

Output: MCSLinv

```
countDat = Import[NotebookDirectory[], "MCSLoutput.csv"]; (* Edit here! *)

{a, b, c,  $\eta$ aMean,  $\mu$ tMean} = Part[countDat, -5 ;; -1];

These two functions convert between  $\eta$ a,  $\mu$ t space and  $\mu$ s,  $\mu$ a space.

 $\mu$ t $\eta$ aToAS[point_] := Module[{ $\mu$ t,  $\eta$ a}, { $\mu$ t,  $\eta$ a} = point;
  {(1 -  $\eta$ a) *  $\mu$ t,  $\eta$ a  $\mu$ t}]

 $\mu$ t $\eta$ aToASinv[point_] := Module[{ $\mu$ s,  $\mu$ a}, { $\mu$ s,  $\mu$ a} = point;
  { $\mu$ s +  $\mu$ a,  $\mu$ a / ( $\mu$ s +  $\mu$ a)}]

style[str_] := Style[str, Black, Bold, 14, FontFamily -> "Helvetica"]

{ $\mu$ sMean,  $\mu$ aMean} =  $\mu$ t $\eta$ aToAS[{ $\mu$ tMean,  $\eta$ aMean}] // Flatten;

pointText = StringForm["(``, ``)", NumberForm[ $\mu$ sMean, 3], NumberForm[ $\mu$ aMean, 3]];

logLik[point_] := Module[{ $\mu$ t,  $\eta$ a}, { $\mu$ t,  $\eta$ a} = point;
  a ( $\eta$ a -  $\eta$ aMean)2 / 2 + b ( $\eta$ a -  $\eta$ aMean) ( $\mu$ t -  $\mu$ tMean) + c ( $\mu$ t -  $\mu$ tMean)2 / 2]

Set the confidence interval:

p = .95; (* Edit here! *)

 $\chi^2$  = 0.5 x /. FindRoot[CDF[ChiSquareDistribution[2], x] == p, {x, 1}];

ellipse = Show[ContourPlot[-logLik[ $\mu$ t $\eta$ aToASinv[{ $\mu$ s,  $\mu$ a}]] ==  $\chi^2$ ,
  { $\mu$ s,  $\mu$ sMean * 0.95,  $\mu$ sMean * 1.05}, { $\mu$ a,  $\mu$ aMean * 0.95,  $\mu$ aMean * 1.05},
  ContourStyle -> Blue, PlotLabel -> style[pointText]],
  ListPlot[{ { $\mu$ sMean,  $\mu$ aMean} }, PlotStyle -> Blue], AspectRatio -> 0.6,
  Frame -> True, FrameStyle -> Directive[Thick, Black, Bold, 12],
  FrameLabel -> {" $\mu$ s (mm-1)", " $\mu$ a (mm-1)"}]
```

