      - Add Features:
1126
1127
           - game_count: cumulative number of games
1128
```

```
- "distance" between games is more or less equivalent
1129
                   (except between seasons), so representation as an
                   ordinal continuous value is appropriate. The effects of
                   season changes will still be captures by season_count.
1130
          - home_or_away: home ("vs.") or away ("0")
1131
1132
          - seconds_left_in_game: apply function
1133
1134
          - seconds_left_in_period: min_remaining * 60 +
1135
           \hookrightarrow seconds_remaining
1136
          - season_count: cumulative number of seasons
1137
               - "distance" between seasons is more or less equivalent, so
1138
               \hookrightarrow representation as an ordinal continuous value is
               \hookrightarrow appropriate.
1139
          - num_shots_cumulative: running total of number of shots up to
1140
           \rightarrow the current point in the game
1141
          - (NotYetImplemented) shot_difficulty
1142
1143
     Stretch Features:
1144
1145
          - altitude: obtain from lat/long
1146
1147
          - central_angle_to_basket: instead of x/y
1148
1149
          - vector_length_to_basket: instead of x/y
1150
1151
     Drop Features:
1152
1153
          - team_id: constant
1154
1155
          - team_name: constant
1156
1157
```

```
- season: replace with season_count
1158
1159
          - game_id: replace with game_count
1160
1161
          - matchup: redundant with opponent
1162
1163
      11 11 11
1164
1165
1166
1167
1168
      def desc(df: pd.DataFrame):
1169
          """Produces a summary of the input DataFrame
1170
1171
          Arguments:
1172
               df {pd.DataFrame} -- [description]
1173
1174
          Returns:
1175
              pd.DataFrame -- DataFrame of summary statistics
1176
          11 11 11
1177
1178
          desc = df.describe().T
1179
          desc['missing'] = len(df.index) - desc['count']
1180
          # desc = desc.astype('int')
1181
          desc['median'] = df.median()
1182
          desc['missing %'] = desc.missing / len(df.index) * 100
1183
          return desc.T
1184
1185
      def\ vif(df:\ pd.DataFrame,\ dependent:\ str)\ ->\ pd.DataFrame:
1186
          """Get Variance Inflation Factor for each feature in df via a
1187
        simple, multiple regression.
1188
          Arguments:
1189
               df {pd.DataFrame} -- dataset
1190
               dependent {str} -- column name of dependent feature in df
1191
1192
```

```
Returns:
1193
              pd.DataFrame -- DataFrame containing feature names and VIF
1194
                  measures.
          11 11 11
1195
1196
          {\it \# https://etav.github.io/python/vif\_factor\_python.html}
1197
          df = df.dropna()
1198
          df = df._get_numeric_data() #drop non-numeric cols
1199
1200
          #gather features
1201
          features = "+".join(df.columns.drop(dependent).tolist())
1202
1203
          # get y and X dataframes based on this regression:
1204
          y, X = dmatrices('{} ~'.format(dependent) + features, df,
1205
        return_type='dataframe')
1206
          # For each X, calculate VIF and save in dataframe
1207
          vif = pd.DataFrame()
1208
          vif["VIF Factor"] = [variance_inflation_factor(X.values, i) for
1209
        i in range(X.shape[1])]
          vif["features"] = X.columns
1210
1211
          return vif.round(1)
1212
1213
      def angle(a: float, b: float, c: float) -> float:
1214
          """ Calculate central angle for three known side lengths using
1215
       Law of Cosines
          Arguments:
1216
              a {Side} -- A side length
1217
              b {Side} -- B side length
1218
              c {Side} -- C side length
1219
1220
          Returns:
1221
              Angle {float} -- central angle of A in degrees
1222
          11 11 11
1223
1224
```

```
return degrees (acos((c**2 - b**2 - a**2)/(-2.0 * a * b)))
1225
1226
      def central_angle(x: float, y:float) -> float:
1227
          """Calculate central angle of shot using NBA court grid
1228
        coordinates.
1229
          Arguments:
1230
               x {float} -- X coordinate of shot
1231
               y {float} -- Y coordinate of shot
1232
1233
          Returns:
1234
              float -- angle in degrees of shot
1235
          n n n
1236
1237
          # Hack
1238
          if (y == 0) \& (x < 0):
1239
              return -90
1240
1241
          if (y == 0) \& (x > 0):
1242
               return 90
1243
1244
          if (y == 0) & (x == 0):
1245
              return 0
1246
1247
          # Vertices
1248
          vc_a = (x, y) # shot loation
1249
          vc_b = (0,0) \# origin
1250
          vc_c = (0, y) # reference point (0, y)
1251
1252
          side_a = distance.euclidean(vc_b, vc_c)
1253
          side_b = distance.euclidean(vc_a, vc_c)
1254
          side_c = distance.euclidean(vc_a, vc_b)
1255
1256
          # A = angle(side_a, side_b, side_c)
1257
          # C = angle(side_c, side_a, side_b)
1258
          B = angle(side_b, side_c, side_a)
1259
```

```
1260
           return B if x > 0 else -B
1261
1262
      def wrangle_features(data: pd.DataFrame) -> pd.DataFrame:
1263
           feats = pd.Series(
1264
                         data = False,
1265
                         index = ['recId',
1266
                                   'action_type',
1267
                                   'combined_shot_type',
1268
                                   'game_event_id',
1269
                                   'game_id',
1270
                                   'lat',
1271
                                   'loc_x',
1272
                                   'loc_y',
1273
                                   'lon',
1274
                                   'minutes_remaining',
1275
                                   'period',
1276
                                   'playoffs',
1277
                                   'season',
1278
                                   'seconds_remaining',
1279
                                   'shot_distance',
1280
                                   'shot_made_flag',
1281
                                   'shot_type',
1282
                                   'shot_zone_area',
1283
                                   'shot_zone_basic',
1284
                                   'shot_zone_range',
1285
                                   'team_id',
1286
                                   'team_name',
1287
                                   'game_date',
1288
                                   'matchup',
1289
                                   'opponent',
1290
                                   'shot_id',
1291
                                   'attendance',
1292
                                   'arena_temp',
1293
                                   'avgnoisedb'],
1294
                         dtype = bool
1295
```

```
)
1296
1297
          # Flag features that were passed to the function
1298
          feats.loc[feats.index.isin(data.columns)] = True
1299
          try:
1300
              if feats.minutes_remaining & feats.seconds_remaining:
1301
                   data['seconds_left_in_period'] = data.minutes_remaining
1302
        * 60 + data.seconds_remaining
          except Exception as e:
1303
              print('Failed to add feature: seconds_left_in_period.
1304
        ({})'.format(e))
1305
          try:
1306
                   data['last_seconds_of_period'] =
1307
        data.seconds\_left\_in\_period < 2
                   data.last_seconds_of_period =
1308
        data.last\_seconds\_of\_period.astype(int)
          except Exception as e:
1309
              print('Failed to add feature: last_seconds_of_period.
1310
        ({})'.format(e))
1311
1312
          try:
1313
              if feats.period:
1314
                   data['seconds_elapsed_in_game'] = SECONDS_IN_PERIOD *
1315
        data.period - data.seconds_left_in_period
          except:
1316
              print('Failed to add feature: seconds_elapsed_in_game')
1317
1318
          try:
1319
              if True:
1320
                   data['seconds_left_in_qame'] = SECONDS_IN_GAME -
1321
        data.seconds\_elapsed\_in\_game
          except:
1322
              print('Failed to add feature: seconds_left_in_game')
1323
1324
```

```
try:
1325
              if feats.matchup:
1326
                   data['home_or_away'] =
1327
        data.matchup.str.contains("@").astype(int)
          except:
1328
              print('Failed to add feature: home_or_away')
1329
1330
          try:
1331
              if feats.game_id:
1332
                   data['num_shots_cumulative'] =
1333
        data.groupby(['game_id']).cumcount()
          except:
1334
              print('Failed to add feature: num_shots_cumulative')
1335
1336
          try:
1337
              if feats.loc_x & feats.loc_y:
1338
                   data['angle_from_basket'] = data.apply(lambda row:
1339
        central_angle(row.loc_x, row.loc_y), axis = 1)
          except:
1340
              print('Failed to add feature: angle_from_basket')
1341
1342
          try:
1343
              if feats.season:
1344
                   # Convert season to ordered Categorical (Factor) type
1345
                   data.season = pd.Categorical(data.season,
1346
        data.season.sort_values().unique().tolist(), ordered = True)
                   data['season_count'] = data.season.cat.codes
1347
          except:
1348
              print('Failed to add feature: season_count')
1349
1350
          try:
1351
              if len(data.select_dtypes('object').columns):
1352
                   # Convert other string fields to unordered Categorical
1353
                   data[data.select_dtypes('object').columns.tolist()] =
1354
        data.select_dtypes('object').astype('category')
          except:
1355
```

```
print('Failed to convert objects to categories')
1356
1357
          return data
1358
1359
      def drop_features(data, columns):
1360
1361
          # Remove columns in the 'remove' list if they are present in
1362
        the dataset
          data = data.drop(columns = [x for x in columns if x in
1363
        data.columns])
          return data
1364
1365
      def eigen_solver():
1366
          """Assess using Eigen values and vectors
1367
1368
1369
             https://stackoverflow.com/questions/25676145/capturing-high-multi-collinea
1370
          An almost zero eigen value shows a direction with zero
1371
              variation, hence collinearity.
1372
          n n n
1373
          # TODO: Implement, time permitting
1374
          raise NotImplementedError()
1375
1376
      def check_collinearity(data: pd.DataFrame):
1377
          return vif(data, DEPENDENT) \
1378
                       .set_index('features') \
1379
                       .rename(columns = {'VIF Factor' : 'VIF'}) \
1380
                       .sort_values(by = 'VIF', ascending = False) \
1381
                       .drop('Intercept')
1382
1383
      def check_collinearity_recursive(data: pd.DataFrame, vifs = None):
1384
```

```
"""Recursively check the multicollinearity (MC) associated
1385
       with each feature. Each iteration, the feature with the largest
       MC is dropped if the MC is infinite or if MC > x, where x is the
       standard deviation of the finite VIFs of the original features. A
       matrix containing VIFs for each iteration is returned once an
       iteration is reached where MC <= x.
1386
         Arguments:
1387
             data {pd.DataFrame} -- Matrix or DataFrame with
1388
              1389
         Keyword Arguments:
1390
             vifs {None} -- Recursive control parameter (default:
1391
              → {None})
1392
         Returns:
1393
              [pd.DataFrame] -- Matrix of VIFs per iteration. Nan (not a
1394
                 number) values represent features dropped from the
                  assessment in either a previous or the current
                  iteration.
          11 11 11
1395
1396
         prev_vifs = vifs
1397
1398
         vifs = vif(data, DEPENDENT) \
1399
                      .set_index('features') \
1400
                      .rename(columns = {'VIF Factor' : 'VIF'}) \
1401
                      .sort_values(by = 'VIF', ascending = False) \
1402
                      .drop('Intercept') # Drop intercept term
1403
1404
1405
         vifO_name, vifO_val = vifs.iloc[0].name,
1406
       vifs.iloc[0].values[0]
1407
         drop_feature = False
1408
          limit = None
1409
```

```
thresh = prev_vifs.VIF[np.isfinite(prev_vifs.VIF)].max() if
1410
        prev_vifs is not None else O
          # If inflated feature VIF is infinite, drop the feature
1411
          if vif0_val == float('inf'):
1412
              drop_feature = True
1413
          else:
1414
              # Otherwise, drop feature if VIF within 2.5 stds.
1415
              limit = (vifs[vifs != float('inf')].std()*2.5).values[0]
1416
              if vif0_val > limit > thresh:
1417
                   drop_feature = True
1418
1419
          if prev_vifs is not None:
1420
              # print('\n\nprev_vifs')
1421
              # print(prev_vifs)
1422
              vifs = prev_vifs.join(vifs, rsuffix = '_'+str(len(vifs)))
1423
1424
1425
1426
          print(f'VIF: Dropping: {vif0_name} / limit: {limit or 0:.2f} /
1427
        thresh: {thresh or 0:.2f}')
1428
          if drop_feature:
1429
              return check_collinearity_recursive(
1430
                       data.drop(columns = [vif0_name]),
1431
                       vifs = vifs
1432
                       )
1433
1434
          print('\n\nvifs')
1435
          print(vifs)
1436
1437
          return vifs
1438
1439
      def fix_mulitcollinearity(data: pd.DataFrame):
1440
          """Remove multicollinear variables by assessing variance
1441
        inflation factors.
1442
```

```
Arguments:
1443
              data {pd.DataFrame} -- (n_obs, n_features)
1444
1445
          Returns:
1446
              pd.DataFrame -- data
1447
1448
          print(' \ n \ n')
1449
          vifs = check_collinearity_recursive(data)
1450
          # vifs = check_collinearity(data)
1451
          vifs = vifs.iloc[:, -1] # Get last column (the last iteration)
1452
1453
          # remove features with high MC from data set
1454
          data = data.drop(columns = vifs[vifs.isna()].index)
1455
          return data
1456
1457
      def prepare_data(data: pd.DataFrame, drop_categorical = False,
1458
        drop_columns: list = None) -> pd.DataFrame:
          """Template procedue to ingest new dataset.
1459
1460
1461
          Arguments:
              data {pd.DataFrame} -- new dataset
1462
1463
          Returns:
1464
              pd.DataFrame -- dataset for further prep or analysis
1465
1466
1467
          data = wrangle_features(data)
1468
          if drop_columns is not None:
1469
              data = drop_features(data, drop_columns)
1470
          data = fix_mulitcollinearity(data)
1471
1472
          # Drop remaining categoricals
1473
          if \ drop\_categorical:
1474
              data = data.select_dtypes(exclude = ['object',
1475
        'category'])
1476
```

```
return data
1477
1478
      def identify_outliers(data):
1479
          pass
1480
1481
1482
1483
      # action_counts =
1484
    → DATA['action_type'].value_counts().sort_values(ascending =
    → False)
1485
      # from scipy import stats
1486
      \# d2[(np.abs(stats.zscore(d2)) < 3).any(axis=1)]
1487
      \# d2[np.abs(d2-d2.mean()) \le (3*d2.std())]
1488
      # stats.trimb
1489
1490
      # data = data.drop(columns = [
1491
             'minutes_remaining',
1492
             'seconds_remaining',
1493
             'seconds_elapsed_in_game',
1494
             'lat',
1495
             'lon',
      #
1496
             'game_event_id',
1497
             'period',
1498
             'seconds_left_in_period',]
1499
             )
1500
      #
1501
      # Sort features by VIF
1502
1503
      # NOTE: PLOTS
1504
1505
      # fig, ax = plt.subplots(figsize=(12,8))
1506
      # ax = sns.scatterplot('loc_x', 'loc_y', hue = 'shot_made_flag',
1507
    \rightarrow data = data)
      # ax.set_title('Shot Location')
1508
      # ax.set_xlabel('X')
1509
```

```
# ax.set_ylabel('Y')
1510
      # ax.set_ylim(0, 400)
1511
      # fig.savefig('figs/p2-3_price-v-months.png')
1512
1513
      # fig, ax = plt.subplots(figsize=(12,8))
1514
      \# ax = data.boxplot()
1515
      # ax.set_xticklabels(data.columns, rotation=90)
1516
      # fiq.tight_layout()
1517
1518
      # fig, ax = plt.subplots(figsize=(12,8))
1519
      # ax = data.select_dtypes(include=[np.number]).hist()
1520
      # # ax.set_xticklabels(data.columns, rotation=90)
1521
      # fig.tight_layout()
1522
1523
     # import time
1524
      # from sklearn.linear_model import LassoCV
1525
      # print("Computing regularization path using the coordinate descent
1526
    → lasso...")
     # t1 = time.time()
1527
      \# model = LassoCV(cv=5).fit(X, y)
1528
      \# t_{lasso_cv} = time.time() - t1
1529
1530
      # # Display results
1531
     \# m_log_alphas = -np.log10(model.alphas_)
1532
1533
     # plt.figure()
1534
     # ymin, ymax = 2300, 3800
1535
      # plt.plot(m_log_alphas, model.mse_path_, ':')
1536
      # plt.plot(m_log_alphas, model.mse_path_.mean(axis=-1), 'k',
1537
                  label='Average across the folds', linewidth=2)
1538
      # plt.axvline(-np.log10(model.alpha_), linestyle='--', color='k',
1539
                     label='alpha: CV estimate')
1540
1541
      # plt.legend()
1542
1543
     # plt.xlabel('-log(alpha)')
1544
```

```
# plt.ylabel('Mean square error')
1545
      # plt.title('Mean square error on each fold: coordinate descent '
1546
                   '(train time: %.2fs)' % t_lasso_cv)
1547
      # plt.axis('tight')
1548
      # plt.ylim(ymin, ymax)
1549
1550
1551
      # def correct_multicollinearity(data: pd.DataFrame) ->
1552
       pd.DataFrame:
                print('Anterior VIF')
1553
                print(vif(data, DEPENDENT))
1554
1555
                 # Drop multicolinear features
1556
                 data = data.drop(columns = [
1557
                          'minutes_remaining',
1558
                          'seconds_remaining',
1559
      #
                          'seconds_elapsed_in_game',
1560
                          'lat'.
1561
                          'lon',
1562
                          'game_event_id',
1563
                          'period',
1564
                          'seconds_left_in_period',
1565
1566
                1)
1567
1568
                print('Posterior VIF')
1569
                v = vif(data, DEPENDENT)
1570
                print(v)
1571
                 return data
1572
1573
1574
     plot a pretty confusion matrix with seaborn
1575
      Created on Mon Jun 25 14:17:37 2018
1576
      @author: Wagner Cipriano - wagnerbhbr - gmail - CEFETMG / MMC
1577
     @repository:
1578
      → https://github.com/wcipriano/pretty-print-confusion-matrix/blob/master/confusi
```

```
References:
1579
       https://www.mathworks.com/help/nnet/ref/plotconfusion.html
1580
1581
        → https://stackoverflow.com/questions/28200786/how-to-plot-scikit-learn-classificat
1582
          https://stackoverflow.com/questions/5821125/how-to-plot-confusion-matrix-with-str
       https://www.programcreek.com/python/example/96197/seaborn.heatmap
1583
1584
           https://stackoverflow.com/questions/19233771/sklearn-plot-confusion-matrix-with-l
1585
           http://scikit-learn.org/stable/auto_examples/model_selection/plot_confusion_matri
      11 11 11
1586
1587
      #imports
1588
     from pandas import DataFrame
1589
      import numpy as np
1590
      import matplotlib.pyplot as plt
1591
     import matplotlib.font_manager as fm
1592
     from matplotlib.collections import QuadMesh
1593
      import seaborn as sns
1594
1595
1596
     def _get_new_fig(fn, figsize=[9,9]):
1597
          """ Init graphics """
1598
          fig1 = plt.figure(fn, figsize)
1599
          ax1 = fig1.gca()
                            #Get Current Axis
1600
          ax1.cla() # clear existing plot
1601
         return fig1, ax1
1602
1603
1604
     def _configcell_text_and_colors(array_df, lin, col, oText,
1605

→ facecolors, posi, fz, fmt, show_null_values=0):
1606
            config cell text and colors
1607
            and return text elements to add and to dell
1608
            @TODO: use fmt
1609
```

```
1610
          text_add = []; text_del = [];
1611
          cell_val = array_df[lin][col]
1612
          tot_all = array_df[-1][-1]
1613
          per = (float(cell_val) / tot_all) * 100
1614
          curr_column = array_df[:,col]
1615
          ccl = len(curr_column)
1616
1617
          #last line and/or last column
1618
          if(col == (ccl - 1)) \ or \ (lin == (ccl - 1)):
1619
              #tots and percents
1620
              if(cell_val != 0):
1621
                   if(col == ccl - 1) and (lin == ccl - 1):
1622
                       tot_riq = 0
1623
                       for i in range(array_df.shape[0] - 1):
1624
                            tot_rig += array_df[i][i]
1625
                       per_ok = (float(tot_rig) / cell_val) * 100
1626
                   elif(col == ccl - 1):
1627
                       tot_riq = array_df[lin][lin]
1628
                       per_ok = (float(tot_rig) / cell_val) * 100
1629
                   elif(lin == ccl - 1):
1630
                       tot_rig = array_df[col][col]
1631
                       per_ok = (float(tot_rig) / cell_val) * 100
1632
                   per\_err = 100 - per\_ok
1633
              else:
1634
                   per_ok = per_err = 0
1635
1636
              per_ok_s = ['%.2f\%'\%(per_ok), '100\%'] [per_ok == 100]
1637
1638
              #text to DEL
1639
              text_del.append(oText)
1640
1641
              #text to ADD
1642
              font_prop = fm.FontProperties(weight='bold', size=fz)
1643
              text_kwargs = dict(color='w', ha="center", va="center",
1644
        qid='sum', fontproperties=font_prop)
```

```
lis_txt = ['\%d'\%(cell_val), per_ok_s, '\%.2f\%'\%(per_err)]
1645
               lis\_kwa = [text\_kwarqs]
1646
               dic = text_kwargs.copy(); dic['color'] = 'g';
1647
        lis_kwa.append(dic);
               dic = text_kwargs.copy(); dic['color'] = 'r';
1648
        lis_kwa.append(dic);
               lis_pos = [(oText._x, oText._y-0.3), (oText._x, oText._y),
1649
        (oText._x, oText._y+0.3)]
               for i in range(len(lis_txt)):
1650
                   newText = dict(x=lis\_pos[i][0], y=lis\_pos[i][1],
1651
        text=lis_txt[i], kw=lis_kwa[i])
                   #print 'lin: %s, col: %s, newText: %s' %(lin, col,
1652
        newText)
                   text_add.append(newText)
1653
               #print '\n'
1654
1655
               #set background color for sum cells (last line and last
1656
        column)
               carr = [0.27, 0.30, 0.27, 1.0]
1657
               if(col == ccl - 1) and (lin == ccl - 1):
1658
                   carr = [0.17, 0.20, 0.17, 1.0]
1659
               facecolors[posi] = carr
1660
1661
          else:
1662
               if(per > 0):
1663
                    txt = \frac{1}{s} \frac{1}{n} . 2f\%'' \% (cell_val, per)
1664
               else:
1665
                   if(show_null_values == 0):
1666
                        txt = ''
1667
                   elif(show_null_values == 1):
1668
                        txt = '0'
1669
                    else:
1670
                        txt = 'O \setminus nO.0\%'
1671
               oText.set_text(txt)
1672
1673
               #main diagonal
1674
```

```
if(col == lin):
1675
                   #set color of the textin the diagonal to white
1676
                   oText.set_color('w')
1677
                   # set background color in the diagonal to blue
1678
                   facecolors[posi] = [0.35, 0.8, 0.55, 1.0]
1679
              else:
1680
                   oText.set_color('r')
1681
1682
          return text_add, text_del
1683
1684
1685
      def _insert_totals(df_cm):
1686
          """ insert total column and line (the last ones) """
1687
          sum_col = []
1688
          for c in df_cm.columns:
1689
              sum_col.append( df_cm[c].sum() )
1690
          sum_lin = []
1691
          for item_line in df_cm.iterrows():
1692
              sum_lin.append( item_line[1].sum() )
1693
          df_cm['sum_lin'] = sum_lin
1694
          sum_col.append(np.sum(sum_lin))
1695
          df_cm.loc['sum_col'] = sum_col
1696
          #print ('\ndf_cm:\n', df_cm, '\n\b\n')
1697
1698
1699
     def pretty_plot_confusion_matrix(df_cm, annot=True, cmap="Oranges",
1700
        fmt='.2f', fz=11,
            lw=0.5, cbar=False, figsize=[8,8], show_null_values=0,
1701
        pred_val_axis='y'):
          11 11 11
1702
            print conf matrix with default layout (like matlab)
1703
            params:
1704
              df_cm
                               dataframe (pandas) without totals
1705
              annot
                               print text in each cell
1706
              cmap
                               Oranges_r,YlGnBu,Blues,RdBu, ...
1707

    see:
```

```
fz
                                fontsize
1708
                                linewidth
               lw
1709
                               where to show the prediction values (x or y
               pred_val_axis
1710
               \rightarrow axis)
                                 'col' or 'x': show predicted values in
1711
                                 \hookrightarrow columns (x axis) instead lines
                                 'lin' or 'y': show predicted values in
1712
                                 \hookrightarrow lines
                                              (y axis)
           11 11 11
1713
          if(pred_val_axis in ('col', 'x')):
1714
               xlbl = 'Predicted'
1715
               ylbl = 'Actual'
1716
          else:
1717
               xlbl = 'Actual'
1718
               ylbl = 'Predicted'
1719
               df_cm = df_cm.T
1720
1721
          # create "Total" column
1722
          _insert_totals(df_cm)
1723
1724
          #this is for print allways in the same window
1725
          fig, ax1 = _get_new_fig('Conf matrix default', figsize)
1726
1727
          #thanks for seaborn
1728
          ax = sns.heatmap(df_cm, annot=annot, annot_kws={"size": fz},
1729
        linewidths=lw, ax=ax1,
                            cbar=cbar, cmap=cmap, linecolor='w', fmt=fmt)
1730
1731
          #set ticklabels rotation
1732
          ax.set_xticklabels(ax.get_xticklabels(), rotation = 45,
1733
        fontsize = 10)
          ax.set_yticklabels(ax.get_yticklabels(), rotation = 25,
1734
        fontsize = 10)
1735
          # Turn off all the ticks
1736
          for t in ax.xaxis.get_major_ticks():
1737
```

```
t.tick10n = False
1738
              t.tick20n = False
1739
          for t in ax.yaxis.get_major_ticks():
1740
              t.tick10n = False
1741
              t.tick20n = False
1742
1743
          #face colors list
1744
          quadmesh = ax.findobj(QuadMesh)[0]
1745
          facecolors = quadmesh.get_facecolors()
1746
1747
          #iter in text elements
1748
          array_df = np.array( df_cm.to_records(index=False).tolist() )
1749
          text_add = []; text_del = [];
1750
          posi = -1 #from left to right, bottom to top.
1751
          for t in ax.collections[0].axes.texts: #ax.texts:
1752
              pos = np.array(t.get_position()) - [0.5, 0.5]
1753
              lin = int(pos[1]); col = int(pos[0]);
1754
              posi += 1
1755
              #print ('>>> pos: %s, posi: %s, val: %s, txt: %s' %(pos,
1756
       posi, array_df[lin][col], t.get_text()))
1757
              #set text
1758
              txt_res = _configcell_text_and_colors(array_df, lin, col,
1759
        t, facecolors, posi, fz, fmt, show_null_values)
1760
              text_add.extend(txt_res[0])
1761
              text_del.extend(txt_res[1])
1762
1763
          #remove the old ones
1764
          for item in text_del:
1765
              item.remove()
1766
          #append the new ones
1767
          for item in text_add:
1768
              ax.text(item['x'], item['y'], item['text'], **item['kw'])
1769
1770
          #titles and legends
1771
```

```
ax.set_title('Confusion matrix')
1772
          ax.set_xlabel(xlbl)
1773
          ax.set\_ylabel(ylbl)
1774
          plt.tight_layout() #set layout slim
1775
          plt.show()
1776
          return ax
1777
1778
1779
      def\ plot\_confusion\_matrix\_from\_data(y\_test,\ predictions,
1780
        columns=None, annot=True, cmap="Oranges",
            fmt='.2f', fz=11, lw=0.5, cbar=False, figsize=[8,8],
1781
        show_null_values=0, pred_val_axis='lin'):
1782
              plot confusion matrix function with y_test (actual values)
1783
               \rightarrow and predictions (predic),
              whitout a confusion matrix yet
1784
          11 11 11
1785
          from sklearn.metrics import confusion_matrix
1786
          from pandas import DataFrame
1787
1788
          #data
1789
          if(not columns):
1790
               #labels axis integer:
1791
               \# columns = range(1, len(np.unique(y_test))+1)
1792
               #labels axis string:
1793
              from string import ascii_uppercase
1794
               columns = ['class %s' %(i) for i in
1795
        list(ascii_uppercase)[0:len(np.unique(y_test))]]
1796
          confm = confusion_matrix(y_test, predictions)
1797
          cmap = 'Oranges';
1798
          fz = 11;
1799
          figsize=[9,9];
1800
          show_null_values = 2
1801
          df\_cm = DataFrame(confm, index=columns, columns=columns)
1802
```

```
pretty_plot_confusion_matrix(df_cm, fz=fz, cmap=cmap,
1803
       fiqsize=fiqsize, show_null_values=show_null_values,
       pred_val_axis=pred_val_axis)
1804
1805
1806
1807
1808
      #TEST functions
1809
1810
      def _test_cm():
1811
          #test function with confusion matrix done
1812
          array = np.array([[13, 0, 1, 0,
1813
                              [ 0, 50, 2,
                                                      0],
                                            0, 10,
1814
                              [ 0, 13, 16,
                                            0, 0,
                                                      3],
1815
                              [ 0, 0, 0, 13,
                                                      0],
                                                 1,
1816
                              [0,40,0,
                                            1, 15,
                                                      0],
1817
                              [0, 0, 0,
                                            0, 0, 20]])
1818
          #get pandas dataframe
1819
          df_cm = DataFrame(array, index=range(1,7), columns=range(1,7))
1820
          #colormap: see this and choose your more dear
1821
          cmap = 'Oranges'
1822
          pretty_plot_confusion_matrix(df_cm, cmap=cmap)
1823
1824
1825
      def _test_data_class():
1826
          """ test function with y_test (actual values) and predictions
1827
       (predic) """
          #data
1828
          y_{test} = np.array([1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5,
1829
       1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5,
    \rightarrow 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5,
      1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5,
    \rightarrow 1,2,3,4,5])
```

```
predic = np.array([1,2,4,3,5, 1,2,4,3,5, 1,2,3,4,4, 1,4,3,4,5,
1830
      1,2,4,4,5, 1,2,4,4,5, 1,2,4,4,5, 1,2,4,4,5, 1,2,3,3,5, 1,2,3,3,5,
    \rightarrow 1,2,3,4,4, 1,2,3,4,1, 1,2,3,4,1, 1,2,3,4,1, 1,2,4,4,5, 1,2,4,4,5,
    \rightarrow 1,2,4,4,5, 1,2,4,4,5, 1,2,3,4,5, 1,2,3,4,5, 1,2,3,4,5,
      1,2,3,4,5])
          0.00
1831
            Examples to validate output (confusion matrix plot)
1832
                                                   3
              actual: 5 and prediction 1
1833
              actual: 2 and prediction 4
                                                   1
                                               >>
1834
              actual: 3 and prediction 4
                                               >> 10
1835
          0.00
1836
          columns = []
1837
          annot = True;
1838
          cmap = 'Oranges';
1839
          fmt = '.2f'
1840
          lw = 0.5
1841
          cbar = False
1842
          show_null_values = 2
1843
          pred_val_axis = 'y'
1844
          #size::
1845
          fz = 12;
1846
          figsize = [9,9];
1847
          if(len(y_test) > 10):
1848
              fz=9; figsize=[14,14];
1849
          plot_confusion_matrix_from_data(y_test, predic, columns,
1850
            annot, cmap, fmt, fz, lw, cbar, figsize, show_null_values,
1851
        pred_val_axis)
1852
1853
1854
1855
      #MAIN function
1856
1857
      if(__name__ == '__main__'):
1858
          print('__main__')
1859
```

```
print('_test_cm: test function with confusion matrix done\nand

pause')

test_cm()

plt.pause(5)

print('_test_data_class: test function with y_test (actual

values) and predictions (predic)')

test_data_class()
```

Alphabetic	List	of	Variables	and	Att
# Variable Type Format Description					
2 action type Char 17 The	type	of	shot	that	was
28 arena temp Num BEST12. The	average	temperature	in	the	areı
27 attendance Num BEST12. The	number	of	people	attending	the
29 avgnoisedb Num BEST12. The	average	noise	(in	decibels)	dur
3 combined_shot_type Char 9 The	type	of	combined	shot	tha
23 game_date Num MMDDYY10. The	date	that	the	game	occ.
4 game_event_id Num BEST12. The	id	of	the	specific	eve
5 game id Num BEST12. The	id	of	the	specific	gan
6 lat Num BEST12. The	location	(in	latitude)	of	$_{ m the}$
7 loc x Num BEST12. The	X	coordinate	of	the	sho
8 loc y Num BEST12. The	У	coordinate	of	the	sho
9 lon Num BEST12. The	location	(in	longitude)	of	the
24 matchup Char 11 The	matchup	of	the	two	tear
10 minutes_remaining Num BEST12. The	number	of	minutes	remaining	in
25 opponent Char 3 The	NBA	abbreviation	of	the	opp
11 period Num BEST12. The	period	of	the	game	in
12 playoffs Num BEST12. Whether	or	not	the	game	was
1 recId Num BEST12. The	unique	id	of	the	obs
13 season Num YYYYYY The	YearYr	indicator	of	the	gan
14 seconds_remaining Num BEST12. The	$\operatorname{number}$	of	seconds	remaining	in
in	which	the	shot	attempt	occ.
15 shot_distance Num BEST12. The	distance	of	the	shot	$\operatorname{atte}$
26 shot_id Num BEST12. The	id	of	the	specific	sho
16 shot_made_flag Num BEST12. Whether	or	not	the	shot	$\operatorname{atte}$
17 shot_type Char 14 The	technical	$\operatorname{term}$	for	the	typ
18 shot_zone_area Char 21 The	zone	location	on	the	cou
19 shot_zone_basic Char 21 The	approximate	zone	location	on	the
Restricted Area)					
20 shot_zone_range Char 15 The	distance	range	in	feet	of
21 team_id Num BEST12. NBA	league	team	$\operatorname{id}$		
22 team_name Char 18 NBA	league	team	name		

## Bibliography

- $[1] \begin{tabular}{ll} Sports & Analytics & Market Sports & Analytics & Market & Research & Firm, \\ www.markets.andmarkets.com/Market-Reports/sports-analytics-market- \\ 35276513.html. \\ \end{tabular}$
- [2] Confusion Matrix Pretty Print: Wagner Cipriano, https://github.com/wcipriano/pretty-print-confusion-matrix/blob/master/confusion\_ $matrix_pretty_print.py$