Configurable Network Simulation for TCP Reno and FAST Flows

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1 Overview

The goal of this project was to produce a program that could simulate arbitrary network configurations of flows, routers, and hosts. To this end, we have produced an event-driven simulation in Python 2.7.10 that is able to simulate flows running TCP Reno and TCP FAST as their congestion control algorithms. We have also applied an object-oriented design for our network components (e.g. Routers, Hosts, Links, etc).

In this section, we present an overview of this system, including our statistics collection. In Section 2, we discuss the network components in detail. Section 3 covers three test cases (Test Cases 0-2). And finally, an analytic check on Test Case 2's FAST performance is included to quantitatively validate our results.

1.1 Events

In the context of this simulation, Events are instantaneous occurrences that happen at a specific moment in time (relative to some global clock). Since these occurrences cover a wide range of functionality, from initiating a routing table update to handling a packet receipt, we have defined a general interface for Events with two functions:

- run() Carries out the main actions of an Event and updates statistics.
- schedule_new_events() Adds follow-up Events and updates statistics if necessary.

Events themselves are run as part of an event loop. The event loop represents a priority queue of Events, where priority is based on the execution time of the Event. The execution of this loop simply involves getting the earliest Event, calling run() and schedule_new_events() in turn, and then repeating this until all FlowCompleteEvents are received. In order to facilitate event scheduling, our MainEventLoop class has a schedule_event_with_delay() function.

1.2 Statistics

Our simulator includes a Statistics class, which holds fields that map network components (specifically, Links, Hosts, and Flows) to various collected statistics about them. Specifically, the following statistics are recorded:

• For Links:

 A list of (timestamp, buffer occupancy) tuples that marks changes in buffer occupancy over time. Note that <u>only</u> DataPackets are included in the buffer occupancy statistic, in order to make the Test Case 2 analytic comparison easier (see Subsection 3.4).

- A list of timestamps corresponding to packet losses (due to buffer overflow).
- A list of (timestamp, packet size) tuples that describe each packet transmitted.

• For Hosts:

- A list of (timestamp, packet size) tuples that describe each packet sent.
- Same as the previous field, but for each packet received at the host.

• For Flows:

- A list of (timestamp, packet size) tuples that describes each packet sent.
- Same as the previous field, but for each (ACK) packet received for that flow.
- A list of (timestamp, round-trip time (RTT)) tuples for various packets received.
- A list of (timestamp, window size) tuples describing changes in window size at specific times.

Link statistics are used to plot time traces of the buffer occupancy, packet losses (using time interval windows), and transmission rate (also using time interval windows). Host statistics are used to plot both the send and receive rates of a host as a function of time (using windowing). Flow statistics are used to plot time traces of flow send and receive rates (with windowing), data packet RTTs, and flow window sizes. All of this statistical processing is described in our plot_tool module, which outputs both time traces (using matplotlib) as well as simulation-long averages of the aforementioned statistics.

1.3 Network Topology JSON

NetworkTopology is a wrapper class that holds a list of Links, Hosts, Routers, and Flows. This class is used to conveniently convert network topologies into JSON, using the jsonpickle package. It is important to make sure that a NetworkTopology object's data fields do not hold references to other components since jsonpickle doesn't properly handle saving references (e.g. Routers do not store their connected links as a reference in the original NetworkTopology JSON). All of the necessary component reference connection happens in the NetworkTopology class's complete_initialization() function.

1.4 Overall Program Flow

The overall flow of this simulator is described in Figure 1. The initializer script sets up initial Events, including Flow initiation and routing table updates, which are then passed into the main event loop.

This network simulator uses the initializer script as its entry point. One example usage of this script is as follows:

• Example usage (from root directory of project): python2 initializer.py -v INFO -f log/log.txt data/test_case_0.json -1 LO L1

In this case, the above script call will take data/test_case_0.json as the input NetworkTopology. The log level will be set to "INFO", with the file log/log.txt used as the log file (although stdout may also be used). Lastly, the final optional arguments ("-1 L0 L1") specify desired Links' statistics to be plotted.

2 Network Components

Network components are placed in separate Python modules. Each network component's module (e.g. link.py for Links) contains a class definition for that component, as well as subclasses (e.g. FlowFast is a TCP FAST implementation of Flows) and Events related to that component. The functions defined for each network component are supposed to run "instantaneously" in simulation time.

The following network components are included in this simulation. Each of these is described in more detail in the following subsections.

- Device (an abstract class that simply features an address field).
 - Subclasses: Host and Router
- Link, LinkBuffer, LinkBufferElement
- Packet (abstract class)
 - Subclasses: DataPacket, AckPacket, and RouterPacket
- Flow (abstract class)
 - Subclasses: FlowReno and FlowFast

2.1 Packet

Packets are units of information in the network. They are generated by a Flow; all Packets in the same Flow go back and forth between the same two Hosts. There are three kinds of Packets: DataPackets, AckPackets, and RouterPackets.

2.1.1 Fields

Packet fields include:

- packet_id The id of the Packet.
- flow_id The flow that the Packet is a part of.
- source_id, dest_id The source and destination of the Packet.
- start_time_sec The time when the Packet was sent (from the Host it originated at).
- size_bits The size in bits of the Packet.

2.1.2 Subclasses

Packets have three subclasses:

- DataPacket An 8192-bit Packet used to transfer data between Hosts. This subclass has no additional fields of interest.
- AckPacket A 512-bit Packet used to send ACKs between hosts. This subclass has three additional fields of interest:
 - data_packet_start_time_sec
 The start time
 of the original DataPacket that triggered this ACK.
 - flow_packets_received An ascending sorted list of all of the Packet IDs received by the destination Host for the given Flow. This is used to implement selective repeat on the Flow's side.
 - loss_occurred A boolean that is (later) set to
 True if flow_packets_received has a gap in its list of Packet IDs.
- RouterPacket A 512-bit Packet used to send routing tables between neighboring Routers. This has one field of interest:
 - router_to_host_dists A map from (Router, Host) pairs to the minimum distance (time-wise) between that Router and Host. This map represents a Router's "current" knowledge on the min cost to all known Hosts (accumulated since its last update began).

2.2 Host

Hosts are endpoints of the network. They have network addresses that are distinct from other Device addresses. Each Host keeps track of the Flows that originate from it and the Packets that those Flows receive. A HostReceivedPacketEvent is triggered when a Packet is received. If the Packet is a DataPacket, the list of Packets received by that Host for the given Flow is updated. If the Packet is an AckPacket, a FlowReceivedAckEvent is generated, and the Flow itself handles the receipt. RouterPackets are never received by Hosts.

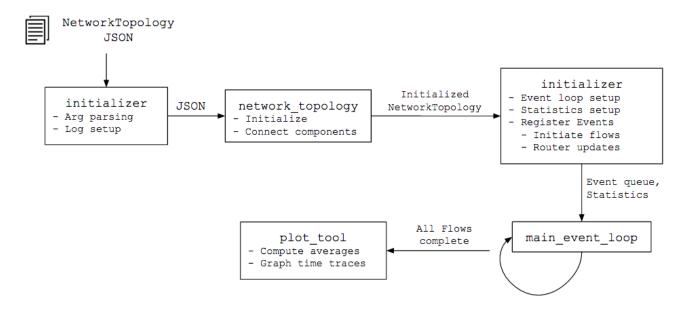


Figure 1: A flow chart describing the flow of control in this network simulator. Titles for each box represent file names, while bullet points describe functionality. The entry point for this simulator is the initializer script, which takes a NetworkTopology JSON file (and optional arguments). After the topology is set up and connected together, initial Events are set up and passed into the MainEventLoop. Once all Flows finish running, the loop exits and statistics are outputted.

2.2.1 Fields

Some of the fields of a Host are:

- flows The Flows originating from this Host.
- flow_packets_received A map from the flow_id to a sorted list of packet_ids that have been received for that Flow.
- link The Link connected to the host.

2.2.2 Events

Host has the following Events:

- HostReceivedPacketEvent Represents a Host receiving a Packet. The behavior of this Event depends on the kind of Packet received:
 - If the Packet received is a DataPacket, then the run() function puts the Packet's ID into flow_packets_received via binary search (to maintain sorted order) and updates statistics. The schedule_new_events() function then generates an AckPacket to send back to the DataPacket's original Host.
 - If the Packet received is an AckPacket, then the run() function just updates statistics, and the schedule_new_events() function simply generates a FlowReceivedAckEvent.

2.3 Link

Links connect Devices together and carry Packets along this connection. In this simulation, every Link is half-duplex (only one direction may be traveled at a time) and has a specified capacity. As such, there is only one buffer per Link, and Packets in this buffer may be going towards either end of the Link.

2.3.1 Fields

Link fields include but are not limited to:

- end_1_device, end_2_device These record the end-points of the Link. A get_other_end(Device) function is provided so one Device can ask a connected Link what Device is on the other end.
- static_delay_sec The propagation delay (in seconds). This represents one component of the queuing-independent link delay (the other being the transmission delay).
- capacity_bps The Link's capacity in bits per second.
 This allows us to compute the transmission delay for a given Packet size.
- LinkBuffer A class containing the following fields:
 - max_buffer_size_bits The maximum buffer size in bits.
 - queue A FIFO queue of LinkBufferElements,
 which represents a Link's buffer. These elements,
 in turn, contain the following fields:

- * packet The Packet being sent.
- * dest_dev The end of the Link that the Packet is going towards. Must be one of {end_1_device, end_2_device}.
- entry_time The time at which the Packet entered the buffer.
- queuing_delays A deque of up to 30 queuing delays of packets that exited less than 1 second ago, which is used to compute an average queuing delay.

2.3.2 Functions

Some of the functions in the Link class are:

- get_link_cost() Computes the Link's cost (in seconds) as a sum of propagation delay (static_time_delay) and average queuing delay (computed using the aforementioned deque of queuing delays). The transmission delay is ignored.
- push() Pushes a Packet onto the LinkBuffer. This Packet will later be sent to one end of the Link via LinkSendEvents. RouterPackets are always pushed onto the buffer even if it forces the LinkBuffer's maximum size to be exceeded. In other words, for the purposes of this simulation, the possibility of dropped RouterPackets was not considered, as this would greatly disrupt Bellman-Ford. On the other hand, DataPackets and AckPackets are dropped if the LinkBuffer's maximum size is exceeded.

The LinkBuffer class also has a pop() function that pops off the top LinkBufferElement and updates metadata (including the queuing_delays deque).

2.3.3 Events

Links have the following Events governing their logic:

- DeviceToLinkEvent Represents a Packet arriving at this Link. When this Event runs, it pushes the Packet and, if the Link is not busy, it immediately schedules a LinkSendEvent. Otherwise, it lets the preexisting LinkCheckStatusEvent (which is already in the event loop's priority queue) automatically schedule the next LinkSendEvent.
- LinkSendEvent Represents a Packet leaving the LinkBuffer and heading to the next Device on its route. This Event schedules a HostReceivedPacketEvent or a RouterReceivedPacketEvent for a time get_link_cost() seconds in the future. It also schedules a CheckLinkStatusEvent a single transmission delay in the future (which represents the time needed before the next Packet can be transmitted). Finally, this Event sets the Link's status to busy.

 CheckLinkStatusEvent — Checks whether the Link's buffer is empty and, if so, sets the Link's status as nonbusy and does nothing. Otherwise, a LinkSendEvent is immediately scheduled. Note that this LinkSendEvent is delayed from the previous LinkSendEvent by a transmission time, as expected.

2.4 Router

Routers route packets through the network and sit between Devices. They have distinct network addresses (from other Devices), can have an arbitrary number of links connected, and are assumed to route Packets instantaneously.

In our simulation, Routers periodically initiate routing table updates, and use the Bellman-Ford algorithm to compute the next-hop Link to get to a given Host. These updates begin with the Router updating its costs to direct neighbors, and broadcasting those costs to all of its neighboring Routers via RouterPackets. As each neighboring Router receives RouterPackets, they account for their neighbors' data and recompute their own routing tables via Bellman-Ford. If their own cost estimates (i.e. time to go from that Router to any Host) changed, those Routers simply rebroadcast their routing tables, with the new information included. For the topologies tested, this procedure eventually leads to convergence.

2.4.1 Fields

Some noteworthy fields for Routers are:

- links List of Links connected to Router
- neighbors List of directly-connected Devices.
- stable_routing_table A stable version of the routing table, which maps (destination) Host addresses to a next-hop Link.
- new_routing_table An (initially) unstable version of the routing table, which is used to build up a new routing table after an update is initiated. This table can only be used if 0.15s have passed since the routing table update initiation, or if the stable routing table doesn't contain a given Host.
- last_table_update_timestamp The global time (in seconds) when the last routing table update began.
- self_to_neighb_dists The known (time) costs to go from this Router to a neighbor. This includes queuing delays (from when they were last measured, at the beginning of an update).
- neighb_to_host_dists The minimum cost (in seconds) to go from a neighboring Router to a given Host.
 This is what gets communicated via RouterPackets.
- self_to_host_dists The minimum cost (in seconds) to go from this Router to a given Host, as estimated via Bellman-Ford and message-passing.

2.4.2 Functions

A few significant functions in the Router class are:

- get_link_to_host_id() Finds the next-hop Link to get to a given Host address, based on the routing table. This uses the new routing table if 0.15s passed since the last update, or if the Host of interest is not in the stable table.
- update_routing_table() Uses received information on a neighboring Router's estimated costs to various Hosts, in order to update this Router's self → Host costs (via Bellman-Ford) and routing table. This function is called when a RouterPacket is received, or when a routing table update is initiated; in the latter case, the Router's self → neighbor costs are updated to account for the latest queuing delays.
- broadcast_router_packets() Sends RouterPackets to all neighboring Routers.

2.4.3 Events

Some Router-related Events (which are defined in router.py) are:

- InitiateRoutingTableUpdateEvent Initiates a routing table update, and then schedules another similar Event 5s later. These are one of the first Events to be scheduled in the initializer script.
- RouterReceivedPacketEvent Represents a Router receiving a Packet. The behavior of this Event depends on the kind of Packet received:
 - If the Packet received is a DataPacket or an AckPacket, then this Event looks up the next-hop Link (from the routing table) and routes the Packet onto that Link (via a DeviceToLinkEvent).
 - If the Packet received is a RouterPacket, then this
 Event updates this Router's routing table based on
 the information in the RouterPacket. Additional
 RouterPackets are rebroadcasted if the (receiving)
 Router's self → Host minimum (time) cost estimates changed.

2.5 Flow

Flows represent an active connection between a source and destination Host in the network. Their main purpose generate Packets at a rate controlled by the TCP congestion control algorithm for that Flow. They send Packets until they've filled a certain window size (e.g. 8 packets), and adjust this window size in response to losses, successes, or other metrics. If the window size has already been exceeded (which can happen if the window size suddenly dropped in response to a loss), then Flows cannot transmit any new Packets.

Flows are also responsible for retransmitting lost Packets based on (repeated) ACK gaps (i.e. Packet ID gaps in AckPacket data) or timeout. Retransmissions do not increase the number of Packets in transit, and are always immediately allowed even if the window size has (temporarily) been exceeded.

In this simulation, Flow is just an abstract class; there are specific subclasses for TCP Reno (FlowReno) and TCP FAST (FlowFast) implementations.

2.5.1 Common Fields and Functions

The following are some of the fields common to all Flows:

- flow_id The unique ID representing this Flow.
- source, dest The source and destination Hosts for this Flow.
- data_size_bits The size (in bits) of the data being sent.
- start_time_sec The start time of the flow (in seconds), relative to the main event loop's global clock.
- window_size_packets The current window size (in Packets).
- packets_in_transit A set of Packet IDs that are either currently in transit, or scheduled to (soon) be in transit.
- gap_retrans_packets A set of DataPacket IDs that have been retransmitted due to (possibly multiple) gaps in an AckPacket's selective repeat data. This is used to make sure retransmissions due to selective repeat gaps are not repeated (but retransmissions due to timeouts can be repeated).
- num_timeouts_pending A map from Packet ID to the number of timeouts pending for that Packet (can be > 1 due to retransmission). This is used to make sure only the latest timeout scheduled for a given DataPacket is handled.

And these are the abstract functions common to all Flows:

- handle_packet_success() Responds to a successful round trip (i.e. the receipt of an AckPacket). This function also updates metadata (e.g. RTTs), statistics, and window sizes as necessary.
- handle_packet_loss() Responds to a timeout or a single AckPacket indicating a gap. This function updates metadata, statistics, and window sizes as necessary.
 DataPackets are also retransmitted if needed. Note that losses are handled after successes when an AckPacket is received, so the loss handler has the final say on window sizes, etc.

2.5.2 FlowReno

This class is an implementation of TCP Reno, based largely on [1]. There are three states that a FlowReno can be in at a given time: slow start (SS; usually only in the beginning or after timeouts), congestion avoidance, and fast retransmit / fast recovery (FR/FR). The criteria and behavior for entering or leaving FR/FR are described in [2]; the only difference is that this implementation looks for three AckPacket gaps for the same Packet ID (selective repeat), not three "duplicate ACKs."

The ACK success handler simply updates the window size and state based on the current state (see [1] for more details). The loss handler handles two types of losses separately:

- Three separate AckPackets indicating a gap (i.e. a break in the list of Packet IDs received by a destination Host) for the same Packet ID. In this case, the DataPacket is retransmitted and the Flow enters FR/FR.
- Timeouts (0.5s after transmission). In this case, the DataPacket is retransmitted, and the Flow enters SS and updates its SS threshold.

2.5.3 FlowFast

This class is an implementation of TCP FAST, based on both [1] and [3]. Unlike Reno, FAST only makes updates to window size periodically – with a 0.05s period in this simulation. These updates compare the recent RTTs to the smallest-ever RTT (base_rtt), and lower the window size proportionally when the current RTT is too large. Because the FAST formula [3] makes these proportionate window size changes, it is able to achieve stable window sizes more easily than Reno, without overshooting link capacities. Reno, on the other hand, exhibits sawtooth patterns in window size time traces, constantly going back and forth between CA and FR/FR or SS as the network capacity gets exceeded.

In computing the "recent" RTT for FAST, we average the RTTs of the last 40 AckPackets that were received by the Flow. In addition, for our window size formula, we use parameters of $\gamma=0.5$, and either $\alpha=50$ (for Test Cases 0 and 2) or $\alpha=30$ (for Test Case 1). The window size updates happen in the handle_periodic_interrupt() function.

The success and loss handlers for FAST are relatively simple. On success, the base_rtt field is updated, in addition to basic metadata and stats. After a loss, which can either be a timeout or a single ACK gap (not 3 like Reno), the DataPacket is retransmitted. The only caveat is that Packets are not retransmitted after a single ACK gap if they were already retransmitted for that reason (to avoid multiple retransmissions).

2.5.4 Events

The following Flow Events are included in this simulation:

- InitiateFlowEvent Kicks off a Flow by sending the first full window of Packets. These Events are scheduled in the initializer script.
- FlowReceivedAckEvent Called when a Flow receives an AckPacket. This Event calls the success/loss handlers appropriately (e.g. a loss occurs when the AckPacket indicates a gap), and then sends Packets to make sure the new window size is filled.
- PeriodicFlowInterrupt Periodically (with a period of 0.05s) calls handle_periodic_interrupt() on a FlowFast, fills up a window of Packets, and then schedules another periodic interrupt.
- FlowSendPacketsEvent Sends multiple Packets to the Host's connected Link, and schedules timeouts for them (in 0.5s).
- FlowTimeoutPacketEvent Responds to timeouts by calling the loss handler, unless the Packet was already received or there is a later timeout pending (due to the Packet being retransmitted).
- FlowCompleteEvent Called when a Flow finishes sending data. This event does nothing, but notifies the main event loop about the completion.

3 Test Cases

The following three test cases demonstrate the performance of TCP FAST and TCP Reno under various topologies and Flow specifications. Note that only time traces are included, although the simulator is capable of outputting averages as well. In addition, only Link and Flow-specific data is plotted; Host-specific plots have been excluded for space reasons, as have plots of Flow receive rates (which are usually time-delayed versions of the send rate plots, decreased by a factor of 16 due to AckPacket and DataPacket size differences).

3.1 Test Case 0

Test case 0 is a very simple setup. It comprises a single Flow going over a single Link between two Hosts. The setup is provided in Figure 2, and the specs are in Figure 3.

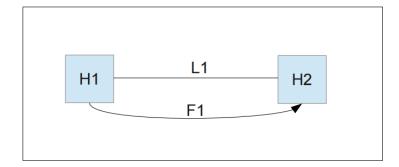


Figure 2: Setup for Test Case 0.

Link Specifications

Link ID	Link Rate (Mbps)	Link Delay (ms)	Link Buffer (KB)
L1	10	10	64

Flow Specifications

Flow ID	Flow Src	Flow Dest	Data Amt (MB)	Flow Start (s)
F1	H1	H2	20	1.0

Figure 3: Specs for Test Case 0.

The results of running this test case with FAST and Reno are provided in Figure 4 and Figure 5 respectively. In the FAST output, the time traces rise steeply upward a couple of seconds after the run has initiated. In particular, the flow window size soon attains a peak value and stabilizes. The send and receive rates oscillate between a small range of values (some of which might be due to the chosen window size) but, overall, they remain at a similar rate of almost 10 Mbps. The Reno output, on the other hand, does not exhibit the same stabilization as FAST. Most plots, including Link buffer occupancy, Flow send and receive rates, and window size, zigzag in a sawtooth fashion. This is expected because, when the FlowReno encounters multiple AckPacket gaps or timeouts (due to Packets being dropped), it cuts down on its window sizes. This in turn reduces congestion and rates. Finally, it is worth noting that the FlowReno case takes a few seconds longer to terminate than the FlowFast case, and also includes more packet losses (due to buffer overflow, which occurs fairly regularly after the first losses at ~ 1 s).

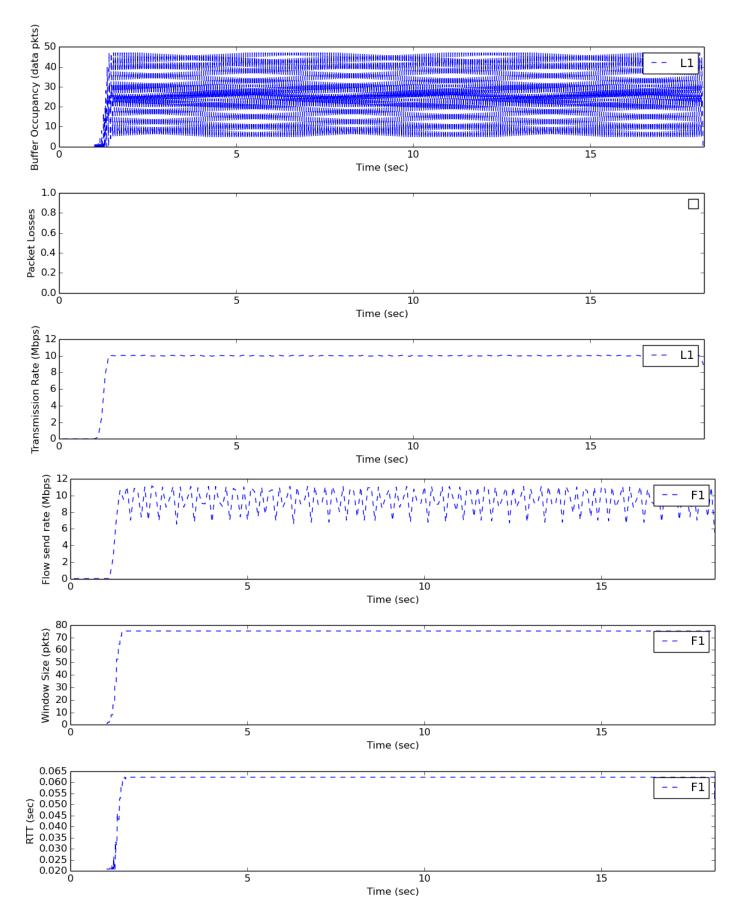


Figure 4: Statistics of Test Case 0 with a TCP FAST Flow.

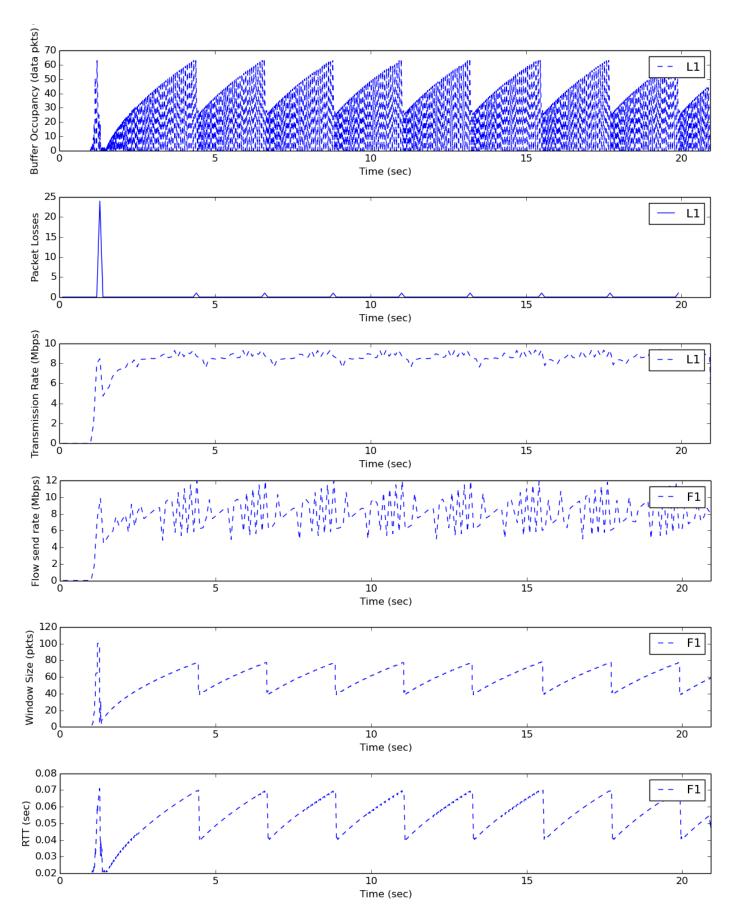


Figure 5: Statistics of Test Case 0 with a TCP Reno Flow.

3.2 Test Case 1

Test case 1 looks at whether Routers can detect and adjust for queuing delays, in recomputing their paths. This case's setup is depicted in Figure 6, and its specs are in Figure 7.

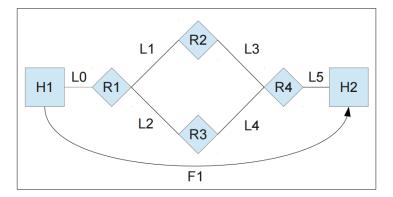


Figure 6: Setup for Test Case 1.

Link Specifications

Link ID	Link Rate (Mbps)	Link Delay (ms)	Link Buffer (KB)
L0	12.5	10	64
L1	10	10	64
L2	10	10	64
L3	10	10	64
L4	10	10	64
L5	12.5	10	64

Flow Specifications

Flow ID	Flow Src	Flow Dest	Data Amt (MB)	Flow Start (s)
F1	H1	H2	20	0.5

Figure 7: Specs for Test Case 1.

There is one source Host (H1) that can choose between two distinct paths to its endpoint Host (H2). The expected behavior is that, when a routing table update is performed, the Routers account for the queuing delay through the current path, and therefore reroute future Packets through the other path. Thus, packets are expected to alternate between the two paths after each routing update (which occurs every 5s).

The results of running the flow using FAST and Reno congestion control algorithms are provided in Figure 8 and Figure 9 respectively. Indeed, as expected, the flow of Packets does swap between the two links L1 and L2 every 5s (with a routing table stabilization delay of 0.15s as explained in Subsection 2.4). Furthermore, as in Subsection 3.1, FAST plots show stabilization and Reno plots exhibit a sawtooth pattern. This increased stability at a high send rate allows FAST to terminate a few seconds quicker, as before.

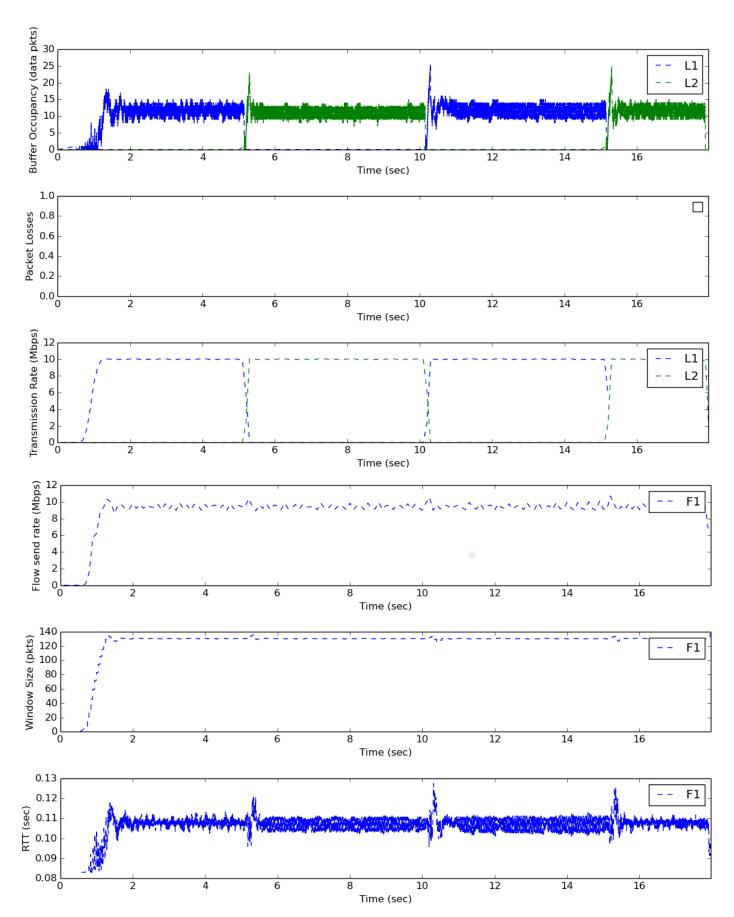


Figure 8: Statistics of Test Case 1 with a TCP FAST Flow. Note that only L1 and L2's statistics are plotted in the Link-related graphs.

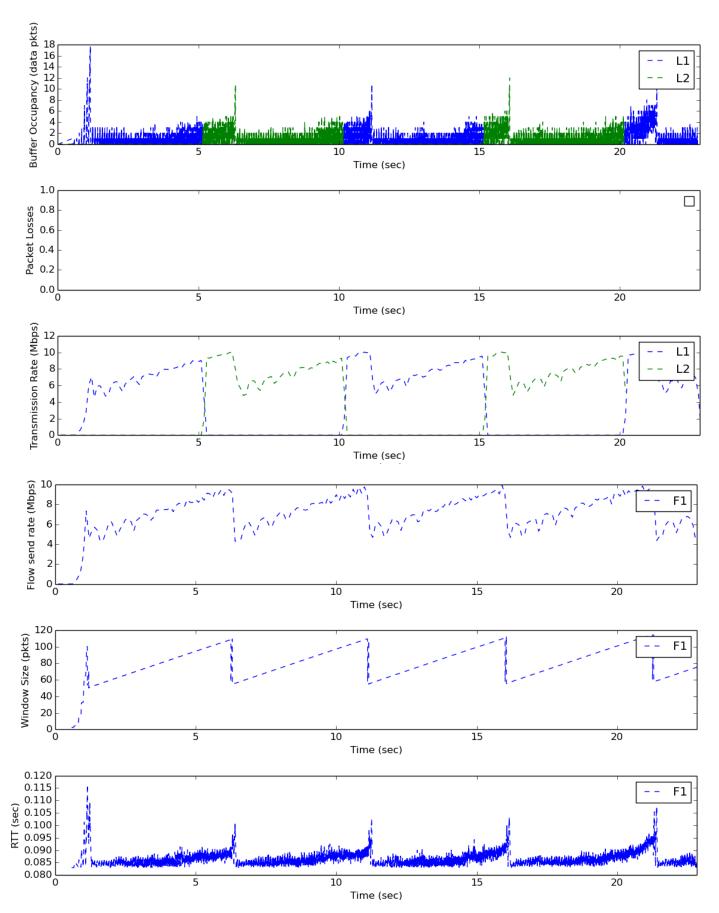


Figure 9: Statistics of Test Case 1 with a TCP Reno Flow. Note that only L1 and L2's statistics are plotted in the Link-related graphs.

3.3 Test Case 2

Test case 2 tests interactions between multiple Flows within the same network. Three Flows start up at different times, between three pairs of distinct sources and destinations, and compete for the same Links' resources. The setup is provided in Figure 10, and the specs are in Figure 11.

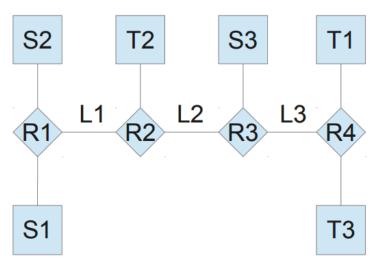


Figure 10: Setup for Test Case 2.

Link Specifications

Link ID	Link Rate (Mbps)	Link Delay (ms)	Link Buffer (KB)	
L1, L2, L3	10	10	128	
All Other Links	12.5	10	128	

Flow Specifications

Flow ID	Flow Src	Flow Dest	Data Amt (MB)	Flow Start (s)
F1	S1	T1	35	0.5
F2	S2	T2	15	10
F3	S3	T3	30	20

Figure 11: Specs for Test Case 2.

The results of running the flow with FAST and Reno are provided in Figure 12 and Figure 13 respectively. Overall, the plots show the same general characteristics of FAST and Reno as described in Subsection 3.1. There are more components in this test case than the previous ones (so the plots are more cluttered), but the FAST plots still present smoother, and more stabilized, time traces. On the other hand, the Reno plots exhibit the same sawtooth nature as before. In addition, FAST terminates around 8 seconds faster than Reno and has fewer Packet losses.

3.4 Test Case 2 Analytic Solution

In this subsection, we analytically predict the equilibrium queue sizes and Flow send rates after each Flow is introduced or terminated. These predictions (calculated in Subsection 3.4.1) are compared to the actual values (see Figure 12) in Subsection 3.4.2.

3.4.1 Calculating Predicted Values

In terms of notation, we will say that C = 1KB = 1024B = 8192b is the constant size of each DataPacket.

All three Flows in this analysis use TCP FAST, with window size $W_i = \frac{RTT_{i,min}}{RTT_i}W_i + \alpha$ (where $\alpha = 50$ is constant but W_i and RTT_i depend on the Flow i). The throughput of each Flow (in bps) will then be given by

$$x_i = \frac{\alpha C}{RTT_i - RTT_{i \ min}}$$

from HW3 Problem 6.8.

We will denote p_l as the queuing delay over Link l, and q_i as the round-trip queuing delay for Flow i. There are then three distinct periods of steady state behavior to examine:

• 0.5s-10s

During this time, all packets are buffered at L1 (the Link between R1 and S1 will not buffer because it has a larger capacity) and there is no queuing delay felt by F1 as no other flows are in the network. Thus, x_1 simply equals 10Mbps. Since there are no other flows in the network yet, $x_1 = \frac{\alpha(1\text{KB})}{q_1}$ (since $RTT_1 - RTT_{1,\text{min}} = p_1 = q_1$ in this case), which solves to $q_1 = \frac{4\alpha}{5120}$ s. For $\alpha = 50$ (as is the case throughout Test Case 2), this gives $p_1 = q_1 = \frac{200}{5120}$ s = 39.063ms. This in turn corresponds to an L1 buffer occupancy (from Little's Law) of 10Mbps · 39.063ms/2 = 200.00Kb = 25.00 data packets, as each DataPacket is 8Kb. The division by 2 comes from the fact that each packet is only delayed by half the round-trip time at each link.

• 10s-20s

It is obvious that L1 will be bottlenecked with the introduction of F2. If we exclusively examine L1 the throughputs must sum to 10 Mbps.

$$x_1 + x_2 = \frac{\alpha C}{p_1} + \frac{\alpha C}{p_1 - 39.063 \text{ms}} = 10 \text{Mbps}$$

Where 39.063ms is the previous round-trip delay on L1 (as mentioned before), and the reasoning behind the subtraction (i.e. $p_1 - 39.063$ ms in the denominator) comes from the fact that $RTT_{2,\rm min}$ includes 39.063ms as part of its min RTT estimate (see HW3 Problem 6.8). For $\alpha = 50$, we find that $p_1 = 102.27$ ms and the resulting throughputs are $x_1 = 3.911$ Mbps and $x_2 = 6.089$ Mbps. This corresponds to a buffer size of 65.46 data packets at L1.

• 20s to F2's termination

At this point, F3 has been initiated. If we then compute throughputs through L1 and L3 respectively, we arrive

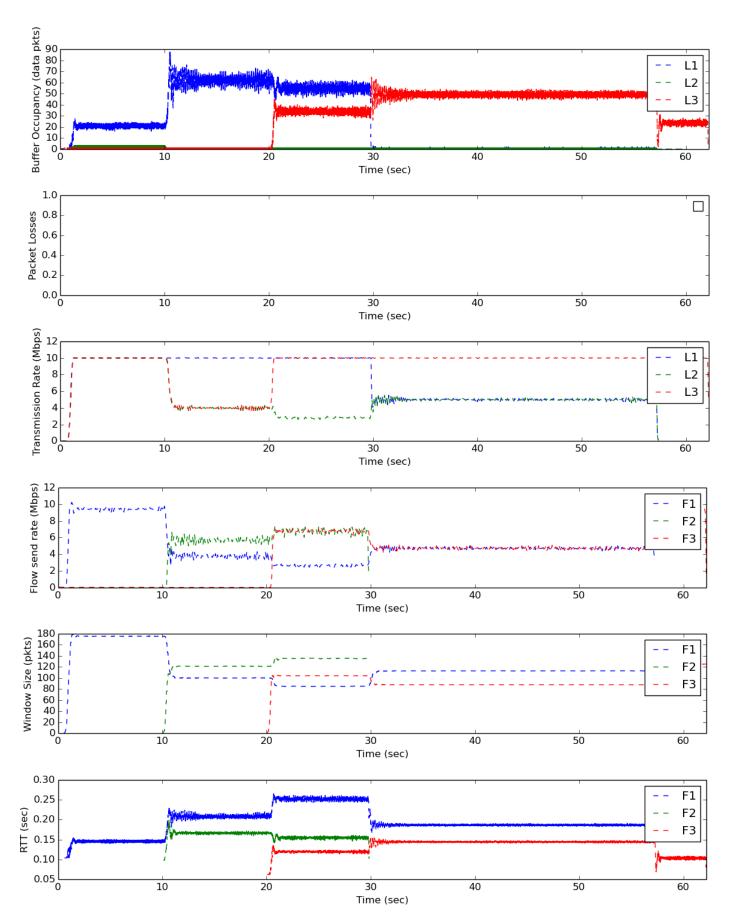


Figure 12: Statistics of Test Case 2, with all Flows running TCP FAST. Note that only L1, L2, and L3's statistics are plotted in the Link-related graphs.

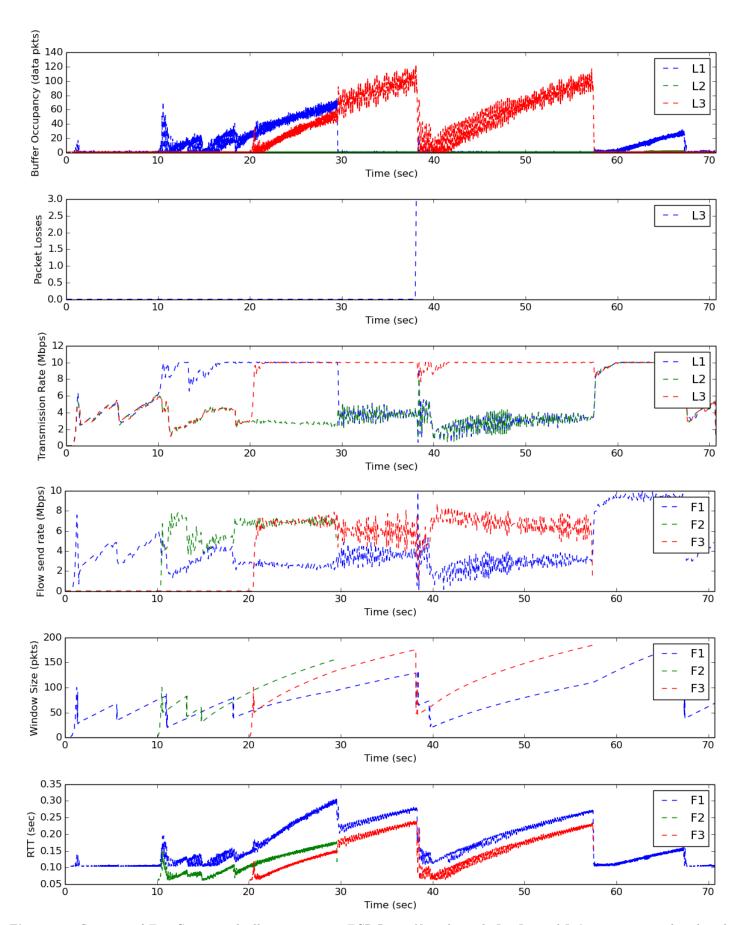


Figure 13: Statistics of Test Case 2, with all Flows running TCP Reno. Note that only L1, L2, and L3's statistics are plotted in the Link-related graphs.

at the following equations

$$x_1 + x_2 = \frac{\alpha C}{p_1 + p_3} + \frac{\alpha C}{p_1 - 39.063 \text{ms}} = 10 \text{Mbps}$$

 $x_1 + x_3 = \frac{\alpha C}{p_1 + p_3} + \frac{\alpha C}{p_3} = 10 \text{Mbps}$

where 39.063ms is the (round-trip) delay over Link L1 due to the preexisting Flow F1. With $\alpha=50$, we find Link (round-trip) delays of $p_1=92.42$ ms and $p_3=53.36$ ms, and so the throughputs are $x_1=2.679$ Mbps and $x_2=x_3=7.321$ Mbps. These correspond to buffer sizes of 59.15 DataPackets on L1 and 34.15 DataPackets on L3.

After the 20s mark, the three Flows send Packets at approximately the aforementioned steady rates, until a flow terminates. The work shown to compute how much each Flow has sent by each time is given in Table 1. To compute these, we just used the steady-state throughputs (in Mbps) for various time intervals (including some of the throughputs mentioned later on) and converted the total data each flow had to send into Megabits (280Mb for F1, 120Mb for F2, 240Mb for F3). Note that analytic predictions using equilibrium rates underpredict termination time because of the non-equilibrium transmission periods where the window is still adjusting.

t (s)	F1(Mb)	F2(Mb)	F3(Mb)
0.5	0	0	0
10	95	0	0
20	134.11	60.89	0
28.07	155.74	120	59.11
52.92	280	120	183.37
58.58	280	120	240

Table 1: Approximate amounts of data sent by each Flow by key times. The simulated termination times were $\{52.92, 28.07, 58.58\}$ s for the three flows $\{F1, F2, F3\}$ (respectively).

After each Flow exits, we have the following rate and buffer capacity predictions:

• t = 28.07s — Flow 2 terminates (predicted).

The network now bottlenecks at L3 with no queuing delay. Thus, the throughputs through L3 satisfy

$$x_1 + x_3 = \frac{\alpha C}{p_3} + \frac{\alpha C}{p_3} = 10$$
Mbps

which gives (by symmetry) $x_1 = x_3 = 5 \text{Mbps}$ and so $p_3 = \frac{\alpha C}{5 \text{Mbps}}$. With $\alpha = 50$, this yields $p_3 = 78.12 \text{ms}$ and an L3 buffer size of 50 DataPackets (simply twice the single-Flow case).

• t = 52.95s — Flow 1 terminates (predicted).

All that remains at this point is just Flow F3 by itself, so $x_3 = 10 \text{Mbps}$. This is effectively the same configuration as the 0.5s-10s case from before, and so we find $p_1 = \frac{4\alpha}{120} \text{s} = 39.063 \text{ms}$ and a buffer size of 25 DataPackets.

• t = 58.58s — Flow 3 terminates (predicted).

3.4.2 Comparing Predicted and Actual Values

We summarize all of the earlier predicted results and compare them to the actual simulation results below:

- 0.5s 10s
 - Expected F1 throughput: 10 Mbps. Actual: ~ 9.6 Mbps.
 - Expected L1 buffer occupancy: 25 pkts. Actual: ~ 20 pkts.
- 10s 20s
 - Expected F1 throughput: 3.91 Mbps. Actual: ~ 3.9 Mbps.
 - Expected F2 throughput: 6.09 Mbps. Actual: ~ 6.0 Mbps.
 - Expected L1 buffer occupancy: 65 pkts. Actual: ~ 60 pkts.
- 20s 30s
 - Expected F1 throughput: 2.68 Mbps. Actual: ~ 2.7 Mbps.
 - Expect F2 throughput = F3 throughput: 7.32 Mbps. Actual: ~ 7.1 Mbps.
 - Expected L1 buffer occupancy: 59 pkts. Actual: ~ 55 pkts.
 - Expected L3 buffer occupancy: 34 pkts. Actual: ~ 33 pkts.
- After Flow 2 drops out ($\sim 30 \mathrm{s} \ \mathrm{to} \sim 57 \ \mathrm{s}$)
 - Expected F1 throughput: 5 Mbps. Actual: ~ 4.9 Mbps.
 - Expected F3 throughput: 5 Mbps. Actual: ~ 4.9 Mbps.
 - Expected L1 buffer occupancy: 0 pkts. Actual: 0 pkts.
 - Expected L3 buffer occupancy: 50 pkts. Actual: ~ 50 pkts.
- After Flow 1 drops out ($\sim 57 \mathrm{s} \ \mathrm{to} \sim 62 \mathrm{s}$)
 - Expected F3 throughput: 10 Mbps. Actual: ~ 9.6 Mbps.
 - Expected L3 buffer occupancy: 25 pkts. Actual: ~ 23 pkts.

• Predicted Termination Times

F2: 28.07 s (Actual: 29.72 s)
F1: 52.92 s (Actual: 57.43 s)
F3: 58.58 s (Actual: 62.23 s)

4 Summary

This network simulator successfully incorporates a variety of features – including dynamic routing, TCP Reno, and TCP FAST – into an event-driven model with statistics tracking. The three test cases examined have the expected qualitative behavior in terms of their time traces. An additional analytic check on Test Case 2 further confirms the accuracy of the simulator.

5 GitHub Repository

A link to our GitHub repository is included in [4].

6 Acknowledgments

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