## K smallest edit distances

Let  $lev_{a,b}(i,j)$  be the set of k smallest edit distances between the first i characters of the string a and the first j characters of the string b.

Let's introduce the following sets:

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\begin{split} I_{a,b}(i,j) &:= \{d+1 \mid d \in lev_{a,b}(i-1,j)\} \\ D_{a,b}(i,j) &:= \{d+1 \mid d \in lev_{a,b}(i,j-1)\} \\ S_{a,b}(i,j) &:= \{d+1_{(a_i \neq b_j)} \mid d \in lev_{a,b}(i-1,j-1)\} \\ E_{a,b}(i,j) &:= I_{a,b}(i,j) \cup D_{a,b}(i,j) \cup D_{a,b}(i,j) \\ \end{split} The set of k edit distances obtained through deletions The set of k edit distances obtained through substitutions E_{a,b}(i,j) := I_{a,b}(i,j) \cup D_{a,b}(i,j) \cup D_{a,b}(i,j) \\ \end{split} The set of k edit distances obtained through substitutions The set of k edit distances obtained through substitutions k edit dis
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Where  $1_{(a_i \neq b_j)}$  is the indicator function equal to 0 when  $a_i = b_j$  and equal to 1 otherwise.

Let's consider the set  $E_{a,b,k}(i,j) \subseteq E_{a,b}(i,j)$ , such that  $|E_{a,b,k}(i,j)| = k$ , and for every  $x \in E_{a,b,k}(i,j)$  and for every  $y \in E_{a,b}(i,j) \setminus E_{a,b,k}(i,j)$  it follows that x < y.

Then the set of k smallest edit distances between the first i characters of the string a and the first j characters of the string b is defined as follows:  $lev_{a,b}(i,j) := E_{a,b,k}(i,j)$ .

Yurii Lahodiuk, 26.11.2017