

# Chapter 6

## *Firms and Production*

### Key issues

1. ownership and management of firms
2. short-run production: one variable and one fixed input
3. long-run production: two variable inputs
4. returns to scale
5. productivity and technical change

## Firm

an organization that converts inputs (labor, materials, and capital) into outputs (goods and services)

## Sources of production: U.S.

- firms: 84% of U.S. national production
- government: 12%
- nonprofit institutions: 4%
- private households: 0.2%

## Government's share of production

- United States: 12%
- Ghana 37%
- Zambia 38%
- Sudan 40%
- Algeria 90%
- Bangladesh, Paraguay, and Nepal 3%

## Legal forms of for-profit firms

- *sole proprietorships*: owned and run by a single individual
- *partnerships*: jointly owned and controlled by two or more people
- *corporations*: owned by shareholders in proportion to the numbers of shares of stock they hold

## Corporations

- shareholders elect a board of directors who run the firm
- board of directors usually hire managers

## Liability

- sole proprietors and partners liable:
  - personally liable for debts of their firms
  - to the extent of all their personal wealth - not just their investments
- owners of corporations have limited liability:
  - cannot lose personal assets
  - liability limited to their investment (value of stock)

	<i>Business Sales</i>	<i>Number of Firms</i>
Sole proprietorships	6%	75%
Partnerships	5%	7%
Corporations	90%	<20%

## Management of Firms

- small firm owner usually manages
- corporations and larger partnerships use managers

## Objectives

- conflicting objectives between owners, managers, and other employees
- employees want to maximize their earnings or utility
- owners want to maximize profit:

$$\pi = R - C$$

- $R$  = revenue =  $pq$  = price x quantity
- $C$  = cost

## Production efficiency

given current knowledge about technology and organization:

- current level of output cannot be produced with fewer inputs
- given quantity of inputs used, no more output could be produced

## Production efficiency and profit

production efficiency is

- a necessary condition to maximize profit
- not a sufficient condition to maximize profit (must produce optimal output level)

## Production

- production process: transform inputs or factors of production into outputs
- common types of inputs:
  - capital ( $K$ ): buildings and equipment
  - labor services ( $L$ )
  - materials ( $M$ ): raw goods and processed products

## Production function

relationship between quantities of inputs used and maximum quantity of output that can be produced, given current knowledge about technology and organization

## Production function with 2 inputs

a production function that uses only labor and capital:

$$q = f(L, K)$$

to produce the maximum amount of output given efficient production



## Variability of inputs over time

- firm can more easily adjust its inputs in the long run (LR) than in the short run (SR)
- *short run*: a period of time so brief that at least one factor of production is fixed
- *fixed input*: a factor that cannot be varied practically in the SR
- *variable input*: a factor whose quantity can be changed readily during the relevant time period
- *long run*: lengthy enough period of time that all inputs can be varied

## Short-run production

- one variable input: Labor ( $L$ )
- one fixed input: Capital ( $K$ )
- thus, firm can increase output only by using more labor

## Example

- service firm assembles computers for a manufacturing firm
- manufacturing firm supplies it with the necessary parts, such as computer chips and disk drives
- assembly firm's capital is fixed: eight workbenches fully equipped with tools, electronic probes, and other equipment for testing computers can vary labor

Capital, $\bar{K}$	Labor, $L$	Output, Total Product of Labor, $Q$	Marginal Product of Labor, $MP_L = \Delta Q / \Delta L$	Average Product of Labor, $AP_L = Q / L$
8	0	0		
8	1	5	5	5
8	2	18	13	9
8	3	36	18	12
8	4	56	20	14
8	5	75	19	15
8	6	90	15	15
8	7	98	8	14
8	8	104	6	13
8	9	108	4	12
8	10	110	2	11
8	11	110	0	10
8	12	108	-2	9
8	13	104	-4	8

## Marginal product of labor ( $MP_L$ )

- should firm hire another worker?
- want to know marginal product of labor:
  - change in total output,  $\Delta q$ , resulting from using an extra unit of labor,  $\Delta L = 1$ , holding the other factor ( $K$ ) constant
  - $MP_L = \Delta q / \Delta L$

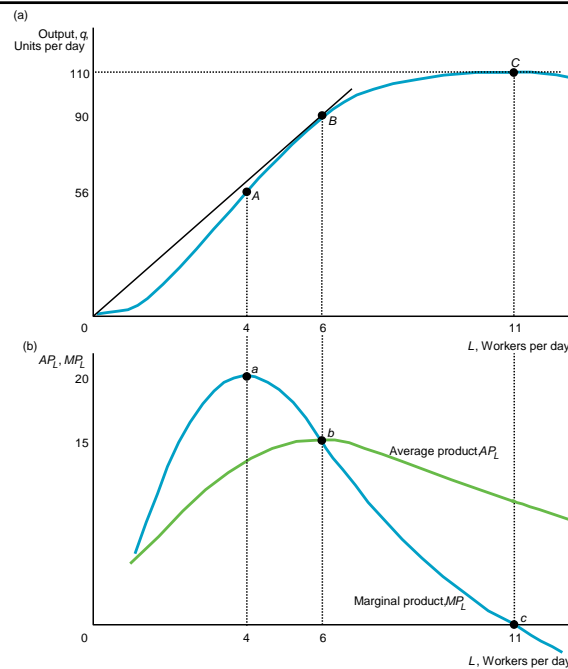
## Average product of labor ( $AP_L$ )

- does output rise in proportion to this extra labor?
- want to know average product of labor:
  - ratio of output to the number of workers used to produce that output
  - $AP_L = q / L$

## Graphical relationships

- total product:  $q$
- marginal product of labor:  $MP_L = \Delta q / \Delta L$
- average product of labor:  $AP_L = q/L$
- smooth curves because firm can hire a "fraction of a worker" (works part of a day)

**Figure 6.1**  
Production  
Relationships with  
Variable Labor



## Effect of extra labor

- $AP_L$ 
  - rises and then falls with labor
  - slope of line from the origin to point on total product curve
- $MP_L$ 
  - first rises and then falls
  - cuts the  $AP_L$  curve at its peak
  - is the slope of the total product curve

## Law of diminishing marginal returns (product)

as a firm increases an input, holding all other inputs and technology constant,

- the corresponding increases in output will become smaller eventually
- that is, the marginal product of that input will diminish eventually
- see Table 6.1 and Figure 6.1b

## Long-run production: Two variable inputs

- both capital and labor are variable
- firm can substitute freely between  $L$  and  $K$
- many combinations of  $L$  and  $K$  produce a given level of output:
- $q = f(L, K)$

## Isoquant

- curve that shows efficient combinations of labor and capital that can produce a single (iso) level of output (*quantity*):

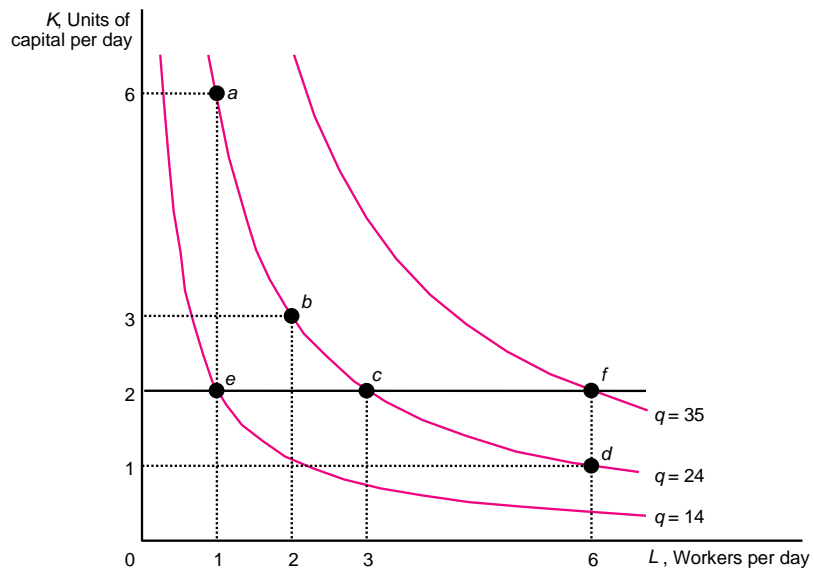
$$\bar{q} = f(L, K)$$

- Examples:
  - 10-unit isoquant for a Norwegian printing firm
$$10 = 1.52 L^{0.6} K^{0.4}$$
  - Table 6.2 shows four  $(L, K)$  pairs that produce  $q = 24$

**Table 6.2 Output Produced with Two Variable Inputs**

Capital, $K$	Labor, $L$					
	1	2	3	4	5	6
1	10	14	17	20	22	24
2	14	20	24	28	32	35
3	17	24	30	35	39	42
4	20	28	35	40	45	49
5	22	32	39	45	50	55
6	24	35	42	49	55	60

**Figure 6.2 Family of Isoquants**



## Isoquants and indifference curves

- have most of the same properties
- biggest difference:
  - isoquant holds something measurable, quantity, constant
  - indifference curve holds something that is unmeasurable, utility, constant

## 3 major properties of isoquants

follow from the assumption that production is efficient:

1. further an isoquant is from the origin, the greater is the level of output
2. isoquants do not cross
3. isoquants slope down



## Shape of isoquants

- curvature of isoquant shows how readily a firm can substitute one input for another
- extreme cases:
  - perfect substitutes:  $q = x + y$
  - perfect complements:  $q = \min(x, y)$
- usual case: bowed away from the origin

Figure 6.3a Perfect Substitutes: Fixed Proportions

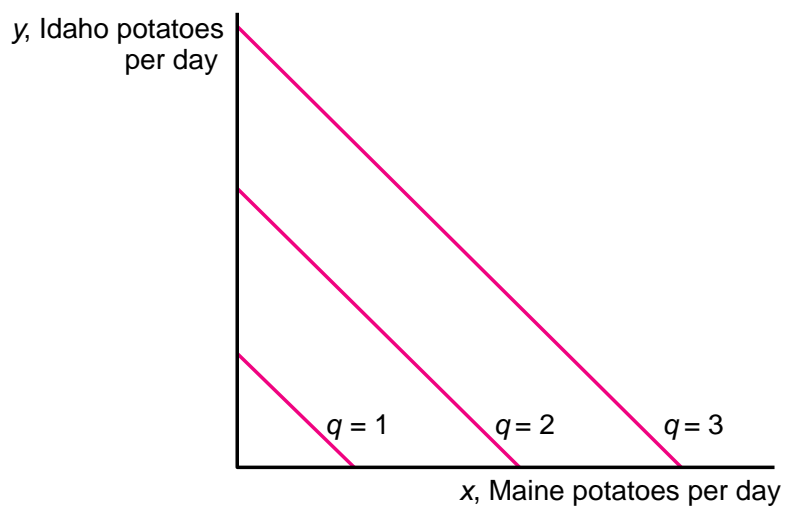


Figure 6.3b Perfect Complements

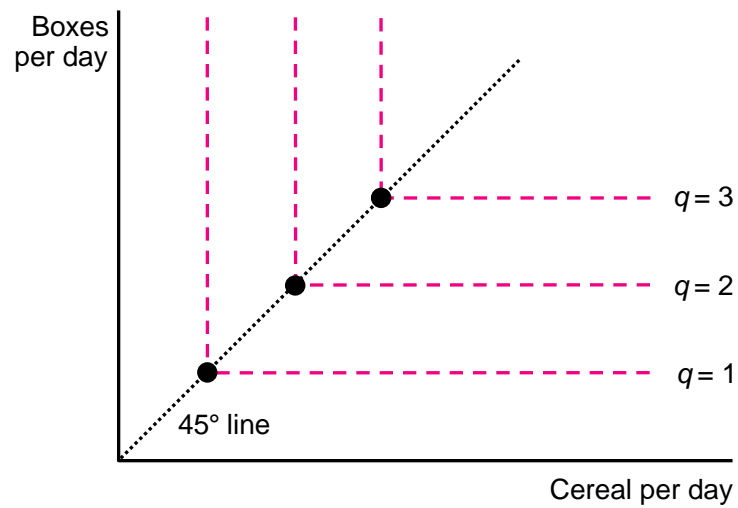
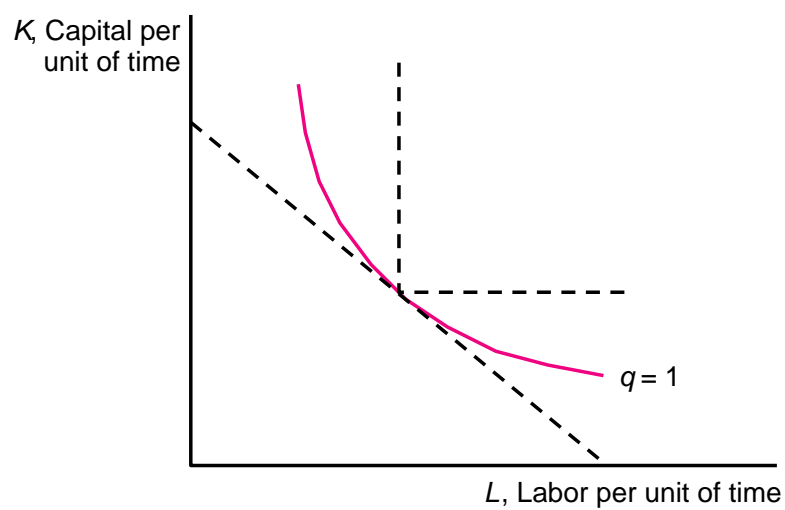


Figure 6.3c Substitutability of Inputs



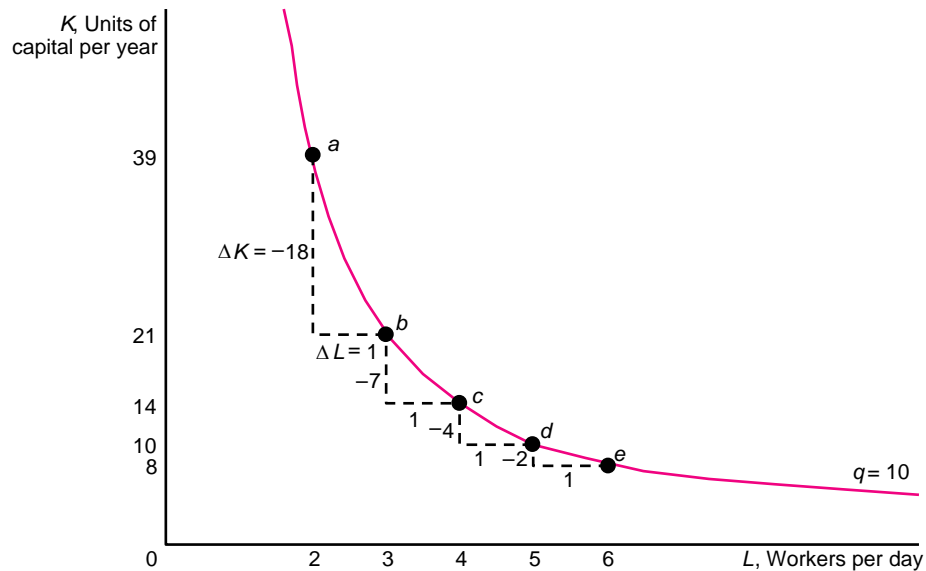
## Substituting inputs

slope of an isoquant shows the ability of a firm to substitute one input for another while holding output constant

## Marginal rate of technical substitution ( $MRTS$ )

- tells how much a firm can increase one input and lower the other so as to stay on an isoquant
- absolute value of the slope of an isoquant =  
| slope of straight line tangent to isoquant |
- tells us how many units of  $K$  firm can replace with an extra unit of  $L$ , holding output constant
- varies along a curved isoquant

**Figure 6.4** How the Marginal Rate of Technical Substitution Varies Along an Isoquant



## Returns to scale

how output changes if all inputs are increased by equal proportions

- how much does output change if a firm increases all its inputs proportionately?
- answer to this question helps a firm to determine its scale or size in LR

## Constant returns to scale (CRS)

- when all inputs are doubled, output doubles

$$f(2L, 2K) = 2f(L, K)$$

- potato-salad production function is CRS

## Increasing returns to scale (IRS)

- when all inputs are doubled, output more than doubles

$$f(2L, 2K) > 2f(L, K)$$

- increasing the size of a cubic storage tank:  
outside surface (two-dimensional) rises less  
than in proportion to the inside capacity  
(three-dimensional)

## Decreasing returns to scale (DRS)

- when all inputs are doubled, output rises less than proportionally

$$f(2L, 2K) < 2f(L, K)$$

- decreasing returns to scale because
  - difficulty organizing, coordinating, and integrating activities rises with firm size
  - large teams of workers may not function as well as small teams

## Cobb-Douglas

- one of the most widely estimated production functions is the Cobb-Douglas:

$$q = AL^{\alpha} K^{\beta}$$

- $A$ ,  $\alpha$ ,  $\beta$  are positive constants

## Solved problem

Under what conditions does a Cobb-Douglas production function exhibit decreasing, constant, or increasing returns to scale?

## Answer

1. *show how output changes if both inputs are doubled:*

$$q_1 = AL^\alpha K^\beta$$

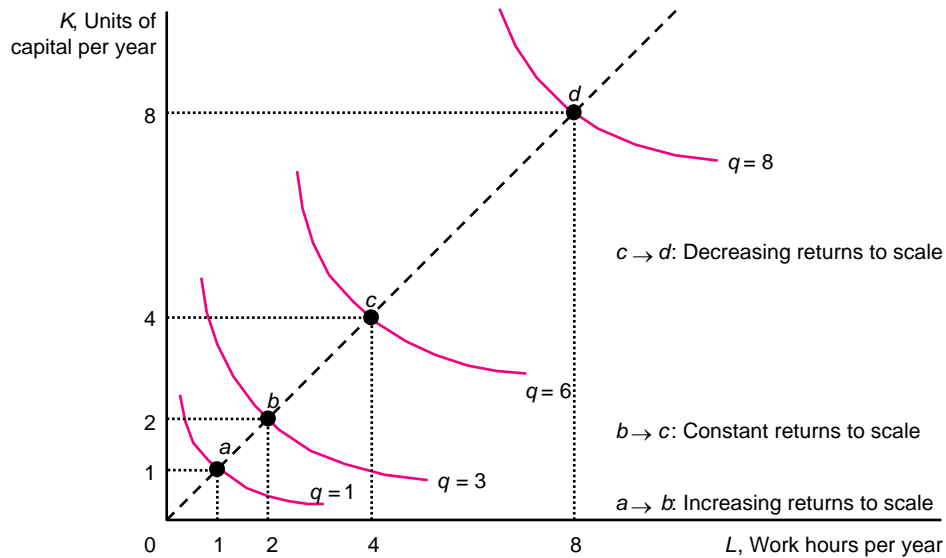
$$q_2 = A(2L)^\alpha (2K)^\beta = 2^{\alpha+\beta} AL^\alpha K^\beta$$

2. *Thus, output increases by*

$$\frac{q_2}{q_1} = \frac{2^{\alpha+\beta} AL^\alpha K^\beta}{AL^\alpha K^\beta} = 2^{\alpha+\beta} \equiv 2^\gamma,$$

where  $\gamma \equiv \alpha + \beta$

Figure 6.5 Varying Scale Economies



## Technical progress

- an advance in knowledge that allows more output to be produced with the same level of inputs
- *nonneutral technical change*: innovation that increases output by altering proportion in which inputs are used
- *neutral technical change*: produce more with same bundle of inputs



## Neutral technical change

- last year a firm produced

$$q_1 = f(L, K)$$

- due to a new invention, this year the firm produces 10% more output with the same inputs:

$$q_2 = 1.1f(L, K)$$

## Organizational change

- may change the production function
- same effect as technological change

## Application: Just-in-time delivery

- Japanese auto manufacturers have parts delivered just-in-time for use so they can reduce inventories
- Dell Computer
  - suppliers deliver parts as needed
  - newest factory has no room for inventory storage
  - redesigned its computers to use many of the same parts
  - computers built only after order is placed