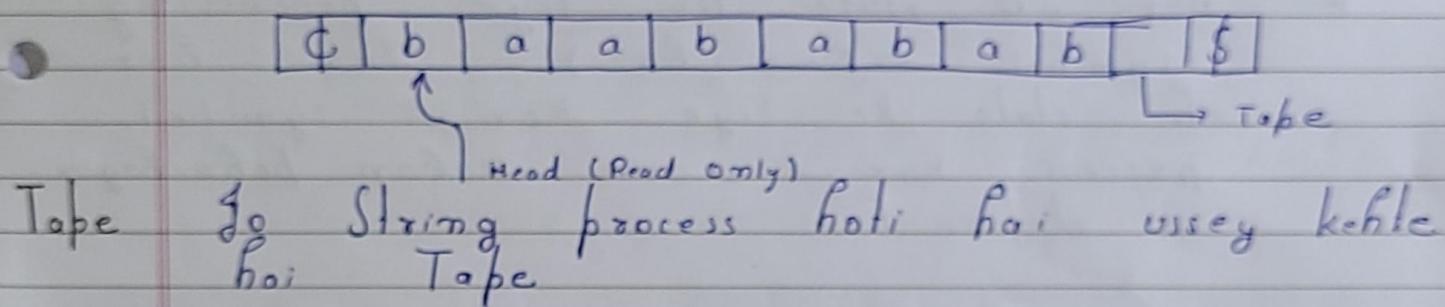


Automata

Ab automata mein machine's ke abstract our problem solving ability sekhenge



Head Vo part Jo read karega aur then
eb hee direction main aage jauta
hai \rightarrow \leftarrow (depends on
manufacture)

Diagram Samjho

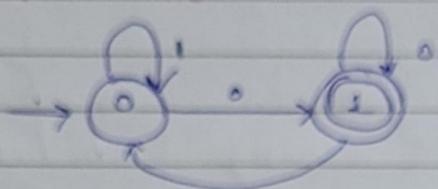
$\rightarrow Q_0$ \longrightarrow Initial State

Q_F \longrightarrow final state

Baahi Saari State Intermediate hoti
hai

Q_1

Ab isme apne state ko relation
bhi likhle ho.



- * Har ek state ke liye processing (symbol define hai) Yani har ek state ke liye Konsa symbol process karega aur kabon bahar hogega vo define hai.

Finite Automata \Rightarrow N - no. of state

Important terms

Symbol Symbol is the smallest building block, which can

Alphabets Set of Symbol always finite

Σ

String String is a finite sequence of symbols from some alphabet.

$|w|$ length of String

Language Language is a collection of appropriate strings. A language that is formed over Σ can be Finite or Infinite

Language of Finite Language

- $L_1 = \{ \text{set of strings of length } 2 \}$
- $L_1 = \{ xy, yx, xx, yy \}$

Grammar It is a finite set of formal rules for generating syntactically correct sentences

Terminal \Rightarrow Component of sentences generated using grammar
 a, b, c - - -

Non Terminal \Rightarrow Symbol which take part in composition of sentence but not part of it
 A, B, C - - -

Grammar can be 4 tuples (V, T, S, P)

V Set of Non Terminal Symbols.
 T Set of Terminal Symbols
 S It is a special symbol called Start Symbol
 P There are Production Rules for Terminals
 $\&$ Non Terminals.

$$\alpha \longrightarrow \beta$$

α & β are strings on $V \cup \Sigma$
 at least one symbol of α belongs
 to VN .

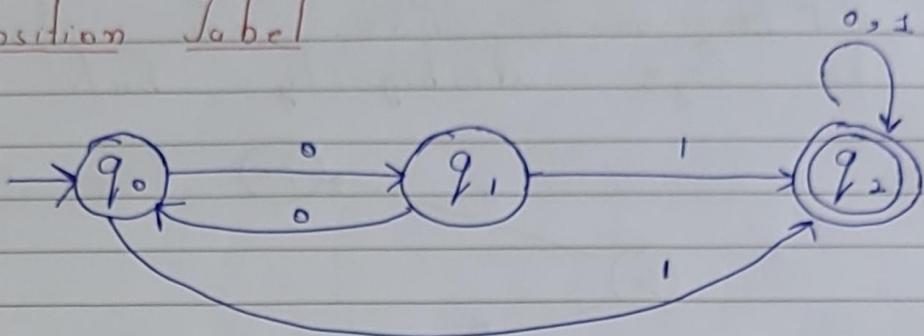
$(\{S, A, B\}, \{a, b\}, S, \{S \rightarrow AB, A \rightarrow a, B \rightarrow b\})$

Finite Automata Five Tuples.

$$(Q, \Sigma, q, F, \delta)$$

Q Finite set of states
 Σ set of Input Symbols
 q initial State
 F set of Final State
 δ Transition Function

Transition Table



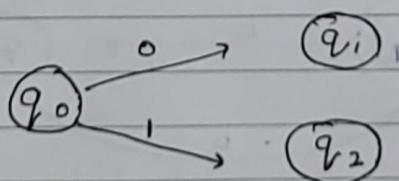
<u>Present State</u>	Next for 0	Next for 1
$\rightarrow q_0$	q_1	q_2
q_1	q_0	q_2
* q_2	q_2	q_2

Finite Automata

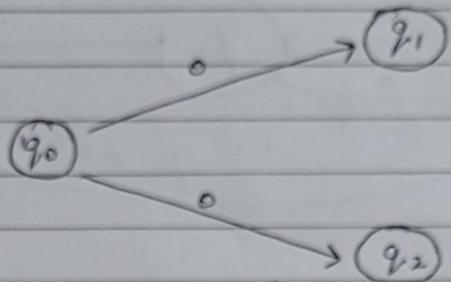
Deterministic
Finite Automata
(DFA)

Non-deterministic
Finite Automata
(NFA)

DFA mein har ek Input Symbol ke liye sirf ekhee path chuna.



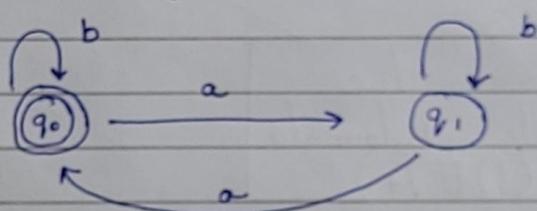
NFA mein has ek Input Symbol ke Liye Ambiguity ho sakti hai.



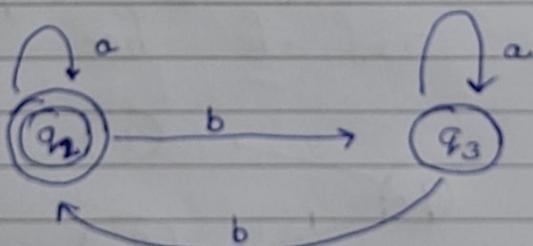
Cross product Seabha

Q Design a DFA which accept even no. of a & b

1 → Even no. of a



Even no. of a.



Even no. of b.

$$\{q_0, q_1\} \times \{q_2, q_3\}$$

$$\{(q_0, q_2), (q_0, q_3), (q_1, q_2), (q_1, q_3)\}$$

$$\begin{matrix} q_0 \\ q_2 \end{matrix} \xrightarrow{a} \begin{bmatrix} q_1 \\ q_2 \end{bmatrix}$$

$$\begin{matrix} q_0 \\ q_2 \end{matrix} \xrightarrow{b} \begin{bmatrix} q_0 \\ q_3 \end{bmatrix}$$

$$\begin{matrix} q_0 \\ q_3 \end{matrix} \xrightarrow{a} \begin{bmatrix} q_1 \\ q_3 \end{bmatrix}$$

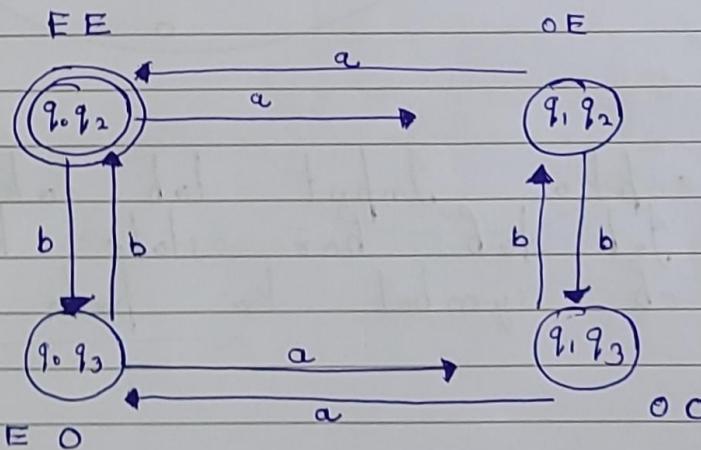
$$\begin{matrix} q_0 \\ q_3 \end{matrix} \xrightarrow{b} \begin{bmatrix} q_0 \\ q_2 \end{bmatrix}$$

$$\begin{matrix} q_1 \\ q_2 \end{matrix} \xrightarrow{a} \begin{bmatrix} q_0 \\ q_2 \end{bmatrix}$$

$$\begin{matrix} q_1 \\ q_2 \end{matrix} \xrightarrow{b} \begin{bmatrix} q_1 \\ q_3 \end{bmatrix}$$

$$\begin{matrix} q_1 \\ q_3 \end{matrix} \xrightarrow{a} \begin{bmatrix} q_0 \\ q_3 \end{bmatrix}$$

$$\begin{matrix} q_1 \\ q_3 \end{matrix} \xrightarrow{b} \begin{bmatrix} q_1 \\ q_2 \end{bmatrix}$$

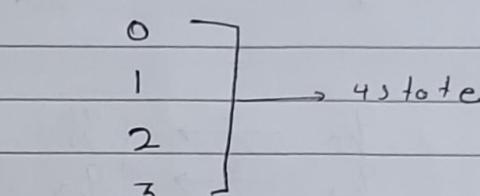
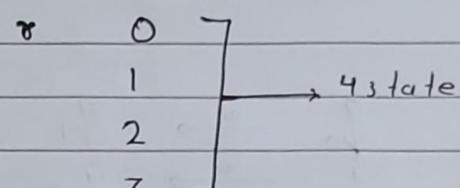


Q Design a DFA such that we check divisibility of a Binary no. with 4

See
Procedure

	✓ 0	0 0 0
	✓ 1	0 0 1
1	2	0 1 0
	3	0 1 1
	4	1 0 0
	5	1 0 1
	6	1 1 0
	7	1 1 1
	8	1 0 0 0

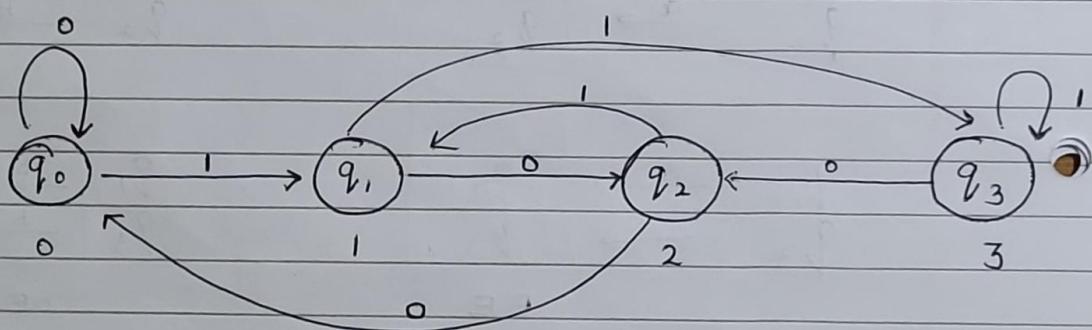
remainder / 4



2

3

0



abko Input tak execute karne
jab tak har state ke liye har
ch symbol ka pata na chal jaye.

Ab NFA se bchle DFA KO

3 Representation

Transition Table

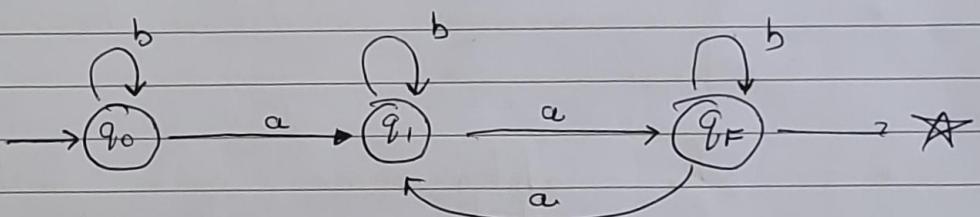
State	a	b
q_0	q_1	q_0
q_1	q_F	q_1
q_F	q_1	q_F

→ *

Transition function

$$\begin{array}{l} \delta(q_0, a) \leftarrow q_1 \\ \delta(q_0, b) \leftarrow q_0 \end{array} \quad \rightarrow *$$

Diagram

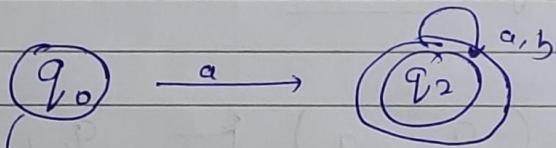


NFA

Jo Complex Soln hota hai uske jyje hum
 bahle NFA design karne hai then
 usko DFA mein convert karne hain.

isme less complexity hoti hai sag
 min condition ko fulfil karne hai
 baaki ki Nahi Sakte

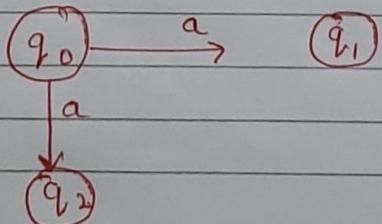
Q String Starts with a



No b specify karna.

* Jo minimum condition hai usko solve
 karo.

* abha abko isme aise milega ki
 ek symbol mein 2 ways ho



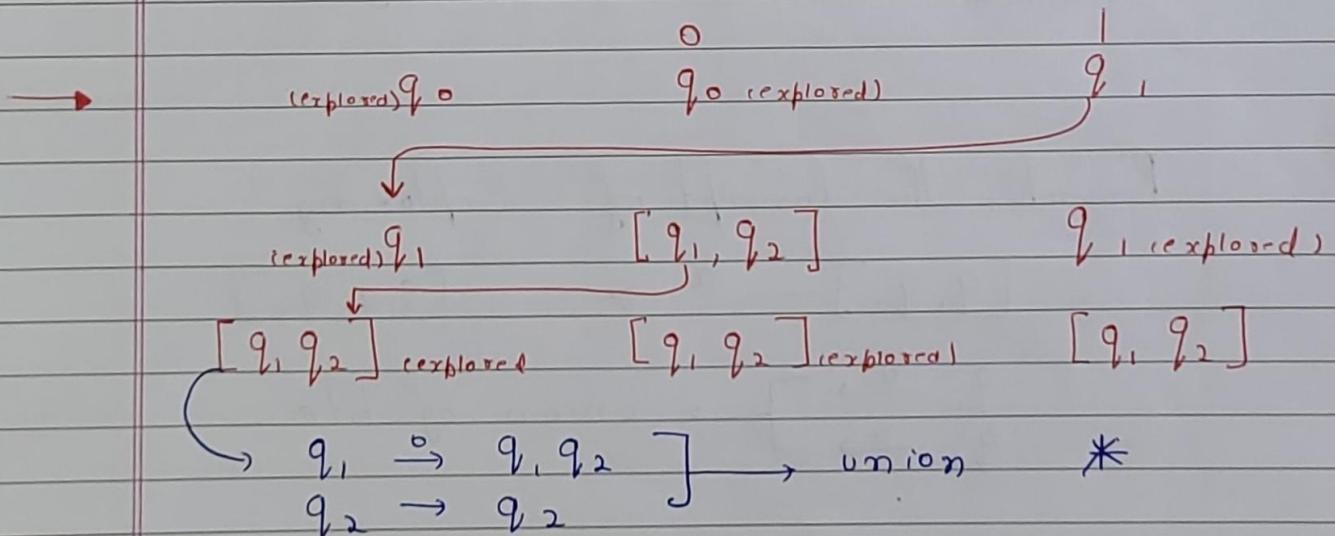
Conversion of NFA to DFA

hamesha koi bhi soln hog vo hamesha DFA mein kaise implement hog ?

Main agenda Samjho sab transition table ki pehle line likho aur jo states achieve ho rahi hai unko explore karo

Yani unhe har symbol ko execute karo until sare explored ho jaaye

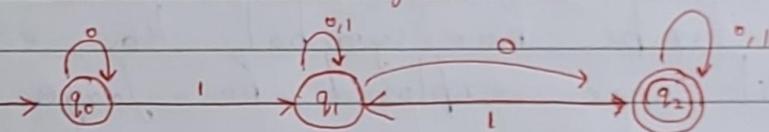
	0	1
→	q_0	q_0
	q_1	$\{q_1, q_2\}$
*	q_2	q_2



* Ab transition table mein jo final state hai vo tabhi be bhi hai vo final

q_0	q_0	q_1
q_1	$[q_1, q_2]$	q_1
$[q_1, q_2]$	$[q_1, q_2]$	$[q_1, q_2]$

Ques



0	1
q_0	q_1
q_1	q_1
$\{q_1, q_2\}$	$\{q_1, q_2\}$

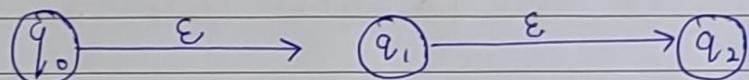
Remember the concept of Exploring

$$[q_1, q_2] \xrightarrow{a} [q_1, q_2, q_3]$$

$q_1 \xrightarrow{a}]$ $q_2 \xrightarrow{a}]$ union of state

NFA with Epsilon

Ab Epsilon yaani null transition ho
mujhe bina kuch process karne aap
state change karao

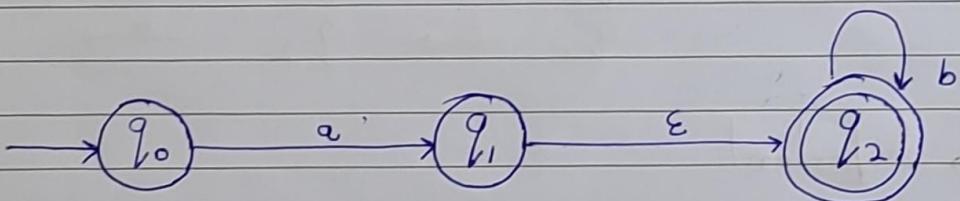


toh hum Null Transition batane hain:

$q_0 \xrightarrow{\epsilon} q_0$ homesha aayega
agar moyement specify hai toh
toh bhii include ho sakti hai

* har ek state ke liye δ' (specify karao)
yaani δ' (transition for - Epsilon)

Ques



$$\delta'(q_0, a) \Rightarrow q_0 \xrightarrow{\epsilon} \xrightarrow{a} \xrightarrow{\epsilon}$$

[, it means three transition,

$$\epsilon a \epsilon = \delta'(q_0, a)$$

$$\epsilon b \epsilon = \delta'(q_0, b)$$

[, initial state be q_0 yo likha

$$\delta'(q_0, a) = \{q_0, q_1\}$$

$$\delta'(q_0, b) = \emptyset \quad (\text{After movement no fa})$$

$$\delta'(q_1, a) = \emptyset$$

$$\delta'(q_1, b) = \{q_2\}$$

$$\delta'(q_2, a) = \emptyset$$

$$\delta'(q_2, b) = \{q_2\}$$

$$\delta'(q_1, b) \Rightarrow$$

$$\epsilon \Rightarrow q_1 \xrightarrow{\epsilon} q_1 \xrightarrow{b} \emptyset \xrightarrow{\epsilon} \emptyset$$

Important

* Then auf usko DFA mein convert
mein kur sahle ho.

* $\emptyset \Rightarrow$ DFA mein Trap state banado
isley.

Minimisation of DFA

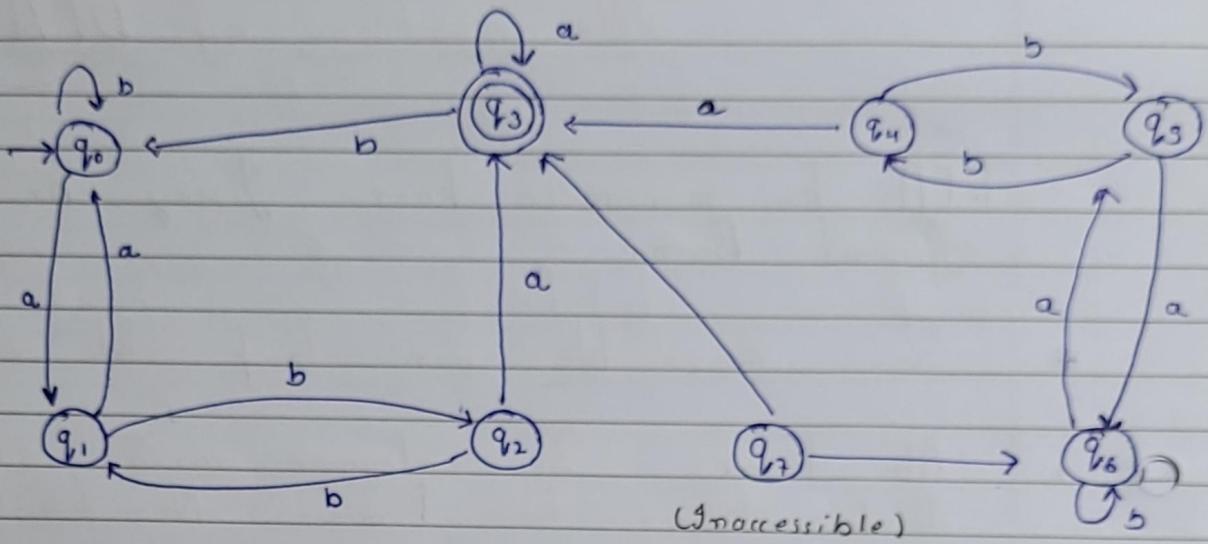
DFA ko minimise karna Jissey hi vo
efficient Bane

- * Some inaccessible aur trap state remove kardo
- * Ab Tumhe 2 categories mein string ko divide karna hai Final Non Final.
- * Make Transition diagram / table -

* Ab kya karna hai ki aap string ko karo process from $k=0 \longrightarrow n$

Aur kya karo Grp. banao Jinka Set
Same cosa hai = $k=0$ (length of String)

* We Will stop if set of $n-1, n$
are same.

QuesTransitionTable

	a	b
q_0	q_1	q_0
q_1	q_0	q_2
q_2	q_3	q_1
q_3	q_3	q_0
q_4	q_3	q_5
q_5	q_6	q_4
q_6	q_5	q_6

$P_i = 0$

F
 q_3

N=F
 $q_1 q_2 q_3 q_4 q_5 q_6$

$P_i = 1$

	a	b
q_0	x	x
q_1	x	x
q_2	v	x
q_4	v	x
q_3	x	x
q_6	x	x

$\{q_0 q_1 q_3 q_6\}$
N=F

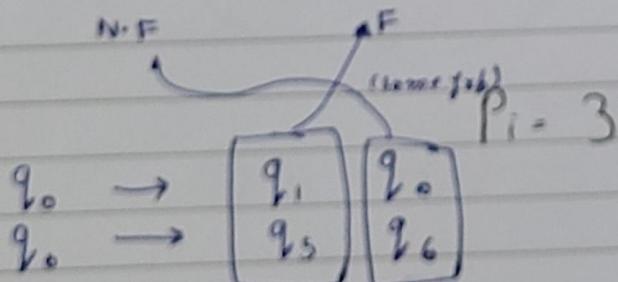
$\{q_2 q_4\}$
F

$\{q_5\}$
F

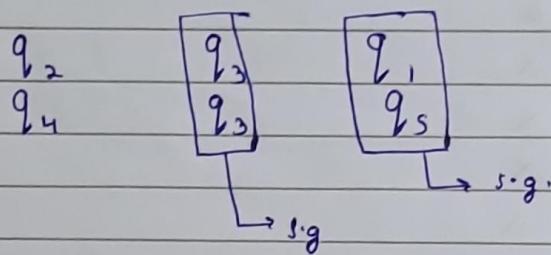
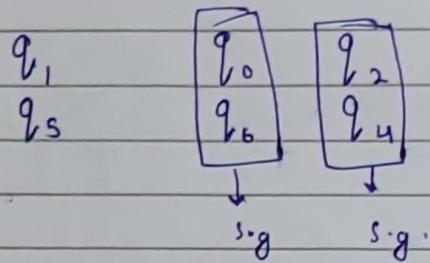
$P_i = 3$

q_0	x	x	x	x	q_2	v	x	x	x
q_1	x	x	v	x	q_4	v	x	x	x
q_5	x	x	v	x					
q_6	x	x	x	x					

$\{q_0 q_6\}$ $\{q_1 q_5\}$ $\{q_2 q_4\}$ $\{q_3\}$
N=F F F



$\{q_0 q_6\} = \text{Same}$



Regular Expression

Ab j. finite automata bundle hai
 toh uski language aap expression
 represent kar sake hai

$$\text{Symbol} \Rightarrow X^* = \{ \epsilon, X, XX, XXX \dots \}$$

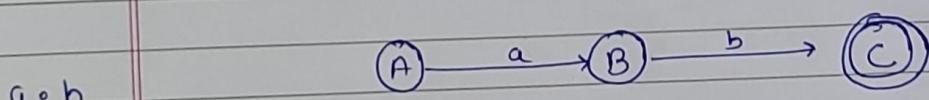
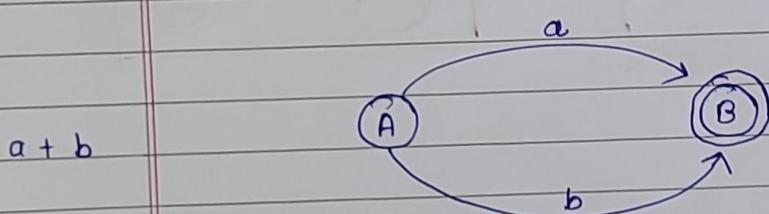
$$X^+ = \{ X, XX, XXX \dots \}$$

Kleene's Theorem

* $RE = a + b \rightarrow$ It will accept a or b

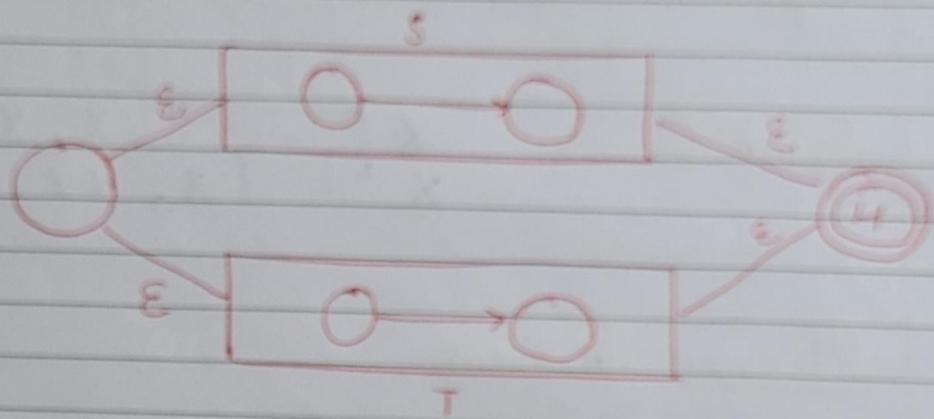
* $RE = (a + b)^* \rightarrow$ It will accept any combination of a,b with NULL

* $RE = ab \rightarrow$ It will accept a then b

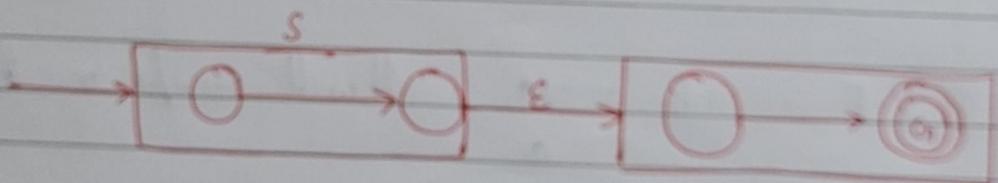


Non-La Two Reg for Expression
 S, T they have separate DFA

$R = S \cup T \Rightarrow$ connect via null transition



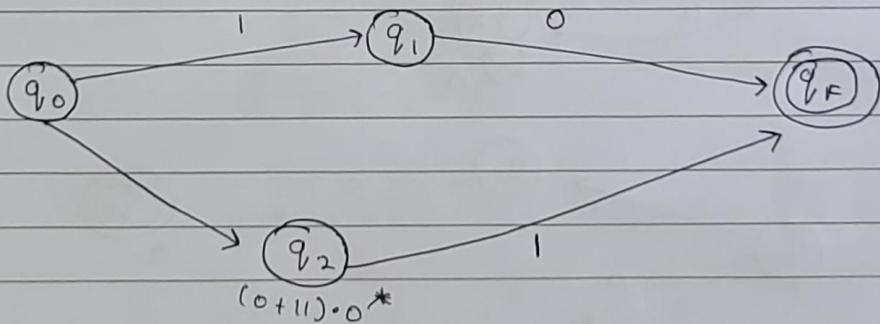
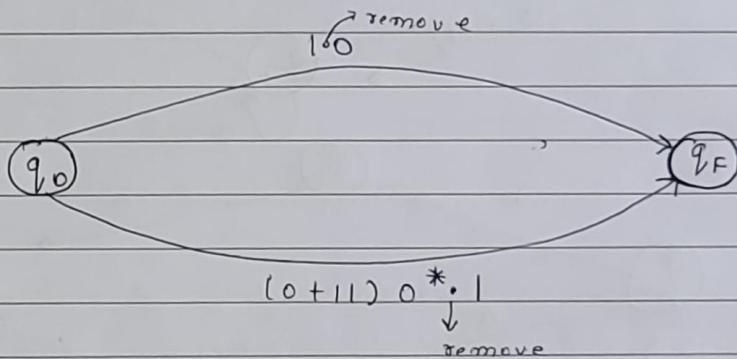
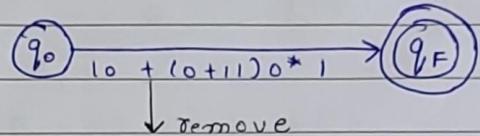
$R = S \circ T$

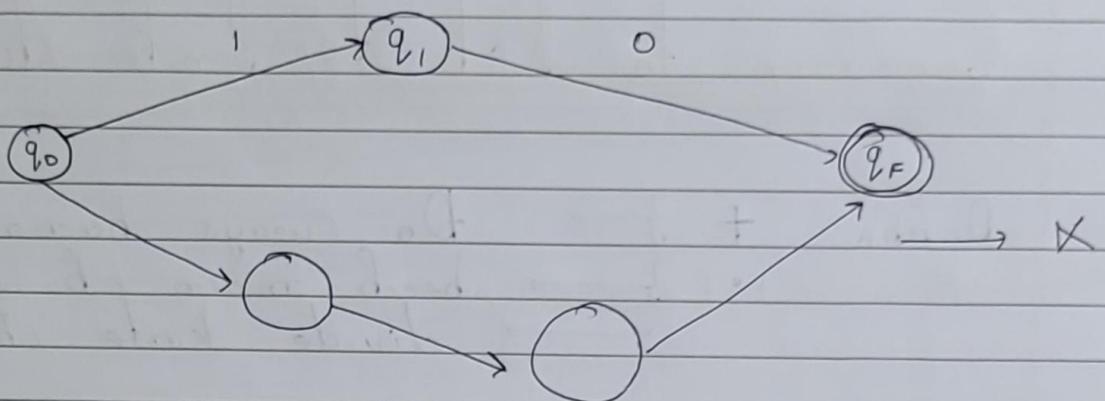


Conversion to R.E to Finite Automata

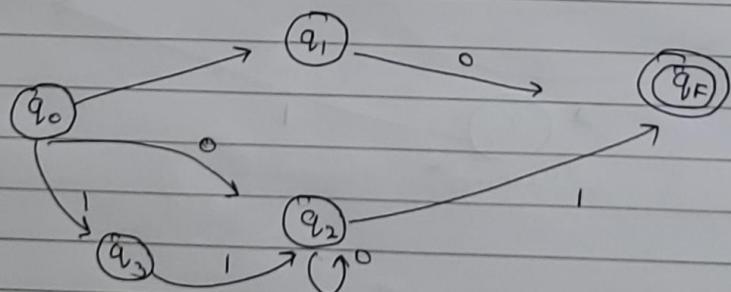
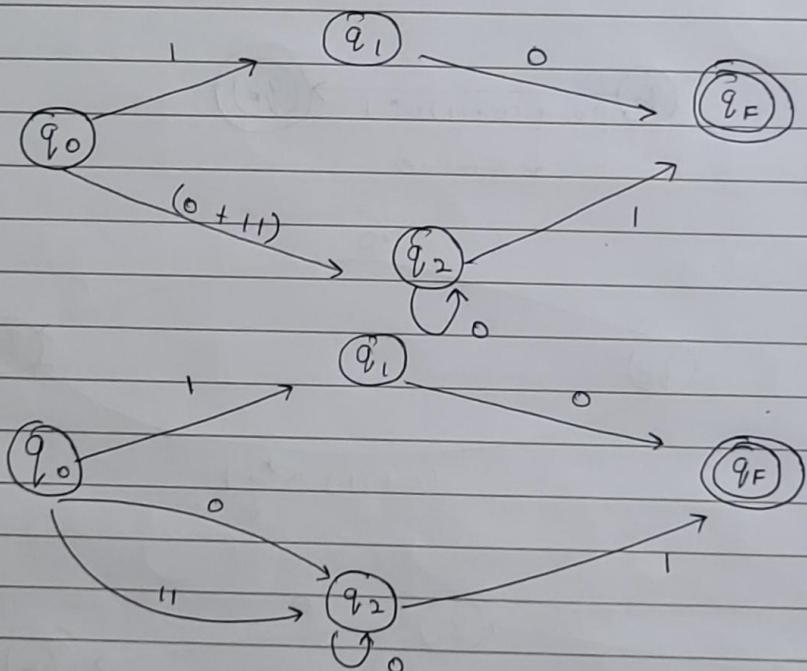
Defn. + } → Do ways banao
 • } → bech mein ek state
 → divide karte chalo

$$| 0 + (0+11)0^* |$$





0^* \Rightarrow some state be self loop

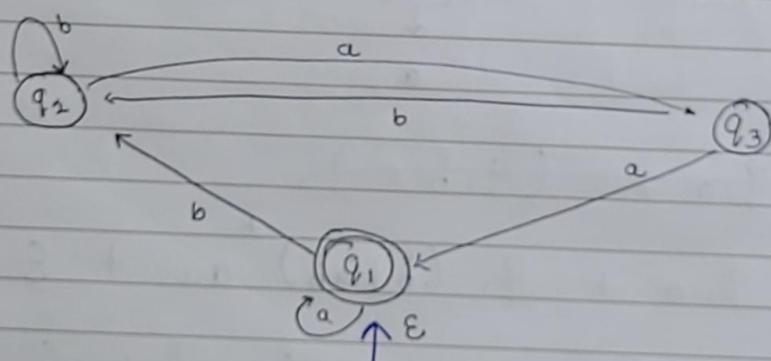


Finite Automata to Regular Expression

$R = \emptyset + RP$ }
 $R = \emptyset P^*$ } \rightarrow Important

• Har ek state ke liye arrows kahan se aur kya aur kaha hai, vo likho.

Important \rightarrow Agar Initial final hai toh E include karo
 \rightarrow before State then symbol $q_1 a$



We will solve for final state

$$F.S \quad q_1 = q_{1a} + q_{3a} + \epsilon \quad \begin{matrix} \nearrow \\ \text{(self loop)} \end{matrix} \quad \begin{matrix} \swarrow \\ \text{(Initial + Final)} \end{matrix}$$

$$q_2 = q_{2b} + q_{1b} + q_{3b}$$

$$q_3 = q_{2a} \quad \uparrow$$

$$q_2 = q_{2b} + q_{1b} + q_{2ab}$$

$$q_2 = q_{1b} + q_2 (b + ab) \quad \begin{matrix} \text{(R)} & \text{(Q)} & \text{R} & \text{(P)} \\ = & = & = & = \end{matrix}$$

$$q_2 = q_{1b} (b + ab) * \quad \begin{matrix} \text{*} \\ \equiv \end{matrix}$$

$$q_1 = q_{1a} + q_{2aa} + \epsilon \quad \begin{matrix} \downarrow \\ a \end{matrix}$$

$$= q_{1a} + (q_{1b} + q_2)$$

$$q_1 = q_{1a} + q_1 (b + ab)^* aa + \epsilon$$

$$q_1 = q_1 [a + (b + ab)^* aa] + \epsilon$$

$$q_1 = [a + (b + ab)^* aa]^* \cdot \epsilon$$

Pumping Lemma for Regular Language

The language accepted by finite Automata is called regular language.

Ek string jo valid ho vo chuno

then chuno something (jo aapne chuna hai) divide karo $x y z$ mein such that

$$|y|^i = 0, \quad x y^i z$$

$$\left. \begin{array}{l} |y| > 0 \\ |x y| \leq n \end{array} \right\} \text{Condition}$$

ab y ki power increase karo then jo resulted string aayega agar vo language satisfy nahi karte toh vo language Regular nahi hai.

Ques

$$\{ = \{a^n b^m \mid n > 1\}$$

$$n = 2$$

$$\begin{matrix} a & a & b & b \\ \sqcup & \sqcup \\ x & y & z \end{matrix} \quad |y| > 0 \quad |xyz| \leq 2$$

$$a \begin{matrix} a \\ \sqcup \\ y \end{matrix} b b = \underbrace{a a a}_{\text{X}} \quad \rightarrow \text{X in Language}$$

$$y^1 \Rightarrow y^2 \Rightarrow y^3 \Rightarrow y^4 \Rightarrow y^5 \rightarrow \text{pumping length.}$$

Ques $\{ = \{a^n b^m \mid n > 1, m > 2\} \quad n=2, m=3$

$$\begin{matrix} a & a & b & b & b \\ \sqcup & \sqcup & \sqcup \\ x & y & z \end{matrix}$$

$$\begin{aligned} \text{Min value} &= n=1 \\ m &= 3 \\ &= 4 \end{aligned}$$

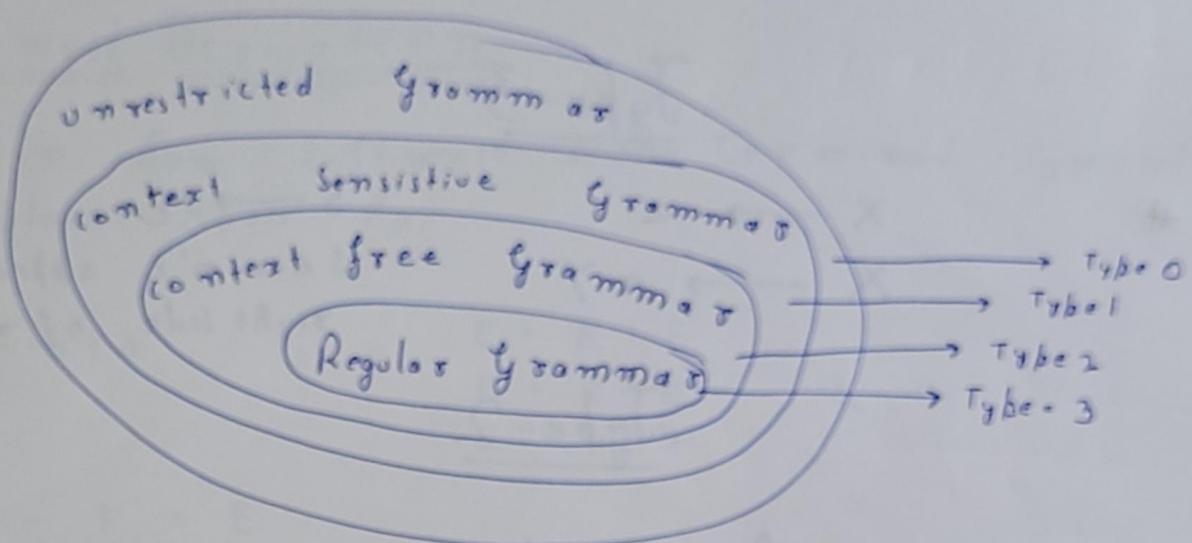
$$a\sigma = \begin{matrix} a & a & b & b & b \\ \sqcup & \sqcup & \sqcup \\ x & y & z \end{matrix}$$

\Rightarrow y ki power increase karo
 \Rightarrow Soasi strings accept hongi

Regular Language \Rightarrow ✓

G Grammars

Grammar kya hai set of rules (production) that generates string's according to pattern + Yani ye vo strings generate kaise hai jo vo Language accept kare



⑤ Grammar G can be formally written as a 4 tuple (V, T, S, P) where

- $V \longrightarrow$ Set of Non Terminal symbols (A, B)
- $T \longrightarrow$ Set of Terminal symbols (a, b)
- $S \longrightarrow$ Start Symbol
- $P \longrightarrow$ Production Rules $\alpha \longrightarrow \beta$

Type 0 => Recognized by Turing Machine

Type 1 => Context Sensitive by Linear Bound Automata

Type 2 => Context free Grammar By push down

Type 3 => Finite Automata (Reg Grammar)

Type-3

$$X \rightarrow a$$

$$S \rightarrow \epsilon$$

$$X \rightarrow a Y$$

S doesn't appear on
right side of any rule

Type-2

$$A \rightarrow \alpha$$

$A \in$ Non Terminal

$\alpha \in$ combination of Terminal & Non Terminal

Type 1

$$\alpha A \beta \xrightarrow{\quad} \alpha Y \beta \quad | \quad S \rightarrow \epsilon$$

$A \in N$

$\alpha, \beta, Y \in (T \cup N)^*$

if S is not allowed
in right

can be empty

Type - 0

$\alpha \longrightarrow \beta$

α = string of Terminal & Non Terminal
= atleast one terminal

Left most Derivation

mean hum left most Non Terminal symbol
replace karne hoi

$$a - b + a \quad ;$$

$$E = E + E$$

$$E = E - E$$

$$E = a \text{ or } b$$

$$E \rightarrow \boxed{E} + E$$



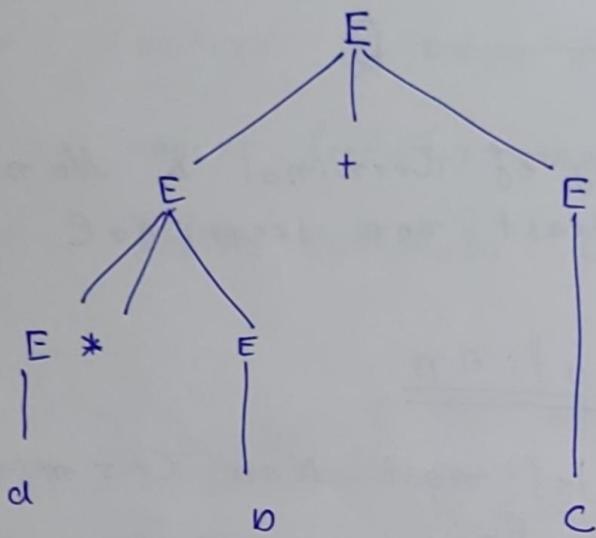
Replace

$$E - E + E$$



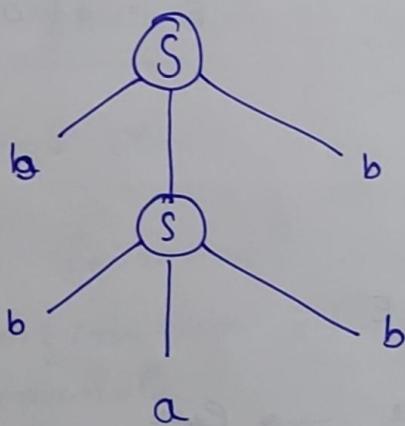
$$\underline{a - b + a} \rightarrow \text{Ans}$$

We can also represent using Parsed Tree



$S \rightarrow b S b \mid a \mid b$

Input string bbabb



Ambiguity in Grammar

Agar aap Left most derivation ke through bhi 2 raaste hai uss particular string tak bahut sarete hai.

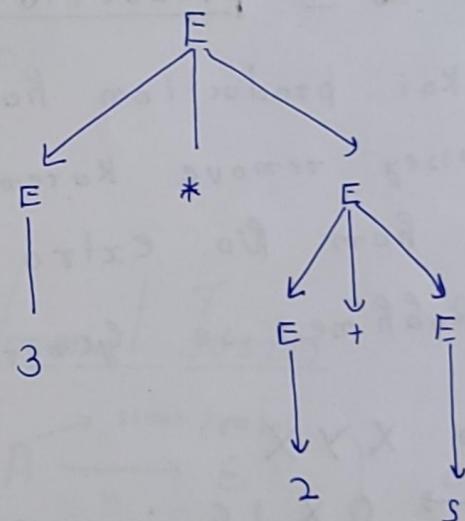
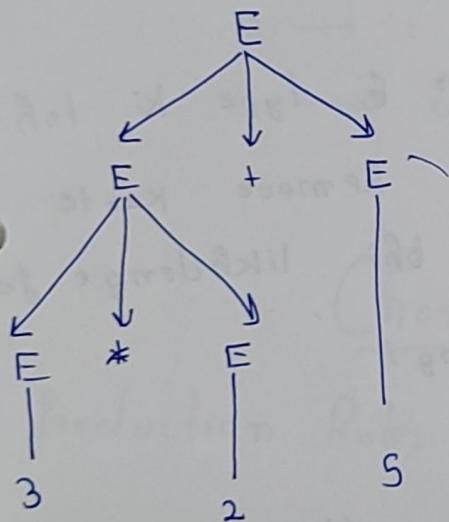
$$E \rightarrow I$$

$$E \rightarrow E + E \mid E * E$$

$$E \rightarrow (E)$$

$$I \rightarrow \epsilon \mid 1 \mid 0 \mid 2 \mid 3 \mid \dots \mid$$

$$3 * 2 + 5$$



Grammars Optimize

Useless Symbol

Ek symbol useless tab hota hai jab vo kisi bhi Production ke right side mein na aaye

$$S \rightarrow AB$$

$$A \rightarrow aA \mid \epsilon$$

$$B \rightarrow bB \mid \epsilon$$

$$\underbrace{C \rightarrow C}_{\text{useless}} \rightarrow \text{useless kyonki } C \text{ backi kisi bhi func ke right side mein nahi aata}$$

Elimination of ϵ production

Agar koi production hai $X \rightarrow \epsilon$ type ki toh hum ussey remove Karenge but Remove Karte Samay hum no extra values bhi likhdenge jo NULL Rakhne se generate hongi

$$S \rightarrow XYX$$

$$X \rightarrow 0X \mid \epsilon \longrightarrow \text{remove (place X Null)}$$

$$Y \rightarrow 1Y \mid \epsilon \longrightarrow \text{(remove) (place Y Null)}$$

$$S \rightarrow XYX \mid YX \mid XX \mid XX \mid X \mid Y$$

$$X \rightarrow 0X \mid 0$$

$$Y \rightarrow 1Y \mid 1$$

Unit production

$$X \longrightarrow Y$$

Non Terminal

$Y \longrightarrow$ symbols.

directly place them

$$S \longrightarrow 0A \mid 1B \mid C$$

$$A \longrightarrow 0S \mid 00$$

$$B \longrightarrow 1 \mid A$$

$$C \longrightarrow 0 \mid 1$$

$$S \longrightarrow C = C \longrightarrow 0 \mid 1$$

$$B \longrightarrow A - A \rightarrow 0S \mid 00$$

$$S \longrightarrow 0A \mid 1B \mid 01$$

$$A \longrightarrow 0S \mid 00$$

$$B \longrightarrow 1 \mid 0S \mid 00$$

$$C \longrightarrow 0 \mid 1$$

Chomsky Normal Form

Production Rules \Rightarrow

$$\left. \begin{array}{l} A \xrightarrow{\text{start symbol}} E \\ S \longrightarrow AB \\ S \longrightarrow a \end{array} \right\}$$

only these
are allowed

$$S \rightarrow a | aA | B$$

$$A \rightarrow aBB | \epsilon$$

$$B \rightarrow Aa | b$$

$$S \rightarrow aA \Rightarrow$$

$$S \rightarrow XA$$

$$X \rightarrow a$$

$$S \rightarrow B \Rightarrow$$

place B value \Rightarrow

$$S \rightarrow Aa$$

$$S \rightarrow b$$

$$S \rightarrow a | XA | Aa | b \Rightarrow S \rightarrow a | XA | AX | b$$

$$X \rightarrow a$$

$$X \rightarrow a$$

$$B \rightarrow Aa | b$$

$$B \rightarrow AX | b$$

$$A \rightarrow aBB | \epsilon \Rightarrow$$

$$A \rightarrow \underset{\text{club}}{XB}B | \epsilon$$

$$A \rightarrow XB B \Rightarrow$$

$$A \rightarrow RB$$

$$R \rightarrow XB$$

$$\left\{ \begin{array}{l} S \rightarrow a | XA | AX | b \\ X \rightarrow a \\ B \rightarrow AX | b | a \\ A \rightarrow RB | \epsilon \xrightarrow{\text{(Remove Null)}} \\ R \rightarrow XB \end{array} \right.$$

Remove Null
Remove Unit
Remove Useless

$$Y \rightarrow 1Y | 1$$

} $\rightarrow \star \star$

Greibach Normal Form

$$S \rightarrow \epsilon$$

$$A \rightarrow a$$

$$S \rightarrow a A s B \dots$$

- # First convert the grammar into C.N.F
- # Left Recursion \Rightarrow Eliminate
- # Convert to GNF

Left Recursion \Rightarrow Grammar mein agar kisi production ke jaise

$$X \rightarrow X a$$

(string of Terminal & Non Terminal)

$$A \rightarrow A \alpha \mid B$$

$$\begin{array}{l} A \rightarrow B A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

remove

$$\begin{array}{l} A \rightarrow B A' \mid B \\ A' \rightarrow \alpha A' \mid \alpha \end{array}$$

$S \rightarrow X B \mid AA$ $A \rightarrow a \mid SA$ $B \rightarrow b$ $X \rightarrow a$

Dekho Agar $A \rightarrow SA \rightarrow$ Gnf mein aajaya to β automatic AA bhi Gnf mein aajayega.

$$\begin{aligned} A \rightarrow SA &\Rightarrow A \rightarrow a \mid XBA \mid AAA \\ &\quad A \rightarrow a \mid aBA \mid AAA \end{aligned}$$
 $S \rightarrow aB \mid AA$ $A \rightarrow a \mid aBA \mid AAA$ $B \rightarrow b$ $X \rightarrow a$ $A \rightarrow AAA \rightarrow \text{remove}$ $A \rightarrow \underbrace{AAA}_{\alpha} \mid a \mid \underbrace{aBA}_{B_2}$ $A \rightarrow ac \mid a \mid aBAC \mid aBA$ $C \rightarrow AAC \mid AA$ $Y \rightarrow YY \mid I$

..... 0

$$S \rightarrow aB \mid AA$$

$$A \rightarrow aC \mid aBAC \mid a \mid aBA$$

$$C \rightarrow AAC \mid AA$$

$$B \rightarrow b$$

$$X \rightarrow a$$

Starting jiska bhi A hai usko
be replacement kardo.

○ $\left\{ \begin{array}{l} S \rightarrow aB \mid aCA \mid aBACA \mid aA \mid aBA \\ A \rightarrow aC \mid aBAC \mid a \mid aBA \\ C \rightarrow aCAC \mid aBACAC \mid aAC \mid aBAAC \\ C \rightarrow aCA \mid aBACA \mid aA \mid aBA \\ B \rightarrow b \\ X \rightarrow a \end{array} \right\} \rightarrow *$

Push Down Automata

Abisme hum ek stack add kardete hui
jissey hamara kaam aasan ho jayega



Initial element
Agar ye hai yaani;
stack empty hai;
(Top be)

PDA \Rightarrow collection of 7 components

Q \rightarrow finite set of states

Σ = input set

Γ = stack symbol which can be pushed

q_0 = initial state

Z = start symbol which is in Γ .

F = final state set

δ = mapping function current to next state

Language = $a^n b^{2n} \rightarrow \text{II}$

$$\delta(q_0, a, z) = (q_0, aa)$$

\uparrow mila
 \downarrow state top element of stack

$$\delta(q_0, a, a) = (q_0, aaa)$$

Now when we read b we will change the state from q_0 to q_1 .

$$\delta(q_0, b, a) = (q_1, \epsilon)$$

$$\delta(q_1, b, a) = (q_1, \epsilon)$$

Final State $\Rightarrow \delta(q_1, \epsilon, z) = (q_f, \epsilon)$

Ques $\Rightarrow \boxed{0^m \mid 1^m \mid 0^n \mid m, n \geq 1} \Rightarrow ??$

ise hamne koi lena dena mali
hai ki agar bagal o ki
Quantity some honi chahiye.

$$(q_0, 0, z_0) = (q_0, 0z_0)$$

$$(q_0, 0, 0) = (q_0, 0\bar{z}_0)$$

$$(q_0, 1, 0) = (q_1, 0)$$

$$(q_1, 1, 0) = (q_1, 0)$$

$$(q_1, 0, 0) = (q_2, \epsilon)$$

$$(q_2, 0, 0) = (q_2, \epsilon)$$

$$(q_2, \epsilon, z_0) = q_f$$

$$(000, \epsilon)$$

$$(1, b, \epsilon)$$

$$(000, \epsilon)$$

$$(0, 0, \epsilon)$$

LL(1) Parsing.

Left factoring.

$$S \longrightarrow a\alpha, \quad S \longrightarrow b\beta$$

we have to generate, Ambiguity.

$$S \longrightarrow a S'$$

$$S' \longrightarrow \alpha \mid \beta$$

Construction of Parsing Table

$$X = \text{terminal} \quad \text{first} = \{x\}$$

$$X \longrightarrow \epsilon \Rightarrow \text{Add Null to first } \{x\}.$$

$$X = \text{Non terminal} \Rightarrow X \longrightarrow a \alpha \quad \boxed{\text{Add}}$$

$$X \longrightarrow Y_1 Y_2 Y_3 \quad \boxed{\text{First of } Y_1} \quad \text{Add to first of } X$$

Now when

Grammar mein No Left Recursion

No Left Factoring

$$E \longrightarrow TE'$$

$$E' \longrightarrow + TE' \mid \epsilon$$

$$T \longrightarrow FT'$$

$$T' \longrightarrow * FT' \mid \epsilon$$

$$F \longrightarrow (E) \mid id$$

$$\text{First} \Rightarrow E - (, id$$

$$E' - + \epsilon - \text{place Null}$$

$$T - (, id$$

$$T' - * \epsilon$$

$$F - (, id$$

$$\text{Follow} \Rightarrow E - \$,)$$

$$\Rightarrow E' - \$,)$$

$$\Rightarrow T - +, \$,)$$

$$\Rightarrow T' - *, +, \$,)$$

$$\Rightarrow F - *, +, \$,)$$

$$\Rightarrow F - *, +, \$,)$$

Follow \Rightarrow Non Terminal \Rightarrow Production ki right side mein Kahan aya

Start symbol = \$

$E \longrightarrow$ like bad Agar terminal hai toh ok

$\rightarrow E \Rightarrow$ Follow of left Non Terminal

\rightarrow Non Terminal (Everything of first of Non Terminal
(Accept E))

Agar Kisi Non Terminal Ke first mein
 Null hai toh ussey place Karo.
 then see what will come.

Tricky

Parsing Table

First()

$$E \Rightarrow (, id$$

$$E' \Rightarrow +, \epsilon \xrightarrow{\text{NULL}}$$

$$T \Rightarrow (, id$$

$$T' \Rightarrow *, \epsilon$$

$$F \Rightarrow (id$$

Follow()

$$E \Rightarrow \$,)$$

$$E' \Rightarrow \$,)$$

$$T \Rightarrow +, \$,)$$

$$T' \Rightarrow +, \$,)$$

$$F \Rightarrow +, *, \$,)$$

Non Terminal	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

Karise

First mein agar Null Nah; hai toh
jo terminal symbol vahan Pe aap produc-
tion jo likhi hai ussey likhdo

If Null hai Toh uske follow mein
Null Transition doo do

hum Isme Ye Dekhte hai ki agar
aab kisi Non Terminal be hai aur
aab ko kisi respective terminal be
jaana hai toh which production to use
lets see it in action. how
Parsing Table works.

stack

input

production

\$ E

id + id * id \$
↑

→ TE' → reverse Karke push kardo

\$ E' T

id + id * id \$ E → TE'

\$ E' T' F

id + id * id \$ T → FT'

\$ E' T' id

id + id * id \$ F → id

\$ E' T'

+ id * id \$ T' → ε

\$ E'

+ id * id \$ E' → +TE'

\$ E' T f

f id * id \$

|
|
|

So on.

\$ f

E' → ε

→ valid.

S R posfix

Böhm Up

Step => Augmented Grammar

Normal =>	$S \rightarrow AA$ $A \rightarrow aA \cup b$		Augmented
			$S' \rightarrow S \rightarrow AAdd$

Canonical Collection of LR(0)

$S' \rightarrow \cdot S$

$S \rightarrow \cdot AA = 1$

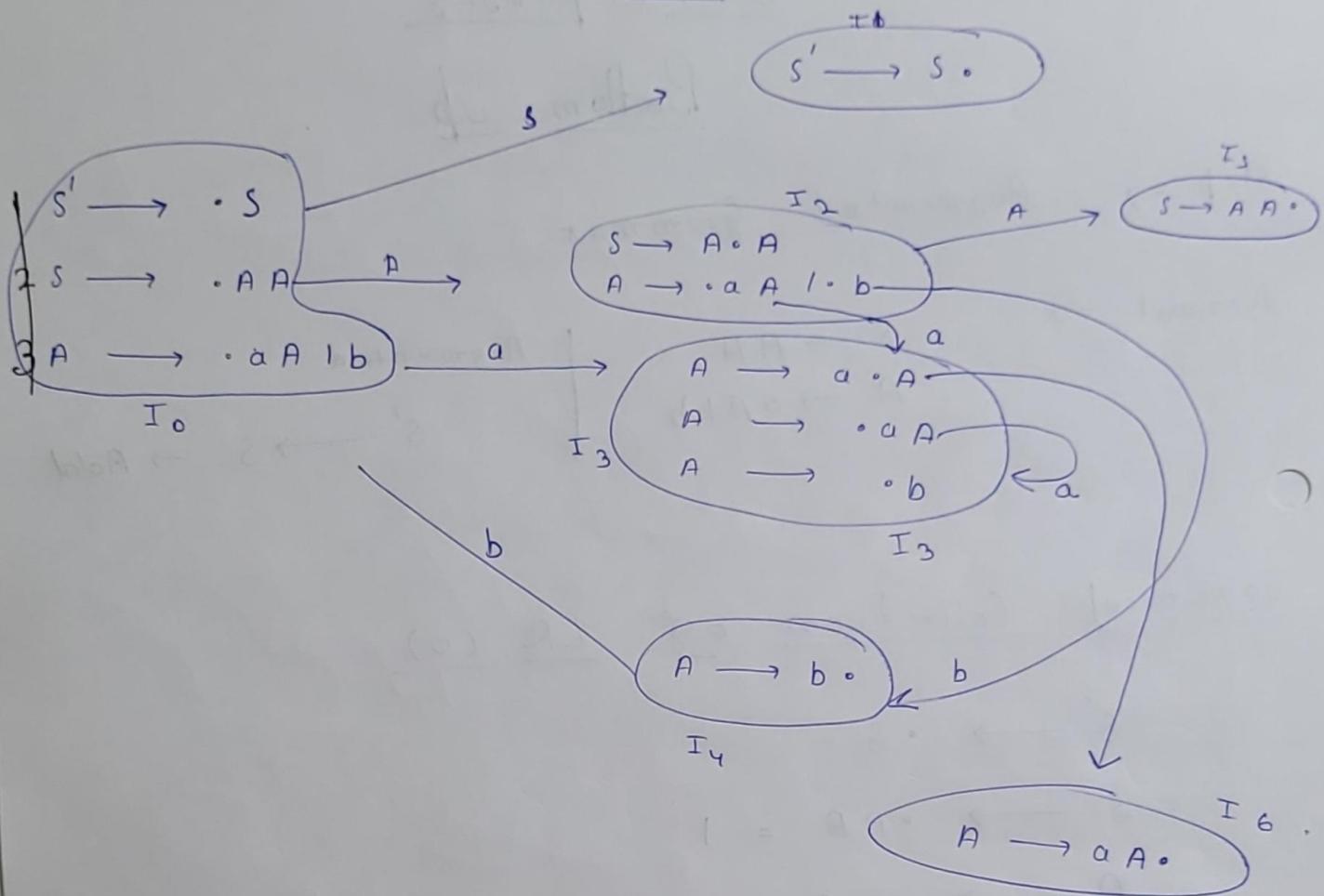
$A \rightarrow \cdot a A = 2$

$A \rightarrow \cdot b = 3$

• ke baad dekhne hai aag e

• • dis bhi Non terminal ke kya hai
uska canonical cover of this Yahan
saari production of uski $\cdot S$

Start



Passing table mein function take ho through

processing To be $S \rightarrow I_1$

Agar vo action mein Rai write $S \rightarrow$
shift

Passing table

Explanation of Closure

- $S \rightarrow S \cdot \text{closure}$ Yooni all production like $\boxed{S \rightarrow \alpha, \beta}$
↳ whatever

- Ko right Karo

$S' \rightarrow S \cdot \rightarrow \text{Nothing.}$

$S \rightarrow A \cdot \underline{A}$? closure of A include

Agoor Koi Some day e

$T_3 \Rightarrow A \rightarrow \cdot \overbrace{a^m A}$

$\boxed{A \rightarrow a \cdot A} \rightarrow$

already Yahi
hai T_3 toh
self loop.

• \rightarrow right mein Jauyegi, Sabke last
meine Schrift Karte Jao,

Parsing Table

State	Action			Goto	
	a	b	\$		
I ₀ S ₃				2	
I ₁			accept		
I ₂ S ₃		S ₄		5	
I ₃ S ₃		S ₄		6	
I ₄ σ ₃		τ ₃	τ ₃		
I ₅ τ ₁		τ ₁			
I ₆ τ ₂		τ ₂	τ ₂		

Agar Augmented production hai to R accepted
under β

Agar koi final item hai to Augmented
nahi hai then we use reduce

I₄ =>
$$\boxed{A \rightarrow b.} \Rightarrow \text{reduce production}$$

in grammar σ₃

Working of LR

Initial State Stack =

S	O	Z	B	D	B	b	A	/	A	b
S	O	A	Z	B	D	b	A	1	8	3

Input String \Rightarrow a a b b

$\boxed{a} \Rightarrow I_0 + a \Rightarrow S_3 \Rightarrow$ push a & 3 (MOVE)

$\boxed{a} \Rightarrow I_2 + a \Rightarrow S_3 \Rightarrow$ push a & 3 (MOVE)

$\boxed{b} \Rightarrow I_3 + b \Rightarrow S_4 \Rightarrow$ push b & 4

$\boxed{b} \Rightarrow I_4 + b \Rightarrow \gamma_3 \Rightarrow$ (NOT MOVE) read

$A \rightarrow \boxed{b}$

length=1 \times 2 \Rightarrow Rotodo Add A

Now 3 A $\rightarrow I_3 A = 6 \rightarrow$ bush

$I_6 b \Rightarrow \gamma_2 \Rightarrow$

$A \rightarrow \boxed{a A}$

$2 \times 2 = 4 \Rightarrow$ Rotodo odd A

$I_3 A \rightarrow \boxed{b} \Rightarrow \boxed{b} \gamma_3$

$6 \rightarrow$ bread \Rightarrow 4 remove

$I_0 A \rightarrow 2 \rightarrow$ bush $\Rightarrow I_2 b \Rightarrow$ bush b & 4

$I_4 \$ \rightarrow \gamma_3$ (continue)

$\boxed{\$ \rightarrow \text{over}}$

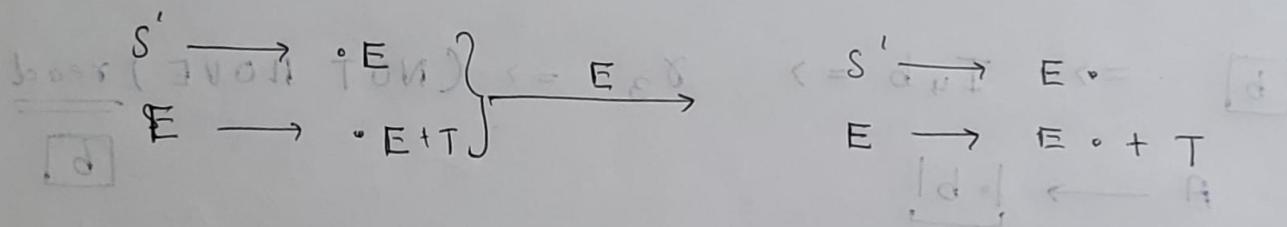
pointing \$

SLP

go homasi production hoti haiisme . end
 mein hota ha A → aA.

isme go remove hai vo sirf follows
 of A mein likhna

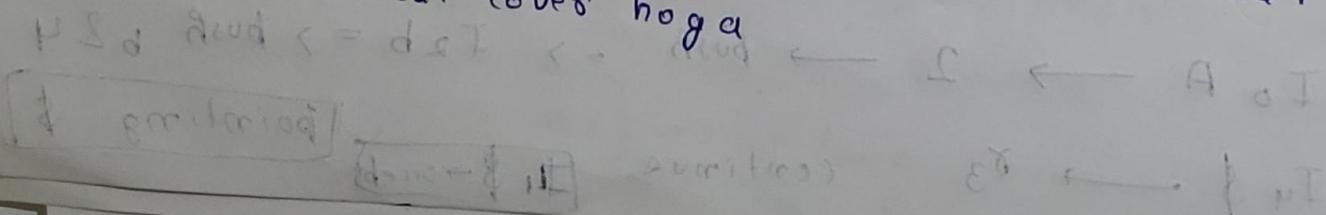
Item Sets banate Samay = has ek set
 se ek Hee arrow mi kalte hai

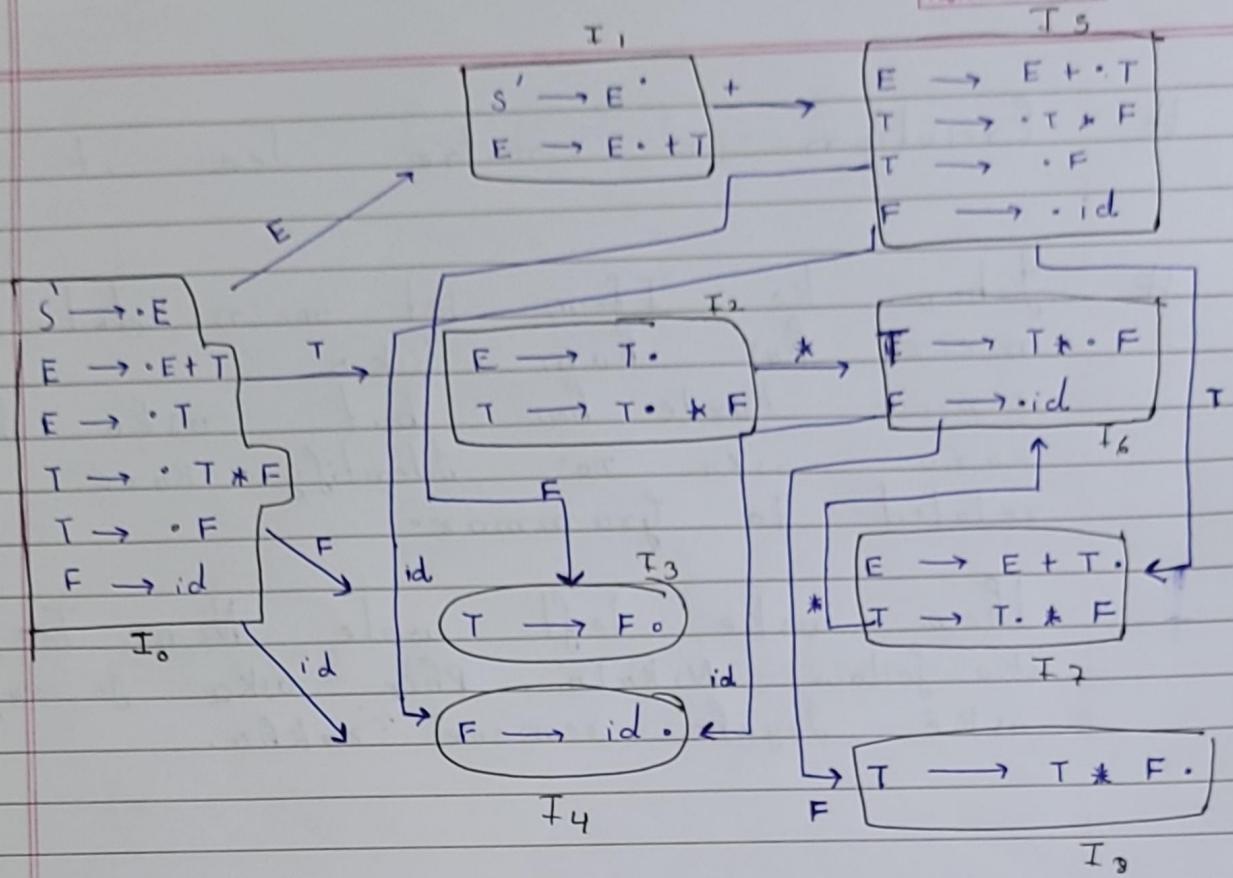


Ab dekho Hum ke baad woale
 symbols → ka Nikalenge closure
 isme . ke baad koi bhi Non Terminal
 Nahin hai.

Toh Yahi hum stop kurdenge.

Has ekvaiker baad woale Non Terminal
 ko Canonical covers hogi





State	Action				goto To
I_0	id	$+$	$*$	$\$$	E
I_1	S^4	$\$$	5	Accept	T
I_2					
I_3	R_2	S_6		R_2	F
I_4	R_5	R_5		R_5	
I_5	S^4				7
I_6	S^4				3
I_7	R_1	S_6		R_1	
I_8	R_3	R_3		R_3	

* Evolution is similar See it

John ke Item set mein dot End
meinai hai hum usko
remove karte hai but usko identify
karo uska no. identify Karo
related to grammar.

Then uske left wale Non-Terminal
ko follow Nikalo Phir uska jo aye
uske jogni remove rakhao.

C LR (parsing)

Ab isne hum kya karenge ki ha ek
item set ke saath jo function
hai wame hoga ek frame symbol
or we can say last ahead.

Compiler Design

Lexical Analyzer

Syntax "

Syntax . - _

,

:

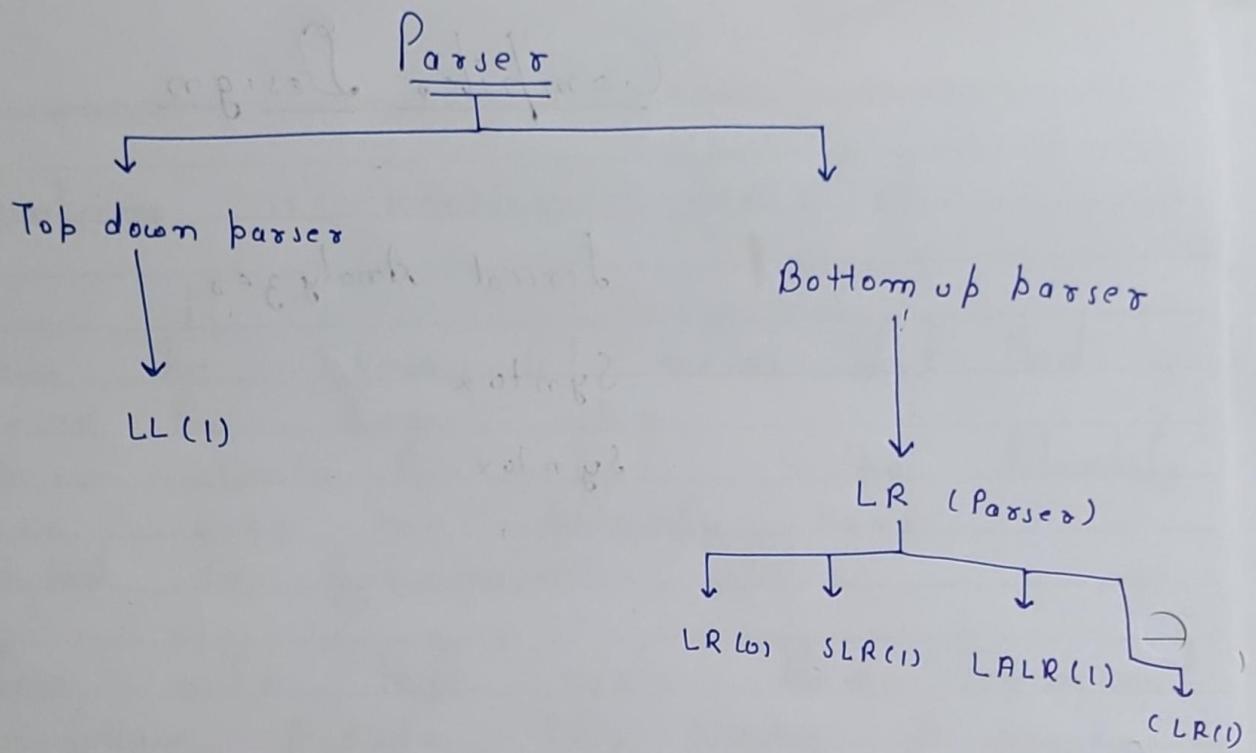
{

}

Lexical Analyzer \Rightarrow Sahi key words ke
according token generate
karte hai.

Syntax

Ab joise Syntax ka matlab hai ki order
of tokens correct hai ya nahi. Uske
liye hota hai. Parser



$LL(1)$ \Rightarrow $L \Rightarrow$ Scanning from Left to Right

$L \Rightarrow$ Left most derivation tree

$1 \Rightarrow$ Look Ahead means How many symbols are you going to see when you want to make a decision

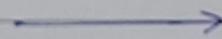
Lexical Analyzer

Lexical Analyzer ka vahi kaam hai tokens mein divide karna

Jo aisa karta hai we can say it is as
Lexer.

Tokens \Rightarrow Identifiers, keywords, operators
separators, constants
({},)^d

Count no of Tokens.



int main () {

 \ast _____ \ast / → Neglect

int a = 20, b = 30 ;

if (a ≤ b) return (b);

else

 return (a);

}

printf (" i = %d , &i = %x ", i, &i);

*

" _____ " => 1 (Inside double
Quotes only 1
taken)

#

Augmented production will contain if

if home likha hai for a production
 toh ussey behli wali production main
 hum dekhte like

$$A \rightarrow \alpha \cdot B \beta$$

$$B \rightarrow \cdot \gamma \rightarrow \underline{\text{Symbol}}$$

B ke baad B hai toh uska first
 include hogu Agar vo Null hai

toh copy, otherwise likho First of B.

Jahan vo symbol hai vahi likho

LALR

Jisme Item ho ki uska predictions
 saari same hai but symbol agar
 different hai toh hum usko
 saath mein kar deke hai

I₆₇ ;

C L R $S \rightarrow AA$ $\text{first of } A = a \mid b$ $A \rightarrow aA$ $A \rightarrow b$ $S' \rightarrow S$ $S \rightarrow AA$ $A \rightarrow aA$ $A \rightarrow b$

Now
 In
 LALR We will see whose production are same but symbol diff we

