HOMEWORK 4

* Problem 1: Sweeping process in one dimension along one angle using diamond diff scheme:

und wn (x) + (x) + (x) yn (x) = 9 m (x)

Integrate over Xi-2 and Xi+2:

μη (χιοξ) - ψη (χι-ξ) +σι Δί γη (χι) = Δί qη (χί)

where: Di = Xi+2 - Xi-2

\$ \\ \times = \(\text{\psi}_n \) (xi)

Half in leger meshpoints. all Centrud points are: ×i = = [xi++ + xi-+]

Define: (x) = (i ; xi-1 < x < xi+1

un [Yi+z,n-Yi-z,n]+oi Di Yin = Diqin

.. Diamond difference scheme has $\alpha = 0$, whereas step difference sets have $\alpha = \pm 1$. 4 in = 1 [4 i+1, n - 4 i-1, n]

a) for 120: Eliminate 41+2, n

Vi-2 => Incoming flux ; Wi+2 => Outgoing flux

Vin : (1+ Ti Ai) [Vi-1, n + Digin 2 lun]

b) for m<0:

46+2 => Incoming flux; Vi-2 => Outgoing flux

Eliminate 4:- 12, m

4in = (1+02 Di) [41+2m+ Diquin]

4:- 2, n = 2 min - 442, in

c) Reflecting boundary on right edge, how to transition from \$170 to \$160:

: Boundary values determine the relationship. We stort there and sweep until reflecting boundary.

Initial Condition: 4I+2, N+1-n = 4I+2, n

d) What data to store in sweeping process?

When using angulor flux to generate flux moments during solution process, we need to store flux moments from one iteration to next.

* Peroblem 2: Ma dya + Et Yak) = 0 => Ma dya = - Et Yak) a) Ma >0; Expression for flex at some location x' in terms of x: The difa = Et dx $\int_{x}^{x} \frac{1}{y_{a}} dy_{a} = \int_{x}^{x'} \frac{-\xi_{b}}{\lambda} dx \implies \ln y_{a}(x') - \ln y_{a}(x) = -\frac{\xi_{b}}{\lambda} (x' - x)$ Ψ. (x') = Ψ. (x) cup [- ΣΕ (x'-x)] b) Expression for 40,i+1 in terms of 40, i-1? Di=Xi+1 - Xi-1 and h= Et Di Zinal Va, i+ = Wa, i- = exp [- Et Di] Yai+ = 40, i- 2 exp [-2h] c) $\forall a, i+\frac{1}{2}$ in terms of $\forall a, i-\frac{1}{2}$ and h? From notes and $\alpha = 0$, we get these two equations: Yijk = = [Ya,i+ + Ya,i-= Li [Ya,i+ 2 - Ya,i-2] + Zijk Yijk =0 1 (Yaji+ 2 - Ya, i-2) = - Eijk (Ya, i+2 + Ya, i-2) 1 40, i+ = + = Eijk Wa, i+ = = 1 40, i- = - = Eijk Wa, i- = 40,1+2 [1 + 1 2 Eijk] = 40,1-2 [1 - 1 Eijk] Ψα, i+ ½ [1+ Σι Δί = Ψα, i- ½ [1 - ξι Δί] Wa, it = 1-h Wa, i- =

d) Accuracy of the rulationship:

Part b cap through power series: 40,1+2=40,1-2 e-2h
= (+(-2h) + (-2h)^2 = (-2h + 2h^2 +

Part c through power series: $\forall a, i+1 = \forall a, i-1 = \begin{pmatrix} 1-h \\ 1+h \end{pmatrix}$ $= 1-2h+2h^2+\dots$

Some through the second order term meaning there relationship is

C) To avoid negative flux h < 1 meaning $\frac{\sum_{i} \Delta i}{2 \mu i} < 1 \Rightarrow \Delta i < \frac{2 \mu i}{\sum_{i} Et}$ is required.

When \sum_{i} is large and μ_{α} is small, much spacing can be come problematic and result in negative flux. More SN order in vecoses more much Size should decrease.

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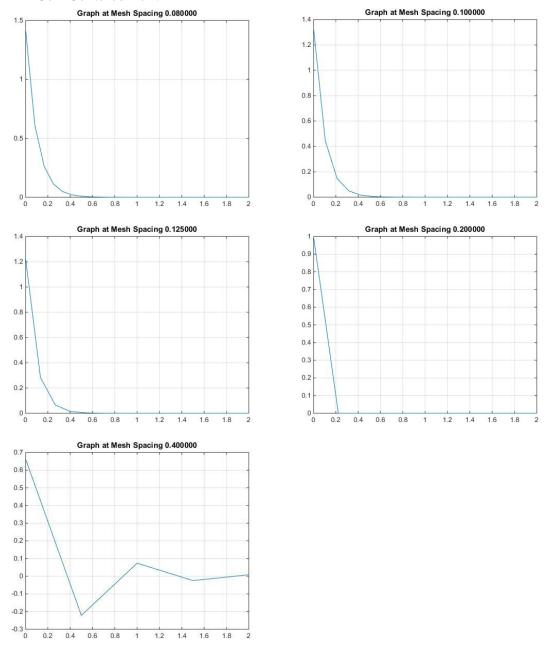
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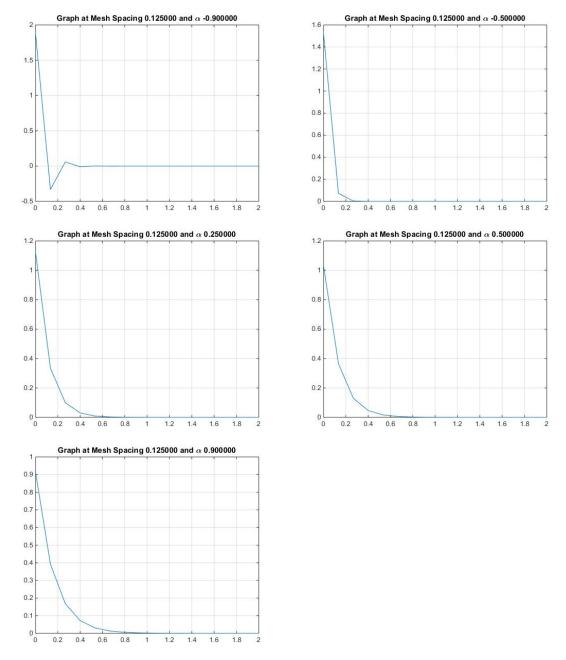
Problem 3:

a) Cell-Centered flux:



In this case, $\alpha=0$ for all graphs. When $\Delta_i=0.4$ we observe negative flux. This is the case as requirement stated in problem 2; mesh spacing $(\Delta_i)<2\mu/\Sigma_t$ doesn't hold true (0.4<0.2).

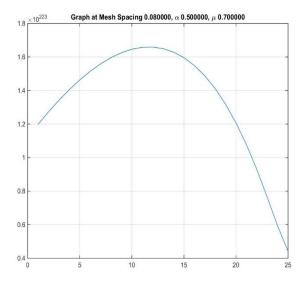
b) Impact of α when $\alpha = [-0.9, -0.5, 0.25, 0.5, 0.9]. Let's look at different <math>\alpha$'s at $\Delta_i = 0.125$. Graphs at other Δ_i are present in the folder.

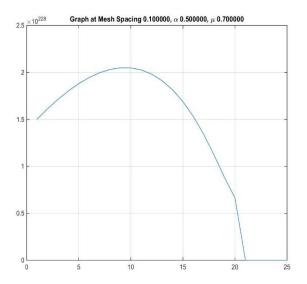


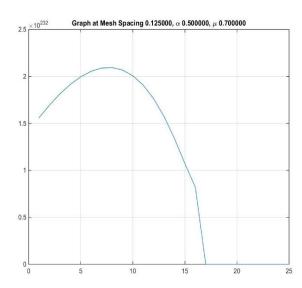
When α term is introduced, the requirement stated in problem 2 is changed by factor of $1+\alpha$ in this case because of going x=0 to x=2. $\Delta_i*(1+\alpha)<2\mu/\Sigma_t$ should hold true to prevent negative flux.

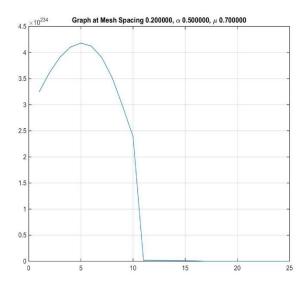
c) Adding source:

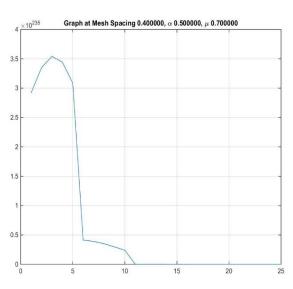
Graphs at $\mu = 0.7$, $\alpha = 0.5$, and for all mesh spaces here. Other graphs are in the folder.











d)
$$\alpha = 0, \Sigma_s = 0.9$$

d) $\alpha=0,\,\Sigma_s=0.9;$ As we increases $\Sigma_s,$ the scalar flux increases.

* Problem 4:

Newhors only downs catter from fact group (land 2) to thurnol group (3, 4,5). Assume thurnol groups can upscatter in other thurnol groups and can downs catter. Assume there is an External source and firsion source.

(3)
$$\frac{\mu_{a}}{h_{i}} \left(\psi_{a,i-\frac{1}{2}}^{3} - \psi_{a,i-\frac{1}{2}}^{3} \right) + \sum_{i,i} \psi_{a,i}^{3} = 2\pi \sum_{a=1}^{\infty} \omega_{a} \sum_{g'=1}^{\infty} \sum_{h,i} \psi_{a,i}^{g'} + \frac{\chi_{a}}{2} \sum_{g'=1}^{2} \psi_{a}^{2} \sum_{h,i}^{2} \psi_{a,i}^{3} + \frac{1}{2} Q^{3}_{i}$$

$$\frac{\mu_{a}}{h_{i}} \left(\psi_{a,i-\frac{1}{2}}^{3} - \psi_{a,i-\frac{1}{2}}^{3} \right) + \sum_{t,i} \psi_{a,i}^{3} = 2\pi \sum_{a=1}^{\infty} \omega_{a} \sum_{g'=1}^{2} \sum_{h,i} \psi_{a,i}^{3} + \frac{1}{2} Q^{3}_{i}$$

$$\frac{4}{h_{i}}\left(\frac{\gamma^{4}}{\gamma^{4}} - \frac{\gamma^{4}}{\gamma^{4}}\right) + \sum_{i,i} \psi^{4}_{a,i} = 2\pi \sum_{a,i} w_{a} \sum_{i,j} \frac{\gamma^{4}}{\gamma^{4}} + \frac{\chi_{4}}{2} \sum_{a',i} \psi_{a',i} + \frac{\chi_{4}}{2} \sum_{a',i} \psi_{a'}^{a'} + \frac{1}{2} Q^{4}_{i}$$

$$\frac{Ma}{h_{i}}\left(\frac{\gamma^{4}}{\gamma^{4}} - \frac{\gamma^{4}}{\gamma^{4}} - \frac{\gamma^{4}}{\gamma^{4}}\right) + \sum_{i,i} \psi^{4}_{a,i} = 2\pi \sum_{a',i} \psi^{4}_{a',i} + \frac{\chi_{4}}{2} \sum_{a',i} \psi^{4}_{a',i} + \frac{1}{2} Q^{4}_{i}$$

$$\frac{Ma}{h_{i}}\left(\frac{\gamma^{4}}{\gamma^{4}} - \frac{\gamma^{4}}{\gamma^{4}} - \frac{\gamma^{4}}{\gamma^{4}}\right) + \sum_{i,i} \psi^{4}_{a',i} = 2\pi \sum_{a',i} \psi^{4}_{a',i} + \frac{1}{2} Q^{4}_{i}$$