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#### STA427 FS2021

Statistical Methods in Infectious Disease Epidemiology Epidemiology, Biostatistics and Prevention Institute University of Zurich, Switzerland



#### Outline

- Monitoring of univariate count data time series
  - Statistical Framework for Aberration Detection
  - Simple Algorithm for Ad-Hoc Detection
  - Farrington algorithm and beyond
- Multivariate Methods
  - Univariate Methods in Parallel
  - Kulldorff's scan statistic
  - Case Study: Meningococcal disease in Germany
- A System for Automated Outbreak Detection
- Discussion

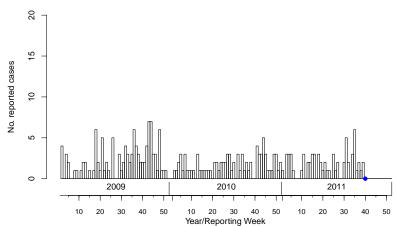
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Monitoring count time series •00000000000000

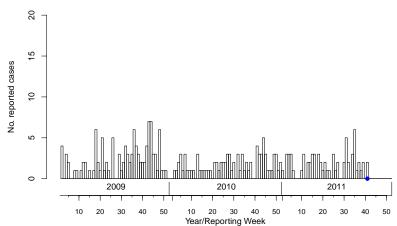
### Example: Monitoring German Salmonella Newport Cases

German Infection Protection Act (IfSG) data from the Robert Koch Institute (up to W40-2011):



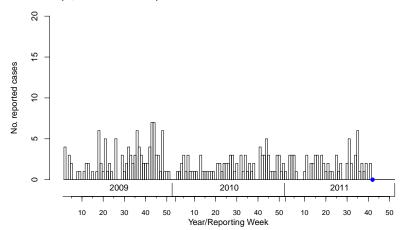
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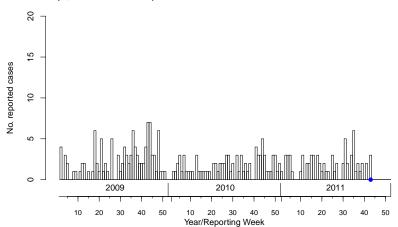
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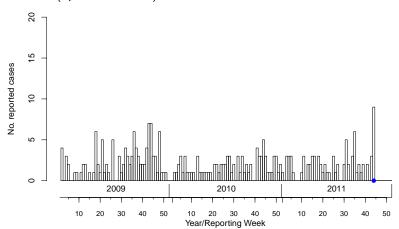


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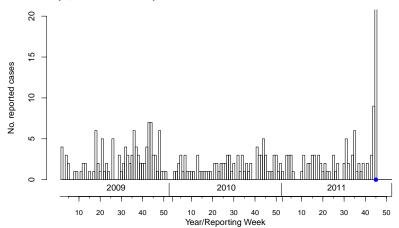


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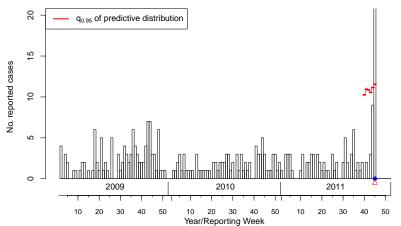
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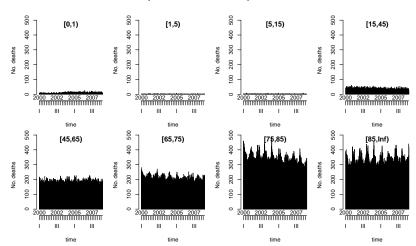
During Oct-Nov 2011 there was an outbreak associated with mung bean sprouts (RKI 2012)

# Example – The EuroMOMO project (1)

- European monitoring of excess mortality for public health action (EuroMOMO)
- Aim: develop and strengthen real-time monitoring of mortality across Europe in order to enhance the management of serious public health risks such as pandemic influenza, heat waves and cold snaps
- Main outcome of mortality monitoring: excess mortality
- In this course: Focus on monitoring aspect

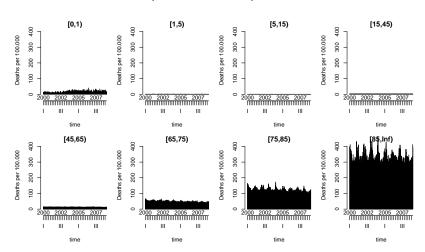
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Weekly danish mortalities 2000-2008 in 8 age-groups as provided by Statens Serum Institute (Höhle et al. 2010).



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Monitoring count time series

- Univariate time series  $\{y_t, t = 1, 2, ...\}$  to monitor
- For each time *t* we differentiate between two underlying states: in-control (everything is fine) or out-of-control (something is wrong).
- At time  $s \ge 1$ , the available information is  $y_s = \{y_t ; t \le s\}$ .
- Based on  $y_s$  an automatic detection procedure has to decide if there is unusual activity at time s (or not).

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# Statistical Framework for Aberration Detection (2)

- The detectors are initially only based on the one-step-ahead predictive distribution at each time point (Shewhart-like control chart):
  - Let  $G(y_s|y_1,\ldots,y_{s-1};\theta)$  be the distribution of  $Y_s$  in case everything is in-control
  - If the actual observed value  $Y_s = y_s$  is extreme in G, this is evidence against things being in-control.
  - The alarm threshold  $a_{1-\alpha,s}$  at each time point is calculated as the  $(1-\alpha)$ 'th quantile of the predictive distribution. If  $y_s>a_{1-\alpha,s}$  then we have an alarm
- This can be generalized to more sequential control charts accumulating information, e.g. cumulative sum (CUSUM) methods.

Monitoring count time series

#### Intermezzo: Estimation, prediction and uncertainty

- Data y are the observed value of a random variable Y characterized by a parametric model with density  $f(y; \theta)$ .
- Aim: predict the value of a random variable Z, which, conditionally on Y = y has distribution function  $G(z|y;\theta)$ , depending on  $\theta$ .
- Simplest form of the prediction problem:

$$Y_1, \ldots, Y_n \stackrel{\text{iid}}{\sim} f(y; \theta),$$

and the task is to predict  $Z = Y_{n+1}$ .

• In time series 1-step-ahead prediction the observations are correlated and the aim is to predict  $Z = Y_{n+1}$ .

# Example: Predicting a new $N(\mu, \sigma^2)$ observation (1)

• Let  $Y_1, \ldots, Y_n \stackrel{\text{iid}}{\sim} \mathcal{N}(\mu, \sigma^2)$  with unknown  $\mu$  and  $\sigma^2$ . Then

$$\frac{Y_{n+1}-\overline{Y}}{s\sqrt{1+\frac{1}{n}}}\sim t(n-1),$$

where  $\overline{Y} = \frac{1}{n} \sum_{i=1}^{n} Y_i$  and  $s^2 = \frac{1}{n-1} \sum_{i=1}^{n} (Y_i - \overline{Y})^2$  are the sample mean and sample variance of **Y**, respectively.

• A  $(1-2\alpha)\cdot 100\%$  two-sided **prediction interval** (PI) is thus given by

$$\overline{Y} \pm t_{1-\alpha}(n-1) \cdot s \cdot \sqrt{1+\frac{1}{n}}$$
.

# Example: Predicting a new $N(\mu, \sigma^2)$ observation (2)

• A plug-in  $(1-2\alpha) \cdot 100\%$  two-sided **prediction interval** for  $Y_{n+1}$  is:

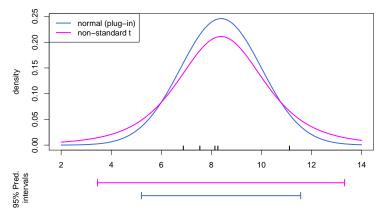
$$\overline{Y} \pm z_{1-\alpha} \cdot s$$
.

• Both of these are not to be confused with a  $(1-2\alpha)\cdot 100\%$ two-sided **confidence interval** for  $\mu$ :

$$\overline{Y} \pm z_{1-\alpha} \cdot \frac{s}{\sqrt{n}}$$
.

## Example: Predicting a new $N(\mu, \sigma^2)$ observation (3)

• Illustration: PIs based on n=5 observations from  $N(\mu, \sigma^2)$ .



• For n = 5 the 95% plug-in PI corresponds to a 85% PI. The 95% CI for  $\mu$  is 7.2–9.6, which only corresponds to a 46% PI.

## Summary: Ad-Hoc Outbreak Detection Algorithm

- Predict value  $y_s$  at time  $s = (s^w, s^y)$  using a set of reference values from window of size 2w + 1 up to b years back.
- Let n = b(2w + 1) and compute threshold as the upper 97.5% quantile of the predictive distribution for  $y_s$ , i.e.

$$a_{0.975,s} = \overline{y} + t_{0.975}(n-1) \cdot s \cdot \sqrt{1 + \frac{1}{n}}.$$

• Sound alarm, if  $y_s > a_{0.975.s}$ .

## Challenges of surveillance data

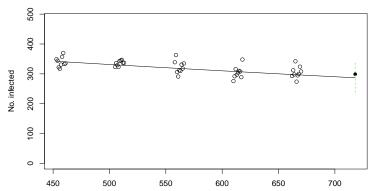
Issues making the statistical modelling and monitoring of surveillance time series a challenge:

- Lack of clear case definitions
- Under-reporting and reporting delays
- Often no denominator data
- Seasonality
- Low number of reported cases
- Presence of past outbreaks
- Existence of concurrent "explanatory" processes

Monitoring count time series

• Predict value  $y_s$  at time  $s = (s^w, s^y)$  using a set of reference values from window of size 2w + 1 up to b years back.

#### Prediction at time t=718 with b=5,w=4



• Fit overdispersed Poisson generalized linear model (GLM) to the b(2w+1) reference values where  $\mathrm{E}(y_t)=\mu_t$ ,  $\mathrm{Var}(y_t)=\phi\cdot\mu_t$  with  $\log\mu_t=\alpha+\beta t$  and  $\phi>0$ .

## Farrington algorithm (2) – outbreak detection

#### Predict and compare:

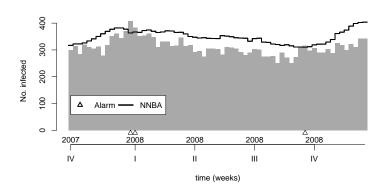
- An approximate  $(1-\alpha)$  one-sided prediction interval for  $y_s$  based on the GLM has upper limit  $a_{1-\alpha,s} = \hat{\mu}_s + z_{1-\alpha} \cdot \sqrt{\operatorname{Var}(y_s - \hat{\mu}_s)}$
- If the oserved  $y_s$  is greater than  $a_{1-\alpha,s}$ , then flag s as outbreak

#### Refinements of the algorithm include:

- Computation of the prediction interval on a transformed scale
- Use a re-weighted fit with weights based on Anscombe residuals in order to correct for outliers
- Low count protection

# Application: Danish mortality data (age group 75-84 years)

• Results of the Farrington algorithm, respectively, with w = 4, b = 5and  $\alpha = 0.005$  starting at W40-2007:



## •

- 2 Multivariate Methods
  - Univariate Methods in Parallel
  - Kulldorff's scan statistic
  - Case Study: Meningococcal disease in Germany
- 3 A System for Automated Outbreak Detection
- 4 Discussion

## Setup

- Instead of a univariate time series  $\{Y_t; t=1,2,\}$  as in the previous section the observation at each time point consists of a *p*-variate vector  $\mathbf{Y}_t = (Y_{t,1}, Y_{t,2}, \dots, Y_{t,p})'$
- Each component  $Y_{t,i}$  could represent the disease incidence (as a count) of a given region/age-group/gender/serotype/pathogen combination at time t
- Aim is to monitor the *p* time series simultaneously. The hope is that this gains strengths to detect vague signals

#### Univariate Methods in Parallel

- Simple approach for multiple data streams is to use one of the univariate methods from the previous section to each time series
- Pros:
  - Easy to use, scales linearly
  - Can aggregate results in suitable fashion
- Cons:
  - False positive probability per time point is  $\alpha$  per series so probability of raising at least one false alarm will be much greater than  $\alpha$  (multiple testing).
  - ullet If one uses a small lpha this might make outbreaks harder to detect.

- Kulldorff (2001) proposed a method for prospective spatio-temporal detection in spatial time series data
- The method assumes that

$$Y_{it} \sim \text{Po}(q_{it} \cdot b_{it}),$$

where  $b_{it}$  is an 'expected count' proportional to the population at risk in region i at time t.

- Note:  $q_{it} > 0$  is assumed to be the same  $q_{it} = q$  for all i and t provided there is no outbreak (null hypothesis)
- However, for areas with outbreaks the relative risk is higher inside a space-time window  $W = Z \times \{T D + 1, \dots, T\}$ , consisting of a subset of regions  $Z \subset \{1, \dots, N\}$  and stretching over the D most recent time periods.

# Kulldorff's prospective scan statistic (2)

- Focus of the method: what W and D combination gives the greatest discrepancy from null-hypothesis?
- Contrast this with the distribution of such a maximum under the null-hypothesis in order to get P-values,
  - ① calculate the MLE of  $q_W$  and  $q_{\overline{W}}$ .
  - 2 calculate the likelihood ratio of W between  $H_0$  and  $H_1$
  - ullet calculate likelihood ratio  $\lambda_W$  for all W of interest
  - the scan statistic is defined  $\lambda^* = \max_W \lambda_W$ . The corresponding window  $W^*$ , often called the most likely cluster
  - $\bullet$  calculate the p-value for  $W^*$  and flag alarm if below threshold

# Step 1

• Estimation of  $q_W$  and  $\hat{q}_{\overline{W}}$ 

$$\hat{q}_W = rac{Y_W}{B_W},$$

$$\hat{q}_{\overline{W}} = rac{Y - Y_W}{B - B_W} = rac{Y_{\overline{W}}}{B_{\overline{W}}},$$

where

$$Y_W = \sum_{(i,t) \not\in W} y_{it}, B_W = \sum_{(i,t) \in W} b_{it}, \text{ and}$$
 $Y = \sum_{i=1}^{N} \sum_{t=1}^{T} y_{it} = \sum_{i=1}^{N} \sum_{t=1}^{T} b_{it}.$ 

ullet Thus, the likelihood ratio statistic conditional on the window W is then given by

$$\lambda_W = \left\{ \begin{array}{ll} \left(\frac{Y_W}{B_W}\right)^{\!\!Y_W} \!\! \left(\frac{Y-Y_W}{Y-B_W}\right)^{\!\!Y-Y_W} & \text{if } Y_W > B_W, \\ 1 & \text{otherwise} \end{array} \right.$$

up to a multiplicative constant not dependent on  $q_W$  or  $q_{\overline{W}}$ .

- No closed formula available for the distribution of  $\lambda^*$
- Instead: Monte Carlo where new data for each region i and time t
  are simulated under the null hypothesis using the expected counts
  b<sub>it</sub>.
- For Kulldorff's scan statistic, the sampling is made conditional on the total observed count Y = C, leading to a multinomial distribution
- Sampling is repeated R times. A Monte Carlo P-value for the observed scan statistic is given by its rank among the simulated values:

$$P = \frac{1 + \sum_{r=1}^{R} 1\{\lambda_r^* > \lambda_{obs}^*\}}{1 + R}.$$

- Typically, a number such as R = 999 or R = 9999 is used in order to get a fixed number of digits for the P-value.
- Note: As for univariate investigations one has a multiple testing problem, because one repeats the analyses for every time point

#### **Implementation**

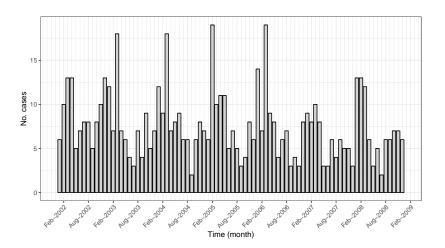
- Kulldorff's scan statistic is implemented in the R package rsatscan, which is just a call-through to the SaTScan™ program
- A true open-source alternative is the function scan\_pb\_poisson in the package scanstatistics

# Case Study: Meningococcal disease in Germany (1)

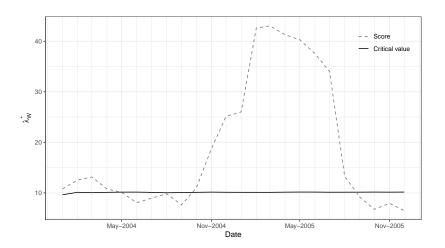
- Application of Kulldorff's prospective scan statistic to German Meningococcal data aggregated to monthly counts for each of Germany's 413 districts
- We show the resulting scan statistics for each month of the study period (2004–2005). At each time step, the statistic was calculated using at most the latest 6 months of data
- The  $b_{it}$  for each district and time point was estimated as

$$\hat{b}_{it} = \frac{Y}{T} \cdot \frac{\mathsf{Pop}_i}{\mathsf{Pop}_{\mathsf{total}}}.$$

## Case Study: Meningococcal disease in Germany (2)



# Case Study: Meningococcal disease in Germany (3)



## Case Study: Meningococcal disease in Germany (4)

 The core cluster consists of four districts in North Rhine-Westphalia, one of them the city Aachen



## Case Study: Meningococcal disease in Germany (5)

- An issue with the scan statistic might be that it is ill-suited for data with an abundance of zeros as the Meningococcal data
- For this type of data, a scan statistic based on e.g. the zero-inflated Poisson distribution (see Allévius et al. 2019) may perform better

#### Outline

- Monitoring of univariate count data time series
- 3 A System for Automated Outbreak Detection

## System Design

 Salmon et al. (2016) describes a system integrating outbreak detection algorithms into the epidemiological workflow

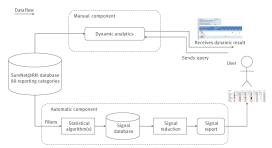
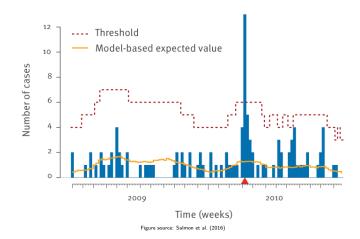


Figure source: Salmon et al. (2016)

 Example of using machine learning methods for the more than 30,000 time series

### Application on Salmonella Montevideo 2009-2010

Results from the extended Farrington procedure using last five years as reference values:



#### Salmonella Report for W41–46 of 2013

#### Weekly Report at National Level:

Serotype	Week 41				Week 42				Week 43				Week 44				Week 45				Week 46			
	Уt	ot	μŧ	Ut	Уt	Ot	$\mu_t$	Ut	Уt	ot	μŧ	Ut	Уt	Ot	μt	Ut	Уt	Ot	μŧ	Ut	Уt	ot	μŧ	Ut
Salmonella, all serotypes	466	27	512	691	373	23	485	650	370	16	461	620	356	15	439	601	411	8	417	580	290	14	390	540
S. Typhimurium	107	2	151	221	103	1	145	214	108	2	140	208	106	5	134	202	142	4	127	191	90	4	120	181
S. Enteritidis	158	11	154	230	123	12	142	212	115	11	131	194	84	4	124	189	80	1	116	182	62	2	107	168
S. Infantis	25	6	9	18	16	3	8	17	8	1	8	18	10	-	8	17	2	-	7	17	5	-	7	16
S. Derby	4	NA	5	11	2	NA	5	11	7	NA	5	11	3	NA	5	11	4	NA	5	11	1	-	5	11
S. Manhattan	7	NA	0	2	4	NA	0	2	4	NA	0	2	3	NA	0	2	3	NA	0	2	NA	NA	0	2
S. Typhimurium, monophasic	2	NA	0	2	2	NA	0	2	2	NA	0	2	6	NA	0	2	5	NA	0	3	3	NA	0	3
S. Agona	2	NA	1	4	7	4	1	4	2	1	1	4	3	2	1	4	1	NA	1	4	3	2	1	4
S. Virchow	4	NA	3	8	1	NA	3	8	3	NA	3	7	1	NA	3	7	5	1	3	7	1	NA	3	7
S. Muenchen	3	NA	1	4	3	NA	1	4	NA	NA	1	4	3	NA	1	4	2	NA	1	4	NA	NA	1	4

Table source: Salmon et al. (2016)

#### Outline

- Monitoring of univariate count data time series

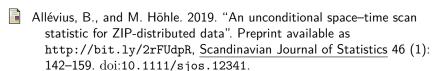
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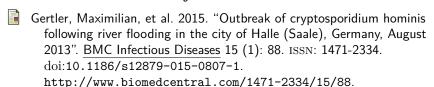
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#### Discussion

- The presented methods are implemented in the R package surveillance (Salmon et al. 2016)
- Developing, maintaining and improving automatic outbreak detection systems is an interdisciplinary activity!
  - Even more work could be put into user adaptation.
  - Delay adjusted monitoring (Salmon et al. 2015)
- The system proved to be a good insurance against missing anything important – see e.g. Gertler et al. (2015)

#### Literature I





Höhle, M., and A. Mazick. 2010. "Aberration detection in R illustrated by Danish mortality monitoring". In <u>Biosurveillance: A Health Protection Priority</u>, ed. by T. Kass-Hout and X. Zhang, 215–238. CRC Press. https://staff.math.su.se/hoehle/pubs/hoehle\_mazick2009-preprint.pdf.

#### Literature II

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  - Journal of the Royal Statistical Society Series a-Statistics in Society 164:61–72.
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- Salmon, M., D. Schumacher, K. Stark, and M. Höhle. 2015. "Bayesian outbreak detection in the presence of reporting delays". http://dx.doi.org/10.1002/bimj.201400159, Biometrical Journal 57 (6): 1051–1067.