

Exercise sheet 5: A model for the maintenance of sexual reproduction

Sex, Ageing and Foraging Theory

In exercise sheet 4, you investigated evolution at L loci under purifying selection in: a population composed of asexual individuals (specifically where the probability σ of reproducing sexually was fixed to zero for all individuals, $\sigma = 0$); and a populations of sexuals (where $\sigma = 1$ for all individuals). Here, we extend this model to investigate when asexuality can and cannot invade a population of sexuals. To do so, we allow for the probability σ of reproducing sexually to also evolve, i.e. each individual i now has a probability σ_i of reproducing sexually. Each haploid individual is thus characterised by $L + 1$ genetic loci: (1) one locus coding for the probability σ of reproducing sexually where two alleles segregate, one for sexual ($\sigma = 1$) and one for asexual reproduction ($\sigma = 0$); and (2) L loci under purifying selection, at each of which a wild type and deleterious mutation can segregate (as in Ex sheet 4).

The life cycle is composed of five steps. (1) First, each adult female i either reproduces sexually with probability σ_i or asexually with probability $1 - \sigma_i$ according to her allele at the locus for sexual reproduction. If a female reproduces sexually, it mates at random with a male in the population. (2) Each female produces a Poisson-distributed number of offspring with mean f_0 . Before mutation, an offspring produced asexually is an exact copy of its parent (e.g. if the parent has the allele for $\sigma = 0$ and 3 deleterious alleles at the L loci under purifying selection, its offspring also has the allele for $\sigma = 0$ and 3 deleterious alleles), while an offspring produced via sexual reproduction is a recombined version of its mother and father, assuming each locus segregates independently (i.e., at each locus, the inherited allele is a copy of the mother with probability $1/2$ or of the father with probability $1/2$). (3) Mutation from the neutral allele to the deleterious allele occurs with probability u at each of the L loci under purifying selection (we assume there is no constant mutation at the locus for sexual reproduction). (4) An offspring survives with a probability that depends on density-dependent competition and on the number of deleterious mutations it carries. Specifically, we assume that the probability ω_i that an offspring i with k_i deleterious mutations survives to adulthood is,

$$\omega_i = \frac{(1 - s)^{(k_i/K)^\epsilon}}{1 + \gamma n_t}, \quad (1)$$

when there are n_t adults in the population. There are two extra parameters compared to eq. (8) of Ex sheet 4 to capture epistasis (see item (b) below). When $\epsilon = 1$ and $K = 1$, we recover eq. (8) of Exercise Sheet 4. Finally, (5) all adults die and the surviving offspring of sexual females becomes an adult male with probability r , or an adult sexual female with probability $1 - r$, so that r is the sex ratio at birth (all offspring of asexual females are also asexual females).

An individual-based simulation program for the life-cycle above has been made available on the course website (lab-mullon.github.io/SAF). We start with 1000 sexual individuals that have no deleterious mutations (i.e. each individual carries the allele for $\sigma = 1$ and the wild-type allele at the L loci under purifying selection). We let the simulation run for 100 generations, which is enough time for the population to reach a distribution of deleterious

mutations that no longer changes very much over time. In the 100-th generation, a random sexual female becomes asexual, i.e. we change the allele σ_i from 1 to 0 for some random i . We let the simulation run for another 100 generations to observe if the asexual lineage invades the sexual resident population.

- a. Familiarise yourself with this program. Discuss the biological interpretation of line 133.
- b. Plot the survival probability ω_i as a function of the number k_i of deleterious mutations for different strengths of epistasis (e.g. with $\epsilon = 0, 0.5, 1, 10$, and 75) for a fixed value of $K = 50$. Do these plots again but for different K (e.g. with $K = 10, 50, 100$) with a fixed value of $\epsilon = 75$. Interpret these plots and use them to conjecture on the implications of epistasis for the maintenance of sexual reproduction.
- c. Run the simulation under no epistasis, $\epsilon = 1$ (and $K = 50$). Do this a few times recording relevant information about the population each replicate (remember it is a stochastic simulation so it is good to have a few replicates). Run the simulations also with high epistatic effects, $\epsilon = 75$. Do the results differ when $\epsilon = 1$ and $\epsilon = 75$? Does this fit with your expectations formulated in part (b)?
- d. Reduce the number L of loci under purifying selection from 200 to 100. Re-run simulations under strong epistasis, $\epsilon = 75$. What can you conclude from these simulations about the effects of the number of loci on the maintenance of sexual reproduction? Why?