

Ex.No: 2

Implementation of Hill and RSA Cipher.

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## Aim

To implement the Hill and RSA Cipher.

## Source Code

### Hill Cipher

Python

```
def generateKeyMatrix(n, key):
    k = 0
    keyMatrix = [[ ord(key[j*n+i]) % 65 for i in range(n) ] for j in range(n)]
    return keyMatrix

def encrypt(cipherMatrix, keyMatrix, msgVctr, n):
    for i in range(n):
        for j in range(1):
            cipherMatrix[i][j] = 0
            for x in range(n):
                cipherMatrix[i][j] += (keyMatrix[i][x] * msgVctr[x][j])

            cipherMatrix[i][j] = cipherMatrix[i][j] % 26

def HillCipher(msg, key):
    n = len(msg)
    keyMatrix = generateKeyMatrix(n, key)
    msgVctr = [[ord(msg[i]) % 65] for i in range(n)]
    cipherMatrix = [[0] for _ in range(n)]

    encrypt(cipherMatrix, keyMatrix, msgVctr, n)

    CipherText = []
    for i in range(n):
        CipherText.append(chr(cipherMatrix[i][0] + 65))

    print("Ciphertext:", "".join(CipherText))

n = int(input("Length of message: "))
msg = input("Message: ")
key = input("Key of length square of message: ")

HillCipher(msg, key)
```

## RSA Cipher

Python

```
def gcd(a, b):
    while b:
        a, b = b, a % b
    return a

def findE(phi):
    e = 2
    while e < phi:
        if gcd(e, phi) == 1:
            return e
        e += 1
    return -1

def modInverse(e, phi):
    for d in range(1, phi):
        if (e * d) % phi == 1:
            return d
    return -1

def encryptRSA(message, e, n):
    messageInt = 0
    for char in message:
        messageInt = messageInt*10 + ord(char)%65

    cipher = (messageInt ** e) % n
    return cipher

p = int(input("Enter a prime number p: "))
q = int(input("Enter another prime number q: "))
n = p * q
phi = (p - 1) * (q - 1)

e = findE(phi)
d = modInverse(e, phi)

print(f"Public key (e, n): ({e}, {n})")
print(f"Private key (d, n): ({d}, {n})")

message = input("Enter the message to encrypt: ")
cipher = encryptRSA(message, e, n)
print("Encrypted message:", cipher)
```

# Sample Input and Output

## Input - Hill Cipher

Length of message: 3

Message: SKV

Key of length square of message: ACBDEGFHI

## Output

Ciphertext: PMQ

Length of message: 3

Message: SKV

Key of length square of message: ACBDEGFHI

Ciphertext: PMQ

## Input - RSA Cipher

Enter a prime number p: 23

Enter another prime number q: 11

Enter the message to encrypt: SKV

## Output

Public key (e, n): (3, 253)

Private key (d, n): (147, 253)

Encrypted message: 233

Enter a prime number p: 23

Enter another prime number q: 11

Public key (e, n): (3, 253)

Private key (d, n): (147, 253)

Enter the message to encrypt: SKV

Encrypted message: 233

## Solved Numericals

### Hill Cipher

MSG: 'SKV'      KEY = 'ACBDEGFIH'

$$\text{KEY MATRIX} = \begin{bmatrix} 0 & 2 & 1 \\ 3 & 4 & 6 \\ 5 & 7 & 8 \end{bmatrix} \quad \text{MSG VECTOR} = \begin{bmatrix} 18 \\ 10 \\ 21 \end{bmatrix}$$

$$\begin{aligned} \text{enciphered vector} &= \begin{bmatrix} 0 & 2 & 1 \\ 3 & 4 & 6 \\ 5 & 7 & 8 \end{bmatrix} \times \begin{bmatrix} 18 \\ 10 \\ 21 \end{bmatrix} \pmod{26} \\ &= \begin{bmatrix} 41 \\ 220 \\ 328 \end{bmatrix} \pmod{26} = \begin{bmatrix} 15 \\ 12 \\ 16 \end{bmatrix} \end{aligned}$$

which corresponds to PMQ.

## RSA Cipher

$$\begin{aligned}P &= 23 & Q &= 11 \\n &= 23 \times 11 = 253 & \phi &= 22 \times 10 = 220 \\&\Rightarrow e = 3 \quad [\text{gcd}(3, 220) = 1] \\d &= (k \times \phi + 1) / e, \text{ such that both } k \text{ \& } d \\&\quad \text{are positive integers} \\&\text{say } k = 2, \Rightarrow d = 147 \\&\text{thus, Public key: } \{3, 253\} \\&\quad \& \text{ Private key: } \{147, 253\} \\&\text{msg} = 'SKV' = [181021] \\&\text{encrypted msg} = (181021^3) \bmod 253 \\&\quad = 2331, 111\end{aligned}$$

## Result

Thus we have implemented the Hill and RSA Ciphers.