```
In [29]: import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
import scipy.stats as stats
from sklearn.decomposition import PCA
```

Load The Data Set

In [79]: data = pd.read_excel('marriage.xlsx',header=5)
 data.head()

Out[79]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	2013	2012
0	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
1	Alabama	6.697687	6.760408	7.047340	7.147821	7.351544	7.806776	7.817785	8.2
2	Alaska	6.512245	6.683952	6.914078	7.103441	7.407588	7.508836	7.293928	7.2
3	Arizona	5.302995	5.534434	5.834867	5.930541	5.922469	5.780449	5.401091	5.6
4	Arkansas	8.377284	8.863156	9.456845	9.860962	10.040279	10.112026	9.751052	10.9

In [80]: data

Out[80]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	20
0	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Nε
1	Alabama	6.697687	6.760408	7.047340	7.147821	7.351544	7.806776	7.8177
2	Alaska	6.512245	6.683952	6.914078	7.103441	7.407588	7.508836	7.2939;
3	Arizona	5.302995	5.534434	5.834867	5.930541	5.922469	5.780449	5.4010!
4	Arkansas	8.377284	8.863156	9.456845	9.860962	10.040279	10.112026	9.7510
5	California 1	5.723191	6.035132	6.278250	6.463590	6.184957	6.441492	6.4604
6	Colorado	7.273297	7.585728	7.333845	7.425443	6.791807	7.061603	6.4526
7	Connecticut	5.048401	5.278133	5.553784	5.617858	5.292009	5.368845	5.0210
8	Delaware	4.951919	5.237957	5.528417	5.613062	5.712872	6.022783	6.5719 ⁻
9	District of Columbia	7.773302	7.835377	8.239526	8.149214	8.220425	11.821343	10.7912
10	Florida	7.070065	7.332063	7.806895	8.125967	8.234362	7.301404	7.0096
11	Georgia	6.038471	6.391479	6.870975	6.753976	6.200379		
12	Hawaii	14.172891	15.263736	15.346702	15.555557	15.940173	17.702656	16.2942
13	Idaho	7.389770	7.810362	7.796997	8.077759	8.151402	8.366045	8.178
14	Illinois	5.162794	5.478499	5.982023	5.800000	5.880873	6.169054	5.3940
15	Indiana	6.176270	6.554662	6.854694	6.935419	6.856525	7.08004	6.6074
16	lowa	5.403684	5.737696	6.176028	6.149566	6.255004	6.863899	7.3909
17	Kansas	5.341683	5.366984	5.970225	6.210941	5.936515	6.101884	5.984
18	Kentucky	6.265454	6.774234	7.174146	7.379354	7.172506	6.941724	7.2786
19	Louisiana	5.094870	5.118908	5.592472	6.106373	6.777108	6.892953	6.3708
20	Maine	7.053203	7.390145	7.585857	7.640376	7.610612	7.745346	8.310
21	Maryland	5.592919	5.867393	6.268158	6.308374	6.187233	6.461575	6.8237
22	Massachusetts	5.019222	6.269931	5.749423	5.777052	5.497009	5.60485	5.5014
23	Michigan	5.183913	5.678220	5.887088	5.935155	5.984938	5.759103	5.81220
24	Minnesota	5.074090	5.304589	5.611836	5.617984	5.578555	5.895727	5.9982
25	Mississippi	6.018516	6.282877	6.720619	7.013691	6.993874	6.930345	6.7156
26	Missouri	5.969276	6.478791	6.594551	6.851633	6.800000	6.725225	6.4498
27	Montana	7.886577	7.713416	7.963880	7.840617	7.962639	7.857723	7.3987
28	Nebraska	5.498323	5.976878	6.313813	6.465784	6.378053	6.415084	6.2948
29	Nevada	25.894792	26.734186	28.556333	28.392297	31.017920	31.85095	32.2801
30	New Hampshire	6.637440	6.932762	7.030857	6.977101	6.938182	7.187147	6.9016
31	New Jersey	5.187009	5.367783	5.450804	5.654780	5.606042	5.403116	5.1308
32	New Mexico	5.981413	6.449279	5.925568	6.366124	6.171860	8.080277	7.2555
33	New York	7.217085	7.106515	7.344656	7.451752	7.056096	6.689784	6.8901;
34	North Carolina	6.181491	6.433883	6.846406	6.967624	6.959910	6.892221	6.5100
35	North Dakota	5.423443	5.682319	5.761240	5.955522	6.172326	6.300356	6.3409
36	Ohio	5.329324	5.617035	5.821192	5.956154	5.905580	5.751515	5.7089

	Unnamed: 0	2019	2018	2017	2016	2015	2014	20 ⁻
37	Oklahoma	6.336918	6.371924	6.815296	6.678882	7.418945	7.075203	7.0833
38	Oregon	5.991839	6.322075	6.660993	6.859226	6.887356	6.834097	6.3347
39	Pennsylvania	5.351512	5.545691	5.724399	5.778683	5.684592	5.84287	5.4322
40	Rhode Island	6.149934	6.297083	6.767399	6.710361	6.353321	6.669996	6.2129
41	South Carolina	6.288172	6.585398	7.034316	6.632979	7.498347	7.624033	7.1420
42	South Dakota	6.144741	6.535674	6.742819	7.247063	7.214005	7.073578	7.0057
43	Tennessee	7.488753	7.951096	8.234385	8.614092	8.502342	8.409229	8.4478
44	Texas	4.867898	6.121488	7.096127	7.077625	7.214466	6.851589	6.9763
45	Utah	8.058122	8.355306	8.720650	8.990183	8.075986	7.317947	7.5036
46	Vermont	7.726098	7.943490	7.908193	8.299792	8.124056	8.698261	9.1553
47	Virginia	6.128508	6.398452	6.783573	6.988628	6.980323	6.744421	6.6577
48	Washington	5.749260	6.023947	6.246909	6.235593	6.219361	6.956141	7.110
49	West Virginia	5.978862	6.067010	6.311620	6.354097	6.574923	6.669095	6.6440
50	Wisconsin	5.037240	5.430056	5.634561	5.616134	5.611351	5.691296	5.2191
51	Wyoming	7.008098	7.051652	7.125657	7.079407	7.341663	7.658952	7.5498
52	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Na
53	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Na
54	Data not available.	NaN	NaN	NaN	NaN	NaN	NaN	Na
55	1 Marriage data includes nonlicensed marriages	NaN	NaN	NaN	NaN	NaN	NaN	Nε
56	Note: Rate for 2015 for Missouri and for 2016	NaN	NaN	NaN	NaN	NaN	NaN	Nε
57	Source: CDC/NCHS, National Vital Statistics Sy	NaN	NaN	NaN	NaN	NaN	NaN	Nε

Cleaning Process

Out[31]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	20
1	Alabama	6.697687	6.760408	7.047340	7.147821	7.351544	7.806776	7.8177
2	Alaska	6.512245	6.683952	6.914078	7.103441	7.407588	7.508836	7.2939
3	Arizona	5.302995	5.534434	5.834867	5.930541	5.922469	5.780449	5.4010!
4	Arkansas	8.377284	8.863156	9.456845	9.860962	10.040279	10.112026	9.7510
5	California 1	5.723191	6.035132	6.278250	6.463590	6.184957	6.441492	6.4604
6	Colorado	7.273297	7.585728	7.333845	7.425443	6.791807	7.061603	6.4526
7	Connecticut	5.048401	5.278133	5.553784	5.617858	5.292009	5.368845	5.0210
8	Delaware	4.951919	5.237957	5.528417	5.613062	5.712872	6.022783	6.5719
9	District of Columbia	7.773302	7.835377	8.239526	8.149214	8.220425	11.821343	10.7912
10	Florida	7.070065	7.332063	7.806895	8.125967	8.234362	7.301404	7.0096
11	Georgia	6.038471	6.391479	6.870975	6.753976	6.200379		
12	Hawaii	14.172891	15.263736	15.346702	15.555557	15.940173	17.702656	16.2942
13	Idaho	7.389770	7.810362	7.796997	8.077759	8.151402	8.366045	8.178
14	Illinois	5.162794	5.478499	5.982023	5.800000	5.880873	6.169054	5.3940
15	Indiana	6.176270	6.554662	6.854694	6.935419	6.856525	7.08004	6.6074
16	lowa	5.403684	5.737696	6.176028	6.149566	6.255004	6.863899	7.3909
17	Kansas	5.341683	5.366984	5.970225	6.210941	5.936515	6.101884	5.984
18	Kentucky	6.265454	6.774234	7.174146	7.379354	7.172506	6.941724	7.2786
19	Louisiana	5.094870	5.118908	5.592472	6.106373	6.777108	6.892953	6.3708
20	Maine	7.053203	7.390145	7.585857	7.640376	7.610612	7.745346	8.310
21	Maryland	5.592919	5.867393	6.268158	6.308374	6.187233	6.461575	6.8237!
22	Massachusetts	5.019222	6.269931	5.749423	5.777052	5.497009	5.60485	5.5014
23	Michigan	5.183913	5.678220	5.887088	5.935155	5.984938	5.759103	5.81220
24	Minnesota	5.074090	5.304589	5.611836	5.617984	5.578555	5.895727	5.9982
25	Mississippi	6.018516	6.282877	6.720619	7.013691	6.993874	6.930345	6.7156
26	Missouri	5.969276	6.478791	6.594551	6.851633	6.800000	6.725225	6.4498
27	Montana	7.886577	7.713416	7.963880	7.840617	7.962639	7.857723	7.3987
28	Nebraska	5.498323	5.976878	6.313813	6.465784	6.378053	6.415084	6.2948
29	Nevada	25.894792	26.734186	28.556333	28.392297	31.017920	31.85095	32.2801
30	New Hampshire	6.637440	6.932762	7.030857	6.977101	6.938182	7.187147	6.9016
31	New Jersey	5.187009	5.367783	5.450804	5.654780	5.606042	5.403116	5.1308
32	New Mexico	5.981413	6.449279	5.925568	6.366124	6.171860	8.080277	7.2555!
33	New York	7.217085	7.106515	7.344656	7.451752	7.056096	6.689784	6.8901;
34	North Carolina	6.181491	6.433883	6.846406	6.967624	6.959910	6.892221	6.5100
35	North Dakota	5.423443	5.682319	5.761240	5.955522	6.172326	6.300356	6.3409
36	Ohio	5.329324	5.617035	5.821192	5.956154	5.905580	5.751515	5.7089
37	Oklahoma	6.336918	6.371924	6.815296	6.678882	7.418945	7.075203	7.0833

	Unnamed: 0	2019	2018	2017	2016	2015	2014	20
38	Oregon	5.991839	6.322075	6.660993	6.859226	6.887356	6.834097	6.3347
39	Pennsylvania	5.351512	5.545691	5.724399	5.778683	5.684592	5.84287	5.4322
40	Rhode Island	6.149934	6.297083	6.767399	6.710361	6.353321	6.669996	6.2129
41	South Carolina	6.288172	6.585398	7.034316	6.632979	7.498347	7.624033	7.1420
42	South Dakota	6.144741	6.535674	6.742819	7.247063	7.214005	7.073578	7.0057
43	Tennessee	7.488753	7.951096	8.234385	8.614092	8.502342	8.409229	8.4478
44	Texas	4.867898	6.121488	7.096127	7.077625	7.214466	6.851589	6.9763
45	Utah	8.058122	8.355306	8.720650	8.990183	8.075986	7.317947	7.5036
46	Vermont	7.726098	7.943490	7.908193	8.299792	8.124056	8.698261	9.1553
47	Virginia	6.128508	6.398452	6.783573	6.988628	6.980323	6.744421	6.6577
48	Washington	5.749260	6.023947	6.246909	6.235593	6.219361	6.956141	7.110
49	West Virginia	5.978862	6.067010	6.311620	6.354097	6.574923	6.669095	6.6440
50	Wisconsin	5.037240	5.430056	5.634561	5.616134	5.611351	5.691296	5.2191;
51	Wyoming	7.008098	7.051652	7.125657	7.079407	7.341663	7.658952	7.5498

In [32]:	data data	a = data.repl	.ace(''	,np.nan)					
	41	South Carolina	6.288172	6.585398	7.034316	6.632979	7.498347	7.624033	7.14 🔺
	42	South Dakota	6.144741	6.535674	6.742819	7.247063	7.214005	7.073578	7.00
	43	Tennessee	7.488753	7.951096	8.234385	8.614092	8.502342	8.409229	8.44
	44	Texas	4.867898	6.121488	7.096127	7.077625	7.214466	6.851589	6.97
	45	Utah	8.058122	8.355306	8.720650	8.990183	8.075986	7.317947	7.50
	46	Vermont	7.726098	7.943490	7.908193	8.299792	8.124056	8.698261	9.15
	47	Virginia	6.128508	6.398452	6.783573	6.988628	6.980323	6.744421	6.65
	48	Washington	5.749260	6.023947	6.246909	6.235593	6.219361	6.956141	7.11
	49	West Virginia	5.978862	6.067010	6.311620	6.354097	6.574923	6.669095	6.64
	50	Wisconsin	5.037240	5.430056	5.634561	5.616134	5.611351	5.691296	5.21
	51	Wyoming	7.008098	7.051652	7.125657	7.079407	7.341663	7.658952	7.54
	51 rc	ows × 24 colum	ins						~

In [33]: data.fillna(data.median(numeric_only=True),inplace=True) #get only numeric data

Out[33]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	20 ⁻
1	Alabama	6.697687	6.760408	7.047340	7.147821	7.351544	7.806776	7.8177
2	Alaska	6.512245	6.683952	6.914078	7.103441	7.407588	7.508836	7.2939
3	Arizona	5.302995	5.534434	5.834867	5.930541	5.922469	5.780449	5.4010!
4	Arkansas	8.377284	8.863156	9.456845	9.860962	10.040279	10.112026	9.7510
5	California 1	5.723191	6.035132	6.278250	6.463590	6.184957	6.441492	6.4604
6	Colorado	7.273297	7.585728	7.333845	7.425443	6.791807	7.061603	6.4526
7	Connecticut	5.048401	5.278133	5.553784	5.617858	5.292009	5.368845	5.0210
8	Delaware	4.951919	5.237957	5.528417	5.613062	5.712872	6.022783	6.5719 ⁻
9	District of Columbia	7.773302	7.835377	8.239526	8.149214	8.220425	11.821343	10.7912
10	Florida	7.070065	7.332063	7.806895	8.125967	8.234362	7.301404	7.0096
11	Georgia	6.038471	6.391479	6.870975	6.753976	6.200379	6.892587	6.7697
12	Hawaii	14.172891	15.263736	15.346702	15.555557	15.940173	17.702656	16.2942
13	Idaho	7.389770	7.810362	7.796997	8.077759	8.151402	8.366045	8.1785
14	Illinois	5.162794	5.478499	5.982023	5.800000	5.880873	6.169054	5.3940
15	Indiana	6.176270	6.554662	6.854694	6.935419	6.856525	7.080040	6.6074
16	Iowa	5.403684	5.737696	6.176028	6.149566	6.255004	6.863899	7.3909
17	Kansas	5.341683	5.366984	5.970225	6.210941	5.936515	6.101884	5.9845
18	Kentucky	6.265454	6.774234	7.174146	7.379354	7.172506	6.941724	7.2786
19	Louisiana	5.094870	5.118908	5.592472	6.106373	6.777108	6.892953	6.3708
20	Maine	7.053203	7.390145	7.585857	7.640376	7.610612	7.745346	8.3106
21	Maryland	5.592919	5.867393	6.268158	6.308374	6.187233	6.461575	6.8237!
22	Massachusetts	5.019222	6.269931	5.749423	5.777052	5.497009	5.604850	5.5014
23	Michigan	5.183913	5.678220	5.887088	5.935155	5.984938	5.759103	5.81220
24	Minnesota	5.074090	5.304589	5.611836	5.617984	5.578555	5.895727	5.9982
25	Mississippi	6.018516	6.282877	6.720619	7.013691	6.993874	6.930345	6.7156
26	Missouri	5.969276	6.478791	6.594551	6.851633	6.800000	6.725225	6.4498
27	Montana	7.886577	7.713416	7.963880	7.840617	7.962639	7.857723	7.3987
28	Nebraska	5.498323	5.976878	6.313813	6.465784	6.378053	6.415084	6.2948
29	Nevada	25.894792	26.734186	28.556333	28.392297	31.017920	31.850950	32.2801
30	New Hampshire	6.637440	6.932762	7.030857	6.977101	6.938182	7.187147	6.9016
31	New Jersey	5.187009	5.367783	5.450804	5.654780	5.606042	5.403116	5.1308
32	New Mexico	5.981413	6.449279	5.925568	6.366124	6.171860	8.080277	7.2555
33	New York	7.217085	7.106515	7.344656	7.451752	7.056096	6.689784	6.8901
34	North Carolina	6.181491	6.433883	6.846406	6.967624	6.959910	6.892221	6.5100
35	North Dakota	5.423443	5.682319	5.761240	5.955522	6.172326	6.300356	6.3409
36	Ohio	5.329324	5.617035	5.821192	5.956154	5.905580	5.751515	5.7089
37	Oklahoma	6.336918	6.371924	6.815296	6.678882	7.418945	7.075203	7.0833

	Unnamed: 0	2019	2018	2017	2016	2015	2014	20
38	Oregon	5.991839	6.322075	6.660993	6.859226	6.887356	6.834097	6.3347
39	Pennsylvania	5.351512	5.545691	5.724399	5.778683	5.684592	5.842870	5.4322
40	Rhode Island	6.149934	6.297083	6.767399	6.710361	6.353321	6.669996	6.2129
41	South Carolina	6.288172	6.585398	7.034316	6.632979	7.498347	7.624033	7.1420
42	South Dakota	6.144741	6.535674	6.742819	7.247063	7.214005	7.073578	7.0057
43	Tennessee	7.488753	7.951096	8.234385	8.614092	8.502342	8.409229	8.4478
44	Texas	4.867898	6.121488	7.096127	7.077625	7.214466	6.851589	6.9763
45	Utah	8.058122	8.355306	8.720650	8.990183	8.075986	7.317947	7.5036
46	Vermont	7.726098	7.943490	7.908193	8.299792	8.124056	8.698261	9.1553
47	Virginia	6.128508	6.398452	6.783573	6.988628	6.980323	6.744421	6.6577
48	Washington	5.749260	6.023947	6.246909	6.235593	6.219361	6.956141	7.1103
49	West Virginia	5.978862	6.067010	6.311620	6.354097	6.574923	6.669095	6.6440
50	Wisconsin	5.037240	5.430056	5.634561	5.616134	5.611351	5.691296	5.2191
51	Wyoming	7.008098	7.051652	7.125657	7.079407	7.341663	7.658952	7.5498

Analysis

```
In [34]: #Extract to Matrix
        yearM = data.columns[1:].to_numpy().astype(float)
        stateM = data.iloc[:,0]
        M = data.iloc[:,1:].to_numpy()
        Μ
Out[34]: array([[ 6.69768732, 6.76040755, 7.0473401 , ..., 10.8
                     , 10.6
               [ 6.51224463, 6.68395174, 6.91407755, ..., 8.6
                     , 10.2
                                      ],
               [ 5.30299502, 5.5344338 ,
                                         5.83486667, ..., 8.2
                 8.8
                         , 10.
                                      ],
               [ 5.97886223, 6.06700956, 6.31162035, ...,
                                                          7.5
                 6.1 , 7.2
               [ 5.03724044, 5.43005603, 5.63456057, ..., 6.7
                      , 7.9
                                      ],
               [ 7.00809836, 7.05165153, 7.12565703, ..., 9.9
                          , 10.7
                10.6
                                      11)
```

```
In [35]:
          #Make Some Plots
          fig,ax = plt.subplots(3,1,figsize=(8,5))
          ax[0].plot(yearM,M.T)
          ax[0].set_title('Marriage Rate Over Time')
          ax[0].set_ylabel('M rate (per 1k)')
          ax[1].plot(yearM, stats.zscore(M.T))
          ax[1].set title('Marriage Rate Over Time Z norm')
          ax[1].set_ylabel('M rate (per 1k)')
          ax[2].plot(yearM,np.mean(M,axis=0),'ks-')
          ax[2].set_title('State Average')
          ax[2].set_ylabel('M rate (per 1k)')
          plt.tight_layout()
          plt.show()
                                           Marriage Rate Over Time
              100
            M rate (per 1k)
               50
                0
                   1990
                               1995
                                                      2005
                                                                             2015
                                                                                        2020
                                        Marriage Rate Over Time Z norm
           rate (per 1k)
              2.5
              0.0
             -2.5
                                          2000
                                                                 2010
                   1990
                               1995
                                                     2005
                                                                             2015
                                                                                        2020
                                                State Average
             rate (per 1k)
               10
               8
             Σ
                               1995
                                          2000
                                                     2005
                   1990
                                                                 2010
                                                                             2015
                                                                                        2020
          meanM = np.mean(M,axis=1)
In [36]:
          sinM = np.argsort(meanM)
          meanM
In [37]:
Out[37]: array([ 8.66214617,
                                               6.52203674, 11.84615666,
                                                                            6.26900344,
                                 7.96626378,
                   7.5445386 ,
                                 5.65130664,
                                               6.00604285,
                                                              6.78393251,
                                                                            8.32088568,
                   6.99206978, 18.3119983 ,
                                               9.74656206,
                                                              6.2116219 ,
                                                                            7.32891628,
                   6.84681698,
                                 6.74838136,
                                               8.42548302,
                                                              7.27189114,
                                                                            7.94070218,
                   6.66562802,
                                 5.93560441,
                                               6.10611667,
                                                              5.99048123,
                                                                            6.35980892,
                   7.06388375,
                                 7.59233254,
                                               6.83664216, 50.32289676,
                                                                            7.50891741,
                   5.63914628,
                                 6.96652681,
                                               7.09808813,
                                                              7.15180648,
                                                                            6.52765902,
                                 7.2795886 ,
                   6.45172763,
                                               7.08653654,
                                                              5.7460886,
                                                                            6.82439382,
                   8.45240286,
                                 7.9766797 , 10.57164091,
                                                              7.71328474,
                                                                            9.19659999,
```

7.75572571,

6.62789308,

7.03476565,

5.93216411,

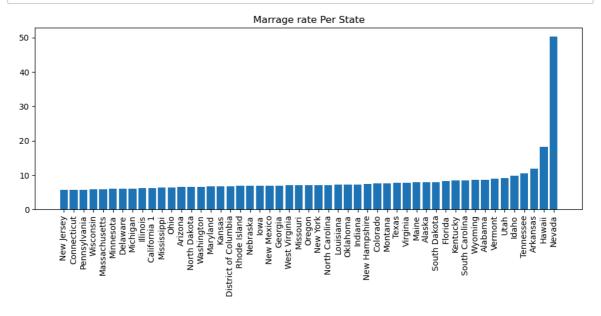
8.96327011,

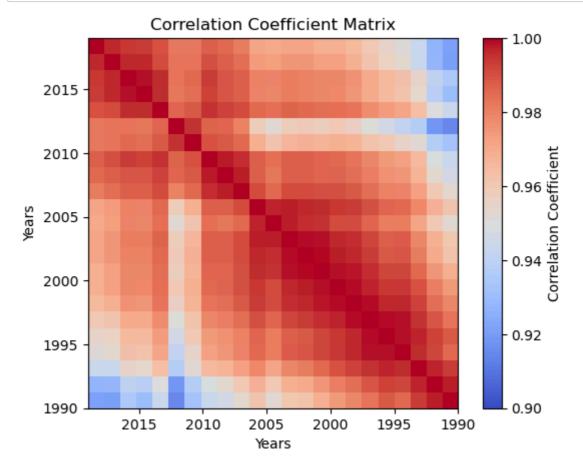
8.57892664])

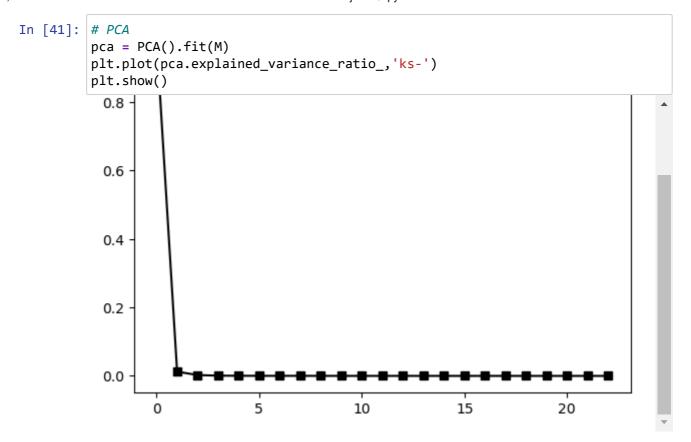
In [38]:	state	М		
Out[38]:	1	Alabama		
	2	Alaska		
	3	Arizona		
	4	Arkansas		
	5	California 1		
	6	Colorado		
	7	Connecticut		
	8	Delaware		
	9	District of Columbia		
	10	Florida		
	11	Georgia		
	12	Hawaii		
	13	Idaho		
	14	Illinois		
	15	Indiana		
	16	Iowa		
	17	Kansas		
	18	Kentucky		
	19	Louisiana		
	20	Maine		
	21	Maryland		
	22	Massachusetts		
	23	Michigan		
	24	Minnesota		
	25	Mississippi		
	26	Missouri		
	27	Montana		
	28	Nebraska		
	29 30	Nevada		
	31	New Hampshire New Jersey		
	32	New Mexico		
	33	New York		
	34	North Carolina		
	35	North Dakota		
	36	Ohio		
	37	Oklahoma		
	38	Oregon		
	39	Pennsylvania		
	40	Rhode Island		
	41	South Carolina		
	42	South Dakota		
	43	Tennessee		
	44	Texas		
	45	Utah		
	46	Vermont		
	47	Virginia		
	48	Washington		
	49	West Virginia		
	50	Wisconsin		
	51	Wyoming		
	Name:	Unnamed: 0, dtype: objec	t	

```
In [39]: fig=plt.figure(figsize=(12,4))
    plt.bar(stateM.iloc[sinM],meanM[sinM])
    plt.xticks(rotation=90)
    plt.title('Marrage rate Per State')
    plt.show()

#Q
#is Navada a non representative data Or Error ?
```







Divorce Data Analysis

```
In [43]: dataD = pd.read_excel('divorce.xlsx',header=5)
dataD.head()
```

Out[43]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	2013	2012	20
0	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Ni
1	Alabama	3.572984	3.714296	3.660498	3.77871	3.85369	3.785022	3.68329	3.6	2
2	Alaska	3.638874	3.734551	3.580722	3.946655	4.138499	3.951233	4.461784	4.5	2
3	Arizona	2.915899	2.954273	3.479199	3.352007	3.578466	3.89201	3.92915	4.3	:
4	Arkansas	4.017159	4.066925	3.719694	3.926381	4.842516	4.845318	5.011872	5.3	ţ

In [44]: dataD.drop([0,52,53,54,55,56,57],axis=0,inplace=True)
 dataD

Out[44]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	2013	2012
1	Alabama	3.572984	3.714296	3.660498	3.77871	3.85369	3.785022	3.68329	3.6
2	Alaska	3.638874	3.734551	3.580722	3.946655	4.138499	3.951233	4.461784	4.5
3	Arizona	2.915899	2.954273	3.479199	3.352007	3.578466	3.89201	3.92915	4.3
4	Arkansas	4.017159	4.066925	3.719694	3.926381	4.842516	4.845318	5.011872	5.3
5	California								
6	Colorado	3.291	3.2736	3.186287	3.566256	3.725048	3.866602	4.073558	4.3
7	Connecticut	2.690386	2.853612	2.870533	3.168503	3.128197	2.577657	2.761618	2.7
8	Delaware	2.915491	2.800952	2.964845	3.079622	3.093239	3.256685	3.383206	3.5
9	District of Columbia	2.422958	2.521158	2.477045	2.739404	2.832372	2.57705	2.838584	2.9
10	Florida	3.489101	3.617673	3.612112	3.865675	3.956535	3.970182	4.110652	4.2
11	Georgia	2.287278	2.502691	3.496277					
12	Hawaii								
13	Idaho	3.857722	3.838199	3.884812	4.034127	4.12525	4.248488	4.495899	4.7
14	Illinois	1.293579	1.506623	1.870798	2.2	2.196579	2.213332	2.270509	2.4
15	Indiana								
16	lowa	2.258904	2.232153	1.963944	1.254668	1.211307	1.50525	1.865768	2.2
17	Kansas	2.32862	2.309802	2.379234	2.692543	2.82109	2.967954	2.972055	3.4
18	Kentucky	3.433107	3.54422	3.726604	3.788167	3.702296	3.849137	4.162633	4.1
19	Louisiana	2.399117	1.736703	1.923219	2.042863	2.772589	2.250479	2.170806	
20	Maine	3.033004	3.197091	3.226272	3.428518	3.428048	3.581715	3.96973	3.9
21	Maryland	2.661901	2.400575	2.542721	2.686968	2.595564	2.541828	2.533559	2.8
22	Massachusetts	1.463184	2.116008	2.165801	2.290151	2.552977	2.680787	2.626694	2.7
23	Michigan	2.328661	2.844962	2.848937	2.908151	3.045681	2.997817	3.259926	3.1
24	Minnesota								
25	Mississippi	2.625541	2.71787	2.900372	3.20471	3.37028	3.371321	3.587181	4
26	Missouri	2.890462	3.040912	3.138448	3.281963	3.177357	3.278092	3.42214	3.7
27	Montana	2.997816	3.033027	3.109968	3.104976	3.425145	3.447707	3.388612	3.9
28	Nebraska	2.663864	2.949305	3.024359	3.136149	3.177952	3.054473	3.278538	3.4
29	Nevada	4.170243	4.376824	4.459582	4.294473	4.636707	5.330212	5.121614	5.ŧ
30	New Hampshire	3.072712	3.089664	3.11291	3.37505	3.328554	3.543077	3.726598	3.6
31	New Jersey	2.519086	2.746809	2.600813	2.668465	2.817924	2.778755	2.785263	2.8
32	New Mexico					3.288078	3.551544	3.437417	•
33	New York	2.89253	2.780085	2.676303	2.681045	2.707495	2.843986	2.735467	2.9
34	North Carolina	3.13327	3.075324	3.109968	3.248319	3.082307	3.401963	3.429203	3.7
35	North Dakota	2.481425	2.557636	2.486123	2.589874	2.839111	2.83036	2.943075	3.′
36	Ohio	2.768733	2.905956	2.922647	3.029867	3.07136	3.174787	3.294843	3.4
37	Oklahoma	3.91082	3.766853	4.070861	4.369755	4.374973	4.538878	4.497778	4.8

	Unnamed: 0	2019	2018	2017	2016	2015	2014	2013	2012
38	Oregon	3.191285	3.368639	3.381066	3.357058	3.422953	3.425235	3.619024	3.8
39	Pennsylvania	2.576553	2.608874	2.559596	2.639894	2.624487	2.662817	2.679782	2.8
40	Rhode Island	2.740331	2.913039	2.88872	2.841657	2.993473	2.84124	3.145949	3.2
41	South Carolina	2.587248	2.526491	2.617841	2.520198	2.77361	2.925619	3.18838	3.2
42	South Dakota	2.622479	2.567343	2.694138	2.784666	2.623275	2.782548	2.89983	:
43	Tennessee	3.48827	3.511221	3.546465	3.764136	3.694833	3.79717	4.132249	4.2
44	Texas	2.115818	2.582621	2.249599	2.6	2.589199	2.700045	2.889763	:
45	Utah	3.500982	3.774313	3.440224	3.587749	3.556838	3.078254	3.095966	3.3
46	Vermont	2.823768	3.081595	2.921478	3.098012	3.078068	3.460152	3.549144	3.5
47	Virginia	2.901522	3.07971	3.035766	3.373948	3.300969	3.481623	3.558905	3.7
48	Washington	2.844557	3.298481	3.406951	3.483672	3.383098	3.649351	3.821467	3.9
49	West Virginia	3.578947	3.254456	3.478798	3.7573	3.980201	4.1998	4.587166	4.7
50	Wisconsin	2.33064	2.457527	2.433102	2.597986	2.596625	2.656853	2.775866	2.9
51	Wyoming	3.799509	3.754303	3.961575	4.203238	4.149413	4.603246	4.259789	4.4

In [45]: dataD = dataD.replace('---',np.nan)
 dataD.fillna(dataD.median(numeric_only=True),inplace=True) #get only numeric
 dataD

Out[45]:

	Unnamed: 0	2019	2018	2017	2016	2015	2014	2013	2012
1	Alabama	3.572984	3.714296	3.660498	3.778710	3.853690	3.785022	3.683290	3.6
2	Alaska	3.638874	3.734551	3.580722	3.946655	4.138499	3.951233	4.461784	4.
3	Arizona	2.915899	2.954273	3.479199	3.352007	3.578466	3.892010	3.929150	4.3
4	Arkansas	4.017159	4.066925	3.719694	3.926381	4.842516	4.845318	5.011872	5.0
5	California	2.867509	2.951789	3.030063	3.168503	3.177654	3.324706	3.405376	3.5
6	Colorado	3.291000	3.273600	3.186287	3.566256	3.725048	3.866602	4.073558	4.3
7	Connecticut	2.690386	2.853612	2.870533	3.168503	3.128197	2.577657	2.761618	2.7
8	Delaware	2.915491	2.800952	2.964845	3.079622	3.093239	3.256685	3.383206	3.5
9	District of Columbia	2.422958	2.521158	2.477045	2.739404	2.832372	2.577050	2.838584	2.9
10	Florida	3.489101	3.617673	3.612112	3.865675	3.956535	3.970182	4.110652	4.2
11	Georgia	2.287278	2.502691	3.496277	3.168503	3.177654	3.324706	3.405376	3.5
12	Hawaii	2.867509	2.951789	3.030063	3.168503	3.177654	3.324706	3.405376	3.5
13	Idaho	3.857722	3.838199	3.884812	4.034127	4.125250	4.248488	4.495899	4.7
14	Illinois	1.293579	1.506623	1.870798	2.200000	2.196579	2.213332	2.270509	2.4
15	Indiana	2.867509	2.951789	3.030063	3.168503	3.177654	3.324706	3.405376	3.5
16	lowa	2.258904	2.232153	1.963944	1.254668	1.211307	1.505250	1.865768	2.2
17	Kansas	2.328620	2.309802	2.379234	2.692543	2.821090	2.967954	2.972055	3.4
18	Kentucky	3.433107	3.544220	3.726604	3.788167	3.702296	3.849137	4.162633	4.1
19	Louisiana	2.399117	1.736703	1.923219	2.042863	2.772589	2.250479	2.170806	3.
20	Maine	3.033004	3.197091	3.226272	3.428518	3.428048	3.581715	3.969730	3.9
21	Maryland	2.661901	2.400575	2.542721	2.686968	2.595564	2.541828	2.533559	2.8
22	Massachusetts	1.463184	2.116008	2.165801	2.290151	2.552977	2.680787	2.626694	2.7
23	Michigan	2.328661	2.844962	2.848937	2.908151	3.045681	2.997817	3.259926	3.0
24	Minnesota	2.867509	2.951789	3.030063	3.168503	3.177654	3.324706	3.405376	3.5
25	Mississippi	2.625541	2.717870	2.900372	3.204710	3.370280	3.371321	3.587181	4.(
26	Missouri	2.890462	3.040912	3.138448	3.281963	3.177357	3.278092	3.422140	3.7
27	Montana	2.997816	3.033027	3.109968	3.104976	3.425145	3.447707	3.388612	3.9
28	Nebraska	2.663864	2.949305	3.024359	3.136149	3.177952	3.054473	3.278538	3.4
29	Nevada	4.170243	4.376824	4.459582	4.294473	4.636707	5.330212	5.121614	5.ŧ
30	New Hampshire	3.072712	3.089664	3.112910	3.375050	3.328554	3.543077	3.726598	3.6
31	New Jersey	2.519086	2.746809	2.600813	2.668465	2.817924	2.778755	2.785263	2.8
32	New Mexico	2.867509	2.951789	3.030063	3.168503	3.288078	3.551544	3.437417	3.0
33	New York	2.892530	2.780085	2.676303	2.681045	2.707495	2.843986	2.735467	2.9
34	North Carolina	3.133270	3.075324	3.109968	3.248319	3.082307	3.401963	3.429203	3.7
35	North Dakota	2.481425	2.557636	2.486123	2.589874	2.839111	2.830360	2.943075	3.′
36	Ohio	2.768733	2.905956	2.922647	3.029867	3.071360	3.174787	3.294843	3.4
37	Oklahoma	3.910820	3.766853	4.070861	4.369755	4.374973	4.538878	4.497778	4.8

	Unnamed: 0	2019	2018	2017	2016	2015	2014	2013	2012
38	Oregon	3.191285	3.368639	3.381066	3.357058	3.422953	3.425235	3.619024	3.8
39	Pennsylvania	2.576553	2.608874	2.559596	2.639894	2.624487	2.662817	2.679782	2.8
40	Rhode Island	2.740331	2.913039	2.888720	2.841657	2.993473	2.841240	3.145949	3.2
41	South Carolina	2.587248	2.526491	2.617841	2.520198	2.773610	2.925619	3.188380	3.2
42	South Dakota	2.622479	2.567343	2.694138	2.784666	2.623275	2.782548	2.899830	3.0
43	Tennessee	3.488270	3.511221	3.546465	3.764136	3.694833	3.797170	4.132249	4.2
44	Texas	2.115818	2.582621	2.249599	2.600000	2.589199	2.700045	2.889763	3.0
45	Utah	3.500982	3.774313	3.440224	3.587749	3.556838	3.078254	3.095966	3.0
46	Vermont	2.823768	3.081595	2.921478	3.098012	3.078068	3.460152	3.549144	3.5
47	Virginia	2.901522	3.079710	3.035766	3.373948	3.300969	3.481623	3.558905	3.7
48	Washington	2.844557	3.298481	3.406951	3.483672	3.383098	3.649351	3.821467	3.9
49	West Virginia	3.578947	3.254456	3.478798	3.757300	3.980201	4.199800	4.587166	4.7
50	Wisconsin	2.330640	2.457527	2.433102	2.597986	2.596625	2.656853	2.775866	2.9
51	Wyoming	3.799509	3.754303	3.961575	4.203238	4.149413	4.603246	4.259789	4.4

```
In [46]: yearD = dataD.columns[1:].to_numpy().astype(float)
         stateD = dataD.iloc[:,0]
         D = dataD.iloc[:,1:].to_numpy()
         D
Out[46]: array([[3.57298368, 3.71429606, 3.66049766, ..., 5.7
                                                                     , 6.
                 6.1
                [3.63887389, 3.73455124, 3.58072169, ..., 5.
                                                                     , 5.
                 5.5
                [2.9158985, 2.95427298, 3.47919906, ..., 4.6]
                                                                     , 6.2
                 6.9
                . . . ,
                [3.57894749, 3.25445556, 3.47879817, ..., 4.9
                                                                     , 5.2
                [2.33064042, 2.45752694, 2.43310178, ..., 3.2
                                                                     , 3.4
                 3.6
                           ],
                [3.79950895, 3.75430343, 3.96157531, ..., 5.7
                                                                     , 6.6
                 6.6
                           ]])
```

```
In [47]:
           #Make Some PLots
           fig,ax = plt.subplots(3,1,figsize=(8,5))
           ax[0].plot(yearD,D.T)
           ax[0].set_title('Divorce Rate Over Time')
           ax[0].set_ylabel('D rate (per 1k)')
           ax[1].plot(yearD, stats.zscore(D.T))
           ax[1].set_title('Divorce Rate Over Time Z norm')
           ax[1].set_ylabel('D rate (per 1k)')
           ax[2].plot(yearD,np.mean(D,axis=0),'ks-')
           ax[2].set_title('State Average')
           ax[2].set_ylabel('D rate (per 1k)')
           plt.tight_layout()
           plt.show()
                                               Divorce Rate Over Time
             D rate (per 1k)
2 01
                     1990
                                 1995
                                                         2005
                                                                                 2015
                                                                                             2020
                                           Divorce Rate Over Time Z norm
            D rate (per 1k)
               2.5
               0.0
              -2.5
                     1990
                                 1995
                                             2000
                                                         2005
                                                                     2010
                                                                                 2015
                                                                                             2020
                                                   State Average
              D rate (per 1k)
ω <sub>6</sub> σ
```

1990

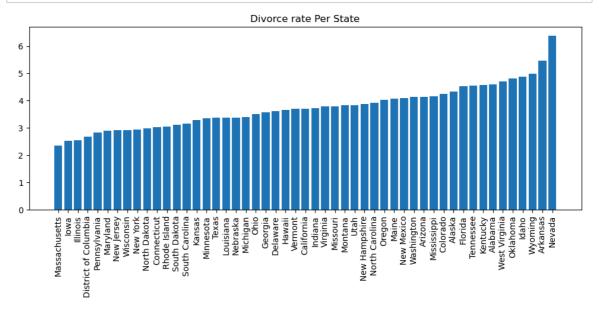
1995

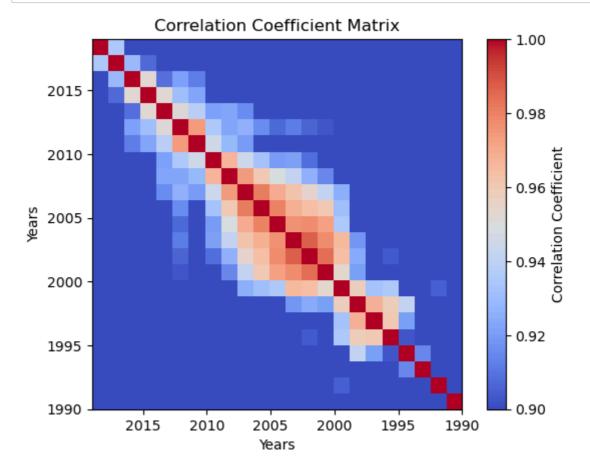
วกกก

วกกร

วก่าก

วก่วก





```
In [50]: # PCA
pca = PCA().fit(D)
plt.plot(pca.explained_variance_ratio_,'ks-')
plt.show()

0.8 -

0.4 -

0.2 -
```

Comparison

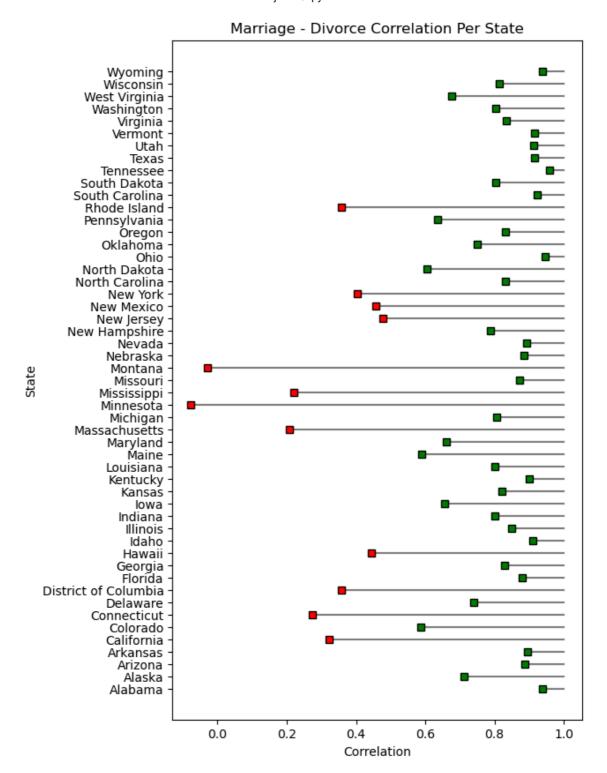
```
In [54]: statenames = pd.concat([stateM,stateD],axis=1)
    print(statenames)
```

	Unnamed: 0	Unnamed: 0
1	Alabama	Alabama
2	Alaska	Alaska
3	Arizona	Arizona
4	Arkansas	Arkansas
5	California 1	California
6	Colorado	Colorado
7	Connecticut	Connecticut
8	Delaware	Delaware
9	District of Columbia	District of Columbia
10	Florida	Florida
11	Georgia	Georgia
12	Hawaii	Hawaii
		Idaho
13	Idaho	
14	Illinois	Illinois
15	Indiana	Indiana
16	Iowa	Iowa
17	Kansas	Kansas
18	Kentucky	Kentucky
19	Louisiana	Louisiana
20	Maine	Maine
21	Maryland	Maryland
22	Massachusetts	Massachusetts
23	Michigan	Michigan
24	Minnesota	Minnesota
25	Mississippi	Mississippi
26	Missouri	Missouri
27	Montana	Montana
28	Nebraska	Nebraska
29	Nevada	Nevada
30	New Hampshire	New Hampshire
31	New Jersey	New Jersey
32	New Mexico	New Mexico
33	New York	New York
34	North Carolina	North Carolina
35	North Dakota	North Dakota
36	Ohio	Ohio
37	Oklahoma	Oklahoma
38	Oregon	Oregon
39	Pennsylvania	Pennsylvania
40	Rhode Island	Rhode Island
41	South Carolina	South Carolina
42	South Dakota	South Dakota
43	Tennessee	Tennessee
44	Texas	Texas
45	Utah	Utah
46	Vermont	Vermont
47	Virginia	Virginia
48	Washington	Washington
49	West Virginia	West Virginia
50	Wisconsin	Wisconsin
51	Wyoming	Wyoming

It just a type error. Do not worry about that

Inferencial Statistics

```
In [78]: #correlate M and D over time per state
         #Bonferroni Correlated Threshold
         pvalT = 0.5/51
         fig = plt.figure(figsize=(6,10))
         color = 'rg'
         for si in range(len(stateM)):
             #Compute Correlation
             r,p = stats.pearsonr(M[si,:],D[si,:])
             #plot
             plt.plot([r,1],[si,si],'-',color=[.5,.5,.5])
             plt.plot(r,si,'ks',markerfacecolor=color[bool(p<pvalT)])</pre>
         plt.ylabel('State')
         plt.xlabel('Correlation')
         plt.title('Marriage - Divorce Correlation Per State')
         plt.yticks(range(len(stateM)),labels=stateD)
         plt.show()
```



By Lahiru Sadakelum