

Electric propulsion

Chemical rockets

Thrust \rightarrow Exhaust velocity \rightarrow Temperature in combustion

I_{sp}

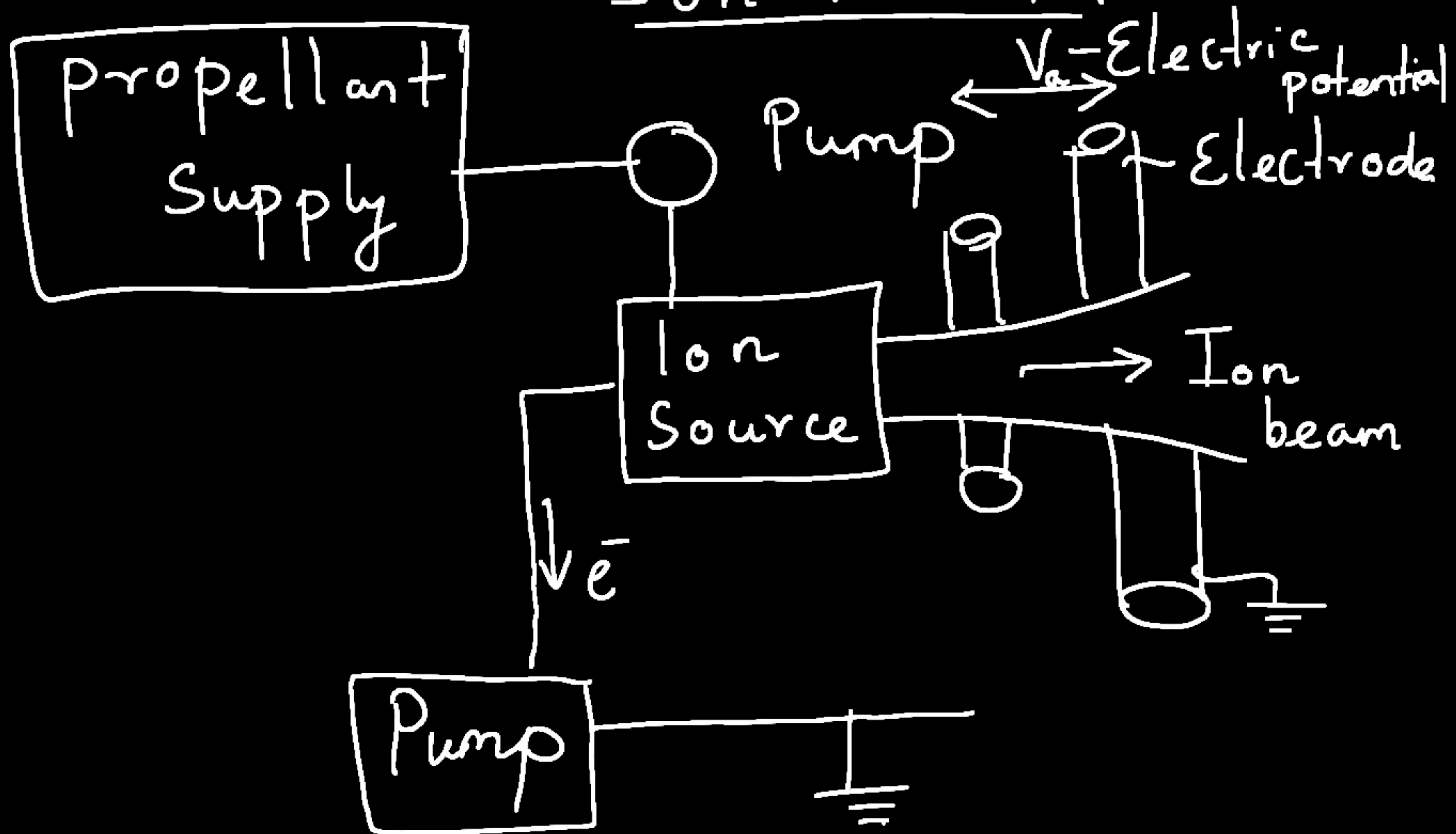
$\sim 500 \text{ s} \leftarrow$

$\sim 3500 \text{ K}$

$$\Delta u = u_{eg} \ln R = g_e I_{sp} \ln R \quad (\text{material limit})$$

Velocity increment $\Delta u \propto I_{sp}$

Ion Thruster



Electric propulsion $I_{sp} \sim 2500s$

Disadv: $T = \dot{m} u_e \rightarrow$ very small

$$\sim m N$$

1) Deep space / interstellar mission (long mission \sim years) $\sim N$ [best]

$$\sim MN \text{ [chemical rockets]}$$

2) Attitude / orbit maneuver
Control of spacecrafts / satellites

Performance calculation

1) Thrust, 2) I_{sp} , 3) Electric power required

Kinetic energy $\frac{1}{2} m u_e^2 = q V_a$

m - mass of a single ion

q - charge

V_a - Electric potential

q/m - charge to mass ratio

$$u_e = \sqrt{2 \left(\frac{q}{m} \right) V_a}$$

$$I_{sp} = \frac{u_e}{g_e} = \frac{1}{g_e} \sqrt{2 \left(\frac{q}{m} \right) V_a}$$

$$T = \dot{m} u_e, \quad \text{Beam current}$$

$$I = \dot{m} (q/m)$$

$$T = \frac{I}{(q/m)} \sqrt{2 (q/m) V_a}$$

$$T = I \sqrt{\frac{2 V_a}{(q/m)}}$$

Electrical power, $P_b = I V_a$
in the beam

$$\frac{P_b}{T} = \frac{g_e I_{sp}}{2}$$

Power required = $P_b + P_{ionization} + P_{loss}$
for the propulsion
System

