# Rosen, Discrete Mathematics and Its Applications, 7th edition Extra Examples

Section 13.5—Turing Machines



Page references correspond to locations of Extra Examples icons in the textbook.

## p.889, icon at Example 1

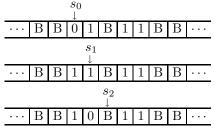
#1. Let T be the Turing machine defined by these five-tuples:

$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If T is run on the following tape, beginning in initial position, what is the final tape when T halts?

#### **Solution:**

Beginning with the above tape, we obtain the following sequence of tapes, ending with the last tape in the sequence:



Machine halts.

## p.889, icon at Example 1

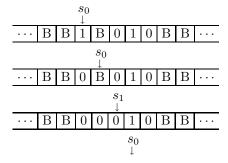
#2. Let T be the Turing machine defined by these five-tuples:

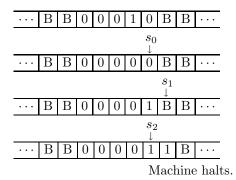
$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If T is run on the following tape, beginning in initial position, what is the final tape when T halts?

#### Solution:

Beginning with the above tape, we obtain the following sequence of tapes, ending with the last tape in the sequence:





# p.889, icon at Example 1

#3. Let T be the Turing machine defined by these five-tuples:

$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If T is run on the following tape, beginning in initial position, what is the final tape when T halts?

### Solution:

Beginning with the above tape, we end with the following tape:

$$\begin{array}{c|c|c} & s_2 \\ \hline \cdots & B & B & 1 & 0 & 1 & 0 & 0 & B & B & \cdots \end{array}$$

# p.889, icon at Example 1

#4. Let T be the Turing machine defined by these five-tuples:

$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If T is run on the following tape, beginning with the third blank from the left, what is the final tape when T halts?

# Solution:

Beginning with the above tape, we end with the following tape: