

# Reasoning with Compositional Concepts

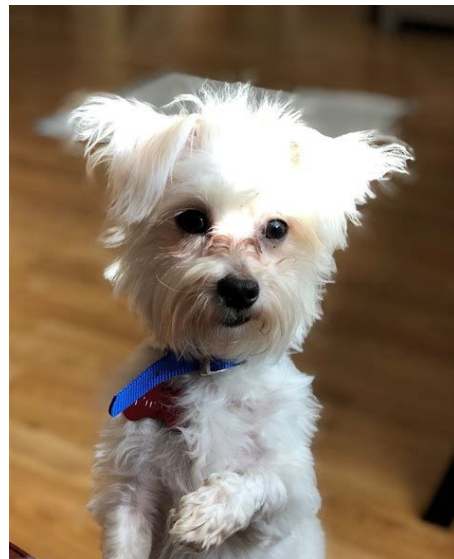
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**Think of dogs**



# What is a dog?

A combination of things

animal

walks on four legs

pet

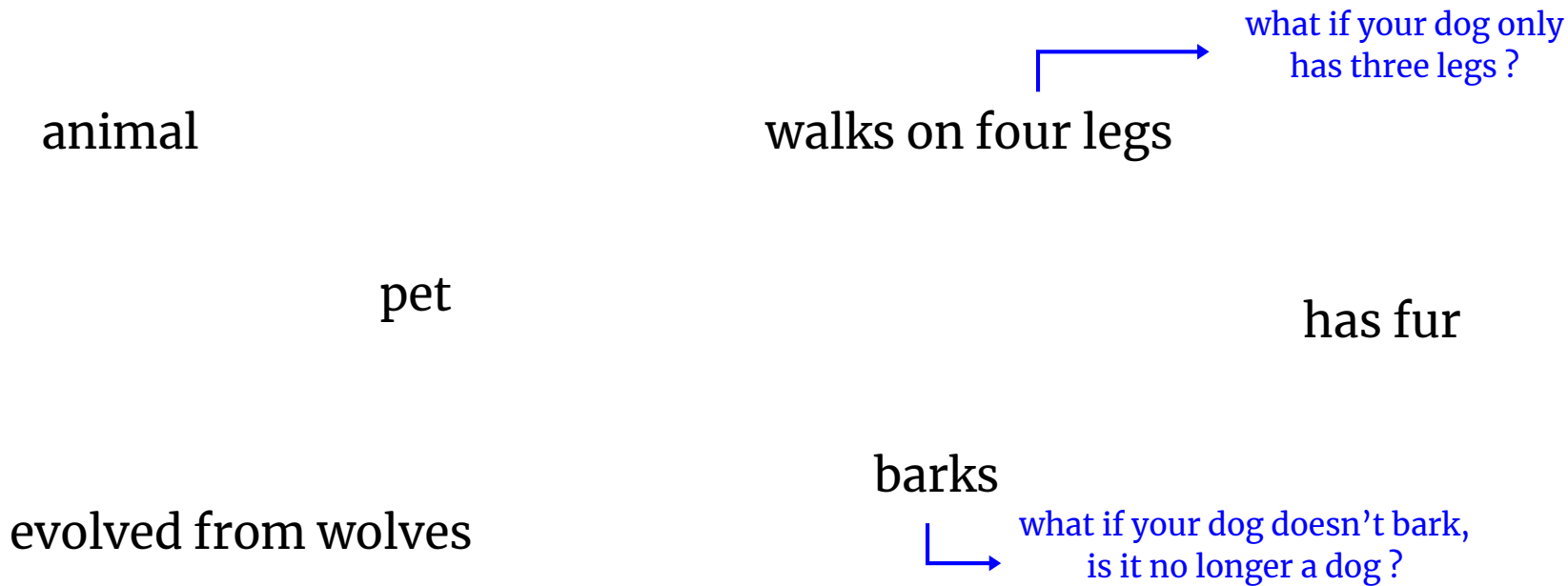
has fur

barks

evolved from wolves

# What is a dog?

A combination of things but some uncertainty



# So what is a dog?!?

- Very hard for us to come up with a definition of dog even though we all know what a dog is
- How do we know when there's so much uncertainty?
- How does our concept of dog form from other concepts like animal and pet?
- And how are we so easily able to tell the difference between a dog, cat, wolf, sheep, horse?

# Previous theories of concepts: Symbolic approaches

- Explicitly define the meaning of concepts
- New concepts can be created by combining existing concepts (concepts are compositional)

- **Example:**

dog = animal + pet + walks on four legs + barks + has fur

flying = moving in the air

flying dog = moving in the air + animal + pet + walks on four legs + barks + has fur

- **Doesn't account for uncertainty**

dog = animal + pet + walks on four legs + barks + has fur

but this is not always true



Note: Being compositional is not just adding, can do any amount of logical operations

# Previous theories of concepts: **Statistical approaches**

- Concepts have associated probabilities
- Example:
  - It's probably true that dogs have four legs but some don't
  - We can say that we are 80% certain that a dog has four legs
- Captures uncertainty well but can't capture compositionality

# A new theory of concepts: Probabilistic language of thought hypothesis

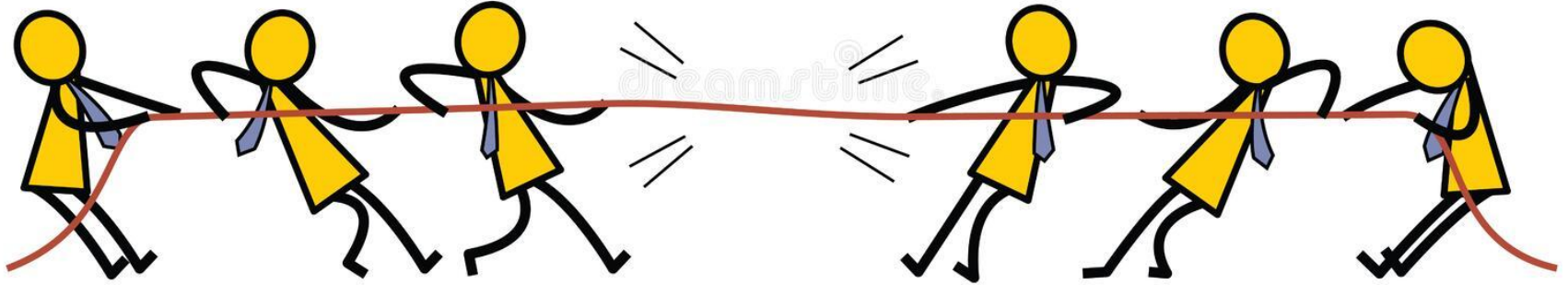
- Unifies the symbolic and statistical nature of concepts
- Because concepts are probabilities they can support reasoning under uncertainty
- And because concepts are compositional they can be combined and recombined to describe new situations
- **Example:**  
flying dog = moving in the air + animal + pet + walks on four legs  
+ barks + has fur + 80% confidence has four legs



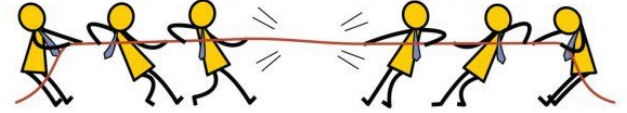
Imagine a tug of war tournament



Imagine a tug of war tournament



# Imagine a tug of war tournament



## Concepts:

person

team

lazy

winner

strength

pulling

# Concepts in our computational model

(concepts are in blue)

probabilistic      `var strength = mem(function (person) {return gaussian(50, 10)})`

probabilistic      `var lazy = function(person) {return flip(0.1) }`

compositional      `var pulling = function(person) {  
    return lazy(person) ? strength(person) / 2 : strength(person) }`

compositional      `var totalPulling = function (team) {return sum(map(pulling, team))}`

compositional      `var winner = function (team1, team2) {  
    totalPulling(team1) > totalPulling(team2) ? team1 : team2 }`

# We can ask this model arbitrary queries

concepts

```
var tug_of_war_model = function() {  
  var strength = mem(function (person) {return gaussian(50, 10)})  
  
  var lazy = function(person) {return flip(0.1) }  
  
  var pulling = function(person) {  
    return lazy(person) ? strength(person) / 2 : strength(person) }  
  
  var totalPulling = function (team) {return sum(map(pulling, team))}  
  
  var winner = function (team1, team2) {  
    totalPulling(team1) > totalPulling(team2) ? team1 : team2 }  
  
  var beat = function(team1,team2){_.isEqual(winner(team1,team2), team1)}
```

evidence

```
{  
  condition(beat(['bob', 'mary'], ['tom', 'sue']))  
  condition(beat(['bob', 'sue'], ['tom', 'jim']))  
}
```

query

```
{  
  return strength('bob')  
}
```

We want to investigate if the model predictions match human predictions.

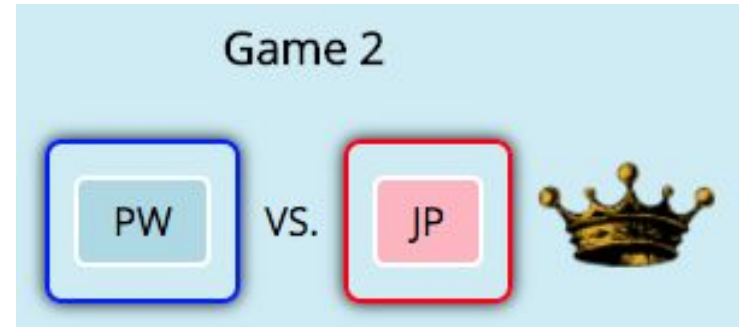
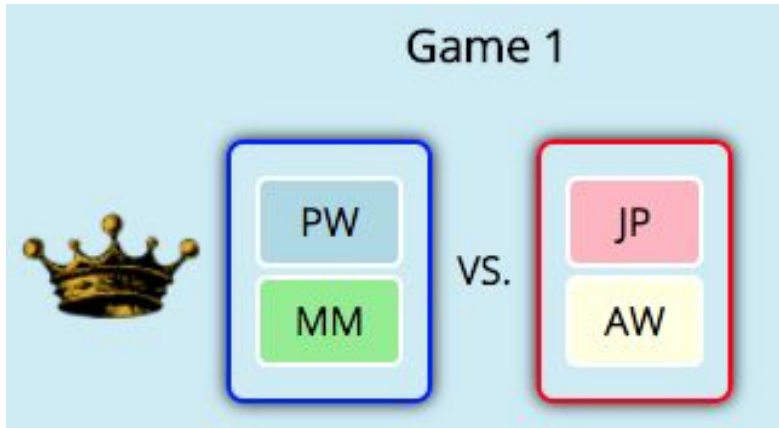
If so, that suggests that humans represent concepts in a similar way to the model.

That is, the representation of concepts in the mind is compositional and probabilistic.

So we did an experiment...

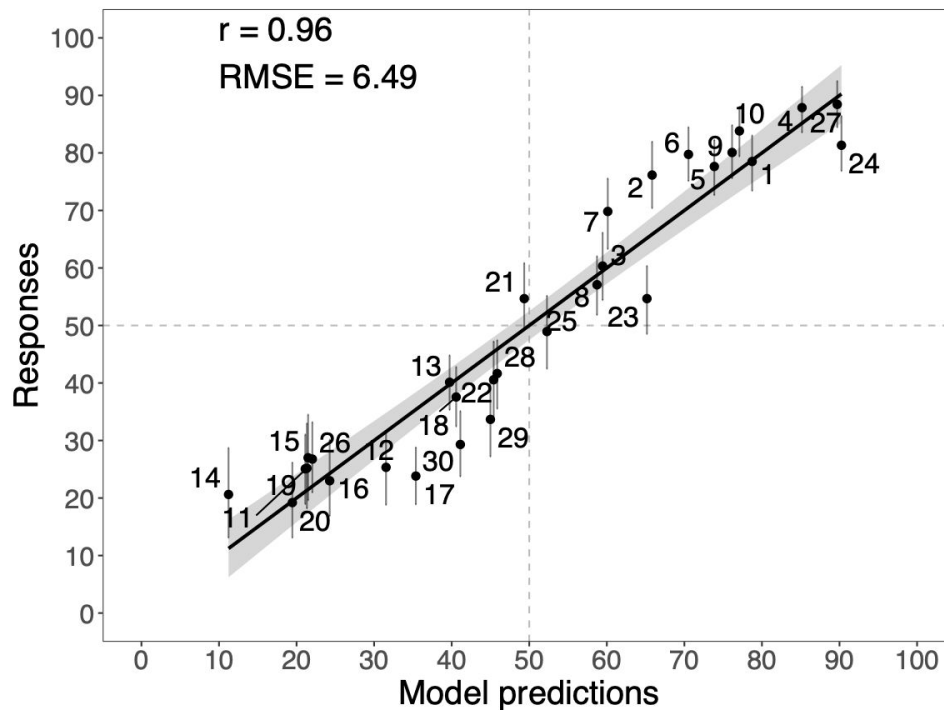
# Tug of war: Experiment 1

How strong do you think player PW is ?



# Tug of war: Experiment 1 Results

How strong is player X

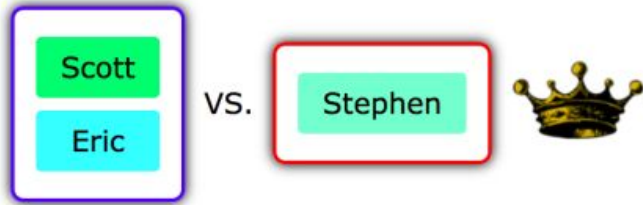




# Tug of war: Experiment 2

How likely is it that **Eric** tried hard in Game 1?

**Game 1**

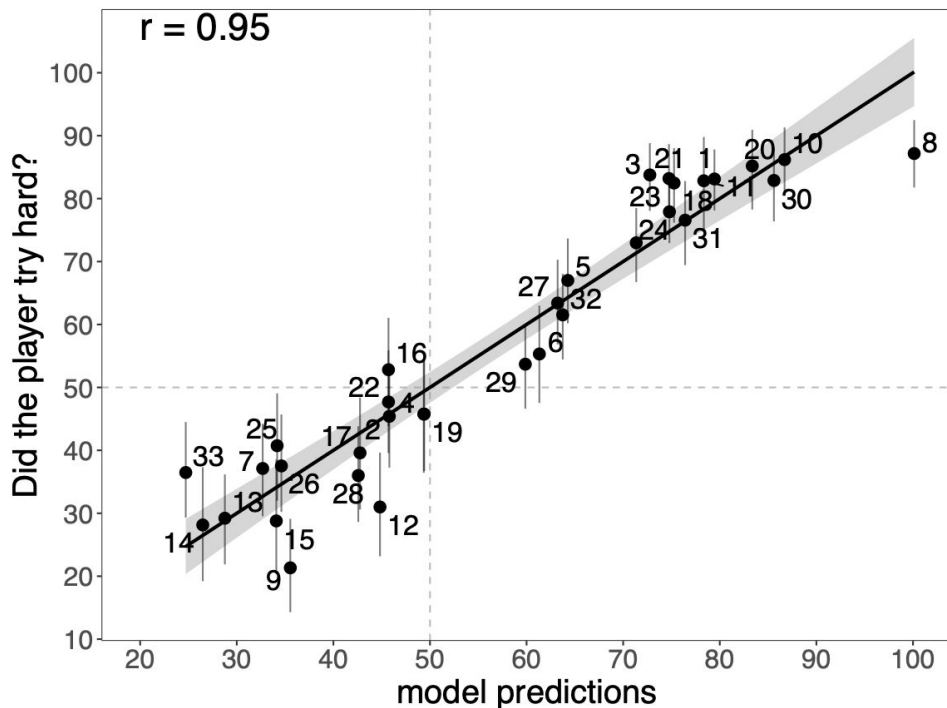


**Game 2**



# Tug of war: Experiment 2 Results

How likely is it that player X tried hard




# Tug of war: Experiment 3

First answer the question based on game information, then respond to the question again after seeing the commentary

Interested in seeing how participants updated their beliefs given this new information

**Game 1**




Bradley

VS.

Herbert

**Commentary**



---

Herbert won 9 out of 10 games in the past.

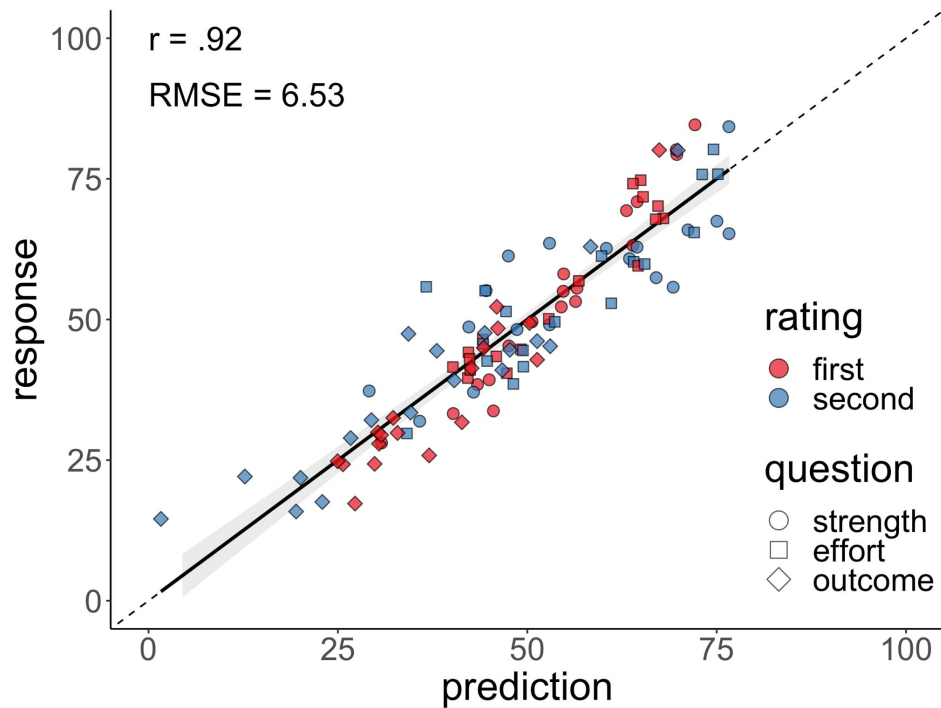
Who would win in another match?

definitely Bradley

definitely Herbert

# Tug of war: Experiment 3 Results

## Updated beliefs



# Summary

- We still don't understand the nature of concepts
- Two Basic Theories
  - Symbolic theories: Compositional but not probabilistic
  - Statistical theories: Probabilistic but not compositional
- Probabilistic language of thought hypothesis
  - Compositional and probabilistic !!
- Computational model that instantiates this hypothesis in a tug of war scenario
- Close correspondence between model and human predictions
- Candidate for theory of human concepts

# Acknowledgements

Thank you!



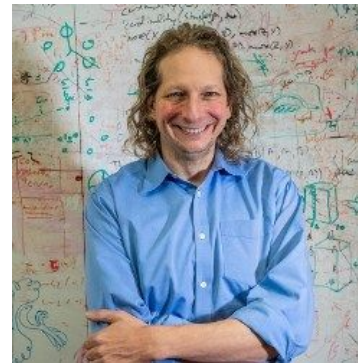
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Questions ?