Testing for spatial autocorrelation in Stata*

Keisuke Kondo[†]

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Abstract

This paper introduces the new Stata command moransi, which allows users to easily compute global and local Moran's I statistics in Stata. The fundamental feature of the moransi command is that the spatial weight matrix is constructed internally within a sequence of the program code. The additional information required in the dataset to implement this command are the latitude and longitude of regions. This paper presents two applied examples of the moransi command to deepen the understanding of global and local spatial autocorrelation.

Keywords: moransi, Moran's I, Global indicators of spatial association, local indicators of spatial association, Spatial lag

1 Introduction

There is an increasing demand for spatial analysis using Stata among researchers, as the Stata version 15 newly released the Sp estimation commands in 2017 (StataCorp, 2023). The increasing availability of geographically disaggregated data and shapefile is making spatial analysis easier.

The objective of this paper is to introduce the novel Stata command, moransi, which facilitates the calculation of global and local Moran's I statistics (Moran, 1950; Anselin, 1995). In the literature on spatial statistical analysis, spatial autocorrelation constitutes a pivotal concept, which can be further categorized into two distinct classes. Primarily, global spatial autocorrelation quantifies the degree to which regions exhibit interdependence. The global Moran's I statistic is a principal statistical approach to test for spatial autocorrelation. Secondarily, the local Moran's I statistic is used to identify local spatial clusters in terms of local similarities to neighboring regions.¹

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[†]Research Institute of Economy, Trade and Industry. 1-3-1 Kasumigaseki, Chiyoda-ku, Tokyo, 100–8901, Japan. (e-mail: kondo-keisuke@rieti.go.jp).

¹The Getis–Ord $G_i^*(d)$ is also used to detect hot and cold spots as spatial outliers (Getis and Ord, 1992; Ord and Getis, 1995; Anselin, 1995). Kondo (2016) provides the Stata command, getisord, which calculates Getis–Ord $G_i^*(d)$ statistic.

The concept of local indicator of spatial association (LISA), which was initially proposed by Anselin (1995), establishes a coherent link between global and local Moran's I statistics. To illustrate, the global Moran's I statistic can be interpreted as the average of local Moran's I statistics for individual regions. As discussed later in two applied examples, this integration enables a coherent interpretation of local Moran's I statistics through the lens of the Moran scatterplot, such as high-high and low-low spatial clusters.

The moransi command facilitates the calculation of global and local Moran's I in Stata. Stata users may frequently encounter challenges when constructing a spatial weight matrix. For example, there are some helpful packages for Moran's I in Stata. Pisati (2001) provides the spatgsa command. Additionally, Jeanty (2010) offers the splagvar command. However, it should be noted that the use of these packages requires the exogenous inclusion of the spatial weight matrix.²

The fundamental feature of the moransi command is that the spatial weight matrix is constructed internally within a sequence of the program code. This method was originally employed by Kondo (2016). Although a disadvantage of this method is its computational inefficiency, which stems from the fact that the spatial weight matrix is constructed every time, automating the construction of the spatial weight matrix provides a more intuitive manipulability for users.

In order to execute the moransi command, it is necessary to provide the latitude and longitude in the dataset. Even in the absence of an adequate shapefile of the study area, the moransi command enables researchers to implement spatial analysis using the latitude and longitude of the regions. In the event that a dataset is missing coordinate information, a recent geocoding technique can be employed to add this information.

This paper presents two interesting and compelling examples of the moransi command. First, the moransi command can identify unemployment clusters in Japan using municipal unemployment rates. Second, the moransi command can capture residential clusters in the Tokyo metropolitan area using Grid Square Statistics from the population census in Japan. The present study utilizes elementary yet efficacious spatial analyses to ascertain that residential clusters are formed along urban railroads when combined with data from the rail network.

The rest of this paper is organized as follows. Section 2 explains details of spatial weight matrix and Moran's *I* statistic. Section 3 describes the moransi command. Section 4 offers two applied examples using the moransi command. Finally, Section 5 presents the conclusions.

2 Moran's *I*

Based on Cliff and Ord (1970), Anselin (1995), and Sokal et al. (1998), this section explains details of global and local Moran's I statistics.

²Stata version 15 or later offers the **spset** command, which facilitates keeping the consistency of the spatial weight matrix. On Stata version 14 or earlier, matching regional IDs between data and spatial weight matrix was not easy since regions with missing values were dropped in some situations.

2.1 Spatial weight matrix

The matrix that expresses spatial structure is called the spatial weight matrix, which plays an important role in spatial analysis. The spatial weight matrix W takes the following formula:

$$\boldsymbol{W} = \begin{pmatrix} 0 & w_{1,2} & w_{1,3} & \cdots & w_{1,n} \\ w_{2,1} & 0 & w_{2,3} & \cdots & w_{2,n} \\ w_{3,1} & w_{3,2} & 0 & \cdots & w_{3,n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ w_{n,1} & w_{n,2} & w_{n,3} & \cdots & 0 \end{pmatrix},$$

where diagonal elements take the value of 0, and the sum of each row takes the value of 1 (i.e., row-standardization). The spatial weight matrix is always row-standardized throughout the paper.

The spatial weight matrix is generally constructed from the contiguity or distance matrix. The interregional contiguity relationship is generally constructed from shapefiles. The distance matrix is easily obtained from longitude and latitude information. If transport network data is available, the spatial weight matrix can also be constructed using road distance or travel time between regions. In circumstances where adequate shapefiles are not available, this paper elects to utilize the distance matrix.³

Various types of spatial weight matrices are proposed in the literature. The moransi command deals with four types of spatial weight matrices.

The first case of power functional type is shown below:

$$w_{ij} = \begin{cases} \frac{d_{ij}^{-\delta}}{\sum_{j=1}^{n} d_{ij}^{-\delta}}, & \text{if } d_{ij} < d, \quad i \neq j, \quad \delta > 0, \\ 0, & \text{otherwise,} \end{cases}$$
 (1)

where δ is a distance decay parameter and d is a threshold distance.

The second case of the exponential type of spatial weight matrix is shown as follows:

$$w_{ij} = \begin{cases} \frac{\exp(-\delta d_{ij})}{\sum_{j=1}^{n} \exp(-\delta d_{ij})}, & \text{if } d_{ij} < d, \quad i \neq j, \quad \delta > 0, \\ 0, & \text{otherwise,} \end{cases}$$
 (2)

where δ is the distance decay parameter.

The third case considers a uniform weight for regions located within d km as follows:

$$w_{ij} = \begin{cases} \frac{I(d_{ij} < d)}{\sum_{j=1}^{n} I(d_{ij} < d)}, & \text{if } d_{ij} < d, \quad i \neq j, \\ 0, & \text{otherwise.} \end{cases}$$
(3)

³A commonly used spatial weight matrix is constructed by a contiguity matrix, whose element w_{ij} takes a value of 1 if two regions i and j share the same border and 0 otherwise. Note that the moransi command is limited to a distance-based spatial weight matrix.

where $I(d_{ij} < d)$ is the indicator function that takes the value of 1 if a bilateral distance between i and j, d_{ij} , is shorter than the threshold distance d and 0 otherwise.

The fourth case considers the k-nearest neighbor weight as follows:

$$w_{ij} = \begin{cases} \frac{I(d_{ij} \le d_{ij,(k)})}{\sum_{j=1}^{n} I(d_{ij} \le d_{ij,(k)})}, & \text{if } i \ne j, \\ 0, & \text{otherwise,} \end{cases}$$

$$(4)$$

where $I(d_{ij} \leq d_{ij,(k)})$ is the indicator function that takes the value of 1 if a bilateral distance between i and j, d_{ij} , is shorter than or equal to the distance of the kth nearest neighbor $d_{ij,(k)}$ and 0 otherwise.

2.2 Spatial weight matrix with weight variable

The degree of interregional dependence may vary according to economic relationships between regions even if a geographical distance is identical. It is possible to consider economic distance using an additional weight variable in the spatial weight matrix.

In line with the gravity equation (Anderson, 1979), values in origin and destination regions i and j are incorporated into the spatial weight matrix. For example, Molho (1995) uses employment size in destination region j as a weight variable when constructing the spatial weight matrix. It is noteworthy that the value of the origin region i is offset by the row-standardization.

In accordance with Kondo (2015b), the moransi command facilitates the incorporation of a weight variable v into the spatial weight matrix. The power functional form of the spatial weight matrix in Equation (1) is extended as follows:

$$w_{ij} = \begin{cases} \frac{v_j d_{ij}^{-\delta}}{\sum_{j=1}^n v_j d_{ij}^{-\delta}}, & \text{if } d_{ij} < d, \quad i \neq j, \quad \delta > 0, \\ 0, & \text{otherwise,} \end{cases}$$

where v_j is a value of weight variable v in region j.

Second, the exponential type of spatial weight matrix in Equation (2) is extended as follows:

$$w_{ij} = \begin{cases} \frac{v_j \exp(-\delta d_{ij})}{\sum_{j=1}^n v_j \exp(-\delta d_{ij})}, & \text{if } d_{ij} < d, \quad i \neq j, \quad \delta > 0, \\ 0, & \text{otherwise.} \end{cases}$$

Third, the binary type of spatial weight matrix in Equation (3) is extended as follows:

$$w_{ij} = \begin{cases} \frac{v_j I(d_{ij} < d)}{\sum_{j=1}^n v_j I(d_{ij} < d)}, & \text{if } i \neq j, \\ 0, & \text{otherwise.} \end{cases}$$

Fourth, the k-nearest neighbor type of spatial weight matrix in Equation (4) is extended as

follows:

$$w_{ij} = \begin{cases} \frac{v_j I(d_{ij} < d_{ij,(k)})}{\sum_{j=1}^n v_j I(d_{ij} < d_{ij,(k)})}, & \text{if } i \neq j, \\ 0, & \text{otherwise,} \end{cases}$$
(5)

Note that, in the context of the spatial econometric model, elements of the spatial weight matrix are assumed to be non-stochastic and exogenous (Anselin, 1988, 2006). The exogeneity assumption for the spatial weight matrix might be violated if a weight variable v_j is endogenous.

2.3 Global Moran's *I*

The formula of Moran's I is given by

$$I = \frac{\sum_{i=1}^{n} \sum_{j=1}^{n} w_{ij} z_{i} z_{j}}{\sum_{i=1}^{n} z_{i}^{2}},$$
(6)

where n is the number of regions, z_i is the value of region i of variable z, which is standardized or centered to the mean, and w_{ij} is the ijth element of the row-standardized spatial weight matrix W. This formula can be expressed using the matrix form as follows:

$$I = \frac{z^{\top} W z}{z^{\top} z}. (7)$$

Note again that W is a row-standardized spatial weight matrix.

Moran's I lies within the range [-1,1].⁴ When values in the variable z are randomly distributed in space, the statistic asymptotically tends to zero. When a positive (negative) value of Moran's I is observed, this indicates that positive (negative) spatial autocorrelation exists across the regions; that is, the regions neighboring a region with high (low) value also show high (low) value.

The hypothesis testing for spatial autocorrelation can be conducted under the null hypothesis of the spatial randomization, under which the statistic asymptotically follows a standard normal distribution. The test statistic z(I) is computed as follows:

$$z(I) = \frac{I - E(I)}{\sqrt{Var(I)}}$$

where $\mathrm{E}(I)$ is the expected value of I and $\mathrm{Var}(I)$ is the variance of I under the spatial randomization, and these terms are calculated as follows:

$$E(I) = -\frac{1}{n-1}$$
 and $Var(I) = E(I^2) - [E(I)]^2$.

The first term on the right hand side in the variance is given by

$$E(I^2) = \frac{n\left[(n^2 - 3n + 3)S_1 - nS_2 + 3S_0^2\right] - m_4/m_2^2[(n^2 - n)S_1 - 2nS_2 + 6S_0^2]}{(n - 1)(n - 2)(n - 3)S_0^2},$$

⁴This is not guaranteed when the spatial weight matrix is not row-standardized.

where m_h is the hth sample moment about the sample mean:

$$\frac{m_4}{m_2^2} = \frac{1/n\sum_{i=1}^n z_i^4}{(1/n\sum_{i=1}^n z_i^2)^2},\tag{8}$$

and the terms S_0 , S_1 , and S_2 denote, respectively,

$$S_0 = \sum_{i=1}^n \sum_{j=1}^n w_{ij}, \quad S_1 = \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n (w_{ij} + w_{ji})^2, \quad \text{and} \quad S_2 = \sum_{i=1}^n \left(\sum_{j=1}^n w_{ij} + \sum_{j=1}^n w_{ji} \right)^2.$$

Note that S_0 is equal to n since the spatial weight matrix is row-standardized. See Cliff and Ord (1970) for further details.

2.4 Local Moran's *I*

The formula of local Moran's I_i is given by

$$I_i = z_i \sum_{j=1}^n w_{ij} z_j, \tag{9}$$

where n is the number of regions, z_i is the value of region i of variable z, which is standardized or centered to the mean, and w_{ij} is the ijth element of the row-standardized spatial weight matrix W.

The term on the right hand side of Equation (9) is the product of the standardized value of region i, z_i , and its spatial lag. Note that if the both are negative, the product takes a positive value, which complicates the direct interpretation of local Moran's I. However, the statistical significance of local Moran's I statistics provides a powerful interpretation through the lens of the Moran scatterplot, which integrates the global and local spatial autocorrelation.

As a class of the LISA, the sum of local Moran's I_i is connected to the global Moran's I, as follows:

$$I = \frac{1}{\sum_{i=1}^{n} z_i^2} \sum_{i=1}^{n} I_i.$$

The hypothesis testing for local spatial autocorrelation can also be conducted under the null hypothesis of the spatial randomization (Anselin, 1995).

The test statistic of local Moran's I_i , $z(I_i)$, is computed as follows:

$$z(I_i) = \frac{I_i - E(I_i)}{\sqrt{\operatorname{Var}(I_i)}}.$$

where $E(I_i)$ is the expected value of I_i of region i and $Var(I_i)$ is the variance of I_i of region i under the spatial randomization.

The expected value of local Moran's I_i , $E(I_i)$, under the spatial randomization is as follows:

$$E(I_i) = -\frac{\sum_{j=1}^{n} w_{ij}}{n-1},$$

where $\sum_{j=1}^{n} w_{ij} = 1$ when the spatial weight matrix is row-standardized.

The variance of local Moran's I_i , $Var(I_i)$, under the spatial randomization is as follows:

$$\operatorname{Var}(I_i) = \operatorname{E}(I_i^2) - [\operatorname{E}(I_i)]^2. \tag{10}$$

where

$$E(I_i^2) = \frac{\sum_{i=1}^n w_{ij}^2 (n - m_4/m_2^2)}{n - 1} + \frac{\sum_{k=1}^n \sum_{h=1}^n w_{ik} w_{ih} (2m_4/m_2^2 - n)}{(n - 1)(n - 2)}.$$

See Anselin (1995) and Sokal et al. (1998) for further details.

2.5 Moran scatter plot

Anselin (1995) proposes a Moran scatterplot, which illustrates a spatial autocorrelation in terms of Moran's I. Consider the following regression without constant term:

$$Wz = \alpha z + \text{residuals}$$
 (11)

where Wz is called the spatial lag of the variable z, and residuals indicate that any statistical assumption on error terms is not considered.

The OLS estimator of the coefficient α is obtained by

$$\hat{\alpha} = \frac{\boldsymbol{z}^{\top} \boldsymbol{W} \boldsymbol{z}}{\boldsymbol{z}^{\top} \boldsymbol{z}},$$

which is equal to the formula of the Moran's I in Equation (7). Therefore, the Moran scatter plot is a graphical representation of the correlation between $\boldsymbol{W}\boldsymbol{z}$ and \boldsymbol{z} . In the case where the variable is not standardized or centered around the mean, it is necessary to include the constant term, thereby centering the variable around its mean.

3 Implementation in Stata

3.1 Syntax

moransi
$$varname \ [if] \ [in]$$
, lat $(varname) \ lon(varname) \ swm(swmtype)$ dist $(\#)$ dunit $(km|mi) \ [wvar(varname) \ \underline{nomat}$ save dms $\underline{approx} \ \underline{det}$ ail graph \underline{rep} lace]

3.2 Options

lat(varname) specifies the variable of latitude in the dataset. The decimal format is expected in the default setting. The positive value denotes the north latitude. The negative value denotes the south latitude.

lon(varname) specifies the variable of longitude in the dataset. The decimal format is expected in the default setting. The positive value denotes the east longitude. The negative value denotes the west longitude.

swm(swmtype) specifies a type of spatial weight matrix. One of the following types of spatial weight matrix must be specified: bin (binary), knn (k-nearest neighbor), exp (exponential), or pow (power). The parameter k must be specified for the k-nearest neighbor weights as follows: swm(knn #). The distance decay parameter # must be specified for the exponential and power functional types of spatial weight matrix as follows: swm(exp #) and swm(pow #).

dist(#) specifies the threshold distance # for the spatial weight matrix, with the unit of distance specified by the dunit(km|mi) option.

dunit(km|mi) specifies the unit of distance. Either km (kilometers) or mi (miles) must be specified.

wvar(varname) specifies a weight variable for the spatial weight matrix. Weight variable is not used in the default setting.

dms converts the degrees, minutes and seconds (DMS) format to a decimal. The dms option is not used in the default setting.

<u>approx</u> uses bilateral distance approximated by the simplified version of the Vincenty formula (Vincenty, 1975). The approx option is not used in the default setting.

<u>det</u>ail displays descriptive statistics of distance for lower triangular elements of the distance matrix. The <u>det</u>ail option is not used in the default setting.

<u>nomat</u>save does not save the bilateral distance matrix r(D) and the spatial weight matrix r(W) on the memory. The <u>nomat</u>save option is not used in the default setting.

graph draws a Moran scatterplot. The graph option is not used in the default setting.

 $\underline{\underline{\text{replace}}}$ is used to overwrite the existing output variables in the dataset. The $\underline{\underline{\text{replace}}}$ option is not used in the default setting.

3.3 Output

3.3.1 Stored results

The moransi command stores the following results in r-class.

Scalars				
r(I)		Moran's I statistic	r(EI)	expected value of I
r(seI	()	standard error of I	r(zI)	z-value of I
r(pI)		p-value of I	r(N)	number of observations
r(td)		threshold distance	r(dd)	parameter δ of distance decay or k of knn
r(dis	t_mean)	mean of distance	$r(dist_sd)$	standard deviation of distance
r(dis	t_min)	minimum value of distance	$r(dist_max)$	maximum value of distance
Matrices				
r(D)		lower triangular distance matrix	r(W)	spatial weight matrix
Macros				
r(cmd	1)	moransi	r(varname)	name of variable
r(swm	1)	type of spatial weight matrix	r(dunit)	unit of distance
r(dis	t_type)	exact or approximation	r(wvar)	name of weight variable

□ Technical note

When the spatial weight matrix is too large for the computer specs (e.g., the memory size is small), the moransi command may not calculate Moran's I statistic (Stata program or computer may freeze). For example, about $51,842 \times 51,842$ spatial weight matrix uses about

20 GB of memory space during the calculation process. The duration of the calculation process is contingent upon the CPU performance. In addition, the nomatsave option is recommended to release the memory space after the calculation.

4 Example

This section illustrates the use of the moransi command in Stata. Two applied examples are provided below.

4.1 Municipal Unemployment Rates in Japan

This subsection investigates the spatial distribution of unemployment in Japan. The sample data are taken from Kondo (2015b), who investigates the spatial autocorrelation of municipal unemployment rates and unemployment clusters in Japan. Municipal unemployment rates used in Kondo (2015b) are based on the 1980–2005 Population Censuses in Japan.

Figure 1 illustrates geographical distribution of unemployment rates in 2005.⁵ The municipalities are categorized into nine quantile levels. It can be seen that municipalities with high unemployment rates have neighbors with similar characteristic, suggesting a positive spatial autocorrelation in municipal unemployment rates.

To assess the spatial autocorrelation, the fundamental procedure of the moransi command is outlined below:

(Continued on next page)

⁵Stata 14 or lower version can depict maps, like Figure 1, using the shp2dta that command converts shapefile to a DTA file (Crow, 2015) and the spmap command that illustrates data on map (Pisati, 2008). Stata 15 provides corresponding official commands spshape2dta and grmap.

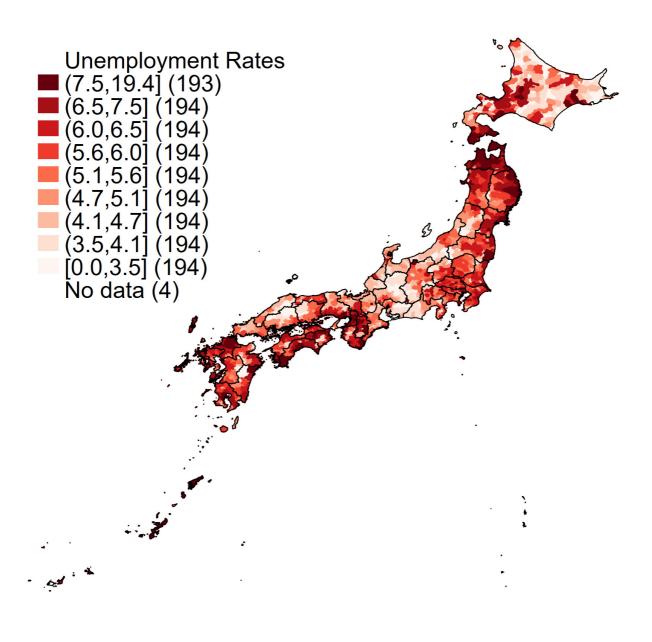


Figure 1: Municipal unemployment rates in 2005

Note: Created by the author using the dataset of Kondo (2015b). Original data source of municipal unemployment rates is Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan).

. moransi std_ur2005, lon(lon) lat(lat) swm(pow 2) dist(.) dunit(km) det graph replace Size of spatial weight matrix: 1745 * 1745 Calculating bilateral distance...

Completed: 10%
Completed: 20%
Completed: 30%
Completed: 50%
Completed: 60%
Completed: 70%
Completed: 80%
Completed: 90%
Completed: 100%

Distance by Vincenty formula (unit: km)

	Obs.	Mean	S.D.	Min.	Max.
Distance	1523385	603.951	432.634	0.854	2961.185

Distance threshold (unit: km):

1745	mber of Obs. =	Nur	Summary of Global Moran's I Statistic				
p-value	Z(I)	SE(I)	E(I)	Moran's I	Variable		
0.00000	48.73934	0.01019	-0.00057	0.49629	std_ur2005		

Null Hypothesis: Spatial Randomization

Summary of Local Moran's I Statistics Number of Obs. = 1745

std_ur2005	Obs.	p < 0.10	p < 0.05	p < 0.01
1: High-High	526	205	188	156
2: High-Low	256	5	3	3
3: Low-High	157	20	14	9
4: Low-Low	806	245	206	130

Null Hypothesis: Spatial Randomization

splag_std_ur2005_p was generated in the dataset.

lmoran_i_std_ur2005_p was generated in the dataset.

 ${\tt lmoran_e_std_ur2005_p\ was\ generated\ in\ the\ dataset.}$

 ${\tt lmoran_v_std_ur2005_p\ was\ generated\ in\ the\ dataset.}$

 ${\tt lmoran_z_std_ur2005_p\ was\ generated\ in\ the\ dataset.}$

 ${\tt lmoran_p_std_ur2005_p\ was\ generated\ in\ the\ dataset.}$

 ${\tt lmoran_cat_std_ur2005_p\ was\ generated\ in\ the\ dataset.}$

. graph export "fig/FIG_moran_ur2005.svg", replace
(file fig/FIG_moran_ur2005.svg written in SVG format)

(Continued on next page)

The moransi command displays a summary result of the global and local Moran's I. In this case, the Moran's I is 0.496 and statistically significant at the 1 % level. The spatial weight matrix is based on the power functional form with the distance decay parameter $\delta = 2$. Additionally, the detail option displays descriptive statistics of distance for lower triangular elements of the distance matrix.⁶

The moransi command includes the graph option, which automatically draws a Moran scatterplot. However, since the spatial lag of the variable is stored in the dataset, users also can make a Moran scatterplot manually using the outcome variables as follows:⁷

```
. twoway (scatter splag_std_ur2005_p std_ur2005, ms(oh) yaxis(1 2) xaxis(1 2)) ///
>
          (lfit splag_std_ur2005_p std_ur2005, lw(medthick) estopts(nocons)), ///
>
          ytitle("W.Standardized Unemployment Rates", tstyle(size(large)) axis(1)) ///
          xtitle("Standardized Unemployment Rates", tstyle(size(large)) height(6) axis(1)) ///
          ytitle("", axis(2)) ///
          xtitle("", axis(2)) ///
          ylabel(-2(2)6, ang(h) labsize(large) format(%2.0f) nogrid axis(1)) ///
          xlabel(-4(2)8, labsize(large) format(%2.0f) nogrid axis(1)) ///
          ylabel(-2(2)6, ang(h) labsize(large) format(%2.0f) nogrid axis(2)) ///
          xlabel(-4(2)8, labsize(large) format(%2.0f) nogrid axis(2)) ///
          ysize(3) xsize(4) ///
          yline(0, lwidth(thin) lcolor(gray) lpattern(dash)) ///
          xline(0, lwidth(thin) lcolor(gray) lpattern(dash)) ///
          legend(off) ///
          graphregion(color(white) fcolor(white))
. graph export "FIG_moran_ur2005.svg", replace
(file FIG_moran_ur2005.svg written in SVG format)
```

Figure 2 shows a Moran scatter plot, which is made in combination with the standard Stata command twoway scatter. The line through the origin depicted in Figure 2 indicates the regression line in Equation (11), which is equal to the Moran's I statistic.

The moransi command shows the summary results of local Moran's I statistics based on the Moran scatterplot. There are 526 municipalities in the high-high category, and 205 municipalities are statistically significant at the 10 % level and detected as high-high spatial clusters. In turn, there are 806 municipalities in the low-low category, and 245 municipalities are statistically significant at the 10 % level and classified as low-low spatial clusters.

Figure 3 shows the statistical significance of the local Moran's I of municipal unemployment rates. This map can be integrated with Moran scatterplot in Figure 2, which provides a coherent interpretation between the global and local spatial autocorrelation.

Figure 4 shows spatial clusters of municipal unemployment rates, based on four categories of the Moran scatterplot in Figure 2. As discussed before, 205 municipalities of high-high unemployment clusters and 245 municipalities of low-low unemployment clusters are visualized on the map.

⁶The supplementary material for replication includes a comparison program between the **spatgsa** command developed by Pisati (2001), the **splagvar** command developed by Jeanty (2010), and the **moransi** command. These three commands show the same calculation results.

 $^{^7{\}rm The}$ spgen command also generates the spatially lagged variables (Kondo, 2015a).

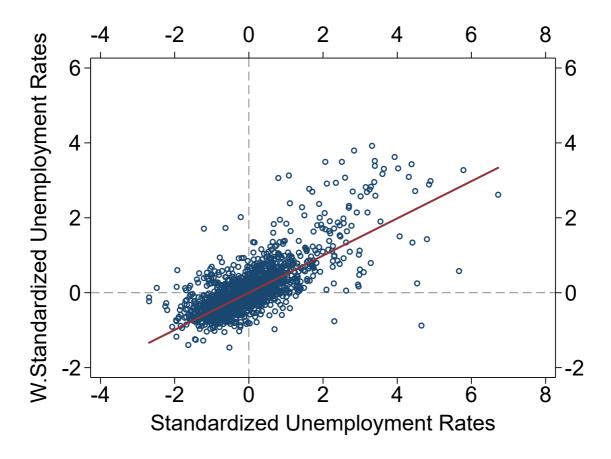


Figure 2: Moran Scatterplot of municipal underemployment rates in 2005

Note: Created by the author using the dataset of Kondo (2015b). Original data source of municipal unemployment rates is Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan) .

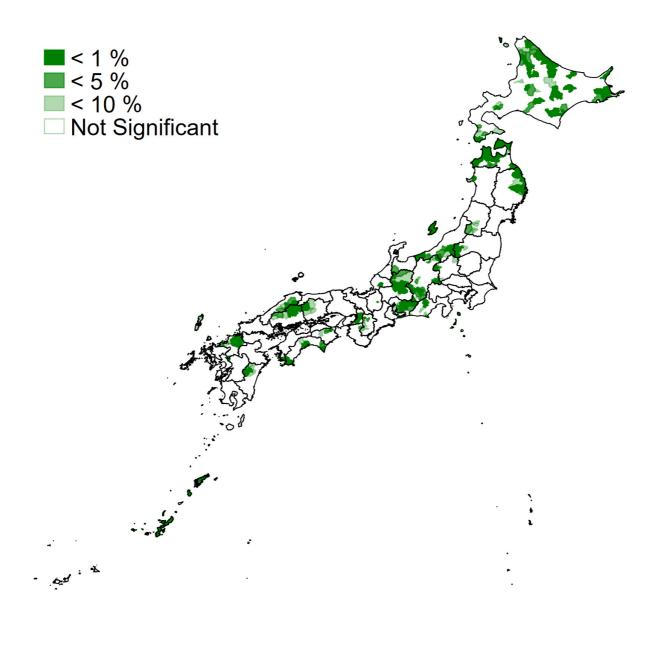


Figure 3: Statistical Significance for Local Moran's I of Municipal Unemployment Rates in 2005 Note: Created by the author using the dataset of Kondo (2015b). Original data source of municipal unemployment rates is Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan).

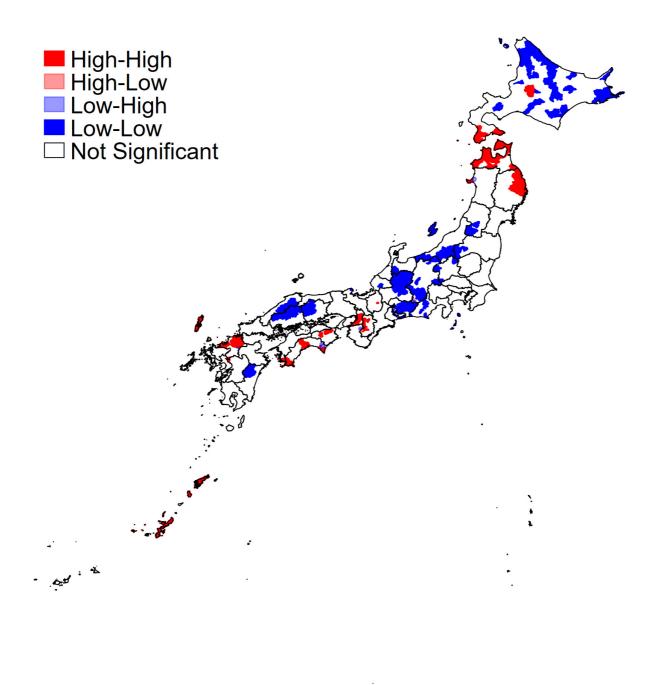


Figure 4: Moran Cluster Map of Municipal Unemployment Rates in 2005

Note: Created by the author using the dataset of Kondo (2015b). Original data source of municipal unemployment rates is Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan). Municipalities with statistical significance at the 10 % level are shown.

4.2 Population in Tokyo Metropolitan Area

This subsection investigates a population distribution using the Grid Square Statistics of 2015 Population Census in Japan Ministry of Internal Affairs and Communications (2025a,b). This paper focuses on the residential population in the Tokyo metropolitan area (i.e., Saitama, Chiba, Tokyo, and Kanagawa prefectures). There are several previous studies in the field of geography that discuss population distribution in the corresponding area in terms of the explanatory spatial data analysis (Koizumi, 2010; Monzur, 2017).

As illustrated in Figure 5, the geographical distribution of the residential population in the Tokyo metropolitan area in 2015 is categorized into nine quantile levels. The population is concentrated within 23 wards of Tokyo, and the mesh grid surrounding the central business district near Tokyo Station and the Imperial Palace exhibits areas with few residents. Residential areas extend in a radial pattern toward suburban areas.

The global and local Moran's I statistics were obtained using the moransi command, and the spatial weight matrix was based on the power functional form with the distance decay parameter $\delta=4$. The global Moran's I statistic was found to be 0.84, which is statistically significant at the 1 % level, thereby confirming the presence of spatial similarities in the population distribution. The local Moran's I analysis identified 1,790 residential clusters among 3,106 mesh grids in the high-high category, reaching a 1

Figure 6 presents a Moran scatter plot of residential population, with the regression line corresponding to the Moran's I statistic indicated by the line in the figure. As previously discussed, a clear positive relationship exists between neighboring mesh grids.

Figure 7 shows the statistical significance of the local Moran's I and a radial pattern of residential areas toward suburban areas. The map, which is integrated with the Moran scatterplot in Figure 6, provides an important implication of the spatial analysis.

Figure 8 shows 1,706 residential clusters detected by local Moran's I statistics in the Tokyo metropolitan area, with the rail network depicted according to Ministry of Land, Infrastructure, Transport and Tourism (2025). Notably, high-high residential clusters are found along the rail network, indicating that enhanced transport accessibility increases the desirability of a location for habitation. Additionally, the analysis reveals a clear limit to the distance from the central business districts of the Tokyo metropolitan area.

. moransi pop_total_all, lon(lon) lat(lat) swm(pow 4) dist(.) dunit(km) approx replace Size of spatial weight matrix: 13291 * 13291 Calculating bilateral distance...

Completed: 10%
Completed: 20%
Completed: 30%
Completed: 40%
Completed: 50%
Completed: 60%
Completed: 70%
Completed: 80%
Completed: 90%
Completed: 100%

Distance by simplified version of Vincenty formula (unit: km)

Summary of Global Moran's I Statistic

Number of Obs. = 13

13291

Variable	Moran´s I	E(I)	SE(I)	Z(I)	p-value
pop_total_all	0.84325	-0.00008	0.00469	179.63289	0.00000

Null Hypothesis: Spatial Randomization

Summary of Local Moran's I Statistics

Number of Obs. =

13291

pop_total_all	Obs.	p < 0.10	p < 0.05	p < 0.01
1: High-High	3106	2044	1958	1790
2: High-Low	328	0	0	0
3: Low-High	610	1	0	0
4: Low-Low	9247	0	0	0

Null Hypothesis: Spatial Randomization

 ${\tt splag_pop_total_all_p}$ was generated in the dataset.

 ${\tt lmoran_i_pop_total_all_p} \ \, {\tt was} \ \, {\tt generated} \ \, {\tt in} \ \, {\tt the} \ \, {\tt dataset}.$

lmoran_e_pop_total_all_p was generated in the dataset.

 ${\tt lmoran_v_pop_total_all_p\ was\ generated\ in\ the\ dataset}.$

 ${\tt lmoran_z_pop_total_all_p} \ \, {\tt was} \ \, {\tt generated} \ \, {\tt in} \ \, {\tt the} \ \, {\tt dataset}.$

 ${\tt lmoran_p_pop_total_all_p\ was\ generated\ in\ the\ dataset.}$

lmoran_cat_pop_total_all_p was generated in the dataset.

(Continued on next page)

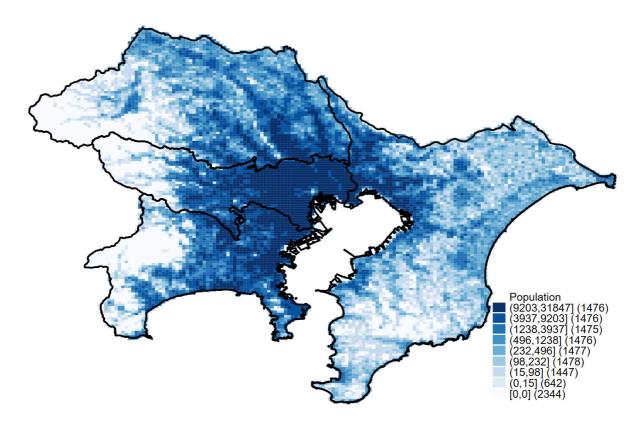


Figure 5: Residential Population Distribution in 2015

Note: Created by the author using the population in 1km-by-1km mesh grid of 2015 Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan).

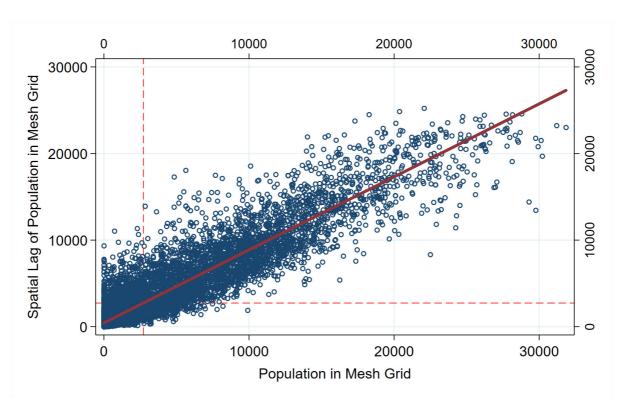


Figure 6: Moran Scatterplot of Population in Tokyo Metropolitan Area Note: Created by the author using the population in 1km-by-1km mesh grid of 2015 Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan).

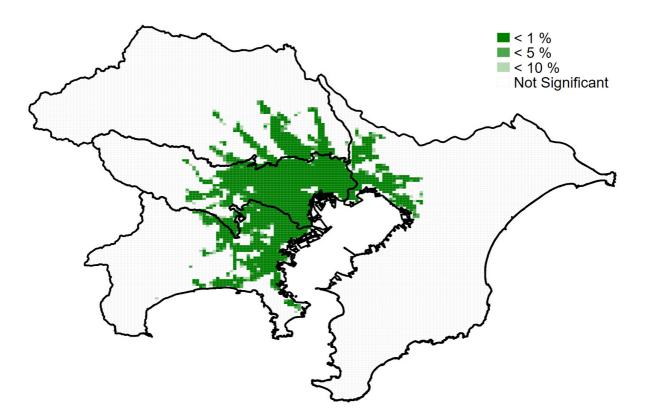


Figure 7: Statistical Significance for Local Moran's I of Population in Tokyo Metropolitan Area Note: Created by the author using the population in 1km-by-1km mesh grid of 2015 Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan).

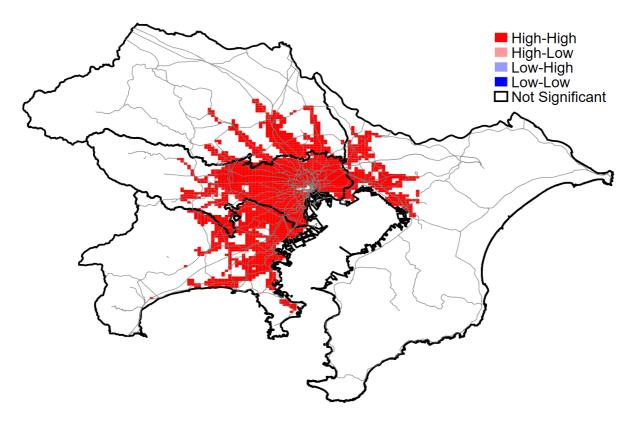


Figure 8: Moran Cluster Map of Population in Tokyo Metropolitan Area Note: Created by the author using the population in 1km-by-1km mesh grid of 2015 Population Census (Statistical Bureau, Ministry of Internal Affairs and Communications of Japan).

5 Concluding remarks

This paper has introduced the moransi command, a novel tool for computing global and local Moran's I in Stata. The moransi command offers a more intuitive interface than previous spatial analysis tools, as it does not require the user to construct a spatial weight matrix in advance. While this approach may result in a slight reduction in computational efficiency, it provides a more straightforward and user-friendly interface for Stata users.

To further expand the reader's comprehension of spatial analysis using the moransi command, this paper has provided two applied examples of spatial analysis in Japan. First, analysis of the global and local Moran's I revealed spatial clusters of high-high and low-low unemployment rates in Japan. Second, analysis of the global and local Moran's I revealed that residential clusters are formed along with the rail network in Tokyo metropolitan area. The incorporation of additional geographical data facilitates a more profound comprehension of spatial analysis.

It is anticipated that the moransi command will contribute to the continued expansion of spatial analysis within the Stata community.

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