Chapter 1

Introduction to Statistics

§ 1.1

An Overview of Statistics

Data and Statistics

Data consists of information coming from observations, counts, measurements, or responses.

Statistics is the science of collecting, organizing, analyzing, and interpreting data in order to make decisions.

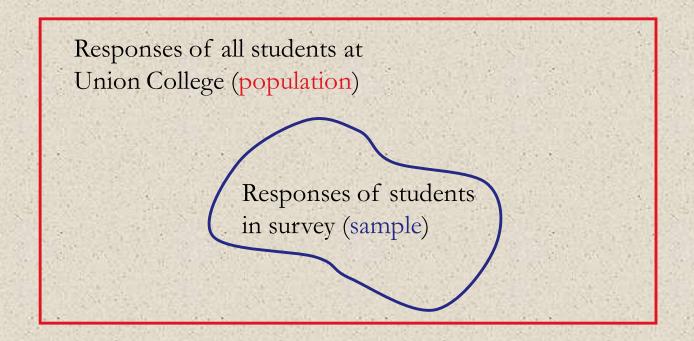
A **population** is the collection of *all* outcomes, responses, measurement, or counts that are of interest.

A sample is a subset of a population.

Populations & Samples

Example:

In a recent survey, 250 college students at Union College were asked if they smoked cigarettes regularly. 35 of the students said yes. Identify the population and the sample.



Parameters & Statistics

A **parameter** is a numerical description of a *population* characteristic. Parameters are denoted by Greek letters

A **statistic** is a numerical description of a *sample* characteristic. Statistics are denoted by Latin letters

$$\begin{array}{c}
\underline{\mathbf{P}}\text{arameter} & \longrightarrow \underline{\mathbf{P}}\text{opulation} \\
\underline{\mathbf{S}}\text{tatistic} & \longrightarrow \underline{\mathbf{S}}\text{ample}
\end{array}$$

Parameters & Statistics

Example:

Decide whether the numerical value describes a population parameter or a sample statistic.

- a.) A recent survey of a sample of 450 college students reported that the average weekly income for students is \$325.
 - Because the average of \$325 is based on a sample, this is a sample statistic.
- b.) The average weekly income for all students is \$405.
 - Because the average of \$405 is based on a population, this is a population parameter.

Branches of Statistics

The study of statistics has two major branches: descriptive statistics and inferential statistics.

Statistics

Descriptive statistics

Involves the organization, summarization, and display of data.

Inferential statistics

Involves using a sample to draw conclusions about a population.

Descriptive and Inferential Statistics

Example:

In a recent study, volunteers who had less than 6 hours of sleep were four times more likely to answer incorrectly on a science test than were participants who had at least 8 hours of sleep. Decide which part is the descriptive statistic and what conclusion might be drawn using inferential statistics.

The statement "four times more likely to answer incorrectly" is a descriptive statistic. An inference drawn from the sample is that all individuals sleeping less than 6 hours are more likely to answer science question incorrectly than individuals who sleep at least 8 hours.

§ 1.2

Data Classification

Types of Data

Data sets can consist of two types of data: qualitative data and quantitative data.

Data Qualitative Quantitative Data Data Consists of Consists of attributes, labels, numerical or nonnumerical measurements or

counts.

entries.

Qualitative and Quantitative Data

Example:

The grade point averages of five students are listed in the table. Which data are qualitative data and which are quantitative data?

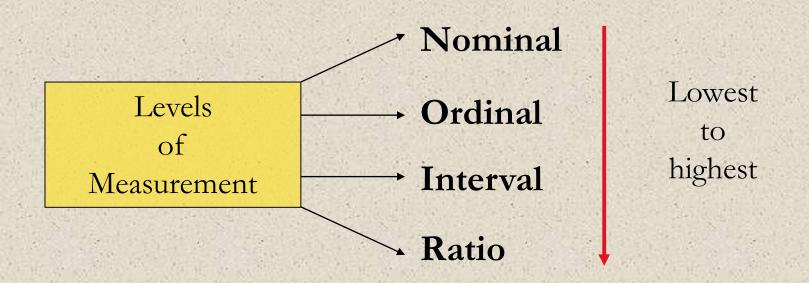
| Student | GPA |
|---------|------|
| Sally | 3.22 |
| Bob | 3.98 |
| Cindy | 2.75 |
| Mark | 2.24 |
| Kathy | 3.84 |

Qualitative data +

Quantitative data

Levels of Measurement

The level of measurement determines which statistical calculations are meaningful. The four levels of measurement are: **nominal**, **ordinal**, **interval**, and **ratio**.



Nominal Level of Measurement

Data at the **nominal level of measurement** are qualitative only.

Levels of Measurement

Nominal

Calculated using names, labels, or qualities. No mathematical computations can be made at this level.

Colors in the US flag

Names of students in your class

Textbooks you are using this semester

Ordinal Level of Measurement

Data at the **ordinal level of measurement** are qualitative or quantitative.

Levels of Measurement

Ordinal

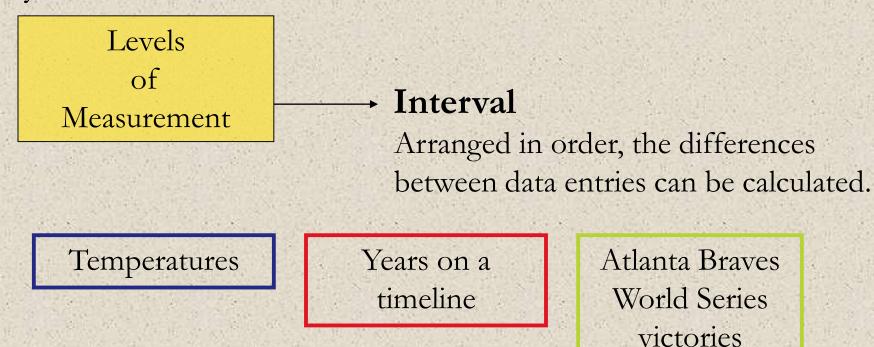
Arranged in order, but differences between data entries are not meaningful.

Class standings: freshman, sophomore, junior, senior Numbers on the back of each player's shirt

Top 50 songs played on the radio

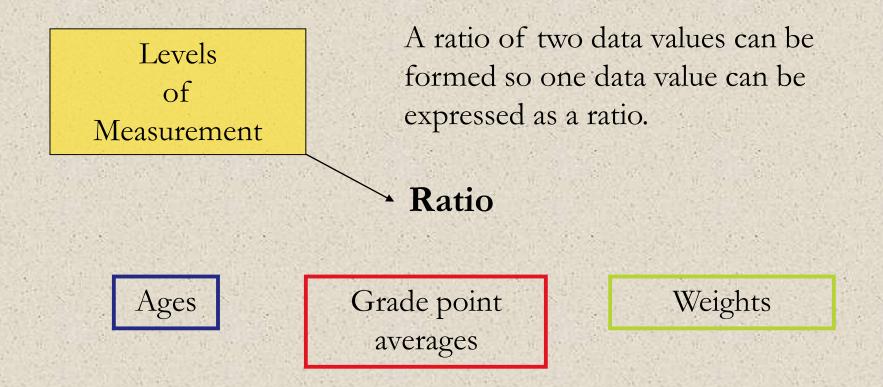
Interval Level of Measurement

Data at the **interval level of measurement** are quantitative. A zero entry simply represents a position on a scale; the entry is not an inherent zero.



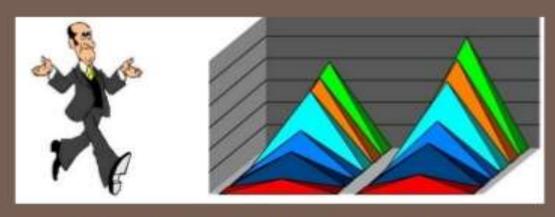
Ratio Level of Measurement

Data at the ratio level of measurement are similar to the interval level, but a zero entry is meaningful.



Summary of Levels of Measurement

| Level of measurement | Put data in categories | Arrange data in order | Subtract data values | Determine if one data value is a multiple of another |
|----------------------|------------------------------|-----------------------------|-------------------------|--|
| Nominal | Yes | No | No | No |
| Ordinal | Yes | Yes | No | No |
| Interval | Yes | Yes | Yes | No |
| Ratio | Yes | Yes | Yes | Yes |



DATA COLLECTION PRIMARY & SECONDARY

INTRODUCTION

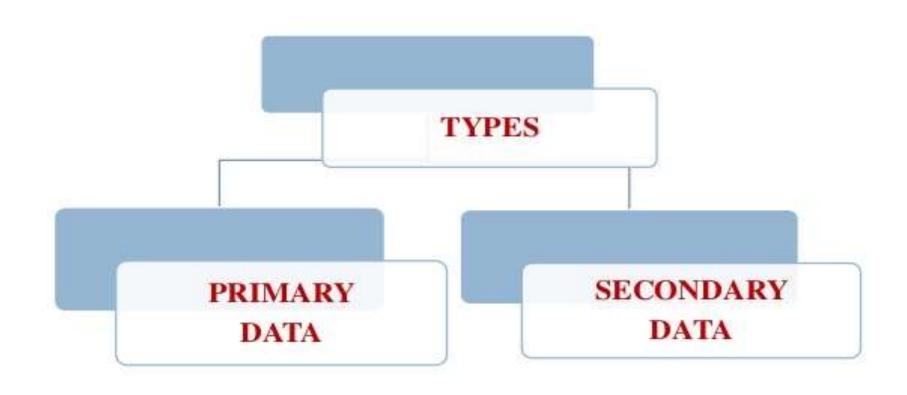
- Data collection is a term used to describe a process of preparing and collecting data
- Systematic gathering of data for a particular purpose from various sources, that has been systematically observed, recorded, organized.
- Data are the basic inputs to any decision making process in business

PURPOSE OF DATA COLLECTION

- The purpose of data collection is-
- to obtain information
- to keep on record
- to make decisions about important issues,
- to pass information on to others



CLASSIFICATION OF DATA



PRIMARY DATA

- The data which are collected from the field under the control and supervision of an investigator
- Primary data means original data that has been collected specially for the purpose in mind
- This type of data are generally afresh and collected for the first time
- It is useful for current studies as well as for future studies
- For example: your own questionnaire.

METHODS

OBSERVATION METHOD

Through personal observation

PERSONAL INTERVIEW

Through Questionnaire

TELEPHONE INTERVIEW

Through Call outcomes, Call timings

MAIL SURVEY

Through Mailed Questionnaire



SECONDARY DATA

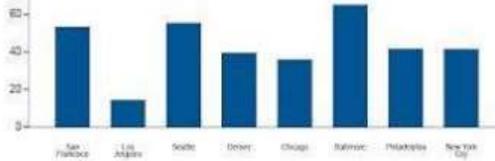
- Data gathered and recorded by someone else prior to and for a purpose other than the current project
- Secondary data is data that has been collected for another purpose.
- It involves less cost, time and effort
- Secondary data is data that is being reused. Usually in a different context.
- For example: data from a book.

SOURCES

□ INTERNAL SOURCES

Internal sources of secondary data are usually for marketing application-

- Sales Records
- Marketing Activity
- Cost Information
- Distributor reports and feedback
- Customer feedback

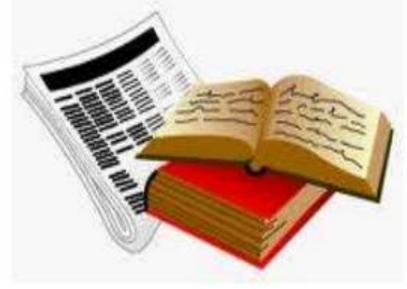


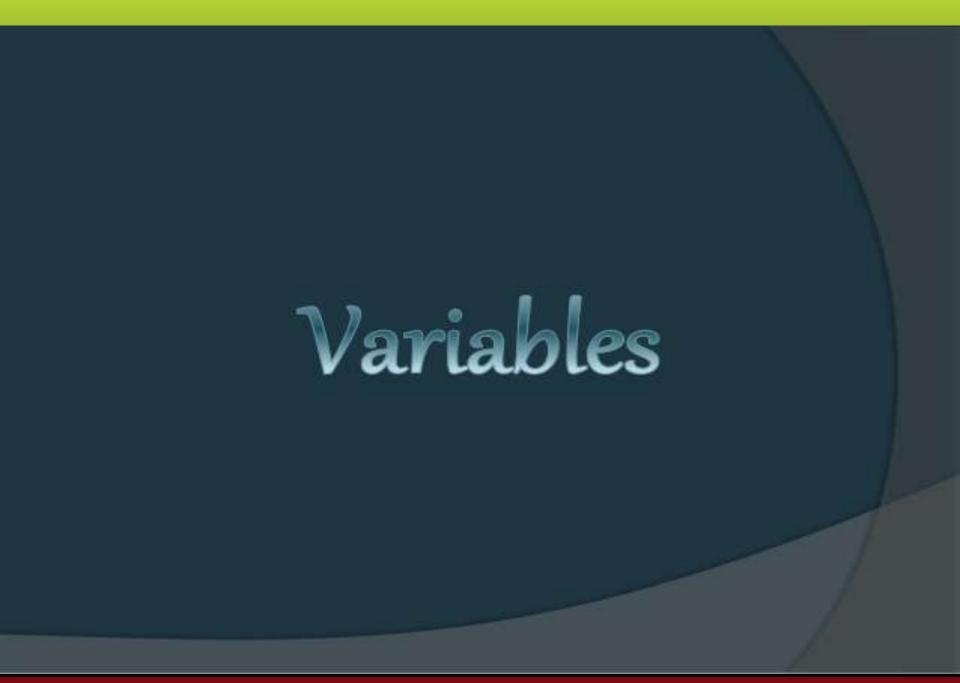
SOURCES

□ EXTERNAL SOURCES

External sources of secondary data are usually for Financial application-

- Journals
- Books
- Magazines
- Newspaper
- Libraries
- The Internet





Variable is any characteristic of an individual. It can take on different values for different individuals

Types of Variables

Variables

Quantitative

- Discrete
- Continuous

Qualitative

- ·Ordinal
- Categorical

Why is the type of variable important?

The methods used to display, summarize, and analyze data depend on whether the variables are categorical or quantitative.

Quantitative Variables

- "A variable that quantifies an element of a population."
- Numeric value that it makes sense to do arithmetic operations (+, -, x, /)
- Finding an arithmetic "average" makes sense
- EX:
 - 1. Height
 - 2. Age
 - 3. Income
 - 4. Test Scores

Two Types of Quantitative Variables

Discrete Variables

It can assume a countable number of values. There is a gap between any two values.

Continuous Variables

It can assume an uncountable number of values, i.e. can assume any value along a line interval, including every possible value between any two values.

Discrete Random Variables

- A discrete random variable is one which may take on only a countable number of distinct values such as 0, 1, 2, 3, 4,....
- Discrete random variables are usually (but not necessarily) counts.

Examples:

- number of children in a family
- the Friday night attendance at a cinema
- the number of patients a doctor sees in one day
- the number of defective light bulbs in a box of ten
- the number of "heads" flipped in 3 trials

Continuous Random Variable

- A continuous random variable is one which takes an **infinite** number of possible values.
- Continuous random variables are usually measurements.
- Examples:
 - height
 - weight
 - the amount of sugar in an orange
 - the time required to run a mile.

Variable we already studied that it can be changed from object to object. Variables are denoted by capital alphabets X, Y, Z.....and so on.

Constant is a fix value which cannot be changed from object to object. Constant are denoted by small alphabets a, b, c,and so on.