# HUDK 4051: ANAIYTICS: PROCESS & THORY

#### Events



https://www.eventbrite.com/e/wids-columbia-university-new-york-tickets-92889798889

**Date And Time** 

Fri, March 6, 2020 3:00 PM – 6:00 PM EST

Date And Time

Sat, March 7, 2020 9:00 AM – 6:00 PM EST



**Smart Cities Center** 

https://www.eventbrite.com/e/nyc-school-of-data-2020-tickets-92389440303

**March 11** | 7:00PM-9:00PM

Mudd: Room 407

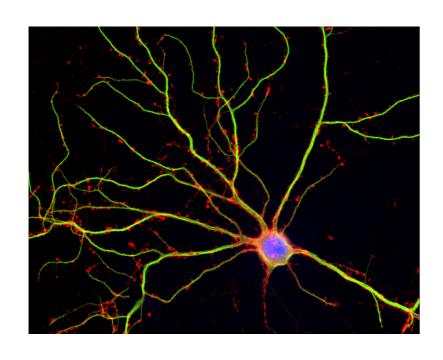


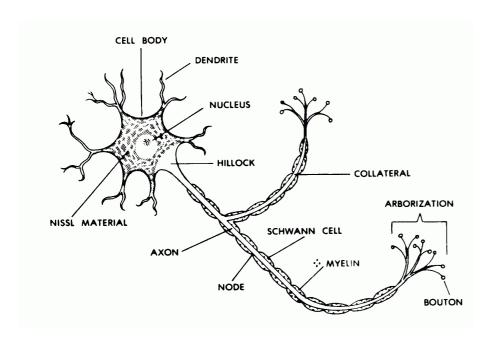
https://www.eventbrite.com/e/poster-session-smart-cities-center-tickets-92729280775? utm\_source=sendinblue&utm\_campaign=Events\_Weekly\_February\_18\_2020&utm\_medium=email

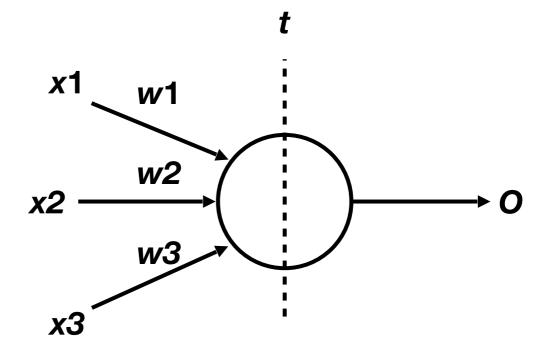
March 10-11
OECD Event on the Future of Data in Ed
Volunteer, email me

#### Today

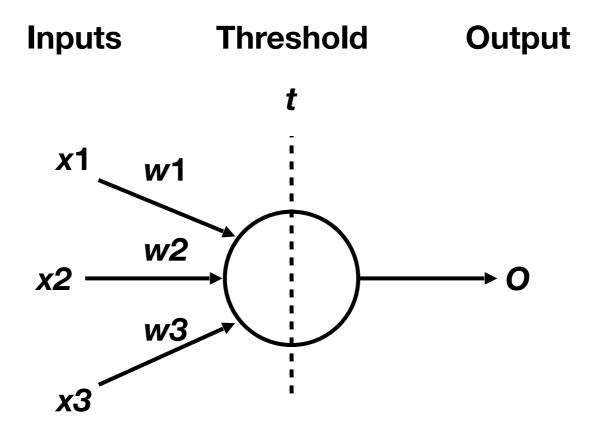
- Artificial Neural Networks
  - Perceptron
  - Sigmoid Function
  - Back propagation

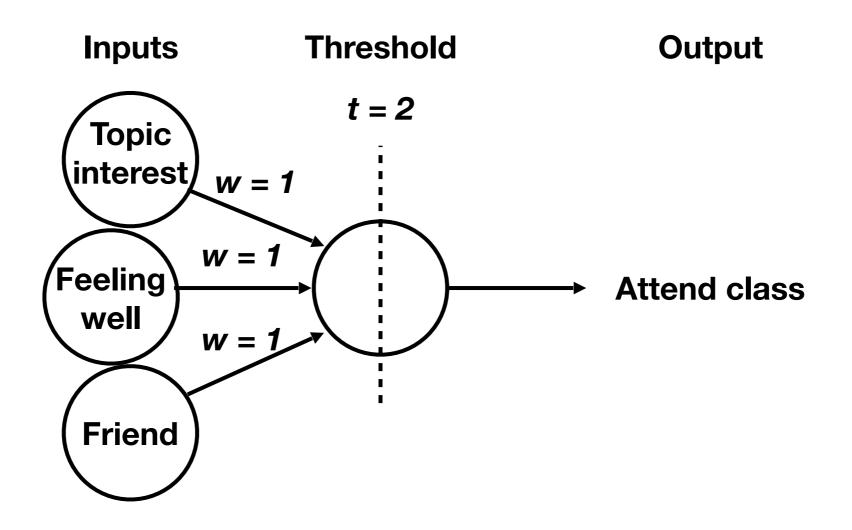






Frank Rosenblatt, 1957





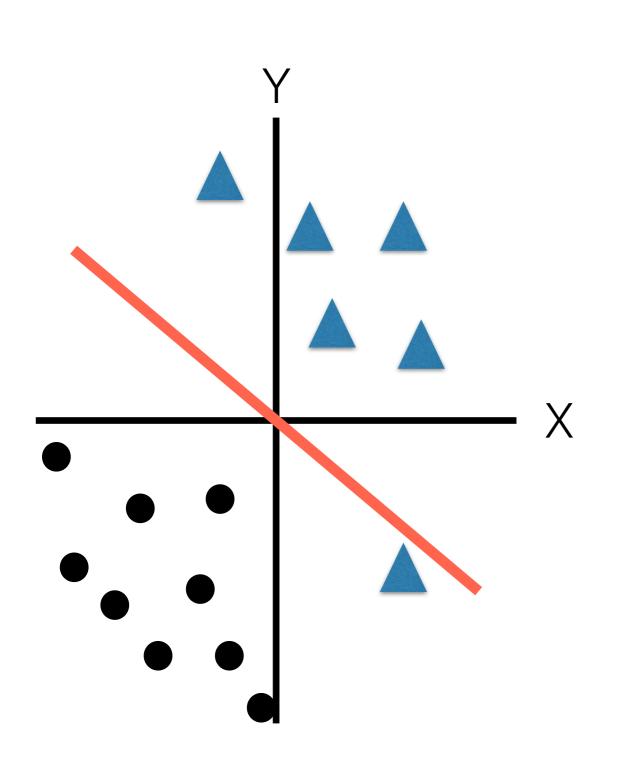
#### Bias (Threshold)

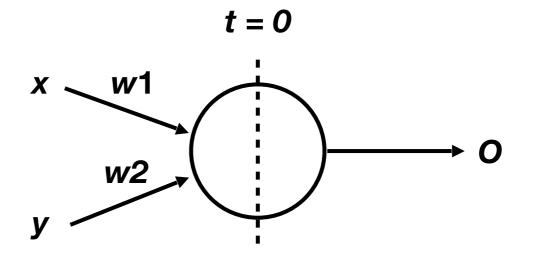
- Another way to describe the threshold
- Negative threshold
- More convenient for notation
- Describes how easy it is to get make the perceptron "fire"

#### Logic

- From the perceptron we can create a NAND gate
- From a NAND gate can create all other logic units (AND, NOR, etc.)
- See Nielson 2016\*

# Notation Example

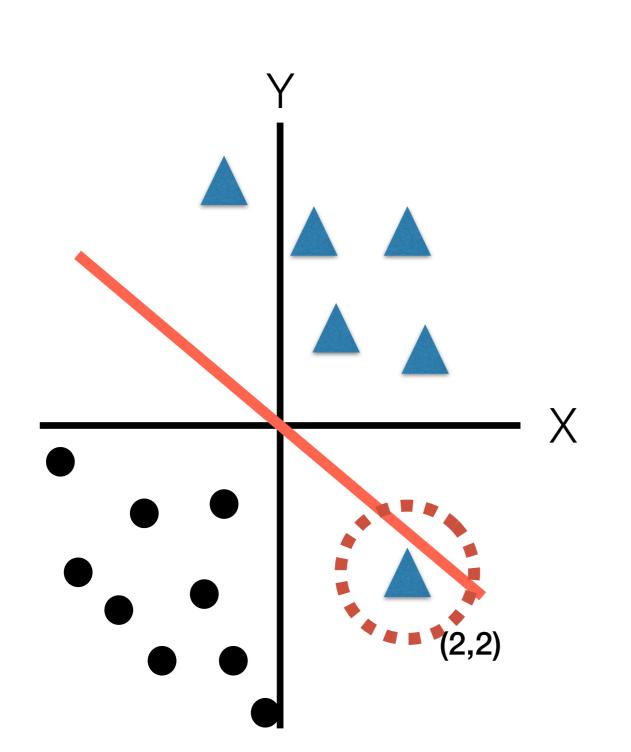




inputs	weights
1	0
$\mathcal{X}$	1
y	0.5

= 1 x 0 + 1 x 
$$x$$
 + 0.5 x  $y$   
=  $x$  + 0.5 $y$   
=  $x$  -2 $y$ 

#### Updating

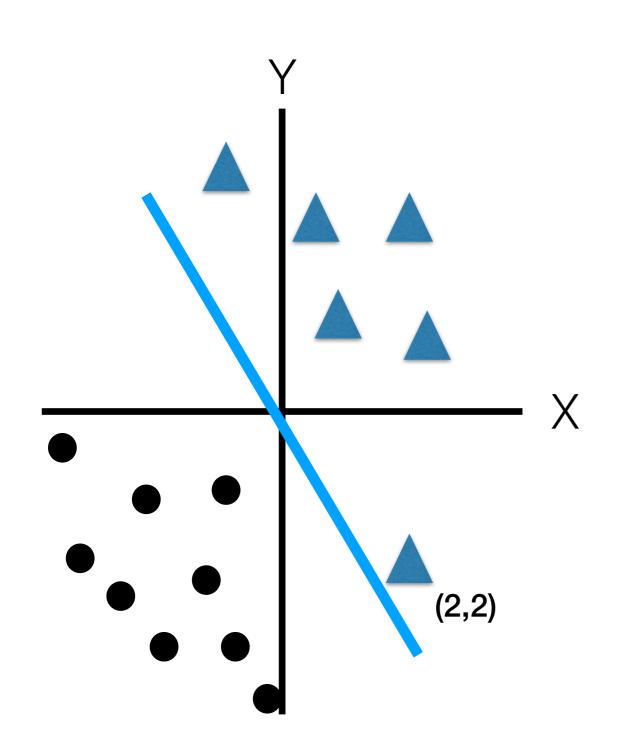


inputs	weights
1	0
$\mathcal X$	1
y	0.5

= 1 x 0 + 1 x 
$$\times$$
 + 0.5 x  $y$   
=  $\times$  + 0.5 $y$   
=  $\times$  -2 $y$ 

For each misclassified point update w:

### Updating



inputs	weights	new w
1	0	-0.2
$\mathcal{X}$	1	0.6
y	0.5	0.9

$$= -2/3x + 2/9$$

#### For each misclassified point update w:

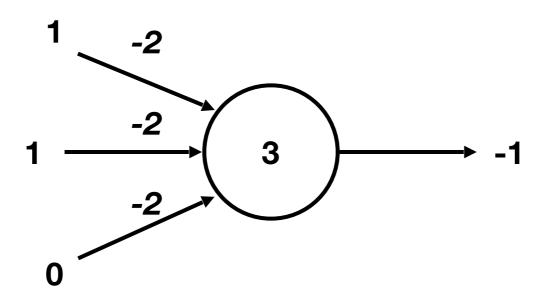
WNEW = WOLD + 
$$Ndx$$

Learning inputs

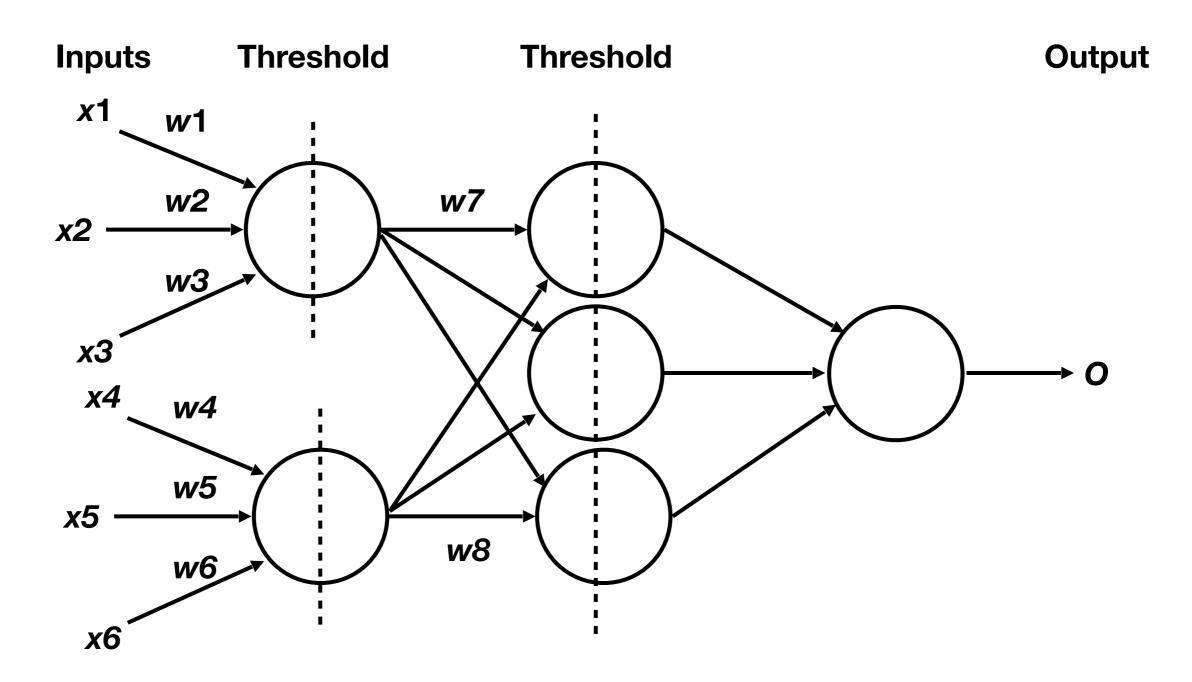
Rate Re-classification (1 or -1)

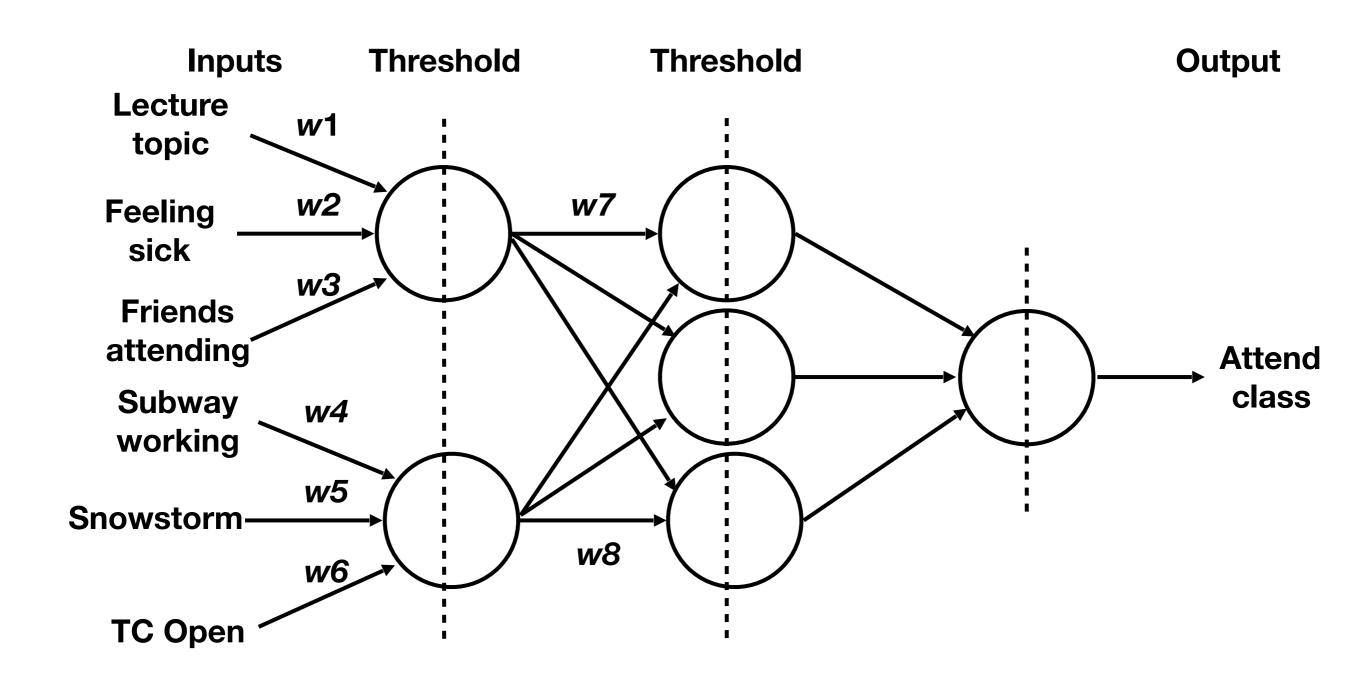
#### Notation

Inputs Bias Output



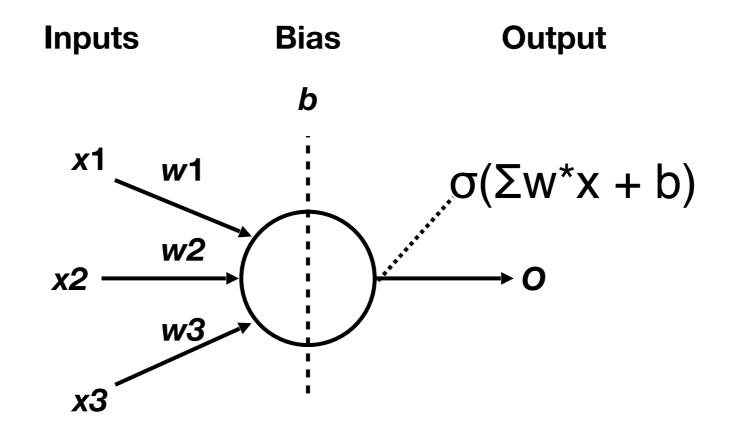
$$(1)^*-2 + (1)^*-2 + (0)^*-2 + 3 = -1$$





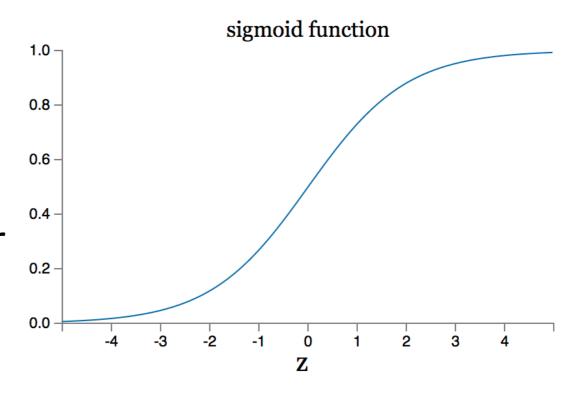
# Activity

- Want to build a learning algorithm
- Could change b or w
- BUT that will cause very large changes
- Network will never "fix"
- Solution: "smooth" the output



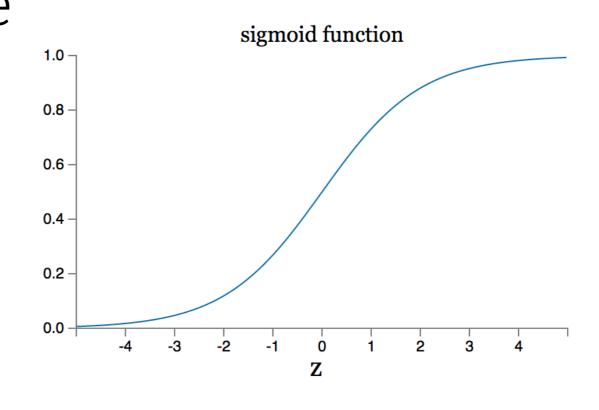
- Sigmoid function
   "smooths" the output
- Makes changing w
   and b less sudden and
   more predictable
- Could use lots of other functions...

$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}.$$

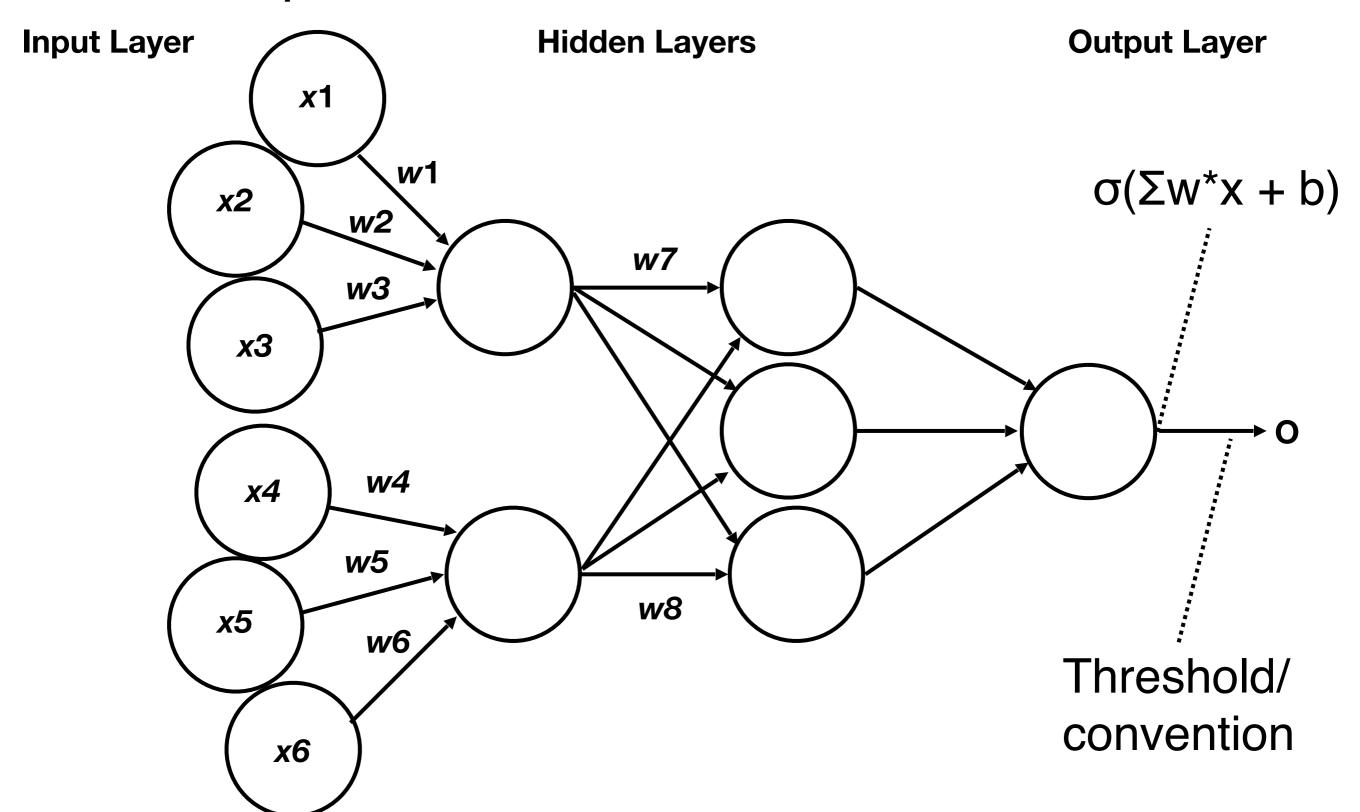


- Perceptrons have 0/1 output
- Sigmoid neurons have
  0 1 output (eg. 0.1,
  0.6778, etc.)
- How to interpret sigmoid neuron output?

$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}.$$



#### Complete Feedfoward Network



#### How many Hidden Layers?

- No foolproof method
- The only method is really trial and error
- Heuristics:
  - Theory based starting point?
  - Number of inputs and outputs?

# Exercise

#### Back Propagation

- Need a way to minimize error
- Error is defined by a cost function
- Then we imagine error as a surface that needs to be "searched" for the minimum

Weight