

$$1.1 \quad E_z = \sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2}$$

$$x'' + Kx = 0 \Rightarrow x'' = -Kx$$

$$\frac{d}{dx} [U^n] = n [U]^{n-1} \cdot U'$$

$$\frac{dE_z}{dz} = \frac{1}{2} \left( \langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2 \right)^{1/2} \cdot \frac{d}{dz} \left( \langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2 \right)^{-1/2}$$

$$= \frac{1}{2E_z} \left( \frac{d}{dz} [\langle x^2 \rangle \langle x'^2 \rangle] - \frac{d}{dz} \langle x x' \rangle^2 \right)$$

$$= \frac{1}{2E_z} \left( \left( \frac{d}{dz} \langle x^2 \rangle \right) \langle x'^2 \rangle + \langle x^2 \rangle \frac{d}{dz} \langle x'^2 \rangle - \frac{d}{dz} \langle x x' \rangle^2 \right)$$

$$= \frac{1}{2E_z} \left( \langle 2xx' \rangle \langle x'^2 \rangle + \langle x^2 \rangle \langle 2x'x'' \rangle - 2 \langle x x' \rangle \left\langle \frac{d}{dz} (x x') \right\rangle \right)$$

$$= \frac{1}{2E_z} \left( \langle 2xx' \rangle \langle x'^2 \rangle + (-K) \langle x^2 \rangle \langle 2x'x \rangle - 2 \langle x x' \rangle \left\langle \frac{d}{dz} (x x') \right\rangle \right)$$

$$= \frac{1}{2E_z} \langle 2xx' \rangle \left( \langle x'^2 \rangle - K \langle x^2 \rangle - \langle x'^2 + x x'' \rangle \right)$$

$$= \frac{1}{2E_z} \langle 2xx' \rangle \left( \cancel{\langle x'^2 \rangle} - K \cancel{\langle x^2 \rangle} - \cancel{\langle x'^2 \rangle} - K \cancel{\langle x^2 \rangle} \right)$$

$$\boxed{\frac{dE_z}{dz} = 0}$$