



## Department of Mathematics

Date: 6.11.2025	CIE - 1	Max. Marks: 50
Semester: III	Third Semester 2025-2026 Branch: AS, BT, CH, IEM, ME	Duration: 2 Hrs.
Course Title: Statistics, Laplace Transform and Numerical Methods		Course Code: MA231TB

Instructions to candidates: Answer all questions.

Sl. No.	Quiz (Part-A)	M	BT	CO																					
1	The first two moments about the point $x = 2$ are 1 and 16 then find the mean and the second central moment.	2	1	1																					
2	If two regression equations of the variables $x$ and $y$ are $x = 18.13 - 0.86y$ , $y = 11.6 - 0.5x$ , then the mean values of $x$ and $y$ are _____ and _____.	2	1	1																					
3	The following data regarding the heights(y) and the weights(x) of twelve college students are given $\sigma_x = 16.8$ , $\sigma_y = 10.8$ , $\sum(x - \bar{x})(y - \bar{y}) = 2020$ , the regression coefficient of $x$ on $y$ is _____.	2	2	3																					
4	In a bivariate data on $x$ and $y$ , $\text{var}(x) = 49$ , $\text{var}(y) = 9$ and $\text{cov}(x, y) = -17.5$ . Find the coefficient of correlation between $x$ and $y$ .	2	2	2																					
5	Obtain the Laplace transform of the function $f(t) = \cos^2(2t)$ .	2	2	4																					
Test (Part-B)																									
1	<p>The marks obtained by 50 students in a Mathematics test are given below:</p> <table border="1"> <tr> <td>Marks</td> <td>10-20</td> <td>20-30</td> <td>30-40</td> <td>40-50</td> <td>50-60</td> <td>60-70</td> </tr> <tr> <td>No. of students</td> <td>4</td> <td>8</td> <td>10</td> <td>15</td> <td>8</td> <td>5</td> </tr> </table> <p>Compute first four moments about the mean and also find the measures <math>\beta_1</math> and <math>\beta_2</math> for the following distribution and comment on the nature of the distribution of students.</p>	Marks	10-20	20-30	30-40	40-50	50-60	60-70	No. of students	4	8	10	15	8	5	10	2	1							
Marks	10-20	20-30	30-40	40-50	50-60	60-70																			
No. of students	4	8	10	15	8	5																			
2	<p>Fit a multiple linear regression plane to the following data and predict wear(<math>y</math>) when oil viscosity is (<math>x_1</math>) is 30 and load (<math>x_2</math>) is 1400.</p> <table border="1"> <tr> <td>Wear(<math>y</math>)</td> <td>193</td> <td>230</td> <td>172</td> <td>91</td> <td>113</td> <td>125</td> </tr> <tr> <td>Oil viscosity (<math>x_1</math>)</td> <td>1.6</td> <td>15.5</td> <td>22.0</td> <td>43.0</td> <td>33.0</td> <td>40.0</td> </tr> <tr> <td>Load(<math>x_2</math>)</td> <td>851</td> <td>816</td> <td>1058</td> <td>1201</td> <td>1357</td> <td>1115</td> </tr> </table>	Wear( $y$ )	193	230	172	91	113	125	Oil viscosity ( $x_1$ )	1.6	15.5	22.0	43.0	33.0	40.0	Load( $x_2$ )	851	816	1058	1201	1357	1115	10	3	2
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Oil viscosity ( $x_1$ )	1.6	15.5	22.0	43.0	33.0	40.0																			
Load( $x_2$ )	851	816	1058	1201	1357	1115																			
3a	<p>Find the rank correlation coefficient for a group of 6 persons between their examination marks and IQ's (intelligent quotients)</p> <table border="1"> <tr> <td>Exam Marks</td> <td>70</td> <td>60</td> <td>80</td> <td>90</td> <td>10</td> <td>20</td> </tr> <tr> <td>I.Q</td> <td>110</td> <td>100</td> <td>140</td> <td>120</td> <td>80</td> <td>90</td> </tr> </table>	Exam Marks	70	60	80	90	10	20	I.Q	110	100	140	120	80	90	6	2	3							
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I.Q	110	100	140	120	80	90																			



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3b	In a partially destroyed record, only the following results are available. Regression equations are $8x - 11y = 66$ , $40x - 18y = 214$ , variance of $x$ is 9 find the correlation between $x$ and $y$ and the standard deviation of $y$ .	4	3	4																
4	The following data represents carbon dioxide emission from coal-fluid boilers (in units of tons) over a period of years 1965 to 1977. Standardizing the year variable( $x$ ), the following table is obtained:  <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="padding: 2px;">Year(x)</td><td style="padding: 2px; text-align: center;">0</td><td style="padding: 2px; text-align: center;">5</td><td style="padding: 2px; text-align: center;">8</td><td style="padding: 2px; text-align: center;">9</td><td style="padding: 2px; text-align: center;">10</td><td style="padding: 2px; text-align: center;">11</td><td style="padding: 2px; text-align: center;">12</td></tr> <tr> <td style="padding: 2px;"><math>CO_2</math> emission(y)</td><td style="padding: 2px; text-align: center;">910</td><td style="padding: 2px; text-align: center;">680</td><td style="padding: 2px; text-align: center;">520</td><td style="padding: 2px; text-align: center;">450</td><td style="padding: 2px; text-align: center;">370</td><td style="padding: 2px; text-align: center;">350</td><td style="padding: 2px; text-align: center;">340</td></tr> </table> Find the regression model of $y$ on $x$ and $x$ on $y$ and correlation coefficient.	Year(x)	0	5	8	9	10	11	12	$CO_2$ emission(y)	910	680	520	450	370	350	340	10	3	3
Year(x)	0	5	8	9	10	11	12													
$CO_2$ emission(y)	910	680	520	450	370	350	340													
5	Determine the transformation in frequency domain, if the function in time domain is given by $f(t) = \frac{(\sqrt{t}-1)^2}{\sqrt{t}} + \sin(2t)\cos(3t) + e^{-t}\cosh^2(3t)$	10	1	2																

BT-Blooms Taxonomy, CO-Course Outcomes, M-Marks

Marks Distributions	Particulars	CO1	CO2	CO3	CO4	L1	L2	L3	L4	L5	L6
		Max Marks	14	22	18	6	14	22	24	--	--

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