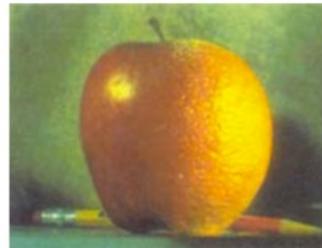


2. Image Formation



3. Image Processing



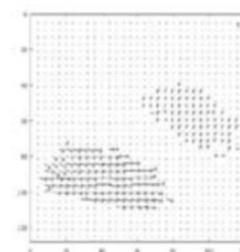
4. Features



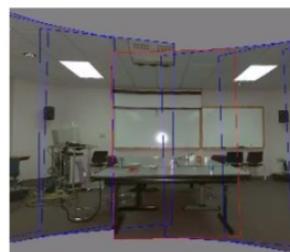
5. Segmentation



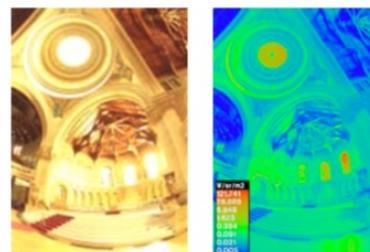
6-7. Structure from Motion



8. Motion



9. Stitching



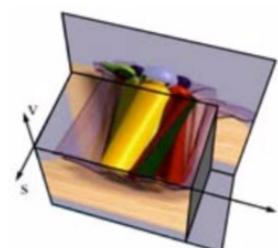
10. Computational Photography



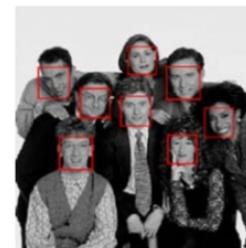
11. Stereo



12. 3D Shape



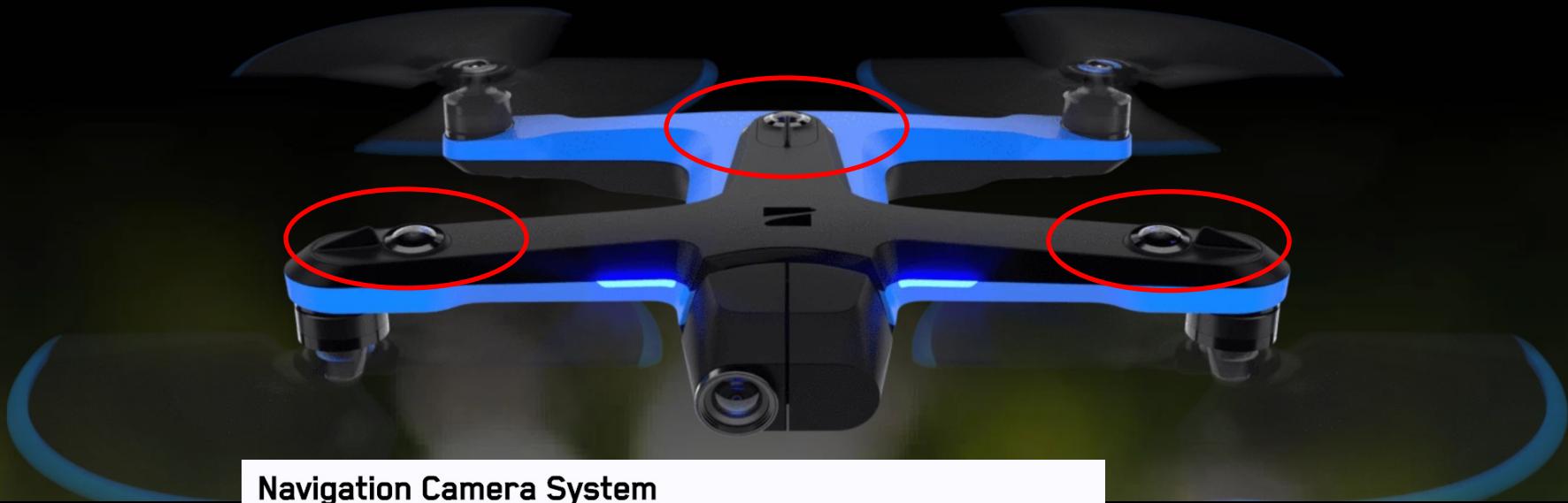
13. Image-based Rendering



14. Recognition

# Trinocular Camera rigs

# Skydio 2



## Navigation Camera System

### CONFIGURATION

6x cameras in trinocular configuration top  
and bottom

### SENSOR TYPE

Sony 1/3" 4K color CMOS

### LENS APERTURE

f/1.8

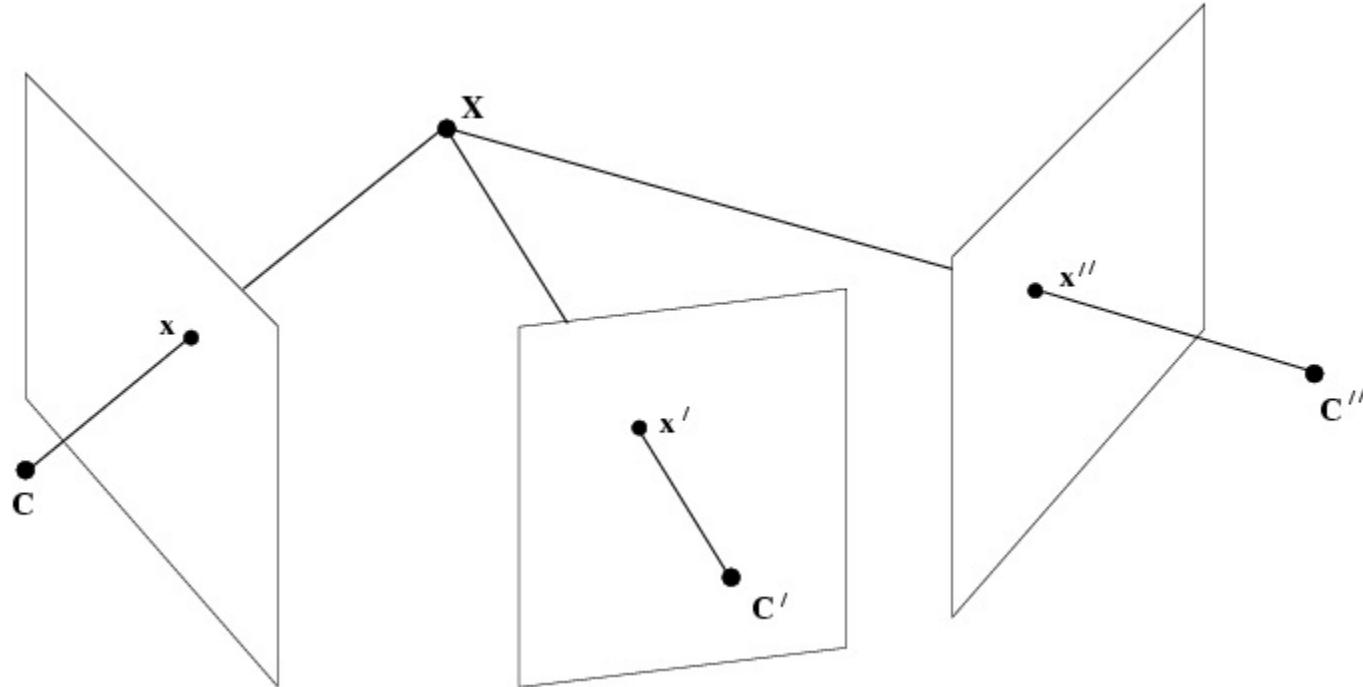
### FIELD-OF-VIEW

200°

### ENVIRONMENT COVERAGE

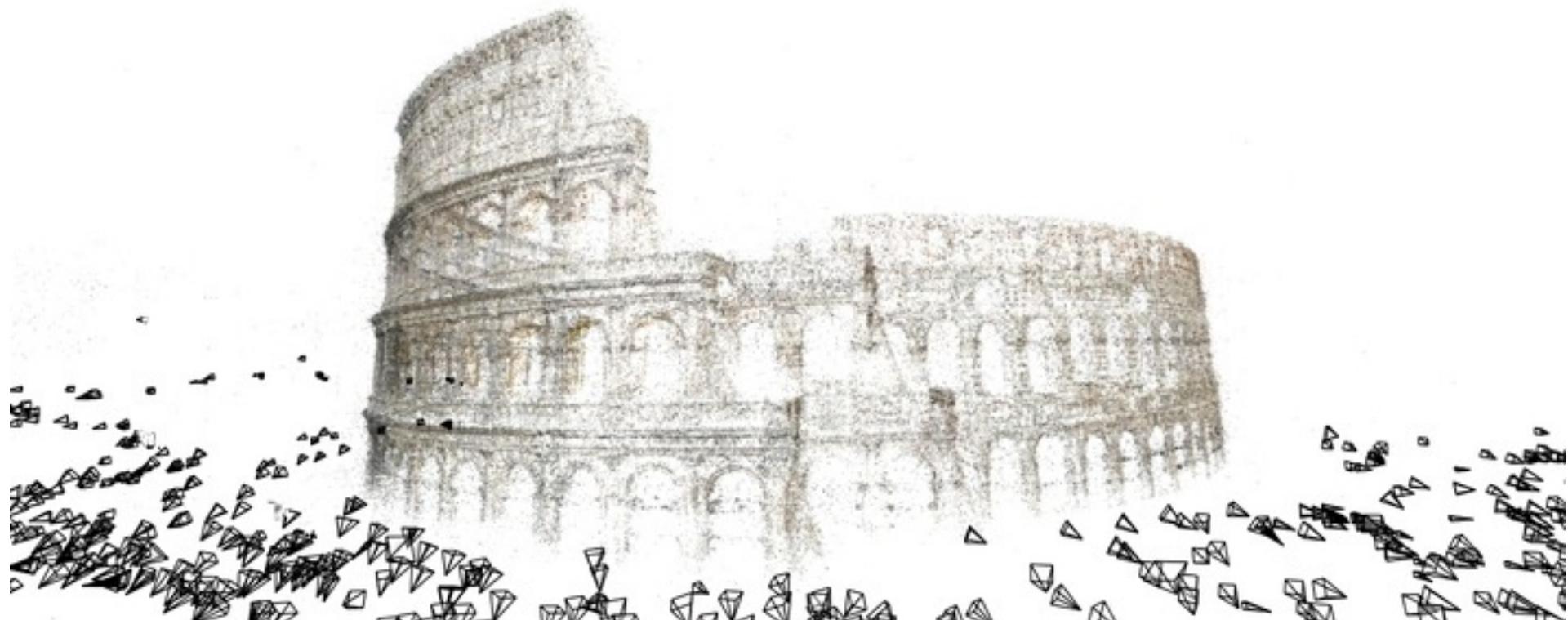
True 360°

# Trifocal Geometry



$$[\mathbf{x}'] \times \left( \sum_i x^i \mathbf{T}_i \right) [\mathbf{x}''] \times = \mathbf{0}_{3 \times 3}$$

# Structure from Motion



Building Rome in a Day  
Agarwal et al

Frank Dellaert Fall 2021

# Motivation

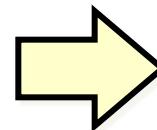
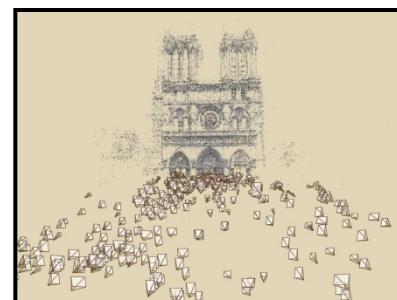
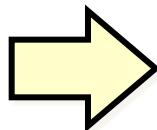
- Photo Tourism
- Photosynth
- Multi-view stereo
- Building Rome in a Day
- Rome on a Cloudless Day

# Photo Tourism

Noah Snavely, Steven M. Seitz, Richard Szeliski, [Photo tourism: Exploring photo collections in 3D," ACM Transactions on Graphics \(SIGGRAPH Proceedings\), 25\(3\), 2006, 835-846.](#)



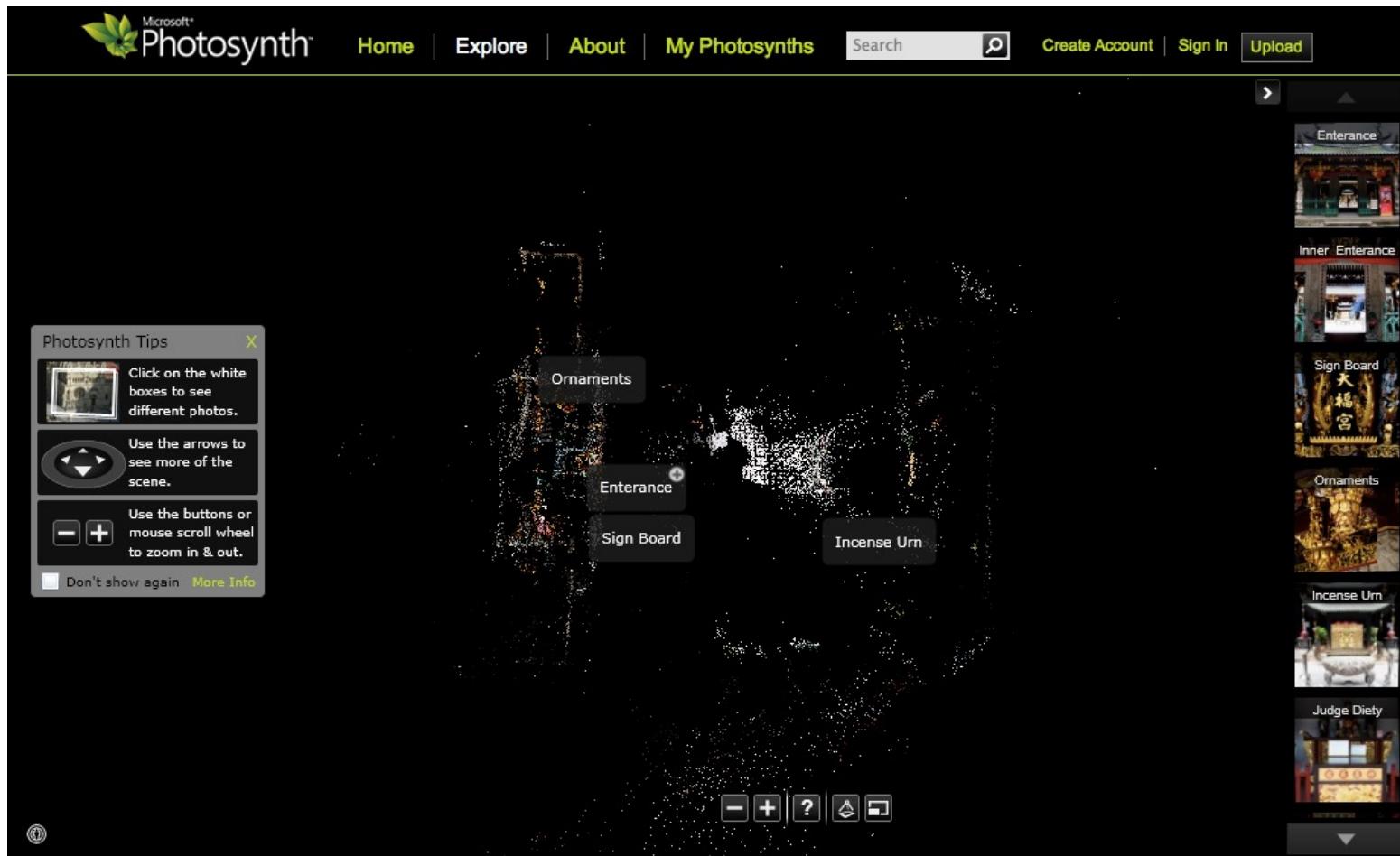
Input photographs



<http://phototour.cs.washington.edu/>

# Photosynth

[photosynth.net](http://photosynth.net)



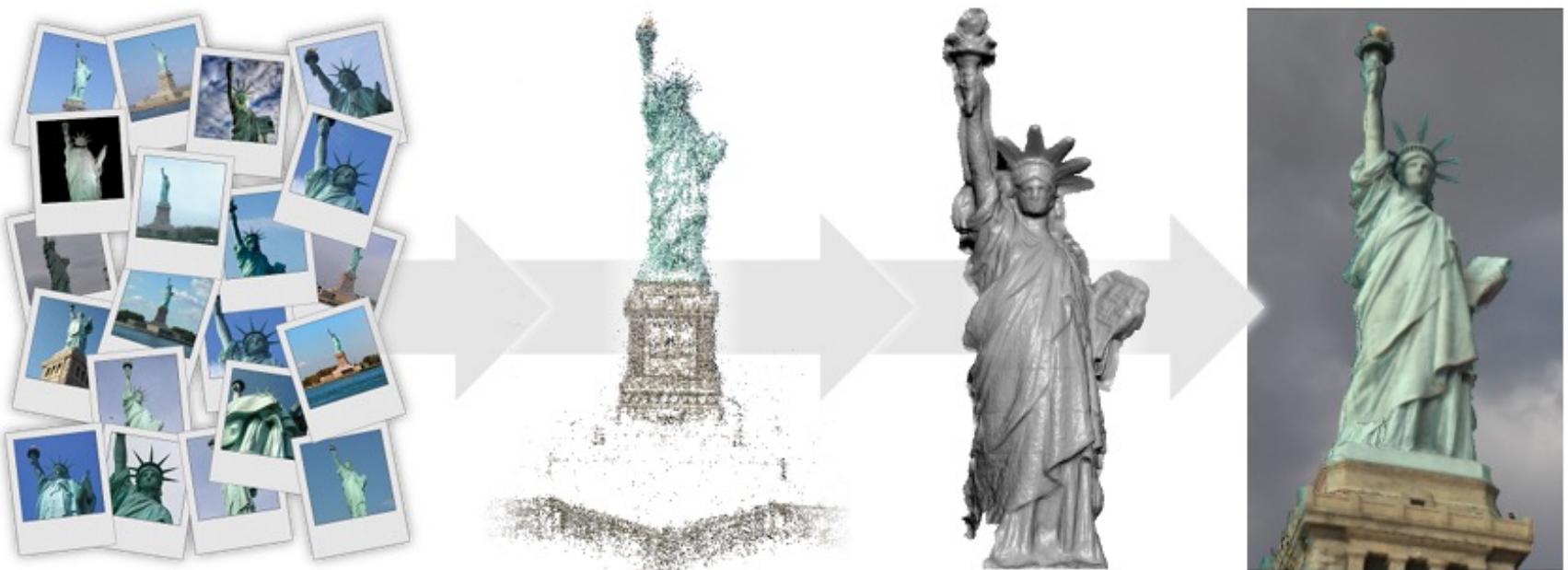
- <http://photosynth.net/view.aspx?cid=29aa8616-a43a-43e4-9d6e-b8ad9b50483e>

# Multi-view Stereo

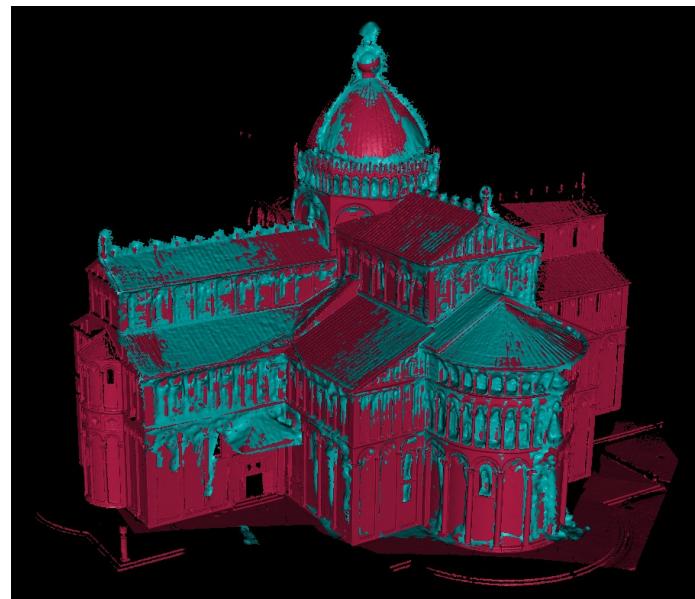
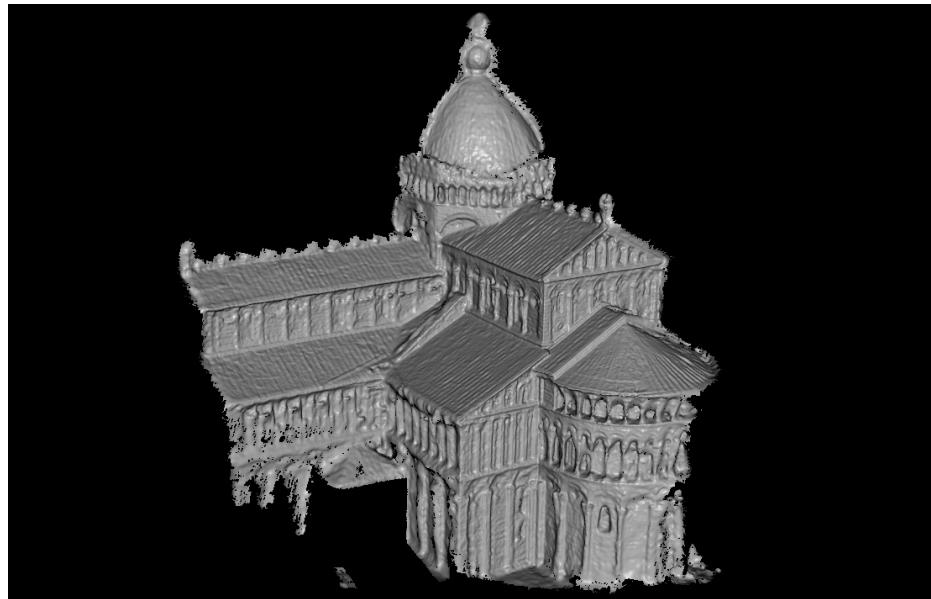
Multi-View Stereo for Community Photo Collections

Michael Goesele, Noah Snavely, Brian Curless, Hugues Hoppe, and Steven M. Seitz

ICCV 2007



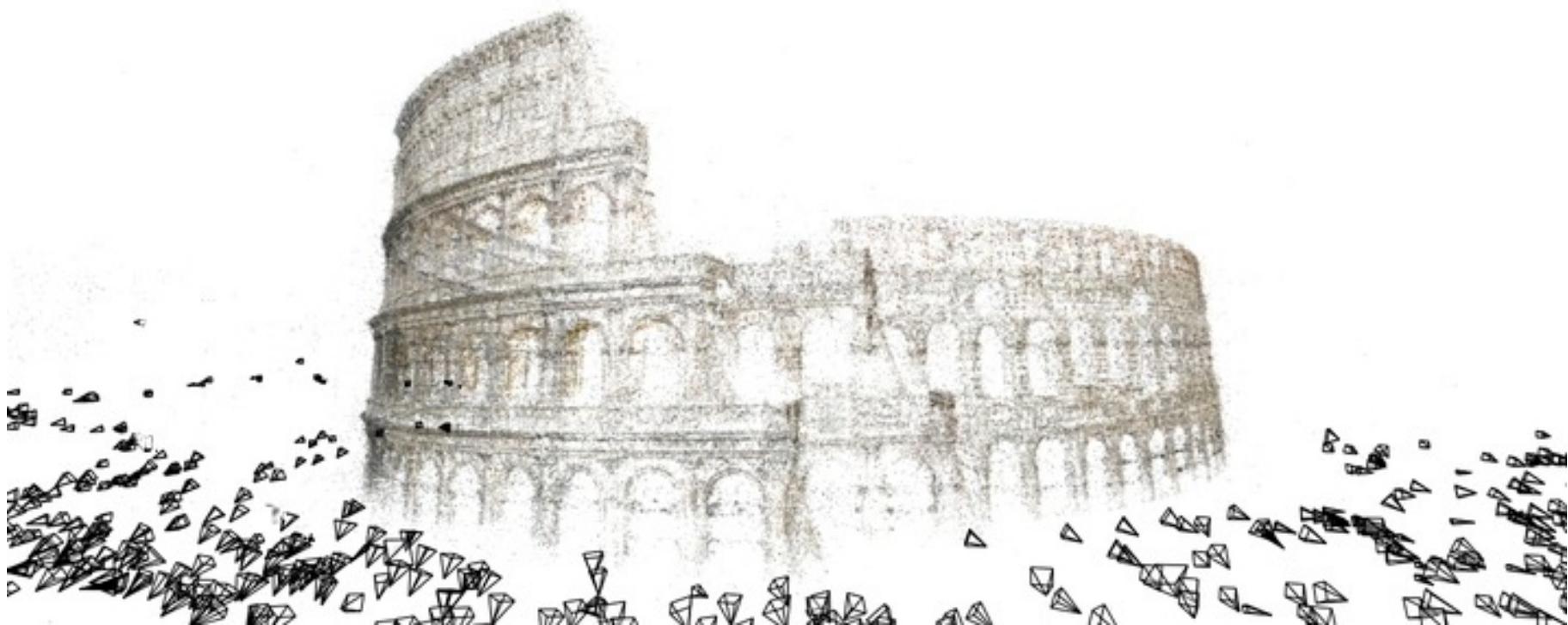
# Multi-view Stereo



Compared with Laser-Scanner

# Building Rome in a Day

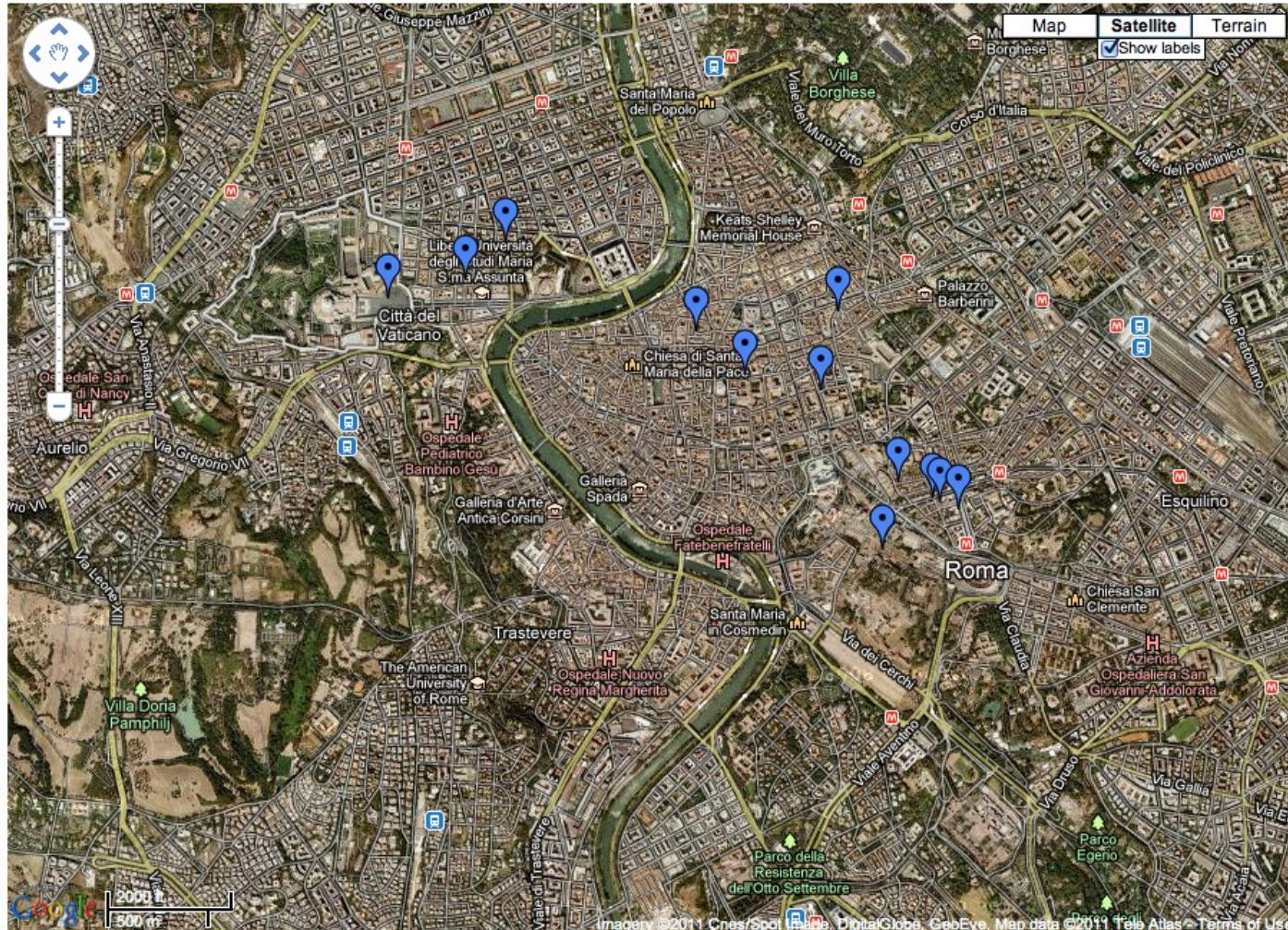
[Building Rome in a Day](#) Sameer Agarwal, Noah Snavely, Ian Simon, Steven M. Seitz and Richard Szeliski International Conference on Computer Vision, 2009, Kyoto, Japan.



<http://grail.cs.washington.edu/rome/>

# Rome on a Cloudless Day

Jan-Michael Frahm, Pierre Georgel, David Gallup, Tim Johnson, Rahul Raguram, Changchang Wu, Yi-Hung Jen, Enrique Dunn, Brian Clipp, Svetlana Lazebnik, Marc Pollefeys, *ECCV 2010*



[http://www.cs.unc.edu/~jmf/rome\\_on\\_a\\_cloudless\\_day/](http://www.cs.unc.edu/~jmf/rome_on_a_cloudless_day/)

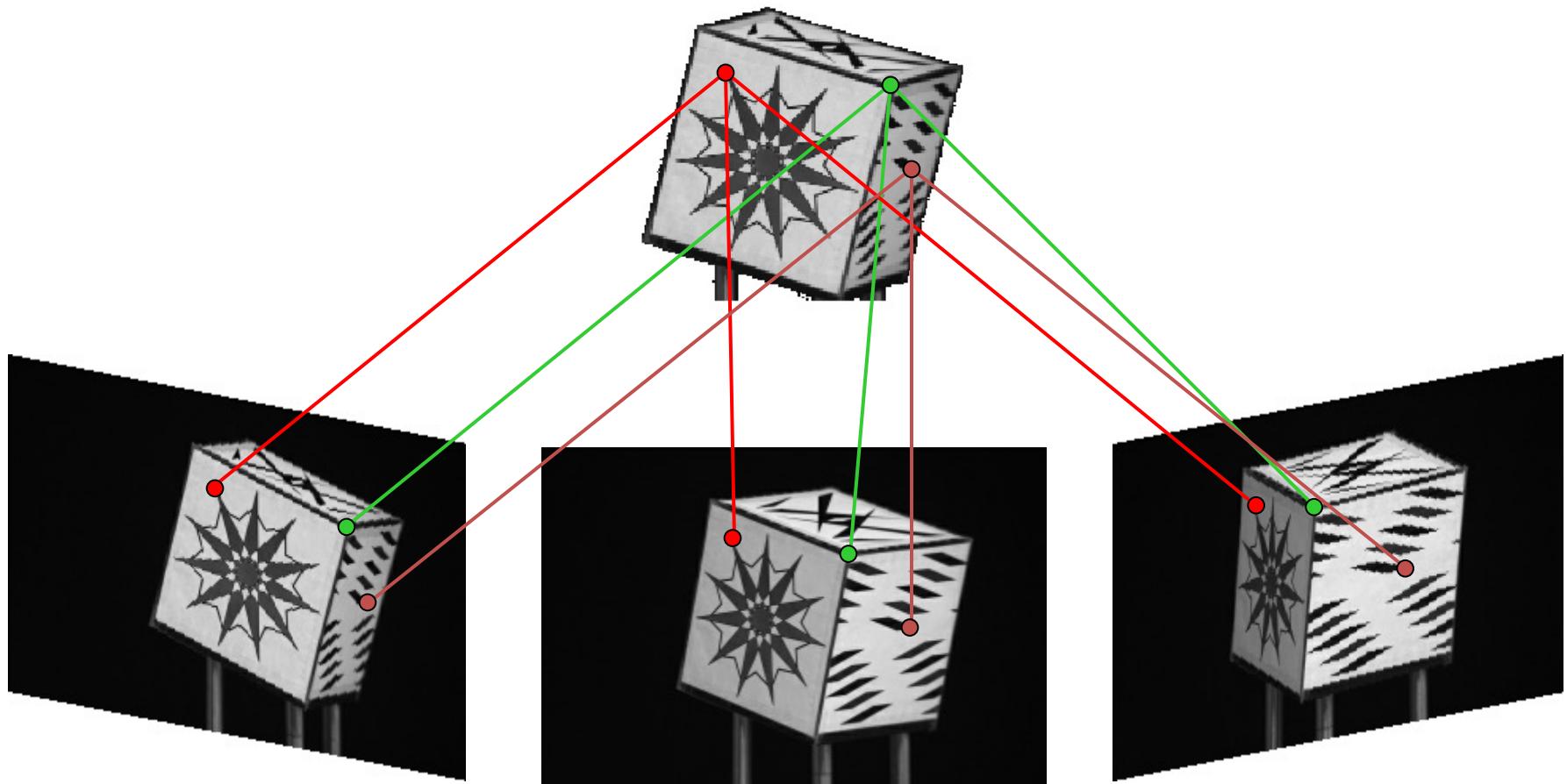
Frank Dellaert Fall 2021

# 2 Problems !

Correspondence

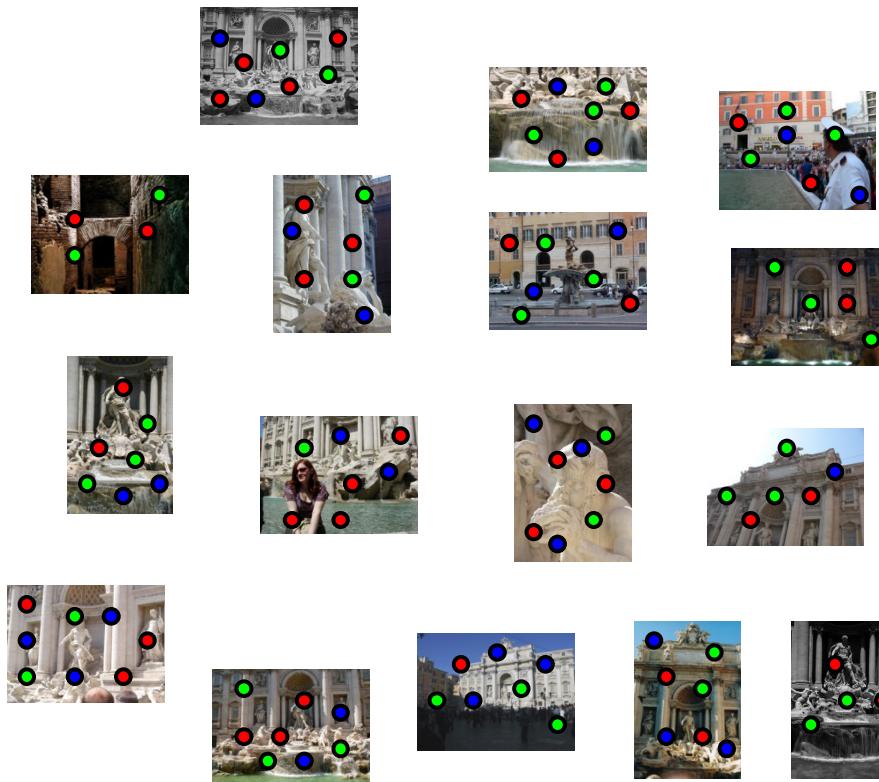
Optimization

# A Correspondence Problem

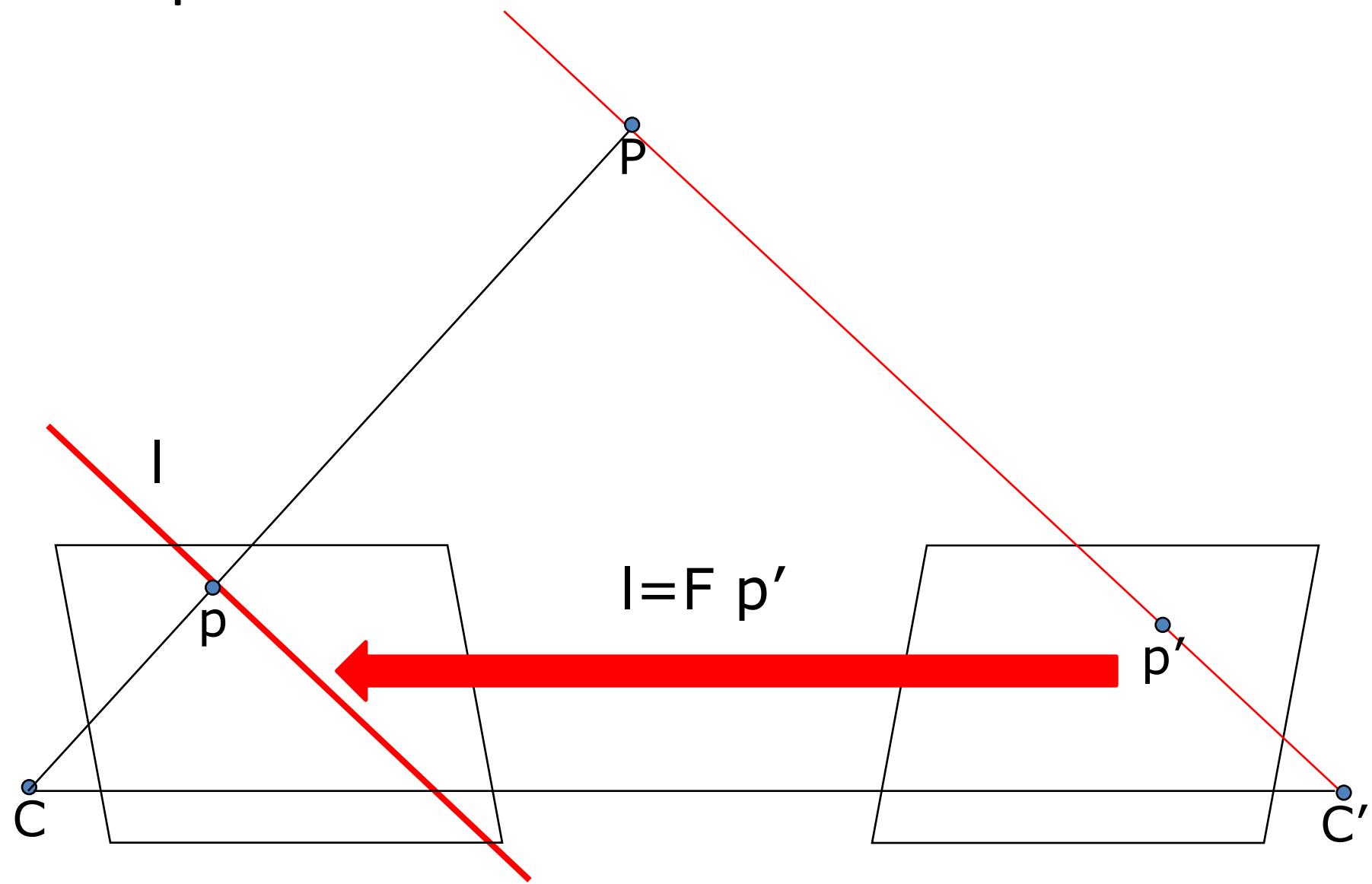


# Feature detection

- Detect features using SIFT [Lowe, IJCV 2004]

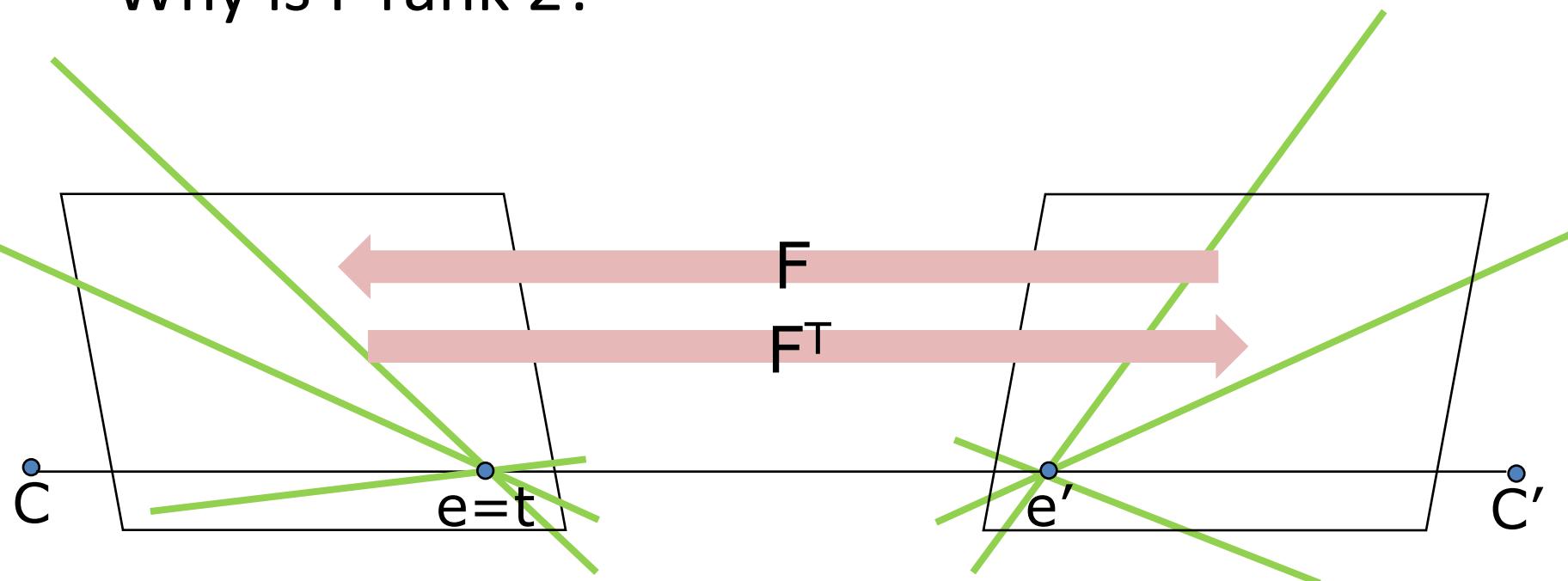


# Recap: Two views and Fundamental Matrix F



# Rank 2 Constraint

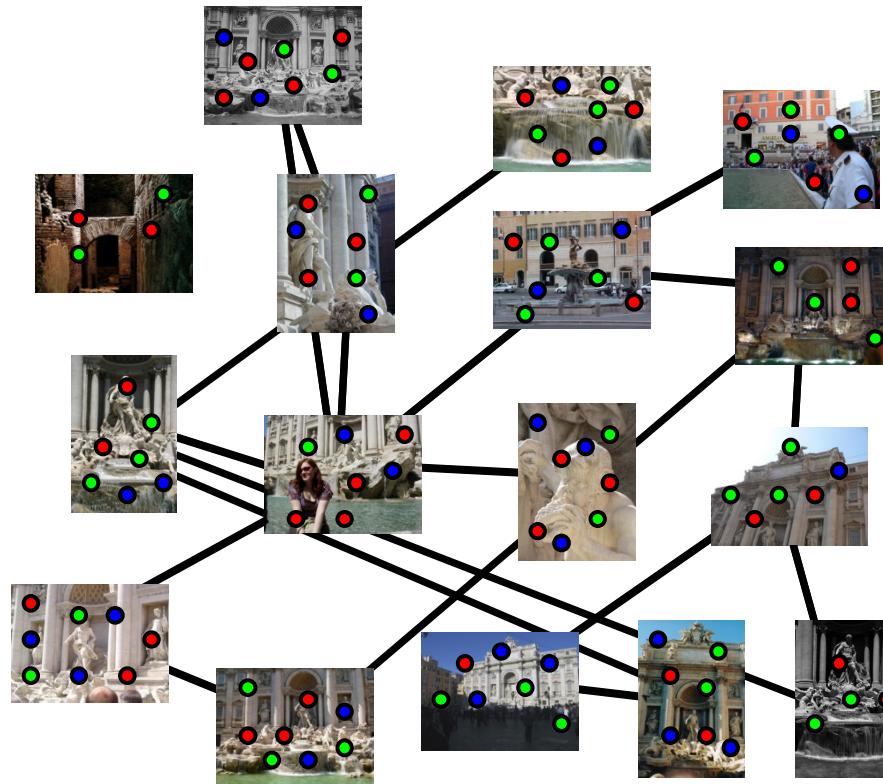
- Why is  $F$  rank 2?



- Not invertible! Collection of points is mapped to a pencil of lines. Epipoles map to zero.
- What would it mean to be rank 1?

# Feature matching

Refine matching using RANSAC [Fischler & Bolles 1987] to estimate fundamental matrices between pairs



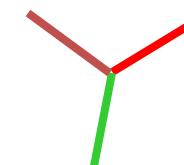
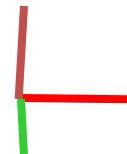
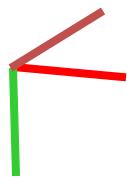
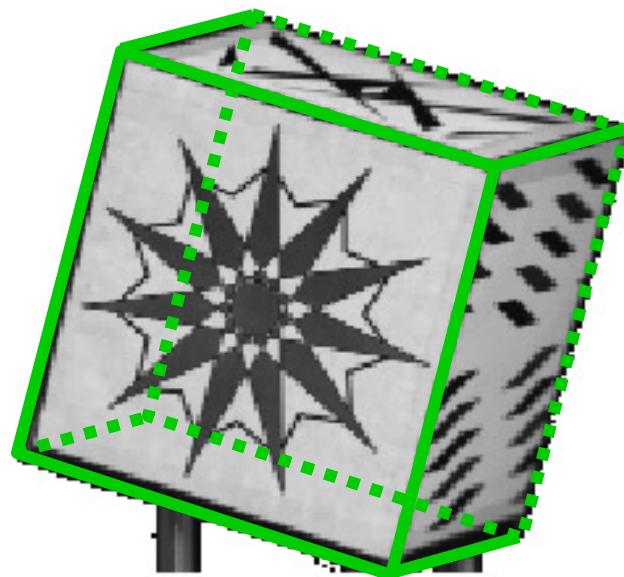
# 2 Problems !

## Correspondence

### Optimization

# An Optimization Problem

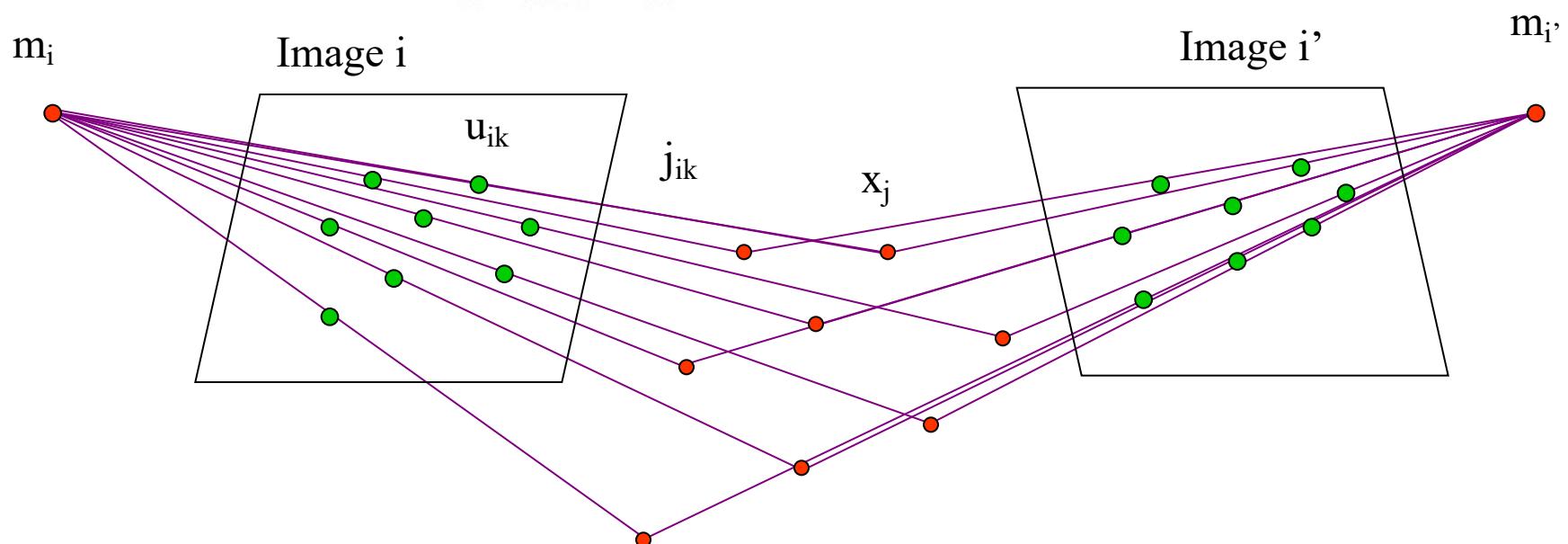
- Find the **most likely** structure and motion  $\Theta$



# Optimization

=Non-linear Least-Squares !

$$\sum_{i=1}^m \sum_{k=1}^{K_i} \|\mathbf{u}_{ik} - \mathbf{h}(\mathbf{m}_i, \mathbf{x}_{j_{ik}})\|^2$$



# Recall: Nonlinear Least Squares

$$E_{NLS} = \sum_i \|f(x_i; p) - x'_i\|^2$$

Linearize around a current guess  $p$ :

$$f(x; p + \Delta p) = f(x; p) + J(x; p)\Delta p$$

$$r = x' - f(x; p) = J(x; p)\Delta p$$

$$E_{NLS} = \sum_i \|f(x; p) + J(x; p)\Delta p - x'_i\|^2 = \sum_i \|J(x; p)\Delta p - r_i\|^2$$

Differentiate and set to 0:

$$2 \sum_i J^T(x_i; p) (J(x_i; p)\Delta p - r_i) = 0$$

$$\text{Normal equations} — \left[ \sum_i J^T(x_i; p) J(x_i; p) \right] \Delta p = \sum_i J^T(x_i; p) r_i$$

$$A\Delta p = b$$

$$\Delta p^* = A^{-1}b$$

Hessian

# 3D Models from Community Databases

- E.g., Google image search on “Dubrovnik”

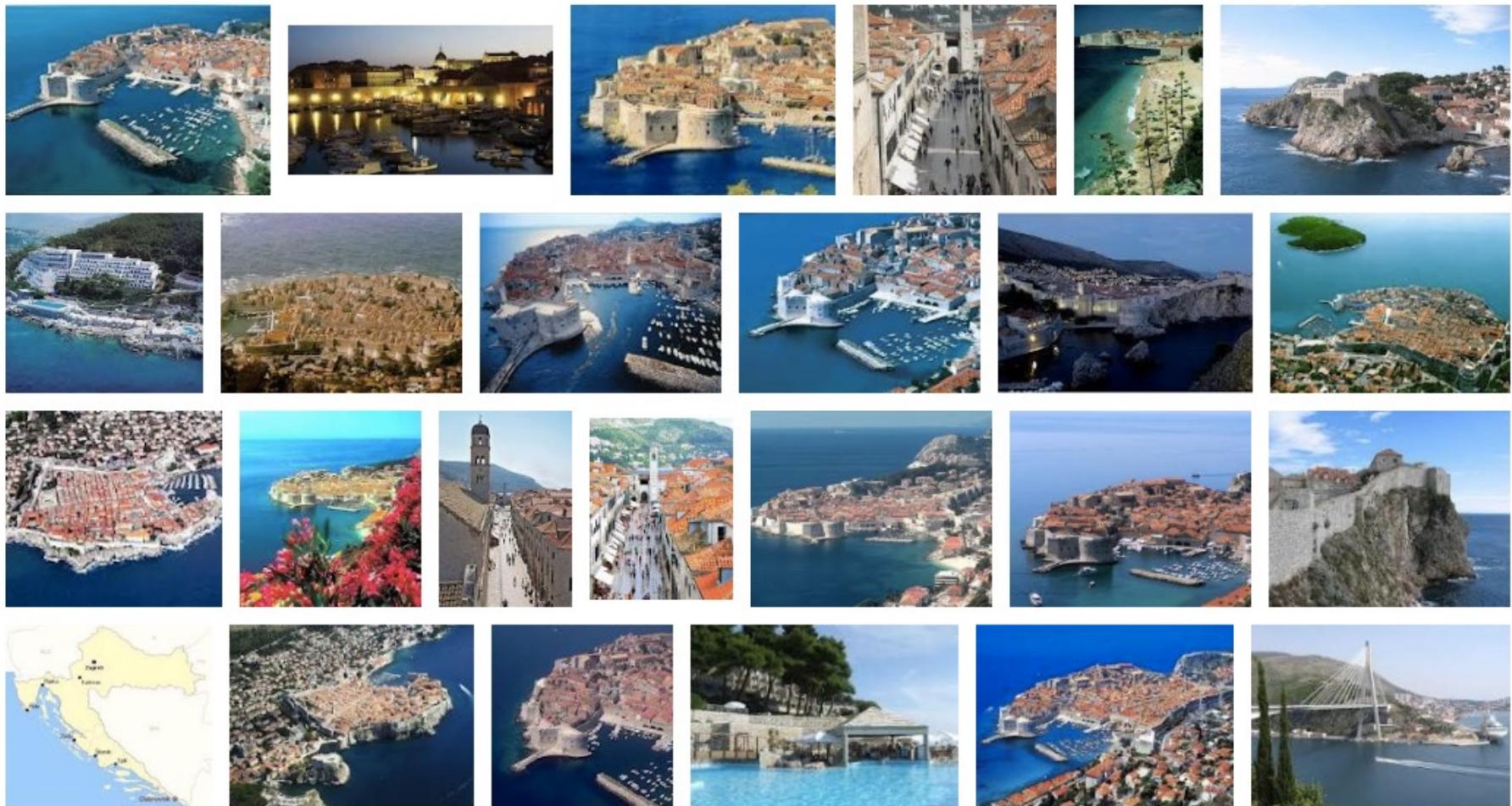


Figure by Aggarwal et al.

# 3D Models from Community Databases

Agarwal, Snavely, Seitz et al. at UW <http://grail.cs.washington.edu/rome/>

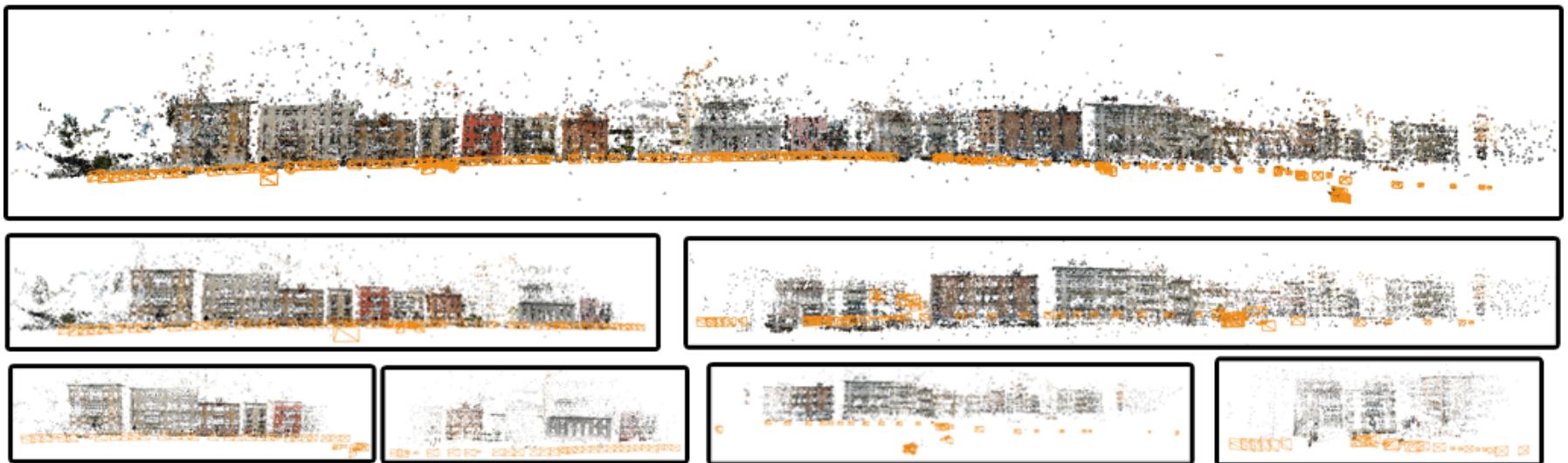


5K images, 3.5M points, >10M factors

Movie by Aggarwal et al.

Frank Dellaert Fall 2021<sup>23</sup>

# Hyper-SFM: Efficient Multi-core

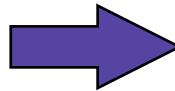


Kai now leads an  
autonomous driving  
startup in China

[Kai Ni](#), and [Frank Dellaert](#), [HyperSfM](#), [IEEE International Conference on 3D Imaging, Modeling, Processing, Visualization and Transmission \(3DIMPVT\)](#), 2012.

# 4D Reconstruction

# Spatiotemporal Reconstruction



Historical Image Collection

4D Cities: 3D + Time



Grant Schindler

Supported by NSF CAREER, Microsoft  
Recent revival: NSF NRI award on 4D  
crops for precision agriculture...

# 4D Reconstruction of Lower Manhattan



[Probabilistic Temporal Inference on Reconstructed 3D Scenes](#), G. Schindler and F. Dellaert,  
IEEE Computer Society Conference on Computer Vision and Pattern Recognition (CVPR), 2010.

# 4D Structure over Time

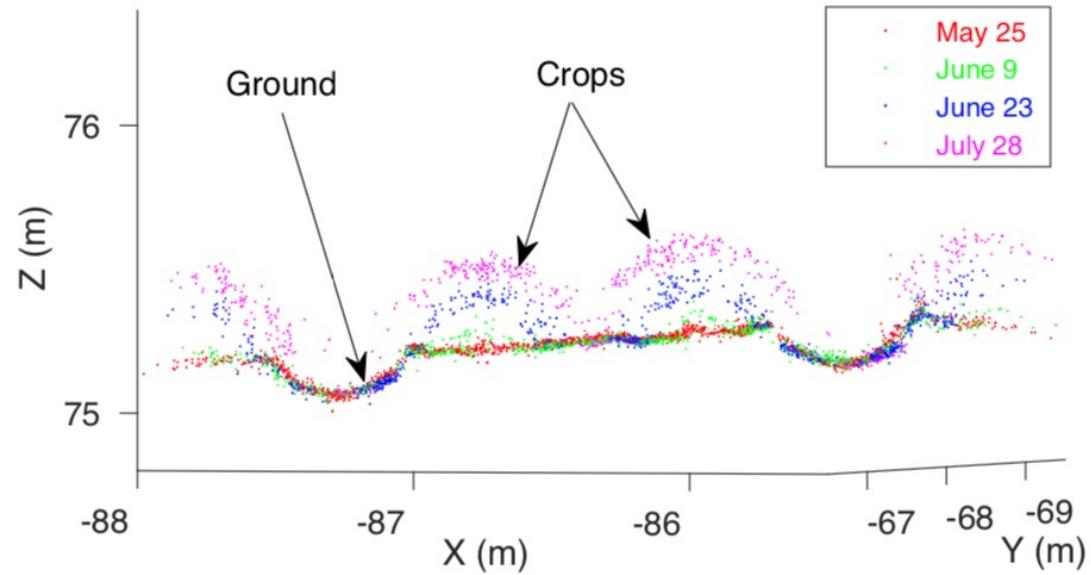
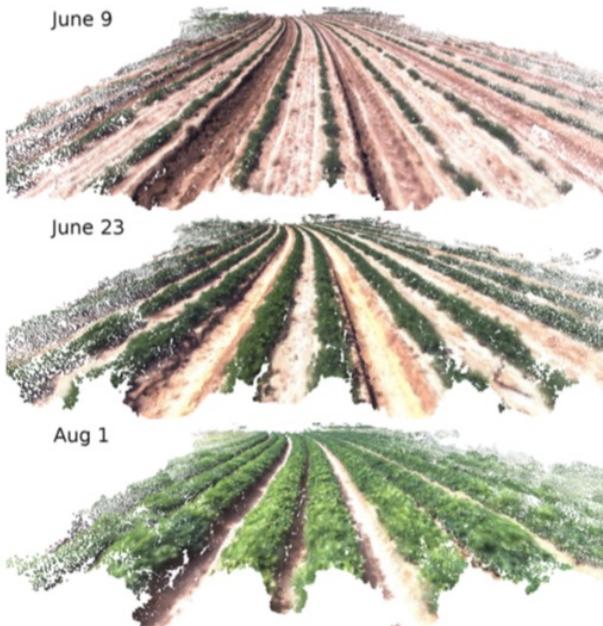


1928

2007 2010

Ilaert Fall 2021 28

# 4D crop monitoring (Jing Dong)



# Results: video (by Jing Dong)

May 25, 2016



May 25, 2016



4D reconstruction results (by PMVS)  
and its cross section