

5.1 For Maxwell's law to be true $\vec{\nabla} \times \vec{B} = 0$, $\vec{\nabla} \cdot \vec{B} = 0$

$$\vec{B} = \frac{-B_0}{K_y} \left[K_x \sinh(K_x X) \sinh(K_y Y) \sin(K_u Z) \hat{x} + K_y \cosh(K_x X) \cosh(K_y Y) \sin(K_u Z) \hat{y} + K_u \cosh(K_x X) \sinh(K_y Y) \cos(K_u Z) \hat{z} \right]$$

$$\vec{\nabla} \times \vec{B} = \left(\frac{\partial B_z}{\partial y} - \frac{\partial B_y}{\partial z} \right) \hat{x} + \left(\frac{\partial B_x}{\partial z} - \frac{\partial B_z}{\partial x} \right) \hat{y} + \left(\frac{\partial B_y}{\partial x} - \frac{\partial B_x}{\partial y} \right) \hat{z} = 0$$

$$\frac{\partial B_z}{\partial y} - \frac{\partial B_y}{\partial z} = K_y K_u \cosh(K_x X) \cosh(K_y Y) \cos(K_u Z) - K_y K_u \cosh(K_x X) \cosh(K_y Y) \cos(K_u Z) = 0$$

$$\frac{\partial B_x}{\partial z} - \frac{\partial B_z}{\partial x} = K_u K_x \sinh(K_x X) \sinh(K_y Y) \cos(K_u Z) - K_u K_x \sinh(K_x X) \sinh(K_y Y) \cos(K_u Z) = 0$$

$$\frac{\partial B_y}{\partial x} - \frac{\partial B_x}{\partial y} = K_y K_x \sinh(K_x X) \cosh(K_y Y) \sin(K_u Z) - K_x K_y \sinh(K_x X) \cosh(K_y Y) \sin(K_u Z) = 0$$

$$\vec{\nabla} \cdot \vec{B} = \frac{\partial}{\partial x} B_x + \frac{\partial}{\partial y} B_y + \frac{\partial}{\partial z} B_z = 0$$

$$\frac{\partial}{\partial x} [K_x \sinh(K_x X) \sinh(K_y Y) \sin(K_u Z)] + \frac{\partial}{\partial y} [K_y \cosh(K_x X) \cosh(K_y Y) \sin(K_u Z)] + \frac{\partial}{\partial z} [K_u \cosh(K_x X) \sinh(K_y Y) \cos(K_u Z)] = 0$$

$$K_x^2 \cosh(K_x X) \sinh(K_y Y) \sin(K_u Z) + K_y^2 \cosh(K_x X) \sinh(K_y Y) \sin(K_u Z) + K_u^2 \cosh(K_x X) \sinh(K_y Y) \sin(K_u Z) = 0$$

$$\Downarrow$$

$$K_x^2 + K_y^2 = K_u^2$$