

Real-Time Motion Compensation with Soft Robots in Robotic Radiosurgery

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Abstract The Accuray CyberKnife® is one of the major robotic radiosurgical devices in clinical use for radiation delivery to cancer tumors. There are developing lines of work that utilize rigid-links in Stewart-Gough kinematic mechanisms for patient motion correction in radiation therapy. A fundamental weakness of a majority of these approaches is that the rigid electro-mechanical components of these robots attenuate ionizing radiation, share their complete workspace with the patient's body (risking safety), and their constant curvature components are hardly suitable for manipulating the soft tissues of the human body. In this report, we highlight some recent advancements that aim to stem these issues in our line of work; these are mostly systems that utilize soft mechanisms for patient motion compensation in robotic radiosurgery.

1 Introduction

Across the world, cancer remains an existential burden on the people of rich and poor nations alike. In 2019 alone, an estimated 1,762,450 new cancer cases will be diagnosed in the United States, out of which 606,880 will lead to fatality [1]. At an approximate cost projection of \$147.3 billion it gulps about 4.2% of overall health care spending (per 2017 budget). Cancer mortality is having pronounced effects on low- and middle-income countries as well with the International Agency for Research on Cancers estimating that the highest cancer incidence over the coming decades will fall on these countries [2].

Means of treating cancers may include one or a combination of drugs, radiation therapy, immunotherapy, stem cell transplant, targeted therapy, precision therapy, chemotherapy, or surgery. Among the different locations where cancers can exist in

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Fig. 1: The Cyberknife and 6-DOF robotic couch system. ©Accuray Inc.

the human body, cancers of the head and neck (H&N) region tend to be the most fatal. A combination of the treatment methods highlighted above is not often suitable when treating H&N cancers due to the sensitive organs in the H&N region.

Radiation Therapy (RT), sometimes in conjunction with surgery and chemotherapy, is an invaluable single cancer treatment modality owing to its cost-effectiveness (accounting for only 5% of the total cost of cancer care [3]), and its advanced mode of radiation production and delivery. By shaping the geometry of high-energy radiation it allows radiation escalation to tumor targets while simultaneously sparing organs-at-risk (OARs). The importance of RT is underscored by the fact that half of all cancer patients undergo RT treatment during the course of their illness; in fact, an estimated 40% of all curative cancer treatment modality are performed with RT [4]. Thus, because of its advanced radiation delivery method, RT is often the most suitable treatment modality for H&N cancers.

1.1 Robots in Radiation Therapy

Traditionally in conventional radiosurgery, a non-static beam is used as an ablative surgical instrument so that the radiation source can move along primitive paths, irradiating the patient on a treatment couch in the process (see Figure 1). Using rectangular fields, blocks and wedges to specify flatness and symmetry, uniform radiation intensity can be produced [5]. However, this radiation uniformity may cause unwanted effects on surrounding tissues.

1.1.1 Beam Repositioning

In order to adaptively reposition the radiation beam during treatment, modern approaches utilize a six degree-of-freedom (DOF) robot arm to overcome the cross-

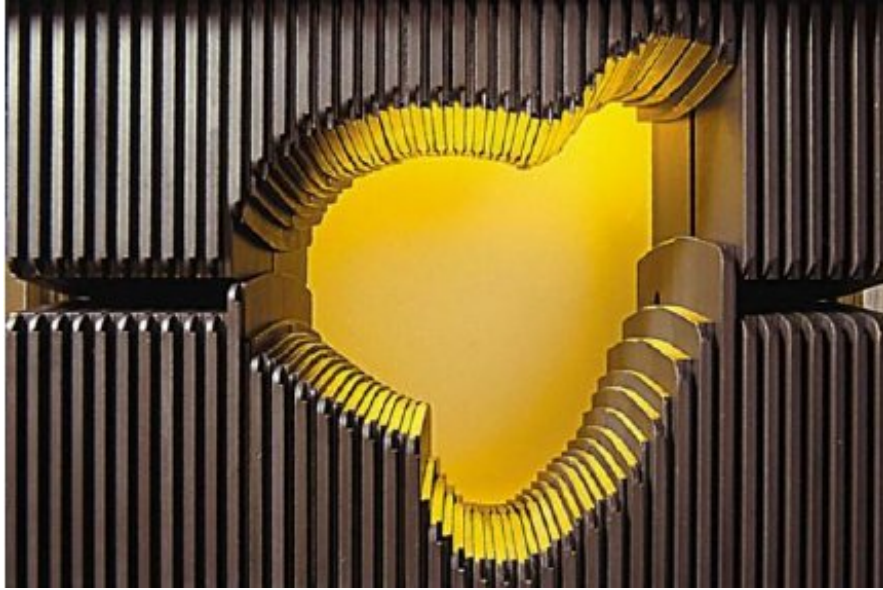


Fig. 2: A multi-leaf collimator (MLC) used in IMRT and 3DCRT. ©Varian Medical Systems.

sectional radiation delivery limitations of conventional systems. High-energy photons are generated in a linear accelerator (LINAC) machine; the LINAC is mounted on the end effector of an open kinematic chain robot arm. By this arrangement, the radiation beam can be delivered to the tumor target e.g. [6] within a patient lying in a supine position on a 6-DOF translational and rotatory robotic *couch* [7, 8].

To conform the radiation to the tumor, minimize sustained damage to normal tissues, and ensure sparing of OARs during irradiation, in an *inverse treatment planning process*, the leaves of a multi-leaf collimator or MLCs (shown in Figure 2) are sequenced in order to conform the geometric field of the ionizing radiation into a non-uniform field [9]. Essentially, the MLCs conform the spatial localization of a high dose volume to a target volume. Because it is constructed from Tungsten (with high absorption properties for ionizing radiation), the dose is computer-controlled (modulated) so that a conventional geometrical field's intensity are varied bixel-wise to generate the fluence (or influence matrix) that is incident on the tumor. Accuray Inc.'s Cyberknife system [10] is such a system that directs the repositioning of the linear accelerator based on the 3D tumor position (see Figure 1).

1.1.2 Patient Motion Correction

An open problem in radiosurgery is that of keeping the patient's position consistent with those in the pre-calculated *treatment planning parameters*. This is a separate



Fig. 3: Masks and Frames for Head Immobilization

problem from robot-delivered radiation. Studies have shown that serious changes do occur in delivered dose when a patient is slightly displaced or when there is a misalignment from the registered patient's pose angle. Ling et. al [11] found that minute changes in couch angles affected target delivery results significantly more than accelerator angular changes. These uncertainties in couch translational and rotatory axial magnitudes reduce or increase minimum target dose or maximum cord dose respectively – to a 5° or $3mm$ order for example [11]. In stereo-tactic radiosurgery (SRS), misalignment between planned and delivered dose can cause eczema or brain lesions [12]. In a geometric miss, for instance, highly conformal potent dose increases the risk of underdose to tumors or undesirable high dose to critical organs and nearby tissues.

Therefore, in order to avoid dose miss, guarantee precision of dose delivery, assure repeatable positioning during interfractional treatments, as well assure the efficacy of dose escalation to a target or minimize OARs' exposure to toxicity, a patient's position on the treatment machine should not fluctuate. *A major research direction in clinical RT today is that of controlling the patient's position in real-time on the 6-DOF robot couch.* Currently, different technologies exist for this, and we provide a brief overview of this *immobilization problem* in § 1.2.

1.2 Limitations of Existing Immobilization Technologies

In spite of the advancements in using robots for radiosurgery over the past three decades, closed-loop control of the patient's pose in real-time during radiation delivery when the treatment beam is on has not reached full maturity. The AAPM Task Group-42 guidelines requires radiation oncological treatment of cancers immobilization devices/systems to achieve below $2mm$ translational and 2° rotatory positioning accuracy [13].

Currently in clinics, rigid frames and masks (see [Figure 3](#)) are used to keep the patient immobilized on the machine so as to mitigate patient motion errors. These devices generally meet AAPM Task Group-42 guidelines for intracranial SRS. Mask-based immobilization uses thermoplastic masks (see left inset of [Figure 3](#), which reduce accuracy as a result of mask flex (producing a drift of up to $6mm$) and changes to the mask's molecular structure (arising from hysteresis and shrinkage). For deep tumors located near critical structures such as the brain stem, and for novel treatment modalities such as single isocenter multiple-target SRS, masks are not suitable due to high sensitivity to rotational head motion.

In frame-based immobilization, a metal ring is screwed to the skull of the patient, and then bolted to the treatment table (see right inset of [Figure 3](#)). The invasive nature and discomfort associated with the frame causes poor patient compliance and clinical efficacy. For certain patients, frame placement is impossible due to their unique cranial anatomy or prior surgical bone flaps. More so, the frame limits the use of multiple RT delivery as patients cannot be subjected to daily attachment and removal of the frame.

Setup errors between fractionated treatments (interfractional) or patient motion errors during a treatment session (intrafractional) often need to be corrected *in real-time* during treatment. Currently in clinics, the treatment is stopped, and the machine is recalibrated when the error is too large for this process to go on. While intrafractional errors can be minimized by highlighting the importance of voluntary stillness to the patient, suitable means of immobilization and adaptive positioning are necessary when the patient moves from a desired pose. The CyberKnife system, in spite of its advanced mode of delivery, requires a frame or immobilization mask, and is incapable of real-time and precise head motion corrections when the treatment beam is on. The CyberKnife Synchrony executes trajectories that are pre-calculated before start of radiation delivery, and is only FDA-approved for lung tumors' treatment; correction requirements in systems such as this require far less accuracy [[14](#)] ($< 5mm$) than brain targets.

Even so, real-time closed-loop head motion compensation for the CyberKnife system is inhibited by its high load-to-weight ratio (at $160kg$ LINAC [[15](#)]): the load at the end of a long robotic arm needs to be moved rapidly in response to random real-time head pose changes. This rigidity, far location from the patient, coupled with the weight of the system magnifies error from the shoulder out to the end effector. As an example, a 1° head rotation would correspond to an $18mm$ robot correction requirement for a $1m$ robot-to-target distance. This is a recipe for large end effector velocities and acceleration that can significantly affect dose delivery.

Attempts to stem these highlighted problems include recent research directions such as the steel-cast assembled 4-DOF robot link components of [[16](#)], the Hexa-POD parallel manipulator of [[17](#)], or the in-house fabricated Stewart-Gough platform of [[18](#)]. For example, the Stewart-Gough-like robotic prototype from Wiersma group [[18](#)] is a lightweight parallel robotic SRS platform with the patient's head as the primary load; located approximately $25cm$ from the tumor target it is capable of correcting a 1° rotatory error with a $4.5mm$ control correction. However, the discomfort caused by head and neck masks and frames in prolonged treatment (i) can

increase the voluntary and involuntary motion of patients; (ii) are time-consuming to calibrate on a treatment machine since doses are usually delivered in fractions over many weeks or months; (iii) lack real-time position correction of the patient's head motion; and (iv) have been known to cause patient discomfort after treatment. However, these systems along with the CyberKnife all share common drawbacks. For example, they

- share their complete workspace with body tissues, a safety concern since rigid robot components lack compliance and their end effectors add hard shocks to the patients body during manipulation;
- are incapable of providing sophisticated 3D manipulation with their constant-curvature components; and
- the inadvertent respiratorial and internal organ motions often induce deviation from a target beyond the recommendations of AAPM Task Group 17 [13], namely 2mm and 2 degrees tolerance.

The cyberknife system is only capable of compensating motion based on pre-calculated trajectories, not in real-time. Furthermore, they have limited effectiveness given their non-compliant parts that assume rigidity of the patient's body. To improve the treatment planning process, these drawbacks need to be addressed. This would require the interdisciplinary effort of engineers, roboticists, physicists, and surgeons alike. In what follows, we present some of our work in soft robotic patient motion correction systems in RT. We remark in passing that some the works here have already appeared in [19–26].

2 Materials

In this section, we describe the mechanical components necessary for the soft actuation system described in [23] and [26].

- Mannequin head and torso simulator(custom-made, $W \times L \times D$: $155 \times 240 \times 200$ mm)¹;
- Craftsman air canister (maximum pressure: 320psi);
- Off-the-shelf suction pump (max. pressure: 12 psi);
- National Instruments (NI) myRIO microcontroller, 1;
- PWM voltage regulator (custom-built for DIO on myRIO), 6;
- 3D camera (Ensenso N35 model, mounted $\approx 45^\circ$ to the vertical above the head)
- Base inflatable air bladder or IAB, 1
 - custom-made from elastomeric polymers;
 - elastomer covered with soft styrofoam to absorb reactive pressure from head manipulation;
 - size in reference configuration: $180mm \times 280mm$;

¹ [Link to Solidworks Model](#)

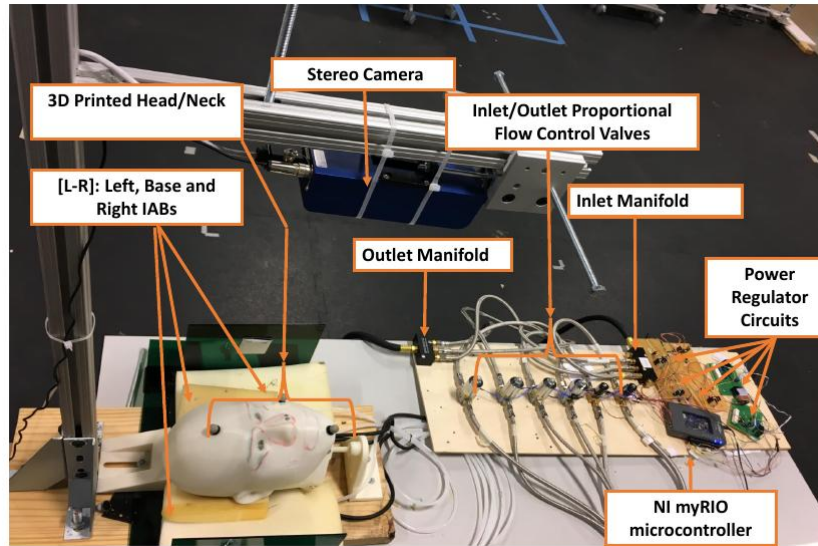


Fig. 4: Hardware Description

- maximum width in current configuration: $\sim 75mm$;
- 2 crack-resistant polyethylene tubing: $1/8''$ internal diameter (ID) and $1/4''$ outer diameter (OD).
- Side IABs, 2
 - custom-made from elastomeric polymers;
 - elastomers encased in breathable foam pads for comfort;
 - size in reference configuration: $180mm \times 140mm$;
 - maximum width in current configuration: $\sim 75mm$;
 - 2 crack-resistant polyethylene tubing: $1/8''$ ID and $1/4''$ OD for each IAB
- Proportional solenoid valves
 - 6 Dakota Instruments EM valves (Model PSV0105, Orangeburg, NY, USA) for proportional torques to the soft actuators

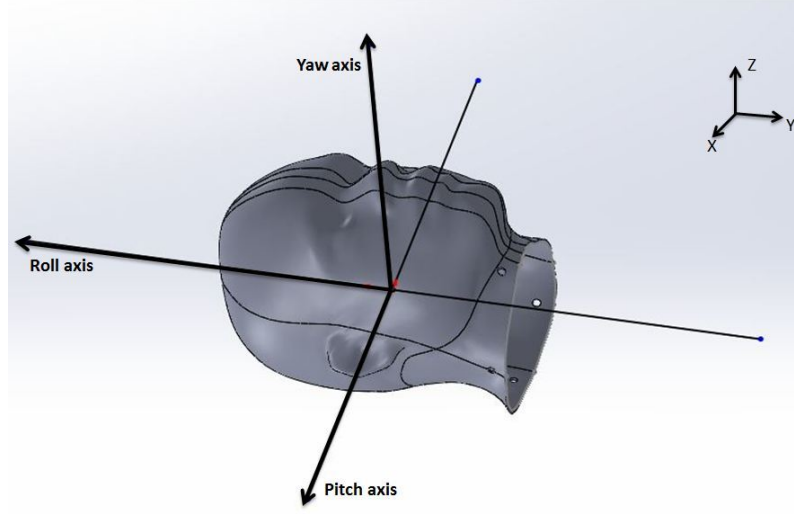


Fig. 5: Head Coordinate System

3 Methods

3.1 Vision-based Pose Estimation

The model head lies in a supine position above a planar table as shown in [Figure 4](#). We employed a 3D camera from Ensensio GmbH (model N35) to reconstruct the surface image and measure head pose. The N35 camera captures multiple image pairs during exposure; each image pair is made up of different patterns, controlled by piezo-actuators. A stereo-matching algorithm gathers the information from all image pairs after capture to produce a high-resolution point cloud (PCL) of the scene [\[27\]](#). We mounted the 3D sensor such that its lens faced the head at approximately 45° from the vertical during experiments. All vision processing, systems modeling and control laws were computed on a CORSAIR PC. We exchange the neuro-control and sensor signals via the publish-subscribe IPC of the ROS middleware installed on the PC. Adaptive control laws were sent via udp packets to the RIO microcontroller. The system setup is shown in [Figure 4](#).

The left and right bladders control the roll angles/x-axes motions while the bladder underneath the head, henceforth referred to as the base bladder, controls the pitch angles and z-axis motions. The reference frame is illustrated in [Figure 5](#). Our goal is to control the motion of the head about three axes, namely z , pitch and roll axes.

3.2 Face Segmentation

The dense point cloud of the scene has (i) marked jump in rendered points along the z-axis of the camera; this is because of the single view angle by the camera; (ii) the scene clutter and lack of multiple camera view angles does not affect the representation of the face; (iii) thus, through spatial decomposition of the scene, we can separate the face from the scene. However, the point cloud is computed from monochromatic IR image pairs (with no texture information) making morphological operations difficult; due to the multiple image pairs used in 3D reconstruction to generate a highly accurate measurement, the camera is limited to a maximum frame rate of 10Hz. Inspired by Rusu's work [28], we divide the segmentation problem into stages, with each stage involving segmenting out candidates that do not belong to the object we want to identify (the frontal face) in the scene. Our engineering philosophy in the segmentation phase is inspired by spatial decomposition methods that determine subdivisions and boundaries to allow retrieval of data that we want given a measure of proximity. In this case, we know that the location of the table cannot exceed a given height during experiments and the camera's position is fixed while the head moves based on bladders' actuation. Separating objects that represent planar 2D geometric shapes from the scene therefore simplifies the face segmentation algorithm. By finding and removing objects that fit primitive geometric shapes from the scene, clustering of the remaining objects would yield the face of the patient in the scene. We fit a simplified 2D planar object to the scene such that searching for points $\mathbf{p}_i \in \mathcal{P}$ that support a 2D plane can be found within a tolerance defined by the inequality $0 \leq |d| \leq |d_{max}|$, where $|d_{max}|$ represents a user-defined threshold to segment out [28].

We proceed as follows:

- The point cloud of the scene was acquired from the computed disparity map of the two raw camera images;
- To minimize sensor noise whilst preserving 3D representation, the acquired point cloud was downsampled using a Sample Consensus (SAC)-based robust moving least squares algorithm (RMLS) [28, §6];
- We then searched for the edges of 2D planar regions in the scene with Maximum Likelihood Sample Consensus (MLESC) [29], and we bound the resulting plane indices by computing their 2D convex hull;
- A model fitting stage extrudes the computed hull (of objects lying above the 2D planar region) into a prism model based on a defined L_1 Manhattan distance; this gives the points whose height threshold is about the region of the face in the scene [30];
- We then cluster the remaining points based on a heuristically determined L_2 distance between points remaining within the polygonal plane. The largest cluster gives us the face.

We now describe these segmentation stages. The downsampling algorithm is an implementation of [28, §6]. We first normalize the coordinates of the original point cloud, \mathcal{P} , ensuring that the distance between points $p \in \mathcal{P}$ is upper-bounded by 1

based on the diagonal of \mathcal{P} 's bounding box. It computes a weighting factor, α , given by

$$\alpha = \mu_x + k \cdot \sigma_x, \quad (1)$$

where μ and σ respectively denote the mean and standard deviation of the mean distance distribution between points and k is a user-chosen variable. Through SAC, an estimate $\hat{\mathcal{P}}$ of the original point cloud is computed and represented as a set of equidistant grid points in the neighborhood of \mathcal{P} . The points of \mathcal{P} are then projected to a local plane of reference through their k nearest neighbors to assure proximity to the surface of \mathcal{P} . Points $\hat{p}_i \in \hat{\mathcal{P}}$ are fitted to the surface that approximates \mathcal{P} with a bivariate polynomial height function in a local Darboux frame (with orthonormal axes \mathbf{U} , \mathbf{V} , \mathbf{N} ; \mathbf{V} is chosen to be parallel to the local reference frame's normal). The polynomial weights are computed for the k nearest neighbors of \mathbf{q} as

$$w_i = \exp\left(-\frac{\|\hat{\mathbf{p}} - \mathbf{p}_i\|^2}{\alpha}\right). \quad (2)$$

Surfaces in the proximity of \hat{p} 's neighbors are approximated using

$$n_{(u,v)} = \sum_{i=1}^N c_i \cdot f_{(u,v)}^i,$$

where u, v , and n are coordinates along the Darboux frame axes, $f_{(u,v)}^i$ are height function members of bivariate polynomials. We refer the reader to [28] for a more detailed treatment of the resampling algorithm. The result of the resampling algorithm is shown in the top-right image of Figure 6.

The world coordinate frame is defined with the z -axis pointing up from the head (towards the camera), and y -axis pointing right from the head; the x -axis is the cross product of y and z . This is chosen as $O(0, 0, 0.712m)$ from the camera origin. To simplify the complexity of the planar structure in the scene, the table is modeled as a 2D planar geometric primitive so that finding points that fit a defined model hypothesis involves estimating a single distance to the frontal plane of the table surface rather than multiple points if the model was represented with points. Searching for horizontal planes that are perpendicular to the z -axis of the head is carried out using the maximum likelihood SAC [29] algorithm implemented in the PCL Library [31] to generate model hypotheses. The plane segmentation algorithm is defined in Table 1. The plane segmentation process is run once. Once the plane model is found, its indices and those of objects lying above it are separated and stored in separate data structures. Every subsequent iteration consists of (i) computing the 2D convex hull of point indices of objects above the table using the *Qhull* library², (ii) using a pre-defined prismatic model candidate to hold extruded points to the approximate facial height above the table; and (iii) separating the face from every other point in the resulting cloud through the Euclidean clustering (EC) method of [32]. A distinct point cluster is defined if the points in cluster $C_i = \{\mathbf{p}_i \in \mathcal{P}\}$ and

² The Qhull library: <http://www.qhull.org/>

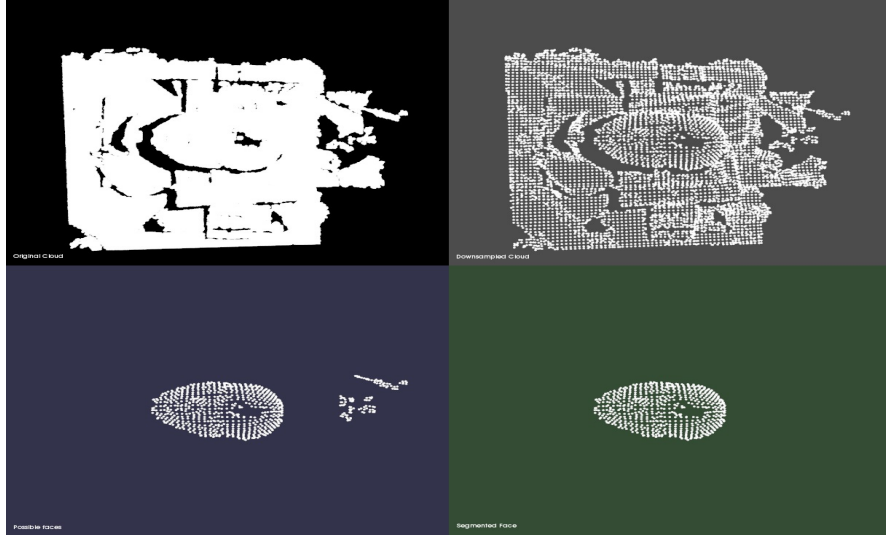


Fig. 6: [Top-left]: Dense point cloud of the experimental setup scene. [Top right]: Downsampled cluttered cloud of the left scene. [Bottom-left]: Using RANSAC, we searched for 2D plane candidates in the scene and compute the convex hull of found planar regions. We then extrude point indices within the hull into a prismatic polygonal model to give the face region. [Bottom-right]: An additional step clusters the resultant cloud based on a Euclidean distance. The largest cluster is taken to be the face.

Table 1: Plane Segmentation Algorithm

-
1. **for** $i = 1$ to N **do**
 2. sample non-collinear points $\{p_i, p_j, p_k\}$ from \mathcal{P}
 3. calculate the model coefficients $ax + by + cz = d$
 4. find distances from all $\mathbf{p} \in \mathcal{P}$ to the plane (a, b, c, d)
 5. store points $\mathbf{p}^* \in \mathcal{P}$ that satisfy the model hypothesis,
 $0 \leq |d| \leq d_{max}$.
 6. **return** maximum of the stored points \mathbf{p}^* .

cluster $C_j = \{\mathbf{p}_j \in \mathcal{P}\}$ satisfy the L_2 -distance threshold

$$x \leq \min \|\mathbf{p}_i - \mathbf{p}_j\|_2 \quad (3)$$

Finding the face in the scene after carrying out EC algorithm is a question of finding the largest index in the list \mathcal{C} . This takes $O(n)$ (linear) time for n clusters. The face segmentation results are presented in Figure 6. We then compute the Cartesian position of the face with respect to the camera origin by taking the center of mass of

Table 2: Euclidean Clustering Algorithm

-
1. create a kd-tree data structure for the PCL \mathcal{P}
 2. initialize a cluster of linked list \mathcal{C} , and a queue, \mathcal{Q}
 3. **for** points $\mathbf{p}_i \in \mathcal{P}$ **do**
 4. enqueue \mathbf{p}_i to \mathcal{Q}
 4. search for neighbors, \mathcal{P}_i^k , of \mathbf{p}_i neighbors in a sphere of radius $r < x$
 5. add neighbors $\mathbf{p}_i^k \in \mathcal{P}_i^k$, not yet processed to \mathcal{Q}
 6. add \mathcal{Q} to \mathcal{C} and reset \mathcal{Q} to an empty list.
 7. **return** \mathcal{C} .

the segmented facial region (bottom-right image of Figure 6). This is obtained by calculating the mean-value of all the points in the resulting cloud (≈ 600 points on average).

3.3 Head Pose Estimation

With the facial point cloud segmented, we define three points on the head. Our goal is to compute the optimal translation and rotation of the head from a model point set $\mathbf{X} = \{\vec{x}_i\}$ to a measured point set $\mathbf{P} = \{\vec{p}_i\}$, where $N_x = N_p = 3$, and the point $\vec{x}_i \in \mathbf{X}$ has the same index as $\vec{p}_i \in \mathbf{P}$. Following the approach of Besl and McKay in [33], we compute the cross-covariance matrix of \mathbf{P} and \mathbf{X} as Σ_{px} , extract the cyclic components of this skew symmetric matrix as Δ , and use it to form the symmetric 4×4 matrix $\mathbf{Q}(\Sigma_{px})$ as follows,

$$\mathbf{Q}(\Sigma_{px}) = \begin{bmatrix} \text{tr}(\Sigma_{px}) & \Delta^T \\ \Delta & \Sigma_{px} + \Sigma_{px}^T - \text{tr}(\Sigma_{px})\mathbf{I}_3 \end{bmatrix}. \quad (4)$$

The unit eigenvector, q_R , that corresponds to the maximum eigenvalue of $\mathbf{Q}(\Sigma_{px})$ is selected as the optimal rotation quaternion; we find the optimal translation vector as

$$\vec{q}_T = \vec{\mu}_x - \mathbf{R}(\vec{q}_R)\vec{\mu}_p \quad (5)$$

where μ_x and μ_p are the mean of point sets \mathbf{X} and \mathbf{P} respectively. Obtaining the roll, pitch and yaw angles from q_R is trivial and the pose of the face is described by tuples $[q_T, q_R] = \{x, y, z, \theta, \phi, \psi\}$ with respect to the world frame. Given the 3-DOF setup, we choose to control three states of the head: z, θ, ϕ (*i.e.* z , roll, and pitch).

3.4 Control Design

We propose an adaptive control strategy in a Bayesian setting, which given an initial prior distribution of controls and 3-DOF head pose, minimizes a cost criterion as the expected value of control laws that will yield a future desired head pose. We consider the pwm voltages that power the valves as input, \mathbf{u} , the head pose as the output, \mathbf{y} and an unknown disturbance $\mathbf{w}(k)$. We first describe the nonlinear function approximator model $\hat{f}(\mathbf{u}(k-d), \mathbf{y}(k), \mathbf{w}(k))$, which is constructed from memory-based input and output experimental data that satisfy

$$Z^N = \{u(k), u(k-1), \dots, u(k-n_u), y(k), y(k-1), \dots, y(k-n_y)\} \quad (6)$$

that satisfy the Lipschitz continuity. (6) implies an input $\mathbf{u}(\cdot)$ at time $k-d$, produces an output $\mathbf{y}(k)$ at d time instants later. The next section describes how we formulate the class of minimum error variance controllers that predict the effect of actions $\mathbf{u}(\cdot)$ on states $\mathbf{y}(\cdot)$ using a self-tuning regulator.

3.5 Adaptive Neuro-Control Formulation

Following our previous approach in [34, §IV.B], we fix a persistently exciting input signal $u_{ex} \in L_2 \cap L_\infty$ to excite the nonlinear modes of the system. We then parameterized the system with a neural network with sufficient number of neurons. The neural network (NN) provided information on the changing parameters of the system during control trials. The adjustment mechanism is computed from inverse Lyapunov analysis, where we choose adaptive laws that guarantee a nonpositive-definite Lyapunov function candidate when evaluated along the trajectories of the error dynamics.

Our contribution is the approximation of the nonlinear system by a long short-term memory (LSTM) [35], equipped with an adequate number of neurons in its hidden layers. We parameterized the last layer of the network with a fully connected layer that outputs control torques to the valves. The neural network can be seen as a memory-based model that remembers effective controls for the adaptation mechanism in the presence of uncertainties and external disturbance.

The neural network is shown in Figure 7. Depending on the region of attraction of the system the network is approximating, it parameterizes the nonlinear dynamical system $f(\cdot)$ and maps the parameterized model to appropriate valve torques. There exists additional feedforward + feedback terms in the global controller (introduced shortly) that guarantee system stability and robustness to uncertainties. Therefore, the global controller keeps the states of the system bounded under closed-loop dynamics, ensures convergence to desired trajectories from states that are initialized outside the domain of attraction, and guarantees robust reference tracking in the presence of non-parametric uncertainties.

For the multi-input, multi-output (MIMO) adjustable system,

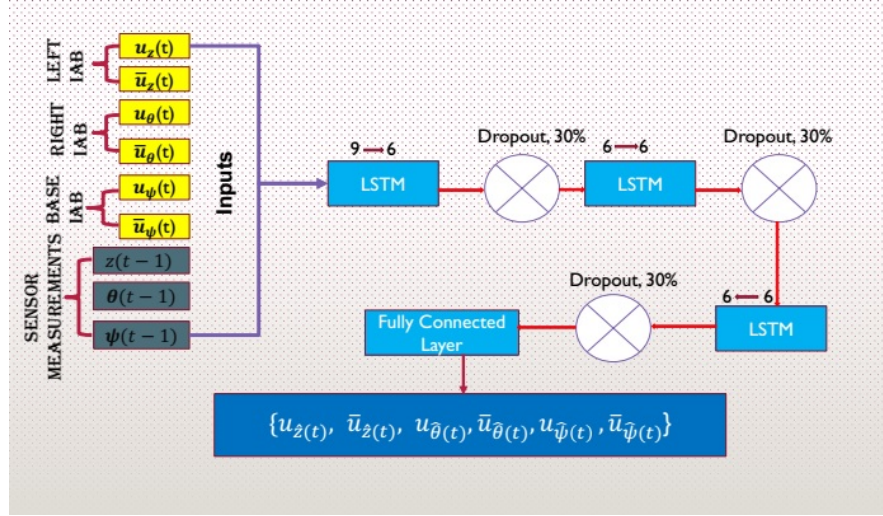


Fig. 7: Function Approximator Model

$$\dot{\mathbf{y}} = \mathbf{A}\mathbf{y} + \mathbf{B}\mathbf{A}(\mathbf{u} - f(\mathbf{y}, \mathbf{u})) + \mathbf{w}(k) \quad (7)$$

where $\mathbf{y} \in R^n$, $\mathbf{u} \in R^m$ are known input and output vectors, and $\mathbf{A} \in R^{n \times n}$, $\mathbf{A} \in R^{m \times m}$ are unknown matrices, $\mathbf{B} \in R^{n \times m}$, $\text{sgn}(\mathbf{A})$ are known matrices, and $\mathbf{w}(k) \in R^n$ is a bounded time-varying unknown disturbance, upper-bounded by a fixed positive scalar \mathbf{w}_{max} . with a Hurwitz matrix $\mathbf{A}_m \in R^{n \times n}$ and $\mathbf{B}_m \in R^{n \times m}$ commanded by a reference signal $\mathbf{r} \in R^m$. For this system, we note that $n = 3$ and $m = 6$. Our objective is to design an model-reference adaptive controller (MRAC) capable of operating in the presence of parametric (ε_f), and non-parametric ($\mathbf{w}(k)$) uncertainties so as to assure the boundedness of all signals within the closed-loop system. We propose the following controller

$$\mathbf{u} = \hat{\mathbf{K}}_y^T \mathbf{y} + \hat{\mathbf{K}}_r^T \mathbf{r} + \hat{f}(\mathbf{y}, \mathbf{u}), \quad (8)$$

where $\hat{\mathbf{K}}_y$ and $\hat{\mathbf{K}}_r$ are adaptive gains to be designed shortly. The $\hat{\mathbf{K}}_y^T \mathbf{y}$ term keeps the states of the approximation set $\mathbf{y} \in \mathbf{B}_R$ stable, while the $\hat{\mathbf{K}}_r^T \mathbf{r}$ term causes the states to follow a given reference trajectory. The function approximator $\hat{f}(\cdot)$ ensures states that start outside the approximation set $\mathbf{y} \in \mathbf{B}_R$ converge to \mathbf{B}_R in finite time (it converges non-parametric errors ε_f that puts certain states out of the approximation set into \mathbf{B}_R). We can generally write the NN model as

$$\hat{f}(y) = \hat{\boldsymbol{\theta}}^T \boldsymbol{\Phi}(\mathbf{y}) + \varepsilon_f,$$

where $\hat{\boldsymbol{\theta}}^T$ denotes the vectorized weights of the neural network and $\boldsymbol{\Phi}(\mathbf{y})$ denotes the vector of inputs and outputs defined as

$$\Phi(\mathbf{y}) = \{\mathbf{y}(k-d) \cdots \mathbf{y}(k-d-4), \mathbf{u}(k-d) \cdots \mathbf{u}(k-d-5)\}, \quad (9)$$

and ε_f is the approximation error. The closed-loop dynamics therefore become

$$\dot{\mathbf{y}} = \mathbf{A}\mathbf{y} + \mathbf{B}\Lambda \left(\hat{\mathbf{K}}_y^T \mathbf{y} + \hat{\mathbf{K}}_r^T \mathbf{r} + \hat{f}(\cdot) - f(\cdot) \right). \quad (10)$$

We assume nonlinear function and approximator matching conditions, $f(\cdot) = \hat{f}(\cdot)$, such that after rearrangement, (10) can be written as

$$\dot{\mathbf{y}} = (\mathbf{A} + \mathbf{B}\Lambda \hat{\mathbf{K}}_y^T) \mathbf{y} + \mathbf{B}\Lambda (\hat{\mathbf{K}}_r^T \mathbf{r} + \varepsilon_f). \quad (11)$$

Furthermore, we assume model matching conditions with ideal constant gains \mathbf{K}_y and \mathbf{K}_r so that

$$\mathbf{A} + \mathbf{B}\Lambda \mathbf{K}_y^T = \mathbf{A}_m, \quad \text{and} \quad \mathbf{B}\Lambda \mathbf{K}_r^T = \mathbf{B}_m, \quad (12)$$

from which

$$\begin{aligned} \mathbf{A} + \mathbf{B}\Lambda \hat{\mathbf{K}}_y^T - \mathbf{A}_m &= \mathbf{B}\Lambda \tilde{\mathbf{K}}_y^T \text{ and} \\ \mathbf{B}\Lambda \hat{\mathbf{K}}_r^T - \mathbf{B}_m &= \mathbf{B}\Lambda \tilde{\mathbf{K}}_r^T, \end{aligned} \quad (13)$$

where $\tilde{\mathbf{K}}_y^T = \mathbf{K}_y^T - \hat{\mathbf{K}}_y^T$ and $\tilde{\mathbf{K}}_r^T = \mathbf{K}_r^T - \hat{\mathbf{K}}_r^T$. The generalized error state vector $\mathbf{e}(k) = \mathbf{y}(k) - \mathbf{y}_m(k)$ has dynamics $\dot{\mathbf{e}}(k) = \dot{\mathbf{y}}(k) - \dot{\mathbf{y}}_m(k)$, so that we have

$$\dot{\mathbf{e}}(k) = \mathbf{A}_m \mathbf{e}(k) + \mathbf{B}\Lambda [\tilde{\mathbf{K}}_r^T \mathbf{r} + \tilde{\mathbf{K}}_y^T \mathbf{y} - \varepsilon_f]. \quad (14)$$

The estimation error will be bounded as long as $\mathbf{y} \in \mathbf{B}_R$. Our goal is to keep $\mathbf{y} \in \mathbf{B}_R$.

Theorem: Given correct choice of adaptive gains $\hat{\mathbf{K}}_y$ and $\hat{\mathbf{K}}_r$, the error vector $\mathbf{e}(k)$, with closed loop time derivative given by (14) will be uniformly ultimately bounded, and the state \mathbf{y} will converge to a neighborhood of \mathbf{r} .

We refer readers to [23] for detailed proof. We find that,

$$\dot{\mathbf{V}}(\cdot) = -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \varepsilon_f + 2 \operatorname{tr} \left(\tilde{\mathbf{K}}_y^T (\Gamma_y^{-1} \dot{\hat{\mathbf{K}}}_y + \mathbf{y} \mathbf{e}^T \mathbf{P} \mathbf{B} \operatorname{sgn}(\Lambda)) \right) |\Lambda| \quad (15)$$

$$+ 2 \operatorname{tr} \left(\tilde{\mathbf{K}}_r^T (\Gamma_r^{-1} \dot{\hat{\mathbf{K}}}_r + \mathbf{r} \mathbf{e}^T \mathbf{P} \mathbf{B} \operatorname{sgn}(\Lambda)) \right) |\Lambda| \quad (16)$$

where for a real-valued x , we have $x = \operatorname{sgn}(x)|x|$. The first two terms in (16) will be negative definite for all $\mathbf{e} \neq 0$ since \mathbf{A}_m is Hurwitz and the other terms in (16) will be identically null if we choose the adaptation laws

$$\dot{\hat{\mathbf{K}}}_y = -\Gamma_y \mathbf{y} \mathbf{e}^T \mathbf{P} \mathbf{B} \operatorname{sgn}(\Lambda), \quad \dot{\hat{\mathbf{K}}}_r = -\Gamma_r \mathbf{r} \mathbf{e}^T \mathbf{P} \mathbf{B} \operatorname{sgn}(\Lambda). \quad (17)$$

The time-derivative of the Lyapunov function can then be written as

$$\begin{aligned}\dot{\mathbf{V}}(\cdot) &= -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \mathbf{A} \varepsilon_f \\ &\leq -\lambda_{low} \|\mathbf{e}\|^2 + 2\|\mathbf{e}\| \|\mathbf{P} \mathbf{B}\| \lambda_{high}(\mathbf{A}) \varepsilon_{max},\end{aligned}\quad (18)$$

where $\lambda_{low}, \lambda_{high}$ represent the minimum and maximum characteristic roots of \mathbf{Q} and \mathbf{A} respectively. $\dot{\mathbf{V}}(\cdot)$ is thus negative definite outside the compact set

$$\chi = \left(\mathbf{e} : \|\mathbf{e}\| \leq \frac{2\|\mathbf{P} \mathbf{B}\| \lambda_{high}(\mathbf{A}) \varepsilon_{max}}{\lambda_{low}(\mathbf{Q})} \right). \quad (19)$$

and we conclude that the error \mathbf{e} is *uniformly ultimately bounded*. As \mathbf{e} converges to a neighborhood of 0, \mathbf{y} converges to a neighborhood of \mathbf{y}_m . From the stable model reference system \mathbf{y} converges to a neighborhood of \mathbf{r} . Note that asymptotic convergence of \mathbf{e} to zero is not guaranteed but the parametric errors are guaranteed to stay bounded.

3.6 Network Design

We require accurate mapping of temporally lagged patterns in inputs to output states, a dynamic nonlinear model of valve encoder values to sensor measurements that accurately maps $f(\cdot)$ in (7). We choose a LSTM [35] due to its capacity for long-term context memorization and inherent multiplicative units that avoid oscillating weights or vanishing gradients when error signals are backpropagated in time [35,36]. LSTMs truncate gradients in the network where it is harmless by enforcing constant error flows through their *constant error carousels*. As a result, LSTMs are robustly more powerful for adaptive sequence-to-sequence modeling or mapping data that temporally evolve in time. Their biological model makes them more suitable for adaptive robotics such as soft robots than previously used artificial NNs such as feedforward networks [37], radial basis-functions [38,39] or vanilla RNNs [40].

The NN model takes a memory-based concatenated vector of current inputs and past outputs as in (9), propagates them through three hidden layers, with each layer made up of $\{9, 6, 6\}$ neurons each, applies 30% dropout and then maps the last layer to a fully connected layer that generates valve torques. The architecture of the neuro-controller is shown in Figure 7. The last layer is designed to generate appropriate valve torques based on an internal model of the plant. A self-tuning adaptive control law (with a feedforward regulation and state feedback component) adapts to the internal parameters of the plant to ensure stability of the system and bounded tracking of given trajectory. The overall network has neuron connection weights and thresholds of approximately 1,400. This makes search for a suitable controller feasible.

The LSTM model estimates a model $f(\mathbf{y})$, that minimizes the mean-squared error between predicted output $\hat{\mathbf{y}}(k)$ and actual output $\mathbf{y}(k)$ according to

$$f(\mathbf{y}(k)) = \arg \min_w \mathbf{V}_N(w, \Phi(\mathbf{y})) \quad (20)$$

$$\text{where } \mathbf{V}_N(\mathbf{w}, \Phi(\mathbf{y})) = \sum_{t=1}^{\mathcal{K}} \sum_{i=1}^n \frac{1}{2} (\hat{\mathbf{y}}_i(t) - \mathbf{y}_i(t))^2,$$

and $\Phi(\mathbf{y})$ is a regression vector as defined in (9) on a bounded interval $[1, N]$. (20) is minimized using stochastic gradient descent so that at each iteration, we update the parameters (weights) of the network \mathbf{w}_i based on the *ordered derivatives* of $\mathbf{V}_N(\mathbf{w}, \Phi(\mathbf{y}))$ (Werbos [41]) *i.e.*

$$\mathbf{w}_{k+1} \leftarrow \eta \mathbf{w}_k - \alpha \sum_{i=1}^n \nabla_{\mathbf{w}} \mathbf{V}(\mathbf{y}_i, \hat{\mathbf{y}}_i(\theta_k)). \quad (21)$$

η (set to 1) hastens the optimization in a direction of low but steepest descent in training error, and α is a sufficiently small learning rate (set to 5×10^{-3}), and $\nabla_w \mathbf{V}(\theta, \Phi(\mathbf{y}))$ is the derivative of \mathbf{V} with respect to w averaged over the k -th batch (we used a batch size of 50). We initialized the weights of Figure 7 from a one-dimensional normal distribution with zero-mean and unit variance.

4 Experiment: IABs Control

The headpose is determined based on our formulation in 3.1. The 3-DOF pose of the head is made up of the state tuple $\{z(k), \theta(k), \phi(k)\}$.

4.1 Adaptive Control Parameters

We sample from the parameters of the trained network and we set $\hat{f}(\cdot)$ in (8) to the fully connected layer of samples from the network. We publish the control law from the neural network and subscribe in a separate node. The gains $\hat{\mathbf{K}}_y$ and $\hat{\mathbf{K}}_r$ in (17), were found by solving the ODEs iteratively using a single step of the integral of the solutions to $\hat{\mathbf{K}}_y(t)$, $\hat{\mathbf{K}}_r(t)$. Our solution is an implementation of the Runge-Kutta Dormand-Prince 5 ODE-solver available in the Boost C++ Libraries³. We found a step-size of 0.01 to be realistic. \mathbf{y}_m is computed based on the solution to the forced response of the linear system,

$$\mathbf{y}_m(t) = e^{\mathbf{A}_m t} \mathbf{y}_m(0) + \int_0^t e^{\mathbf{A}_m(t-\tau)} \mathbf{B}_m \mathbf{r}(\tau) d\tau.$$

We set $\mathbf{y}_m(0) = \mathbf{y}(0)$ at $t = 0$ and for a settling time requirement of $T_s = 5\text{secs}$ at which the response remains within 2% of final value, we find that

³ <https://goo.gl/l7JyYe>

$$\mathbf{A}_m = \begin{bmatrix} -\frac{1334}{1705} & 0 & 0 \\ 0 & -\frac{1334}{1705} & 0 \\ 0 & 0 & -\frac{1334}{1705} \end{bmatrix}. \quad (22)$$

For a nonnegative \mathbf{Q} and a positive definite \mathbf{P} , the pair $(\mathbf{Q}, \mathbf{A}_m)$ will be observable (LaSalle's theorem) so that the dynamical system is globally asymptotically stable. After searching, we picked a positive definite $\mathbf{Q} = \text{diag}(100, 100, 100)$ for the dissipation energy in (18) and set $\mathbf{A} = I_{3 \times 3}$ so that solving the general form of the lyapunov equation, we have

$$\mathbf{P} = \begin{bmatrix} -\frac{170500}{2668} & 0 & 0 \\ 0 & -\frac{170500}{2668} & 0 \\ 0 & 0 & -\frac{170500}{2668} \end{bmatrix} \quad (23)$$

The six solenoid valves operate in pairs so that two valves create a difference in air mass within each IAB at any given time. Therefore, we set

$$\mathbf{B} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix} \quad (24)$$

The non-zero terms in (24) denote the maximum duty-cycle that can be applied to the Dakota valves based on the software configuration of the NI RIO PWM generator.

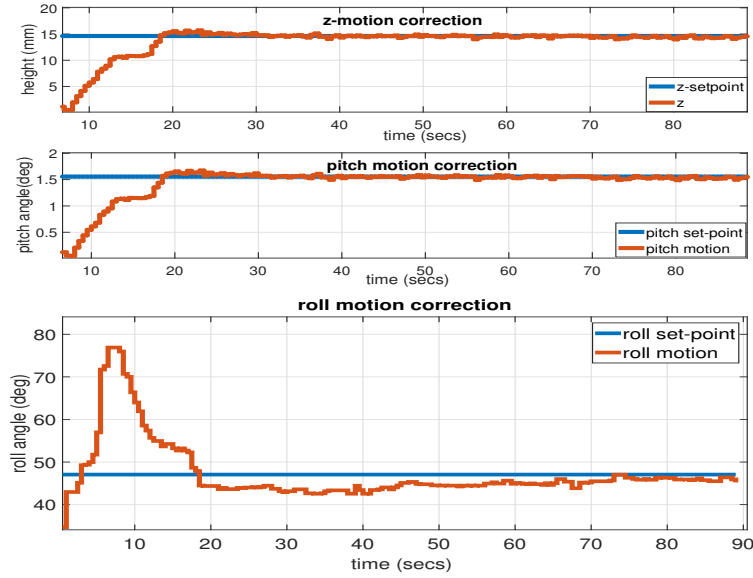


Fig. 8: Head motion correction along z, pitch and roll axes.

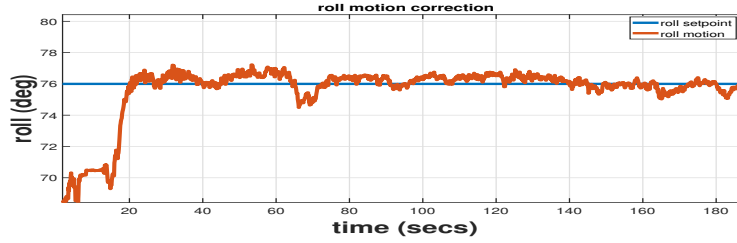


Fig. 9: Head motion correction along roll axis.

4.2 Results and Analysis

The three DoFs of the head are coupled and there is a limited reachable space with the IABs. It is therefore paramount that desired trajectories be ascertained as physically realizable before rolling out control trials. We therefore placed the head to physically realizable positions in open-loop control settings before testing the close-loop control system on such feasible goal poses.

Figure 8 show the performance of the controller when commanded to move the head from $[z, \theta, \phi]^T = [2.5mm, .25^\circ, 35^\circ]^T$ to $[14mm, 1.6^\circ, 45^\circ]^T$. We observe strong steady-state convergence along 2-DoFs, namely z and pitch axes with a 20 second rise time. The roll motion is however characterized by offshoots that may be caused by the coupled DOF. We perform a second experiment, seen in Figure 9, where we evaluate the performance of the controller on the roll angle of the head. We observe that the controller behaves well controlling the roll motion in isolation. The overshoot of Figure 8 are likely due to coupled dynamics not accounted for in our formulation.

While our results are promising, showing the feasibility of the control law along the physically realizable axes of motions, the coupled degrees of freedom need further investigation to achieve independent and precise axial motion control whilst preserving global head goal requirements.

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