

interference

According to Wikipedia, **autocorrelation** is the cross-correlation of a signal with itself. Having high autocorrelation values is not good for wireless signals as it increases interference. If you decide to be a wireless communication researcher in the future that deals with signals, you may face the following problem.

Consider a binary sequence $S = (s_1, \dots, s_N)$ where each $s_i \in \{1, -1\}$. The *off-peak autocorrelations* of S are defined as:

$$C_k(S) = \sum_{i=1}^{N-k} s_i s_{i+k} \quad (k = 1 \dots N-1)$$

and the *energy* of S is defined as:

$$E(S) = \sum_{k=1}^{N-1} C_k^2(S)$$

The problem is to assign values to the s_i such that $E(S)$ is minimized.

Just for general info, in the IEEE 802.11b standard, an 11-chip "Barker" (a researcher's name) sequence is used for the 1 and 2 Mbit/sec rates.

This sequence is $S = \{1, 1, 1, -1, -1, -1, 1, -1, -1, 1, -1\}$ of length $N = 11$ and it has the lowest autocorrelation values $C_k(S)$ for various k in $[1..10]$ which sum to $E(S) = 5$. This is the minimum possible $E(S)$ for a binary sequence of length $N = 11$. This makes for a more uniform spectrum, and better performance in the receivers.

So that you can quickly understand this problem, here are some intermediate computations:

$S = \{1, 1, 1, -1, -1, -1, 1, -1, -1, 1, -1\}$

$N = 11$

$C_1(S) = 0 \implies \text{squared} \implies 0$

$C_2(S) = -1 \quad 1$

$C_3(S) = 0 \quad 0$

$C_4(S) = -1 \quad 1$

$C_5(S) = 0 \quad 0$

$C_6(S) = -1 \quad 1$

$C_7(S) = 0 \quad 0$

$C_8(S) = -1 \quad 1$

$C_9(S) = 0 \quad 0$

$C_{10}(S) = -1 \quad 1$

--- +
 $E(S) = 5$

This sequence $S = \{1, 1, 1, -1, -1, -1, 1, -1, -1, 1, -1\}$ can be written in Run Length Notation (RLN). Each digit in the RLN indicates the number of consecutive elements with the same sign. There are **THREE consecutive +1s**, **THREE consecutive -1s**, **ONE +1**, **TWO consecutive -1s**, **ONE +1**, and finally **ONE -1**, so the RLN is "**331211**".

Note that if the number of consecutive elements are between [10, 11, ..., 35], use **one character [A, B, ..., Z] instead**. We guarantee you that you will not need to deal with 36 consecutive elements or more.

TASK

For each of the following subtasks, generate a string representing the sequence in RLN. The RLN strings will be printed in 11 lines in the order of the sub-task with each line for each subtask. **Save this file as interference.out1.1.**

Subtask 0 [0 points]

$$\text{Score} = \min(0, 10^{(5 / E(S))})$$

This is the sample input described above ($N = 11$). Output the RLN that represents bit string S that minimizes interference/energy $E(S)$ for $N = 11$.

Note that for this subtask (verify this by yourself): Giving RLN = "A2" in the first line of interference.out1.1 will give you score of 0.00 points for subtask 0, because the RLN sums to 12 (remember, A is 10) whereas this is a subtask for $N = 11$.

- RLN = "11111111111" => 1.03
- RLN = "A1" => 1.06
- RLN = "12341" => 1.24
- RLN = "111422" => 2.42
- RLN = "331211" => 10.00, the maximum possible.

Subtask 1 [10 points]

$$N = 20$$

$$\text{Score} = 10^{(26 / E(S))}$$

Subtask 2 [10 points]

$$N = 21$$

$$\text{Score} = 10^{(26 / E(S))}$$

Subtask 3 [10 points]

$$N = 27$$

$$\text{Score} = 10^{(37 / E(S))}$$

Subtask 4 [10 points]

$$N = 28$$

$$\text{Score} = 10^{(50 / E(S))}$$

Subtask 5 [10 points]

$N = 40$

$\text{Score} = 10^{(108 / E(S))}$

Subtask 6 [10 points]

$N = 50$

$\text{Score} = 10^{(153 / E(S))}$

Subtask 7 [10 points]

$N = 55$

$\text{Score} = 10^{(171 / E(S))}$

Subtask 8 [10 points]

$N = 77$

$\text{Score} = 10^{(366 / E(S))}$

Subtask 9 [10 points]

$N = 80$

$\text{Score} = 10^{(400 / E(S))}$

Subtask 10 [10 points]

$N = 100$

$\text{Score} = 10^{(722 / E(S))}$

SUBMISSION DETAILS

This is an **output-only** task, that is, all the test cases are available for you. You do not need to submit any program. Instead, submit only the necessary output. A sample **interference.out1.1** file (containing 11 lines) might look like:

```
331211
1
2
3
4
5
6
7
8
9
A
```

Of course, submitting this output will result in 0 credit being given. Before submission, you are required to gzip compress your file. To do so, use the **tar** command as follows:

```
tar -cvzf interference.tgz interference.out1.1
```

Submit only the compressed **.tgz** file to Mu Judge.

GRADING DETAILS

This is what the grader will do for each line of your output:

1. Convert the RLN in into bit string S (Each 0 is converted to -1).
2. Note that if the RLN is found to be invalid, i.e. the sum of individual digit values $\neq N$ for the subtask, your score for that subtask is automatically 0.
3. Evaluate the bit string using the $E(S)$ formula.
4. Evaluate your score using the marking scheme above and produce a total score for this task rounded to the nearest integer between 0 and 100.

Note that your output must **strictly follow** the output format as specified (e.g characters must be uppercase etc.). Otherwise you might risk getting a complete 0 for your entire submission even if only one line failed to follow the output format.