

An Analysis about Mutant Subsumption in First- and Second- Order Mutation Testing

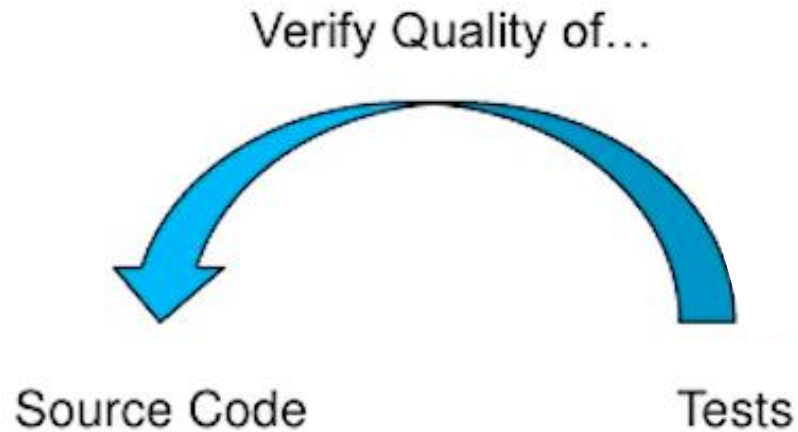
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LabSoft Seminar. Nov 22nd, 2024

Outline

- ❑ Mutation testing
- ❑ Mutants subsumption
- ❑ Dynamic mutant subsumption graphs
- ❑ Second-order mutants subsumption
- ❑ Study design
- ❑ Preliminary results
- ❑ Comparison with SS2OMs reduction
- ❑ Conclusion

Introduction



Mutation Testing

- ❑ Introducing **artificial syntactic changes (mutations)** into original source code
 - Intending to represent real common programming bugs
 - Changed programs are called **mutants**
- ❑ Running test cases on mutants
 - Result different from original: mutant **killed**
 - Otherwise: **alive**

Example of a mutant

Mutation place:

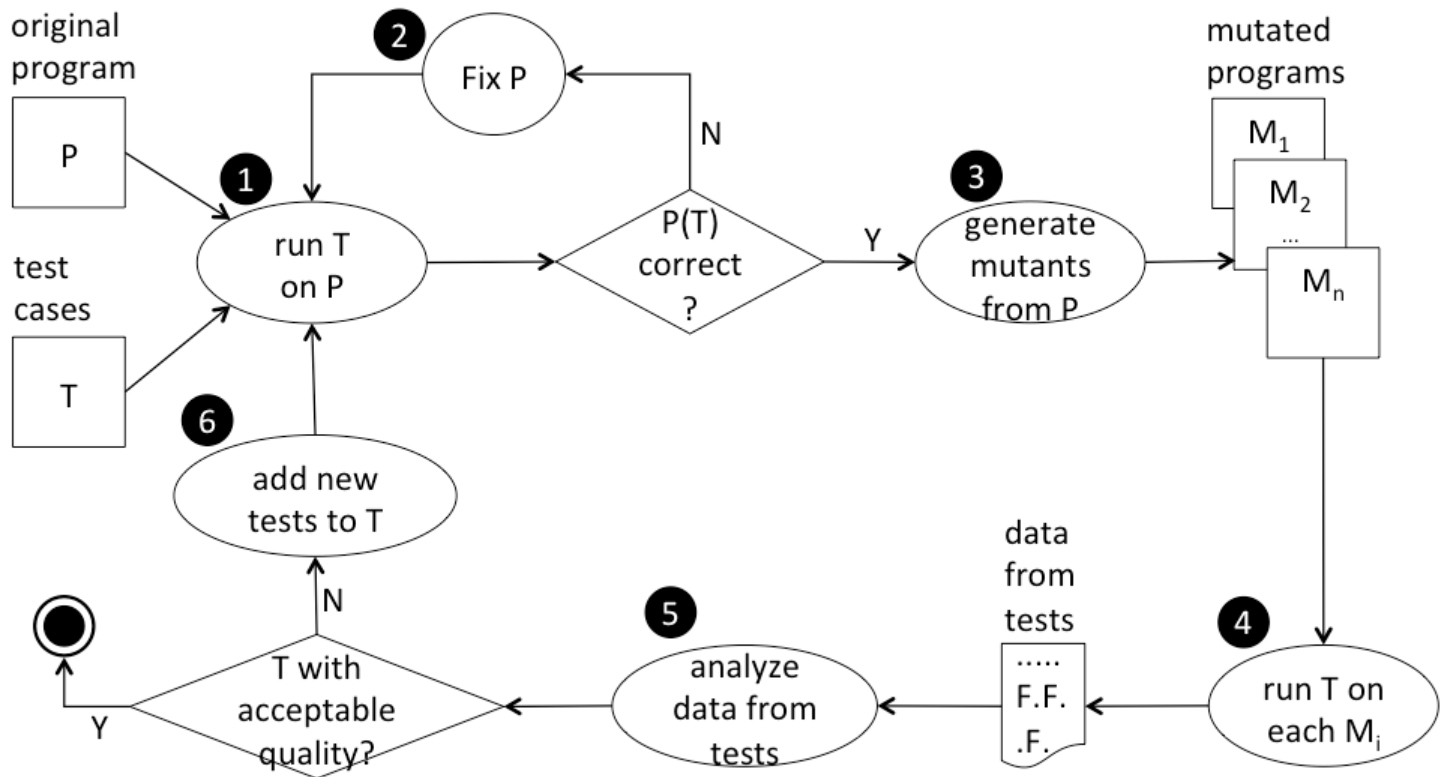
```
public class Taxes {  
  
    double simpleTax(double amount) {  
  
        return amount * 0.2;  
  
    }  
  
}
```

Example of a mutant

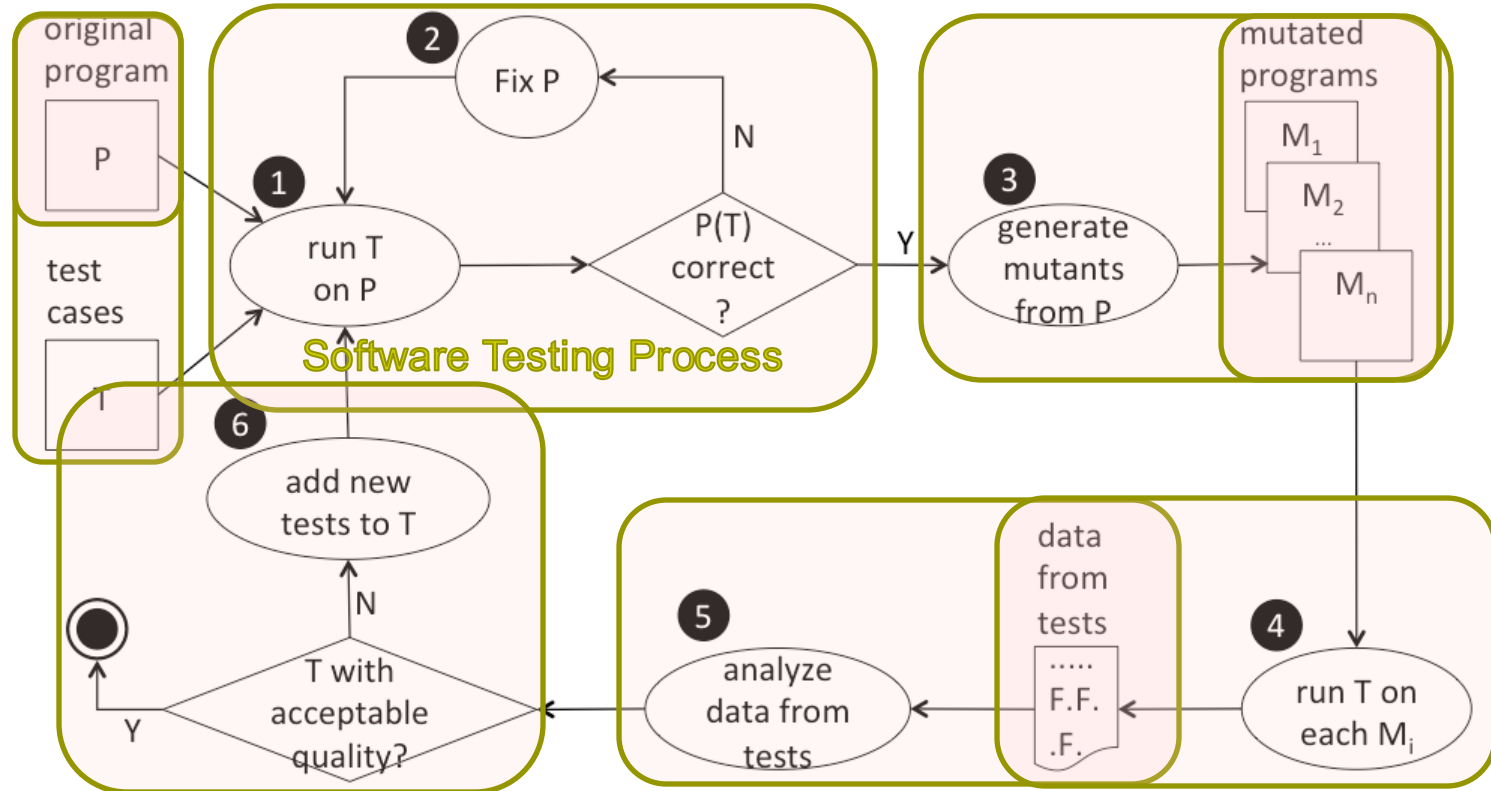
* → +

```
public class Taxes {  
  
    double simpleTax(double amount) {  
  
        return amount + 0.2;  
  
    }  
  
}
```

Mutation testing process



Mutation testing process



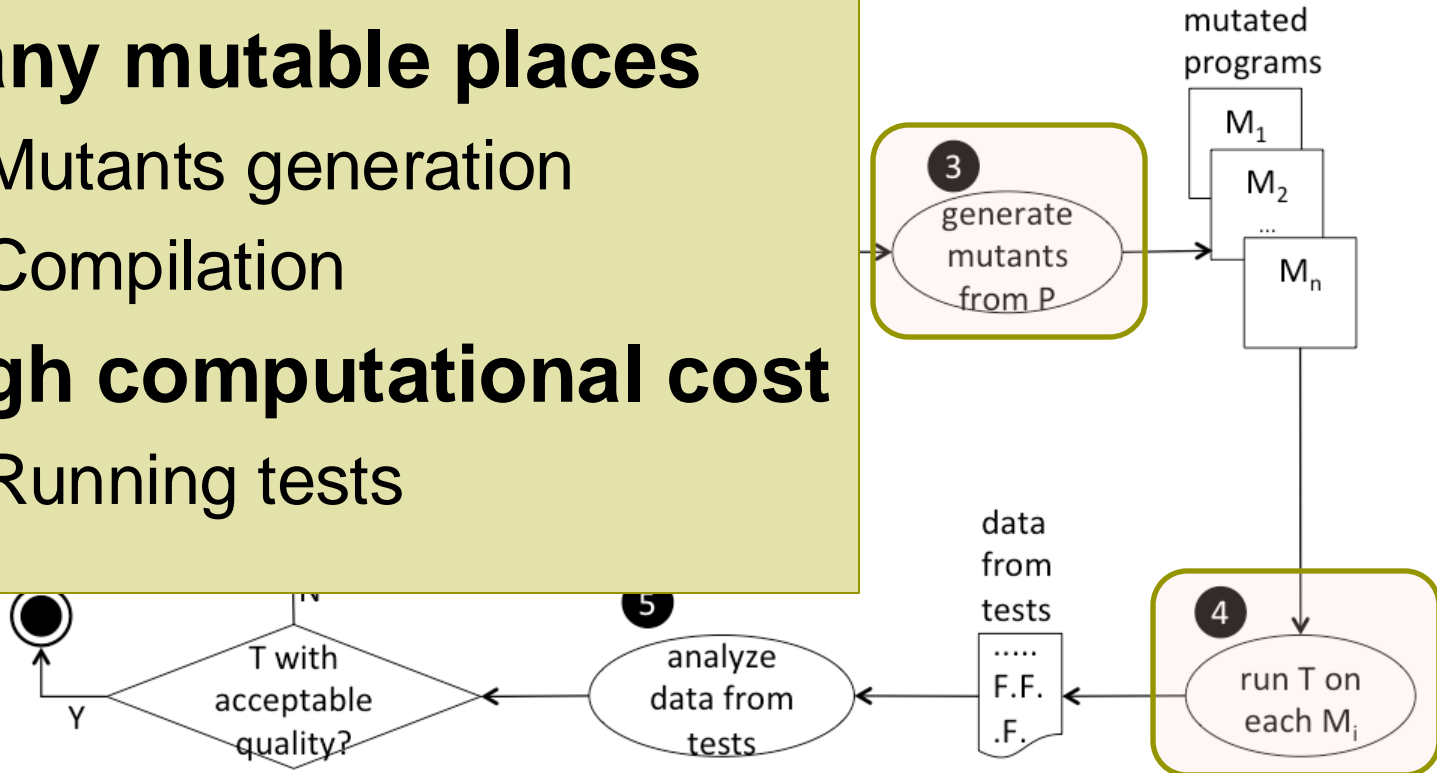
Mutation testing drawbacks

3. Many mutable places

- Mutants generation
- Compilation

4. High computational cost

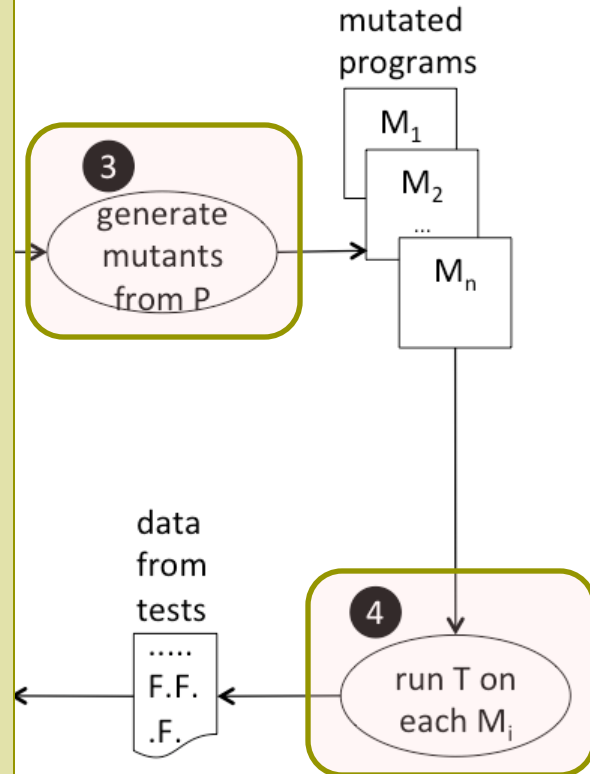
- Running tests



Mutation testing drawbacks

□ Cost reduction techniques

- Number of test cases
- Test case prioritization
- Number of mutants
 - **subsumption**



Mutants subsumption

Contextualization

```
def greaterThan(a, b) :  
    return a > b    # original  
    return a >= b   # mutant 1  
    return a <= b   # mutant 2
```

Contextualization

```
def greaterThan(a, b) :  
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    return a >= b   # mutant 1  
    return a <= b   # mutant 2
```

	Test	orig
t1	assertTrue(greaterThan(6, 5))	✓
t2	assertFalse(greaterThan(5, 5))	✓
t3	assertFalse(greaterThan(5, 6))	✓

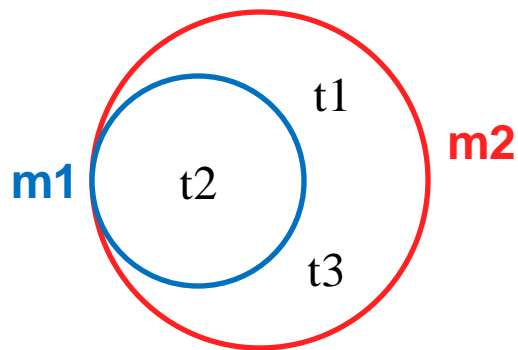
Contextualization

```
def greaterThan(a, b) :  
    return a > b    # original  
    return a >= b   # mutant 1  
    return a <= b   # mutant 2
```

	Test	orig	m1	m2
t1	assertTrue(greaterThan(6, 5))	✓	✓	✗
t2	assertFalse(greaterThan(5, 5))	✓	✗	✗
t3	assertFalse(greaterThan(5, 6))	✓	✓	✗

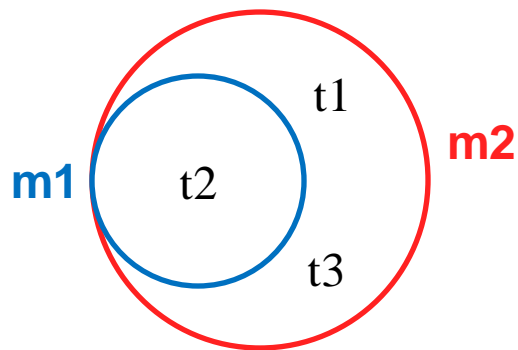
Contextualization

□ Killing tests



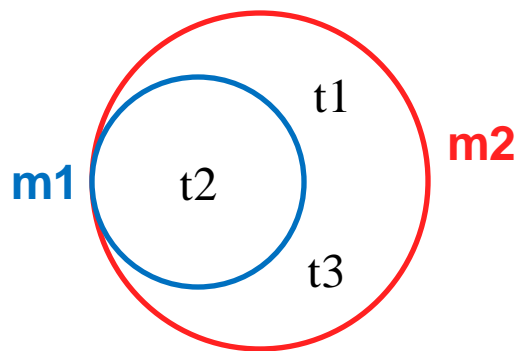
Contextualization

- All test sets that kill **m1** also kill **m2**



Conclusion

□ **m1** subsumes **m2**



Conclusion

- If we know beforehand that
 - **m1** subsumes **m2**
- Therefore,
 - **m2** should not have been generated

Cost reduction: fewer mutants to run the test suite against

Dynamic mutant subsumption graphs

Example

test	m1	m2	m3	m4	m5
t1	×	×		×	×
t2	×		×	×	
t3				×	
t4		×		×	×

Subsumption relationships

test	m1	m2	m3	m4	m5
t1	×	×		×	×
t2	×		×	×	
t3				×	
t4		×		×	×

$m1 \rightarrow m4$

$m2 \rightarrow m4$

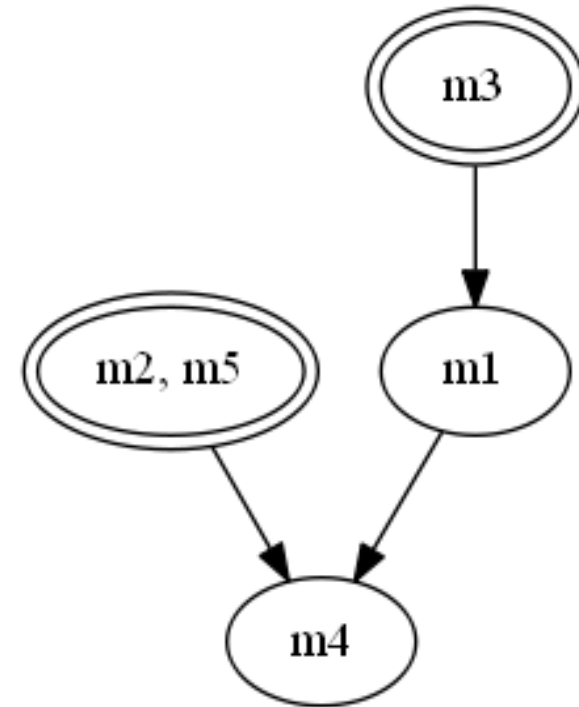
$m3 \rightarrow m1$

$m3 \rightarrow m4$

$m5 \rightarrow m4$

Subsumption graph

Test	m1	m2	m3	m4	m5
t1	×	×		×	×
t2	×		×	×	
t3				×	
t4		×		×	×



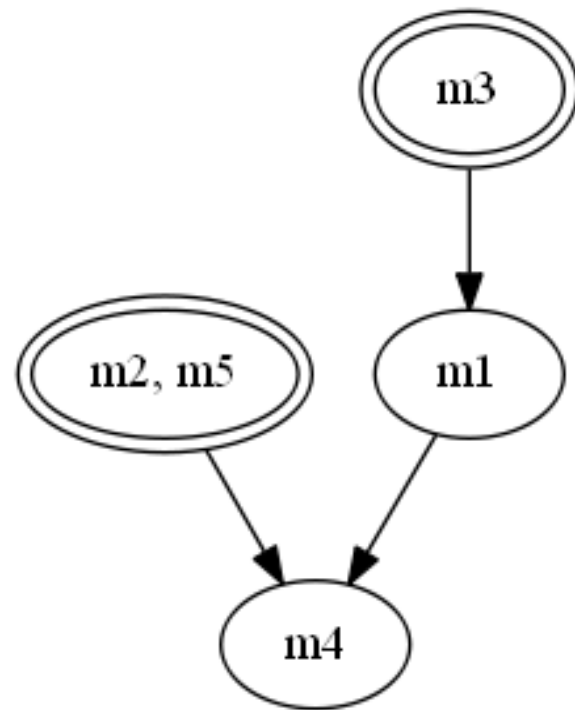
Conclusion

❑ Root nodes are kept

- 2 minimal
- 3 mutants

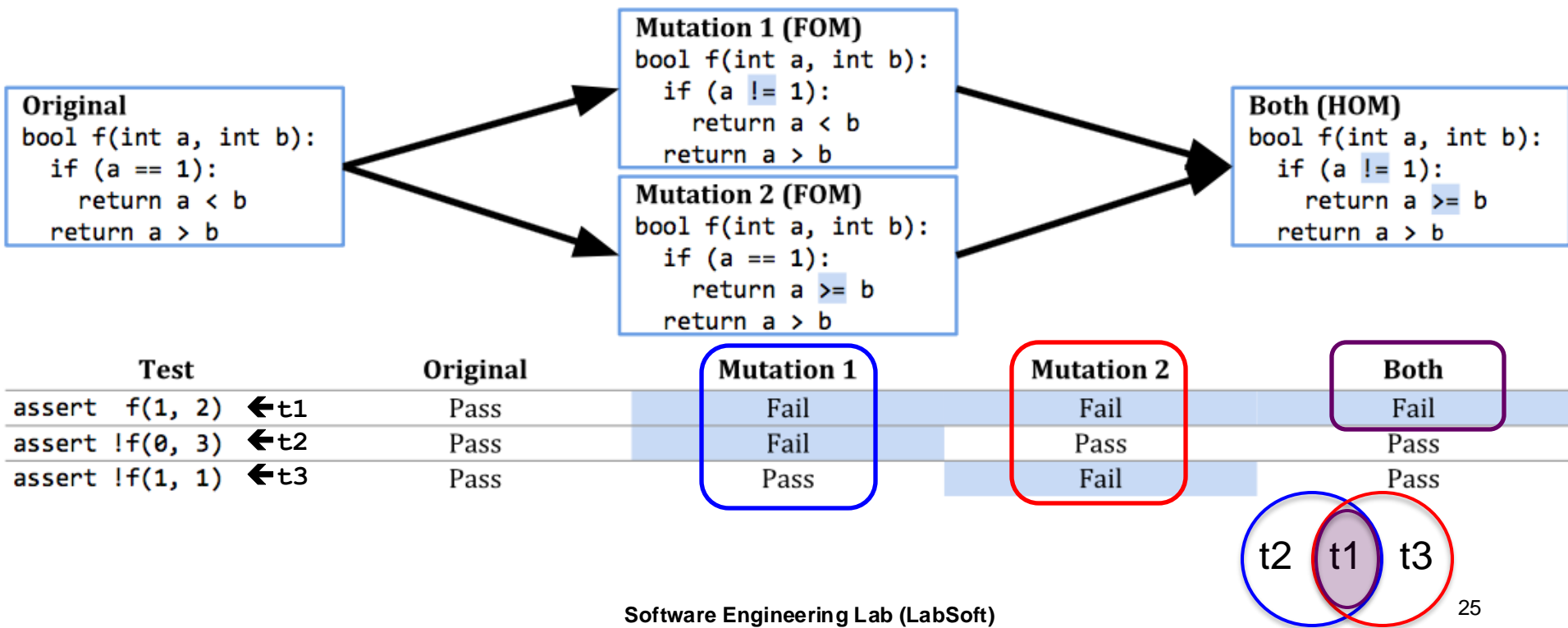
❑ Remaining nodes

- are disregarded
- (redundants)

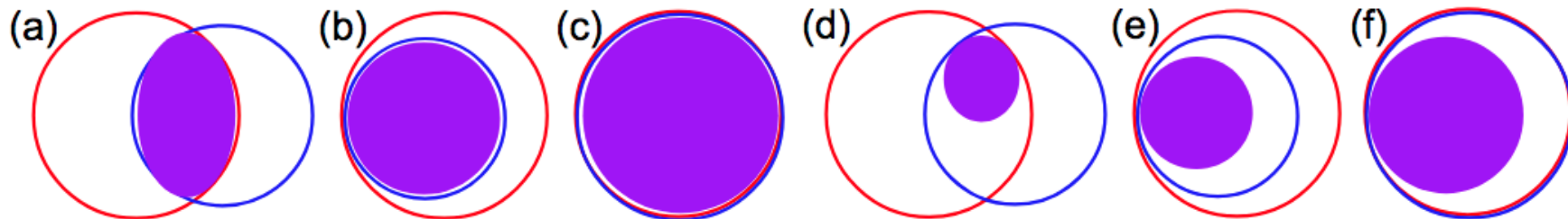
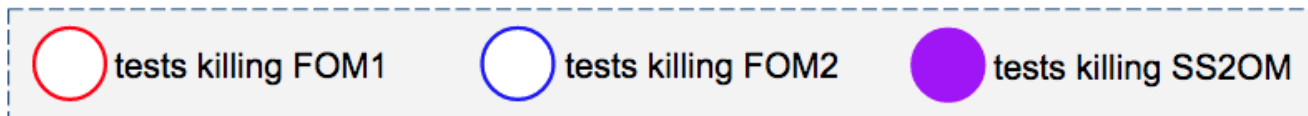


Second-order mutants subsumption

A 2OM subsumption example



Venn Diagram “shapes”



Mutants reduction - example

FOMs

SS2OMs

m1

[m1,m2]

m2

[m3,m4]

m3

[m5,m6]

m4

m5

m6

m7

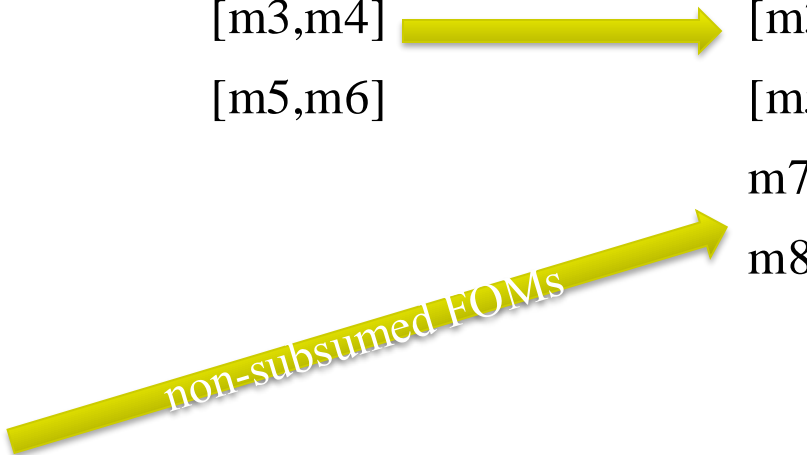
m8

Mutants reduction - example

FOMs	SS2OMs	Resulting mutants
m1	[m1,m2]	[m1,m2]
m2	[m3,m4]	[m3,m4]
m3	[m5,m6]	[m5,m6]
m4		
m5		
m6		
m7		
m8		

Mutants reduction - example

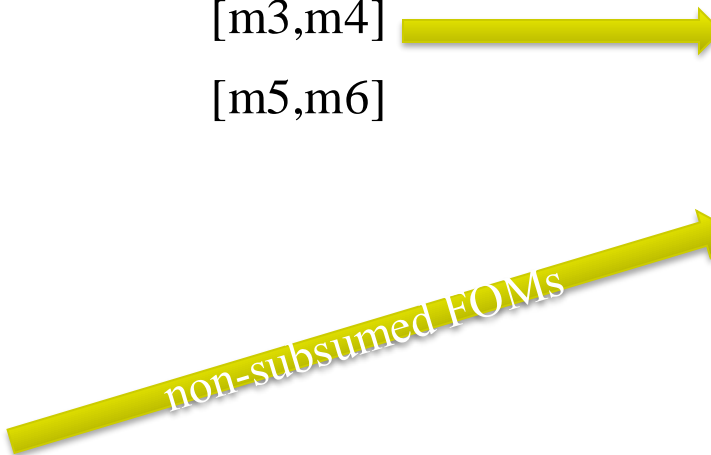
FOMs	SS2OMs	Resulting mutants
m1	[m1,m2]	[m1,m2]
m2	[m3,m4]	[m3,m4]
m3	[m5,m6]	[m5,m6]
m4		m7
m5		m8
m6		
m7		
m8		



non-subsumed FOMs

Mutants reduction - example

FOMs	SS2OMs	Resulting mutants	Reduction
m1	[m1,m2]	[m1,m2]	3 out of 8 mutants (37.5%)
m2	[m3,m4]	[m3,m4]	
m3	[m5,m6]	[m5,m6]	
m4		m7	
m5		m8	
m6			
m7			
m8			



non-subsumed FOMs



Study design

Dataset: 9 Java systems

System	Version	LOC	# Tests	JUnit	#FOMs
Vending Machine	Exceptions	~100	35	4	57
Triangle	n/a	34	12	4	138
Monopoly	n/a	1,181	124	3	866
Commons CSV	1.8	~2k	325	4	925
Commons CLI	1.4	2,699	318	4	1,082
ECal	2003.10	3,626	224	3	1,207
Commons Validator	1.6	7,409	536	4	3,197
Gson	2.9.0	> 10k	1,089	3 and 4	3,712
Chess	n/a	4,924	930	3 and 4	5,287



Study steps

- ❑ Compute the killing tests for each mutant
- ❑ Generate the subsumption graph
- ❑ Retrieve the root (minimal) nodes
- ❑ Compare with SS2OMs subsumption

Preliminary results

Subsumption analysis

Overall	#FOMs	#minimal nodes	#remaining FOMs
9 systems	16,471	1,115	3,376

Highlight on Triangle

{91}

{65, 67, 68, 70, 75, 77, 80, 52, 85, 56, 57, 58, 59, 63}

{35, 37, 38, 39, 108, 112, 114, 115, 116, 118, 119}

{129, 130, 131, 46, 122, 123, 124, 127}

{11}

{62}

{79}

{5}

{96, 132, 136, 121, 106, 111}

{69}

{97, 99, 100, 101, 103, 104, 23, 24, 25, 26, 27, 28, 93}

{0}

#FOMs	#minimal nodes	#remaining FOMs
138	12	59

Comparison with SS2OMs reduction

1st- and 2nd-order reductions

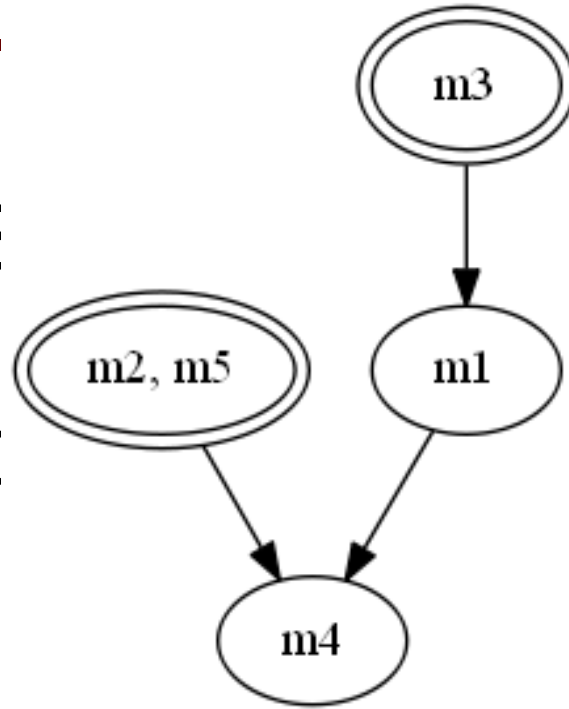
Overall	FOMs	Via subsumption graph	Via SS2OMs
9 systems	16,471	77.35%	22.37%

RQ

- Considering the **FOM** subsumption graphs, how are SS2OMs formed?
- Only by FOMs inside the **same** minimal nodes
(not by FOMs of **distinct** minimal nodes)

RQ

- Consideri
how are Σ
- Only by FC
(not by



assumption graphs,
I?

ne minimal nodes
minimal nodes)

Conclusion

- Can SS2OMs reduce even more mutants than the non-subsumed FOMs?
- **No, they do not contribute to any further reduction.**



Questions?

