

Signaling Equilibrium, Intergenerational Social Mobility and Long Run Growth

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Contents

1	Introduction	2
2	The Basic Model	4
1	Employers' choice problem	6
2	Individual's choice problem	6
3	Signaling equilibrium	8
4	Classifications of equilibria	10
3	Mobility and growth	11
4	Labor Market Practices	14
1	Quits, layoffs, and promotion	15
2	Labor Market Signaling and Job Matching	17
5	Educational Systems: public, private, school voucher	18
6	Policies and conclusions	20
	Bibliography	23

0.1 Abstract This paper provides a signaling model of intergenerational social mobility and economic growth, in which innate ability of workers, and the type of their education and jobs determine the rate of technological progress and social mobility. It is shown that in economies with one-time non-renegotiable wage contracts, there are generally multiple signaling equilibria, producing lower than the maximum attainable rate of social mobility and economic growth. The paper shows that various labor market practices such as quits, layoffs and promotions, can improve some of the inefficiencies, and improve the rate of economic growth and social mobility. The remaining inefficiencies in the economy can be removed by intervening in the educational system. The paper examines the role of school vouchers for the children of poor family backgrounds in improving the rate of economic growth and social mobility.

Keywords: Intergenerational social mobility, signaling equilibrium, and economic growth.

Acknowledgement and disclaimer¹

[I]t is not a story that concludes, Genius will out-though Ramanujan's in the main, did. Because so nearly did events turn out otherwise that we need no imagination to see how the least bit less persistence, or the least bit less luck, might have consigned him to obscurity. In a way, then, this is also a story about social and educational systems, and about how they matter, and how they sometimes nurture talent and sometimes crush it. How many Ramanujans, his life begs us to ask, dwell in India today, unknown and unrecognized? And how many in America and Britain, locked away in racial or economic ghettos, scarcely aware of worlds outside of their own?

Robert Kanigel, *The Man who knew Infinity*, pp.3-4.

1. Introduction

Recent literature on endogenous growth attributes the stock of tested and useful technological knowledge as the main source of economic growth, and provides economic models of such knowledge creation. Lucas (1988) provides a model in which identical workers spend part of their time acquiring skills or vocational training which increases their productivity; the new technologically useful knowledge that the individual workers acquire from their vocational or on the job training adds to the pool of social knowledge. In his model, factors that increase average education level of the work force also create higher long-run growth. Other models also emphasize the creation of human capital in the growth process. There are ample empirical studies document that accumulated basic scientific and engineering knowledge stocks spillover to the rest of the economy or even to the rest of the world (see Adams (1990) for a study using published articles in various scientific fields, Jaffe (1986) for a study on the US manufacturing industry, Coe and Helpman (1995) for international spillover, and Raut (1995) for a study on India).

While the creation of knowledge in the growth literature plays an important role, workers in this literature are generally assumed to be identical in their innate ability to create knowledge and to produce income. But in reality they do differ in their ability, and the heterogeneity in innate ability make a big difference in the process of knowledge creation; while average level of education is important, the distribution of education among the workers of different abilities and the matching of jobs to workers of different ability and schooling are important determinants of the rate of knowledge creation. For instance, when the workers with higher innate ability get educated in technical areas and

¹ An earlier draft of the paper was presented at the Seventh World Congress Meeting of the Econometric Society, Tokyo, 1995 and the winter meeting of the Econometric Society, January 1996, San Francisco. The comments from the participants of the above meetings, and the insightful comments of Boyan Jovanovich, Robert Lucas, Joel Sobel, and T.N. Srinivasan are gratefully acknowledged.

are matched with jobs that are more suitable to generate basic scientific and technological knowledge, we would expect higher rate of technical progress and economic growth. How well these are done, depends on educational system and labor market practices. For instance, children of poor family backgrounds are generally found to acquire less education. Then it is quite clear that if talented individuals from poorer background did not obtain higher schooling, they are not tapped into the growth process. In such economies, therefore, higher social mobility through higher education of talented individuals from all backgrounds, and their assignment to the appropriate jobs in the growth enhancing modern sectors will lead to higher mobility and faster growth. The main barrier is the asymmetric information on innate ability: The innate ability or the talent of an individual is a private knowledge - known to the individual but not to the school administrators and the employers.

To analyze the effect of the above asymmetric information on social mobility and economic growth, and to design policies that can remove bottlenecks, I extend the education signaling model of [Spence \(1973\)](#), incorporating the job matching within an overlapping generations framework.² This model of schooling investment and job matching differs from the existing models on several aspects. First, most theoretical models of job matching formulates the decision making in a search theoretic framework, in which, infinitely lived workers search over time for the best job that can produce the highest life-time earnings (see [Jovanovic \(1979\)](#) who incorporates worker's productivity to vary with the matched job). In these models, however, employers are passive, they do not design complex wage contracts nor use any signals from workers to get an idea about the worker's innate ability and negotiate the wage contracts accordingly. Furthermore, the assumption of agents living infinitely, which is suitable for studying unemployment duration, or labor mobility across jobs, turns out to be technically not suitable for studying intergenerational social mobility. Second, this model differs from the basic models of human capital theory (([Becker, 1962](#); [Ben-Porath, 1967](#); [Mincer, 1958](#); [Rosen, 1977](#); [Willis, 1986](#))) in that the present model agents live effectively only for one period and thus it does not take into account the life cycle events such as on-the-job-training, and more importantly, the borrowing constraints for educational investment.

The rest of the paper is organized as follows: Section [2](#) describes the basic model, and defines the signaling equilibrium with one-time non-renegotiable wage contracts, and a few other equilibrium concepts. Section [3](#) studies the properties of signaling equilibria. Section [4](#), examines various labor market practices such as quits, layoffs and promotions. Section [5](#) briefly discusses the role of education system and education policies that can improve social mobility and economic growth. Section

²There are alternative models of intergenerational social mobility, see for instance, ([Becker and Tomes, 1986](#); [Becker and Tomes, 1979](#)), and ([Loury, 1981a](#); [Loury, 1981b](#)). These models do not feature asymmetric information regarding innate productive ability of workers.

6 discusses the policy implications of our model for intergenerational social mobility and economic growth and concludes the paper.

2. The Basic Model

Consider an overlapping generations model in which in each period one person is born to each parent. Denote by τ an individual's innate ability which affects his productivity at workplace and learning in school. There is some dispute in the sociology, psychometry and economics literature as to whether τ should consist of one component, which is then generally referred to as level of intelligence, or IQ, or should it be a vector allowing individuals to vary in their ability for various skills, such as verbal skill, mathematical or logical skills.³ I assume for simplicity of exposition that τ is one dimensional, and it takes a finite set of discrete ordinal values, $T = \{1, 2, \dots, \hat{\tau}\}$. In the set T , a higher number denotes a greater talent. I assume that a when a child is born to a parent, the child's innate ability $\tau \in T$ with probability $g(\tau)$, and it is independent of parent's innate ability.⁴

The innate ability of an individual is a private information, observed only by him. An individual chooses education to signal his talent type. Education signal is assumed to be a one dimensional variable and it is denoted by s . Realistically, s is a vector, $s = (s^1, s^2, s^3)$, where s^1 represents the number of years of schooling, s^2 represents major specialization, such as Engineering, Medical Science, Physics, Chemistry, Business Administration, and other general subjects, and s^3 may represent quality of education, which is generally associated with the quality of the school from which s^1 , and s^2 are obtained, for instance private, public, the average of the top 25% SAT scores of the school, student faculty ratio, and a host of such variables of the school (see, [Daniel et al. \(1997\)](#), and [J. Heckman et al. \(1995\)](#) for some of these variables in their empirical studies on school quality using NLSY data). Signal s is viewed as quality adjusted number of years of schooling. A higher number represents either a better quality or higher level of schooling. Possible education levels are assumed to be the ordinal numbers in $S = \{1, 2, \dots, \hat{s}\}$, a higher number representing a higher education

³The arguments in the first strand is based on statistical analyses which show that generally many test scores exhibit the presence of a common factor, known as g-loaded factor which has been found to be a good predictor of many socio-political-economic outcomes, especially in the labor market success and educational attainment. (See, for instance, [Herrnstein and Murray \(1994\)](#), and [Gottfredson \(1997\)](#)). There are many economic studies which find the opposite. (See, for instance, Heckman's ([J. J. Heckman \(1995\)](#)) critique of the [Herrnstein and Murray \(1994\)](#) book for arguments and references, and see [Roy \(1951\)](#) model of earnings function that uses a multi-dimensional vector for ability).

⁴There is a long controversy over the issue of whether children's innate ability is genetically inherited from parent's innate ability. The scientific consensus is that the correlation between parent's innate ability and a child's innate ability is somewhere between 0.3 to 0.7. I assumed it to be zero, for simplification. There are other controversies regarding talent, ability and intelligence. Some believe that one is born with a fixed level of intelligence, and training and environment has no effect on intelligence. Others do not agree with it, and believe that ability, intelligence and talent could be improved to some extent with better environment and training. Some believe that intelligence or innate ability is fixed when one is born, and less intelligent people can learn and do complex things that we face in our everyday life, in school curricula, and in modern jobs, except that they might take longer, and thus less productive; this is the view we take in this paper.

level.⁵

A job in our set-up is characterized by its task and is denoted by η . In a job a worker is most productive if he has required abilities and schooling. Less qualified workers can also perform the job but the output will be at a lower level. Assume that η takes finite ordinal numbers from the set $H = \{1, 2, \dots, \hat{\eta}\}$, a higher index represents a more technical and growth enhancing job. It is important to distinguish⁶ between an earnings function and the *productivity function* in order to understand where signaling theory of educational investment differs from human capital investment theory. Productivity function $e(s, \tau, \eta)$ is the number of efficiency unit of labor or productivity level of a worker of schooling level s , innate ability τ , working in job η . The earnings function $w = \phi(s, \tau, \eta)$ is the labor market wage rate of a unit of labor with education level s and ability τ . I assume that labor productivity of all workers are uniformly growing over time, i.e., a unit of labor with schooling level s , innate ability τ , and working in job η in period t is given by $A_t e(s, \tau, \eta)$. The multiplicative factor A_t is endogenously determined as follows: I presume that more able workers with higher education and working in higher up jobs in H can create higher amount of publicly available new scientific and engineering basic knowledge and ideas about how to produce and distribute old products or new products cheaply. Let $a(s, \tau, \eta)$ be the amount of basic scientific and engineering spillover knowledge created by a worker with education level s and innate ability τ when matched with the employer η . Let R_t denote the aggregate flow of spillover knowledge in period t in the economy, aggregated over all s, τ and η in the population. A_t evolves over time according to:

$$A_{t+1} = A_t (1 + \gamma(R_t)) \quad (1)$$

where $\gamma(R_t)$ is the growth rate of productivity level, assumed to be a time invariant function. If $R_t = 0$, $\gamma(R_t) = 0$ and γ may be assumed to be an increasing function as for instance, $\gamma(R_t) = R_t^\mu$, $\mu > 0$.

⁵The general practice in the human capital literature is, however, to treat S as continuous variable, more realistically it is a discrete set.

⁶There is a longstanding controversy as to whether years of education is a significant determinant of earnings, or is it that ability is the main determinant of earnings, and education just picks up the effect of ability (see [Griliches and Mason \(1972\)](#) and [Willis \(1986\)](#)). It has been found that the effect of education on earnings is somewhat lower after ability is controlled for, but it is not insignificant. Much of these empirical studies are carried out in the [Mincer \(1958\)](#) earnings function framework, where they estimate market wage rate $w = \phi(s, \tau)$, where s is the number of years of schooling, and τ is an ability measure. The original Mincer earnings function also includes an experience variable, x , which is generally taken to be number of years of work experience. Since it is not relevant for our issues, we drop it.

2.1. Employers' choice problem

In the economics of imperfect information there are mainly two ways in which the workers' and employers' problems are formulated: the first approach is the Spence model where the employer announces a wage schedule, then workers make their decisions on education levels; the other approach due to [Rothschild and Stiglitz \(1970\)](#) is more appropriate in the insurance context, see for other schemes, [Kreps \(1990\)](#). Spence's approach is more appropriate in our context, and we will follow this approach.

I assume that the production sector is competitive; the producer is risk neutral and he treats A_t as an externality when making his decisions. In each period $t \geq 1$, a producer η_t 's role is to announce a wage schedule $\omega_t(s_t; \eta_t)$ for hiring purposes. He observes the education level s_t of a worker but not his innate productive ability level τ_t . The employer η_t holds a subjective belief about the conditional probability distribution of the productivity level $e(s_t, \tau_t, \eta_t)$ of an worker with education level s_t . Denote this conditional probability by

$$q_t(e|s_t; \eta_t) = \text{Probability}\{e|s_t; \eta_t\}, e \in E, s_t \in S, \eta_t \in H \quad (2)$$

Let $\omega_t(s_t; \eta_t)$ be the wage profile that the producer η_t announces. Perfect competition, and expected profit maximization imply that

$$\begin{aligned} \omega_t(s_t; \eta_t) &= A_t \sum_{e \in \mathcal{E}} e \cdot q_t(e|s_t; \eta_t) \\ &\equiv A_t w_t(s_t; \eta_t), \end{aligned} \quad (3)$$

where $w_t(s_t; \eta_t) \equiv \sum_{e \in \mathcal{E}} e \cdot q_t(e|s_t; \eta_t)$. Notice that $w_t(\cdot)$ depends on the producer's subjective conditional probability distribution, $q_t(e|s_t; \eta_t)$, and dependence of $w_t(\cdot)$ on t is through the dependence of q on t .

2.2. Individual's choice problem

We consider only human capital investment in education, other important forms of human capital investment such as health and nutrition are not considered here. The investment in the level of education of an individual is a complex decision making process. Generally, parents make the initial investments such as preschool investments and investments up to college or so, until an individual reaches enough maturity to make his own schooling decision. Family background can have great

influence on educational attainment in several other ways. For instance, suppose that the quality of preschool investment of parents' time at home affect children's motivation and persistence to continue schooling. Then, of course, more highly educated parents can provide better learning environment for their children at home. Similarly, more highly educated parents with their better knowledge base of child care, or simply because of their higher incomes can provide better prenatal care, and health care for proper cognitive development of their children. Furthermore, innate ability will also affect the time and efforts it takes to complete an academic curriculum, and hence are important determinants of cost of schooling.⁷

We represent these effects of family background in our model simply by assuming that the cost, $\theta_t(s_t, \tau_t, s_{t-1}, \eta_{t-1})$, of obtaining a certain level of education $s_t \in S$ for an individual in period t depends on his innate ability $\tau_t \in T$, and his parent's socio-occupational status $(s_{t-1}, \eta_{t-1}) \in S \times H$. Assume that $\theta_t(s_t, \tau_t, s_{t-1}, \eta_{t-1})$ is increasing in s_t , and decreasing in τ_t , s_{t-1} and η_{t-1} . The assumption that $\theta_t(s_t, \tau_t, s_{t-1}, \eta_{t-1})$ varies with τ_t is necessary for education to act as signal for talent, see [Spence \(1973\)](#), or [Kreps \(1990\)](#) for a justification. We further assume that

$$\theta_t(s_t, \tau_t, s_{t-1}, \eta_{t-1}) = A_t \theta(s_t, \tau, s_{t-1}, \eta_{t-1})$$

where A_t is the productivity shift parameter of the aggregate production function defined earlier, and $\theta(\cdot)$ is a time invariant function.

We assume that all individuals have identical linear⁸ utility function $u(c_t) = c_t$ where c_t is the consumption of an adult of period t . An adult of period t with talent type $\tau_t \in T$ and from a parent of education level s_{t-1} takes the announced wage function $w_t(s_t; \eta_t)$ of period t as given and decides his education level $s_t \in S$ and the expected job to perform by solving the following problem:

$$\max_{s_t \in S, \eta_t \in \mathcal{H}} [\omega_t(s_t; \eta_t) - \theta_t(s_t, \tau_t, s_{t-1}, \eta_{t-1})]$$

which is equivalent to solving the following problem

$$A_t \max_{s_t \in S, \eta_t \in \mathcal{H}} [w_t(s_t; \eta_t) - \theta(s_t, \tau_t, s_{t-1}, \eta_{t-1})] \quad (4)$$

Except for degenerate cases, there is a unique optimal solution s_t for each τ_t and s_{t-1} , which is independent of A_t . Notice that in our framework, all individuals with talent τ_t and family background

⁷There are other ways education of parents can influence the educational achievement of their children, for instance, by providing role models. Also see section 5 and ([Raut, 1990](#); [Spence, 1973](#)) for more on this.

⁸Thus we abstract away from bearings on our results from risk sharing between employers and workers.

s_{t-1} , and η_{t-1} behave identically. We will refer to such an agent as $(\tau_t, s_{t-1}, \eta_{t-1})$. We denote the optimal solution of Eq. (4) for agent $(\tau_t, s_{t-1}, \eta_{t-1})$ by $\sigma_t(\tau_t, s_{t-1}, \eta_{t-1})$ and $\eta_t(\tau_t, s_{t-1}, \eta_{t-1})$. We define a binary function $\chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau_t, s_{t-1}, \eta_{t-1})$ which fully represents the optimal solution of Eq. (4) by

$$\chi_{\eta_t}^{\sigma_t}(s_t, \eta_t', \tau_t, s_{t-1}, \eta_{t-1}) = \begin{cases} 1 & \text{if optimal solution for agent } (\tau_t, s_{t-1}, \eta_{t-1}) \text{ is } s_t \text{ and } \eta_t' \\ 0 & \text{otherwise} \end{cases} \quad (5)$$

for all $s_t, s_{t-1} \in S$ and $\tau_t \in T$, and $\eta_{t-1}, \eta_t' \in H$. We refer to this $\chi_{\eta_t}^{\sigma_t}()$ as optimal schooling and job choices in binary form.

In each period the active members of the society will belong to one of the social groups in $S \times H$. Intergenerational social mobility refers in this paper as the mobility of families across the groups in $S \times H$. Let π_t be the probability mass function of the population distributed over the education levels in $S \times H$ in period t , $t \geq 0$. The economy begins at time $t = 1$ with an adult population whose parents' socio-occupational status is distributed as π_0 . Denote by P_t the transition matrix or mobility matrix, rows corresponds the parent's socio-occupational status (s_{t-1}, η_{t-1}) and the columns corresponds to the socio-occupational status that a child will attain, and the elements of the matrix represents the likelihood of the event. Given π_0 , the transition matrix P_t determines the dynamics of the income distribution π_t , the nature of the intergenerational social and occupational mobility, and how they affect the rate of technological progress and the rate of earnings growth over time. In this paper, I provide a signaling model of human capital investment, and job matching that determine the mobility matrix P_t .

2.3. Signaling equilibrium

The signaling equilibrium is recursively defined over time as follows: At the beginning of time period t , π_{t-1} and A_t are already known. Producer η_t knows these and he knows the distribution of τ in the population, but he does not observe agent's family background (s_{t-1}, η_{t-1}) and his productivity level $e(s, \tau, \eta)$. He anticipates a conditional distribution $q_t(e|s; \eta_t)$ as in Eq. (2), and announces the wage profile $A_t w_t(s; \eta_t)$ as in Eq. (3). Given $A_t w_t(s; \eta_t)$, the worker $(\tau_t, s_{t-1}, \eta_{t-1})$ decides the education level and the job $\chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau_t, s_{t-1})$ as in Eq. (5). The optimal decisions together with the distribution of their family background π_{t-1} and talent $g(\tau_t)$ generate the observed distribution $\hat{q}_t(e'|s; \eta_t)$ of productivity level e' given education level s in the job η_t as follows:

$$\hat{q}_t(e'|s; \eta_t) = \frac{\sum_{\tau, (s_{t-1}, \eta_{t-1})} \mathcal{J}_{e'}(e(s, \tau, \eta_t)) \chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1}) \cdot g(\tau) \pi_{t-1}(s_{t-1}, \eta_{t-1})}{\sum_{\tau, (s_{t-1}, \eta_{t-1})} \chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1}) \cdot g(\tau) \pi_{t-1}(s_{t-1}, \eta_{t-1})}, \quad (6)$$

where $I_e(x)$ is an indicator function, which takes value 1 if $x = e$, otherwise it takes value 0. In signaling equilibrium, the anticipated distribution in Eq. (2) coincides with the above observed distribution for each job and each education level that are chosen by some agent. Notice that optimal schooling choices $\chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1})$ determines the transition probability $p_t((s_{t-1}, \eta_{t-1}), (s_t, \eta_t))$ of an individual born in the family background (s_{t-1}, η_{t-1}) , moves to the family background (s_t, η_t) , for all $(s_{t-1}, \eta_{t-1}), (s_t, \eta_t) \in S \times H$ as follows:

$$p_t((s_{t-1}, \eta_{t-1}), (s_t, \eta_t)) = \sum_{\eta_t, \tau_t} \chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1}) g(\tau_t) \quad (7)$$

Let $P_t = [p_t((s_{t-1}, \eta_{t-1}), (s_t, \eta_t))]_{(s_{t-1}, \eta_{t-1}), (s_t, \eta_t) \in S \times H}$ be the transition matrix in period t . Given π_{t-1} , P_t determines π_t according to the following equation

$$\pi_t = \pi_{t-1} P_t \quad (8)$$

and π_{t-1} and $\chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1})$ determine R_t by

$$R_t = \sum_{s_t, \tau_t, \eta_t, (s_{t-1}, \eta_{t-1})} a(s_t, \tau_t, \eta_t) \chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1}) g(\tau_t) \pi_{t-1}((s_{t-1}, \eta_{t-1})) \quad (9)$$

and thus the growth rate, $\gamma(R_t)$ or equivalently, A_{t+1} according to Eq. (1). The economy moves to the next period with known π_t and A_{t+1} , and the above process starts all over again.

Definition 2.1. Given an initial distribution π^0 of social groups $S \times H$, a signaling equilibrium of labor market is a sequence of anticipated distributions $\{q_t(e|s_t; \eta_t)\}_1^\infty$ defined in Eq. (2) and an associated sequence of wage schedules $\{w_t(s_t; \eta_t)\}_1^\infty$ defined in Eq. (3), optimal schooling and job choices in binary form $\{\chi_{\eta_t}^{\sigma_t}(s_t, \eta_t, \tau, s_{t-1}, \eta_{t-1})\}_1^\infty$ defined in Eq. (5), and an associated sequence of transition probability matrices over $S \times H$, $\{P_t\}_1^\infty$ defined in Eq. (7), such that the anticipated distribution $q_t(e|s_t; \eta_t)$ coincide with the observed distribution $\hat{q}_t(e|s_t; \eta_t)$ defined in Eq. (6) for all $t, t \geq 1$.

I do not pursue the existence issues in this paper. In signaling literature, however, the existence of signaling equilibrium is not a problem, the problem is that there exist many of them. How to find them, and select one of them! One approach to equilibrium selection would be to use some refinement

arguments such as the notion of sequential equilibrium, or Bayesian Perfect Equilibrium. These are not explored in this draft. Our focus is instead on issues such as what kind of intergenerational mobility, wage growth and total factor productivity growth the model generates during the transition to a stationary equilibrium, and in the stationary state? Whether there exists multiple equilibria; whether the economy is generating maximum potential growth? Answers to these questions are mostly contained in the transition matrix P_t .

2.4. Classifications of equilibria

Given an equilibrium path of mobility matrices $\{P_t\}$, the income distributions $\{\pi_t\}$, the equilibrium wage schedules $\{w_t(\cdot)\}$, and the flow of spillover scientific knowledge $\{R_t\}$, I define the wage growth rate due to social mobility between period t and $t + 1$ by $\gamma_w = \sum_{i,j \in \mathcal{S} \times \mathcal{H}} [(w_{t+1}(j) - w_t(i))/w_t(i)] P_t(i, j) \pi_t(i)$, and wage growth rate due to total factor productivity growth between period t and $t + 1$ by $\gamma(R_t)$. Notice that the average growth rate of earnings between period t and $t + 1$ is the sum of γ_w and $\gamma(R_t)$.

It is possible to have different types of signaling equilibria. A pure pooling equilibrium is a signaling equilibrium in which all types of agents from all economic backgrounds use the same signal, i.e., $\sigma_t(\tau_t, s_{t-1}, \eta_{t-1})$ is independent of τ_t , s_{t-1} and η_{t-1} for all $t \geq 1$. A strictly separating equilibrium is a signaling equilibrium in which the agents of different talent type and family background use distinct schooling levels, and jobs i.e., $\sigma_t(\tau_t, s_{t-1}, \eta_{t-1}) = \sigma_t(\tau'_t, s'_{t-1}, \eta'_{t-1})$ or $\eta_t^*(\tau_t, s_{t-1}, \eta_{t-1}) = \eta_t^*(\tau'_t, s'_{t-1}, \eta'_{t-1})$ if and only if $\tau_t = \tau'_t$, $s_{t-1} = s'_{t-1}$ and $\eta_{t-1} = \eta'_{t-1}$ for all $t \geq 1$. These are the kinds of equilibria generally studied in the game theory literature.

I define other kinds of signaling equilibria relevant to our context. An equal opportunity equilibrium is one in which $\sigma_t(\tau_t, s_{t-1}, \eta_{t-1}) = \sigma_t(\tau_t, s'_{t-1}, \eta'_{t-1}) \equiv \bar{s}_t(\tau_t)$ say, or $\eta_t^*(\tau_t, s_{t-1}, \eta_{t-1}) = \eta_t^*(\tau_t, s'_{t-1}, \eta'_{t-1}) \equiv \bar{\eta}_t(\tau_t)$ say $\forall s_{t-1}, s'_{t-1} \in S$, $\eta_{t-1}, \eta'_{t-1} \in H$, i.e., all workers of the same talent type get the same education level or get the same job, and hence get paid the same wages, no matter what their family backgrounds are. An equal opportunity separating equilibrium is an equal opportunity equilibrium such that $\bar{s}_t(\tau) \neq \bar{s}_t(\tau')$ or $\bar{\eta}_t(\tau) \neq \bar{\eta}_t(\tau')$ if $\tau \neq \tau'$.

In our framework, the following result is straightforward.

Proposition 2.1. It is impossible to have a strictly separating equilibrium.

In the next section we will consider implicit contracts and show that it is possible to get strictly separating equilibrium.

It is often difficult to compute the equilibrium path of an economic system, and we often like to study the properties of stationary equilibrium, which we define as follows:

Definition 2.2. A stationary signaling equilibrium is a signaling equilibrium in which in every period t , aggregate flow of spillover knowledge R_t , subjective beliefs of the employers $q_t(\cdot)$, and hence the wage schedule, $w_t(\cdot)$, the transition probability matrix of the social groups, P_t , and the distribution of the social groups π_t are all independent of t .

I denote these stationary variables without a time subscript. Notice that in a stationary equilibrium, we have $\pi = \pi P$, i.e., π is an invariant probability distribution with respect to P , and the stationary distributions of population over the social groups in $S \times H$ are the normalized non-negative eigenvectors of the stationary transition matrix P' .

There is some controversy regarding what is the best measure of mobility corresponding to a mobility matrix, P , see [Conlisk \(1990\)](#). We do not use any of those criteria, instead we propose a criterion suitable in our framework: A growth sensitive mobility measure $\mu(P) \equiv R/R_{\max}$, where R is the flow of spillover knowledge and R_{\max} is the maximum flow of spillover knowledge attainable in the economy out of all possible assignments of jobs and education levels to workers. Thus, this measure is bounded between 0 and 1, higher number represents higher growth enhancing mobility. An equilibrium is maximal growth separating if $\mu(P) = 1$. In a stationary equilibrium with a mobility matrix P and an invariant probability distribution π over $S \times H$ the distribution of income is stationary over time, and hence there is no wage growth due to mobility. The positive wage growth that has been reported in many empirical studies on geographical mobility, (see [Jovanovic and Moffitt \(1990\)](#), [Sicherman and Galor \(1990\)](#), among others) is a phenomenon along the transition path.

Note that not all economies will have stationary transition probabilities, nor all equilibria will converge to a stationary equilibrium. I now examine the nature of equilibrium dynamics for various economies. I assume in the rest of the paper except in section 2 that H is a singleton set, and drop η from the arguments of all the entities.

3. Mobility and growth

For simplicity, I consider the following simple economy for much of this paper. Let $T = \{1, 2\}$, $S = \{1, 2\}$. Assume that $a(s, \tau) = 1$ if $s = 2$ and $\tau = 2$, and $a(s, \tau) = 0$ otherwise.

$$e(s, \tau) = \begin{cases} e_1 & \text{if } s = 1, \forall \tau \in \mathcal{T} \\ e_2 & \text{if } s = 2, \tau = 1 \\ e_3 & \text{if } s = 2, \tau = 2 \end{cases} \quad (10)$$

An interpretation of the above is that the workers with education level 1 are unskilled workers and the talent of the unskilled workers do not affect their productivity; however, higher educated talented workers have higher productivity than higher educated not-so-talented workers.

Does there exist any signaling equilibrium, and if there exists one, are there many equilibria? Is there an equal opportunity separating equilibrium? Does any of these equilibria attain maximal growth and social mobility? The answers to these questions depend on the productivity technology $e(\tau, s)$ and the cost function, $\theta(s_t, \tau_t, s_{t-1})$. I assume that the cost function $\theta(s_t, \tau_t, s_{t-1})$ satisfies the following:

$$\left. \begin{aligned} \theta(1, \tau_t, s_{t-1}) &= 0 \forall \tau_t, s_{t-1}, \text{ and} \\ \theta(2, 2, 2) &< \theta(2, 1, 2) < (e_2 - e_1) + p(e_3 - e_2) < \theta(2, 2, 1) < \theta(2, 1, 1) \end{aligned} \right] \quad (11)$$

Signaling equilibrium 1: Suppose the employers in period t hold the following subjective probability distribution $q_t(e|s)$ of productivity level e given his schooling level s , which in matrix form is given by

$$[q_t(e|s)]_{\substack{e=e_1, e_2, e_3 \\ s=1, 2}} = \begin{bmatrix} 1 & 0 \\ 0 & 1-p \\ 0 & p \end{bmatrix}$$

According to [Eq. \(3\)](#), given the above expectations, the employer announces the following wage schedule:

$$w_t(s_t) = \begin{cases} 1 & \text{if } s_t = 1 \\ e_2 \cdot (1-p) + e_3 \cdot p & \text{if } s_t = 2 \end{cases} \quad \text{for all } t \geq 0$$

Given the above wage schedule, one can easily verify that the equilibrium schooling decisions $\sigma_t(\tau_t, s_{t-1})$ of an agent of talent type τ_t from the family background s_{t-1} is as follows:

$$\sigma_t(\tau_t, s_{t-1}) = \begin{cases} 1 & \forall \tau_t \in \mathcal{T} \text{ if } s_{t-1} = 1 \\ 2 & \forall \tau_t \in \mathcal{T} \text{ if } s_{t-1} = 2 \end{cases} \quad \text{for all } t \geq 0$$

It can be easily checked that given the above optimum solution, the observed conditional probability distribution of e given s_t will coincide with the anticipated one. Note that the transition matrix associated with $\sigma_t(\cdot)$ is the following:

$$P_t = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \forall t \geq 0$$

Thus in this economy there is no intergenerational mobility. Furthermore, the economy is in steady-state from the beginning. Thus, $R_t = p \cdot \pi_0^2$, and hence the productivity growth rate is given by $\gamma(p\pi_0^2)$ which is strictly less than $\gamma(p)$, the maximum attainable productivity growth rate for the economy when all talented individuals from all socio-occupational groups obtain higher education.

This equilibrium is not equal opportunity separating, nor maximal growth separating type. In this equilibrium, all talent types of the children from each type of family backgrounds are pooled.

Could there be any other equilibrium for the above economy? For a certain subclass of the above economies, there is another equilibrium, which is growth enhancing separating and is Pareto superior to the above equilibrium. To see this, consider the following:

Signaling equilibrium 2: let $v_t \equiv \frac{p}{p\pi_{t-1}^1 + \pi_{t-1}^2}$. Note that $v_t > p \forall t \geq 1$. At $t = 1$, v_1 is known. Let us suppose that apart from the assumption [Eq. \(10\)](#), the cost function also satisfies the condition:

$$\theta(2, 2, 1) < (e_2 - e_1) + v_1 (e_3 - e_2) < \theta(2, 1, 1)$$

Suppose the employer holds the following subjective probability distribution for the productivity type E_t given S_t :

$$\bar{q}_t(e|s) = \begin{bmatrix} 1 & 0 \\ 0 & 1 - v_t \\ 0 & v_t \end{bmatrix} \quad \text{for all } t \geq 1 \quad (12)$$

According to [Eq. \(3\)](#), given above expectations, the employer announces the following wage schedule:

$$\bar{w}(s_t) = \begin{cases} 1 & \text{if } s_t = 1 \\ e_2 \cdot (1 - v_t) + e_3 \cdot v_t & \text{if } s_t = 2 \end{cases}$$

Given the above wage schedule, the original $\sigma_t(\tau_t, s_{t-1})$ will be optimal for all (τ_t, s_{t-1}) except for $\tau_t = 2, s_{t-1} = 1$, who will choose $s_t = 2$. It can be easily checked that for this optimal solution,

the observed conditional probability distribution of e_t given s_t will coincide with the anticipated one in equation Eq. (12). Note that the transition matrix associated with this new optimal schooling decision $\bar{s}_t^*(.)$ is as follows:

$$\bar{P}_t = \begin{pmatrix} 1-p & p \\ 0 & 1 \end{pmatrix}$$

Thus in this economy there is intergenerational mobility. The proportion of population with higher education will go on increasing and the proportion of the population with lower education will go on decreasing. This process, however, cannot go on for ever, since in that case $v_t \rightarrow p$, as $t \rightarrow \infty$, which will mean that there will be some finite $t_0 > 1$ such that $v_{t_0} > \theta(2, 2, 1)$ for the first time and then on the equilibrium will switch on to the previous one with no mobility. Note, however that the new steady-state equilibrium growth rate will be $\gamma(\pi_{t_0}^2 \cdot p)$ since $\pi_{t_0}^2 > \pi_0^2$. Furthermore, the short-run growth rate up to period t_0 , is higher in the second equilibrium than in the first type; and the second equilibrium is Pareto superior to the first.

Furthermore, notice that there will be a positive wage growth during all periods $t \leq t_0$, and after t_0 , the source of growth is only from factor productivity growth.

Thus, in this economy there may exist multiple equilibria; which one will actually realize depends on the expectations of the employers. The question is then, how the employer's expectations are formed? We need a theory of expectations formation of the producers to select an equilibrium, and we do not pursue this theory here.

Also note that the first signaling equilibrium will be in stationary state from time $t = 1$, will produce no social mobility in any periods. The second signaling equilibrium will produce upward mobility from social class $s = 1$ to $s = 2$ up to time $t = t_0$ according to the transition matrix \bar{P}_t , and during this period, there will be a positive wage growth due to upward mobility; after period t_0 , however, the process will revert to the mobility pattern of the first signaling equilibrium. Two equilibria, however, will produce two different long-run income distributions.

4. Labor Market Practices

In the previous model, we always have pooling equilibrium, which restricts mobility and wage growth, and hence reduces economic growth. The main reason for the impossibility of having a strictly separated equilibrium is that there are $\hat{s} \cdot \hat{\tau}$ types of agents but there are only \hat{s} signal classes,

and the fact that employers are allowed only to use one-time non-renegotiable wage contracts during the tenure of the employment. Relaxing this assumption, and allowing other kinds of implicit or explicit contracts in which workers may be laid-off or demoted if his productivity is seen to be low, or the worker may be promoted or else he quits if he is found to be more productive worker after working with the firm for a while.

Suppose we allow those labor market practices. Since workers anticipate those practices, some workers with low innate abilities, who found a higher education more lucrative because he was pooled with the higher innate ability workers, may now find it is not lucrative because of the possibility of on the job screening. He will self-select not to have higher education. Thus the possibility of on the screening may lead to more separating equilibria. In the next two subsections, I extend the model of the previous section by introducing wage contracts as gambles, and allow more than one type of employers, and then examine to what extent these labor market features can lead to further separation of signaling equilibrium.

4.1. Quits, layoffs, and promotion

I assume that the productivity function of the worker $e(\cdot)$ does not contain the random shock term ϵ and further assume that the production technology of the economy is such that $e(s, \tau) \neq e(s, \tau')$ whenever $\tau \neq \tau'$ for all s, τ, τ' . In that case, the employer can fully predict the talent type of the worker by observing his output. The employer would like to lay-off the low productive worker or demote him, and encourage the more productive workers to stay with higher pays; both types of workers may quit, however. The problem is that often the employer cannot observe the productivity level of the worker. He might, however, observe another random variable $Y(s, \tau)$ which he uses to predict the productivity level of the worker with school level s and ability τ . To simplify exposition, I assume that $Y(s, \tau) \equiv e(s, \tau)$, i.e., the employer can observe the productivity level of the worker.

To proceed more formally, assume that time period t is divided into two sub periods t and $t.5$. and that total wages during a period will be paid in two installments. Consider the following kind of sorting wage contracts:

If the worker's schooling level is s then he will be paid w_0 in the first subperiod and during the second subperiod will be paid a gamble, $w_{t.5}$, which will take value w_* if his realized productivity level is less than $c > 0$, a constant (i.e., he is not promoted) and w^* if his realized output is larger than c (i.e., he is promoted).

Thus under this contract, a worker receives $w(s) = w_0 + Ew_{t.5}$. Notice that these kind of contracts also include the simpler contracts of the previous section, where $w_0 = w(s)/2$ and $w_{t.5} = w(s)/2$ with probability 1. What kind of labor contracts can evolve in the competitive markets, and could it lead to ability separating and growth enhanced separating equilibrium? As the following proposition shows, it depends on the nature of the schooling cost function, and the nature of the contracts and the value of c .

Consider the following specific sorting wage contract w^* :

If a worker's schooling level is $s = 1$, he will be paid $e_1/2$ in both sub-periods; if his schooling level is $s = 2$, he will receive $e_2/2$ in the first sub-period and in the second sub-period $e_2/2$ if his realized productivity level is $\tau = 1$ (i.e., if he is not promoted) and he will receive $e_3/2$, which is his true productivity, and also a bonus $(e_3 - e_1)/2$, if his realized productivity level is $\tau = 2$ (i.e., if he is promoted).

The following two classes of economies will be used for our result:

$$\begin{aligned} \theta(2, 2, 1) &< (e_3 - e_1) < \theta(2, 1, 1) \dots (a) \\ \theta(2, 2, 2) &< (e_2 - e_1) < \theta(2, 1, 2) \dots (b) \end{aligned} \tag{13}$$

Proposition 4.1. For economies satisfying conditions (a) in Eq. (13), and Eq. (11), the sorting wage contract w^* above is a signaling equilibrium wage contract. If, furthermore, conditions (b) in Eq. (13) are satisfied then the resulting equilibrium is equal opportunity ability separating.

There could be other type of contracts which can produce the same result as in the above proposition, they are basically equivalent to the above contract w^* in the sense that no other contract can pay higher amount while maintaining the zero profit condition on the employers. The situation gets more complicated and interesting when we allow randomness in the productivity function. This will be incorporated in the revised draft.

Notice that the class of economies satisfying conditions in the above proposition is a subclass of economies of the previous section. So the two signaling equilibria considered in the previous section are also signaling equilibria of the economy considered in the above proposition. But if employers are competitive and government regulations did not prevent employers from announcing above type of contracts, the perfect competition will rule out these two pooling equilibrium.

4.2. Labor Market Signaling and Job Matching

We now like to investigate if the presence of various jobs in which productivity level varies for given ability and education levels, can help to achieve further separation. Furthermore, we would like to investigate if market signaling can help in matching workers to jobs, an aspect of job matching that is mostly ignored in the job matching literature.

The basic structure of our model is very similar to that of Jovanovic (1979); the main essential difference between his model and the present model is that we assume signaling based matching, whereas Jovanovich assumes a random matching in a search theoretic framework. To keep our analysis to simplest form, we consider an economy with two productive sectors: $\eta = 1$ and $\eta = 2$. Both sectors employ skilled labor and unskilled labor. Assume that the sector $\eta = 2$ is more research intensive and sector $\eta = 1$ is less research intensive. We assume the flow of spillover knowledge depends on job as follows: $a(s, \tau, \eta) = 1$ if $s = 2$, $\tau = 2$, and $\eta = 2$, and $a(s, \tau, \eta) = 0$ otherwise. The following table summarizes the match specific productivity level $e(s, \tau, \eta)$ to various levels of schooling s , talent τ and sector η combinations.

	$s = 1$		$s = 2$	
	$\tau = 1$	$\tau = 2$	$\tau = 1$	$\tau = 2$
$\eta = 1$	e_1	e_1	e_2	e_3
$\eta = 2$	e_1	e_1	$e_2 - \epsilon$	$e_3 + \frac{1-p}{p} \cdot \epsilon$

Notice that the two signaling equilibria of the previous section are also equilibria of the above economy. As I have illustrated earlier, in these two equilibria, the market does not produce incentive structure for best matching of workers to jobs. If, however, the employers use on-the-job screening device of the previous subsection, the economy generates a better matching of workers to job. In fact, one can attain a maximal growth separating pooling equilibrium. To see this, consider the following wage contracts:

For each employer $\eta = 1$ and $\eta = 2$, the wage contract is of the same form as in the previous subsection, with the exception that in place of e_2 and e_3 of the previous contract, we use the corresponding productivity values from the above table for η .

Proposition 4.2. For the class of economies satisfying conditions in Eq. (11), (a) in Eq. (13), and $e_3 - e_1 > \theta(2, 1, 2)$, job matching is achieved in the market through education signaling and self-selection, and it is more separated than the equilibrium in the previous proposition. In equilibrium

nobody gets fired nor anybody quits.

Notice that we are not able to obtain strictly separating equilibrium in the above proposition because we assumed for $s = 1$ that $e(s, \tau, \eta) = e_1$ for all τ and η . Suppose instead there is an employer for whom $e(s, \tau, \eta)$ varies with τ , we can then find conditions on the cost of schooling that will lead to strictly separating equilibrium.

Notice, however, that strictly separating equilibrium, or even maximal growth separating equilibrium is attained only when schooling costs satisfy the conditions in the above propositions. But there are economies which cannot achieve strict separability or even growth maximizing separability or an equal opportunity separability when talented children from poorer family background have higher costs than what the above propositions imply. Notice also that it is not possible for private employers to subsidize such socially disadvantaged children and tie them to work for the company after completing school, unless the company is subsidized by the government (because the net profit from such wage contract is always negative in equilibrium).⁹ This problem can be handled only in the school system, which we turn next.

5. Educational Systems: public, private, school voucher

What should be the right kind of education policy that can lead to higher mobility and economic growth depends on the school system. There are various types of educational systems adopted by various countries: in some systems, schools are completely public, for instance, in Korea; most countries have dual system with both public and private schools, for instance, in India and the US. Generally the public schools are free but their qualities depend a great deal on the budget it receives from the government, which in turn depends, in some countries such as the US, on the pool of property taxes raised in the neighborhood in which the school is located. Since children living in a particular neighborhood can only attend its public school, we can see immediately that children from poorer family background face higher cost of schooling. There are many other reasons for higher cost, we do not discuss them here.

If one of the objectives of an educational system is to attain higher social mobility and higher income growth, from our analysis so far, it is clear that the talented children must get higher education and get placed in the growth enhancing sectors. Many times competitive labor market may not be able to produce enough economic incentives for the children of the poorer family background to achieve

⁹These kinds of tied transfers are generally observed in army recruiting and rarely in private sector if there are no tax advantages to such subsidies.

higher education. While higher education for all might be an important social goal by itself, but given resource constraints, a society might focus on identifying the more talented individuals of poorer family background, and give them only the required subsidy so that they can attain higher education and work in the growth enhancing technical sectors. Poorer the family background, the higher is the subsidy needed. Where would the money come from for such subsidies? Recall that these talented individuals can create higher income for the future generation by creating a positive knowledge; moreover, assuming that productivity function $e(s, \tau, \eta)$ represents productivity net of pay-roll taxes, with higher mobility, there is higher income growth during the transition to long-run equilibrium, and with progressive or even with proportionate taxes on earnings, the government should be able to raise the required subsidy money. But all children look alike, and they do not wear a tag indicating their talent level, how could the talented ones be identified?

I argue that this could be done with school voucher system. To see it how, assume that only the private schools provide higher quality education and the public schools provide lower quality education. Any one who can afford can attain a private school; however, whether one will pass the curriculum of a private school, depends on the innate ability and family background of the student. These effects are, however, already reflected in the cost differences. If the voucher for a child of particular family background is such that the voucher reduces the cost of the talented child just enough so that he can attain the higher quality education, then the students or their parents will self-select to receive voucher only for talented children and not so talented ones would rather self-select to go to public school system. Alternatively, government can use the subsidy money to improve the quality of the public schools attained by the children of poorer family backgrounds, so much so that the public schools are of the same quality as the private school. This can also lead to higher social mobility and growth. What kind is a better education policy is an area of constant academic research and focus of continuing political debates in the US congress and elsewhere.

To get a better idea, consider the economy of section 3. Suppose the government announces a voucher of \$0.50 to a child of family background 1, which must be used for the sole purpose of attaining school level 3. This policy will move the economy to another stationary equilibrium in which the equilibrium subjective probability matrix expressing employer's beliefs, $q(e|s)$, the mobility matrix of the three income groups P , the associated invariant distribution of income π , and the income levels $w(s)$, $s = 1, 2, 3$ are as follows:

$$q(e|s) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad P = \begin{bmatrix} 1-p & 0 & p \\ 1-p & 0 & p \\ 0 & 1-p & p \end{bmatrix} \quad \pi' = \begin{bmatrix} (1-p)^2 \\ p(1-p) \\ p \end{bmatrix} \quad w = \begin{bmatrix} 1 \\ 2 \\ 4 \end{bmatrix}$$

It is also clear that in this case our measure of mobility $\mu(P) = 1$, and the growth rate is the highest possible. To get a better insight, let us consider the numerical example. For this specific economy, a subsidy of 0.50 per individual will achieve the goal. Total cost to subsidize all the talented individuals of the old stationary equilibrium is \$0.059; but it will improve the total factor productivity growth rate from 2.74% to 14.02%. Thus it might be worthwhile. Also notice that income distribution will become more egalitarian in the long run, which is given by $\pi' = (0.5329, 0.1971, 0.27)$ as compared to the earlier one $\pi = (0.6637, 0.24551, 0.0908)$.

It should be noted that a highly regulated public educational system with competitive bidding for entry into a limited number of higher education slots, can also achieve the same objective of growth and social mobility. This system was introduced by Park regime in South Korea and is believed to have attained a high degree of economic growth and social mobility. There are many other dimensions to the political and academic debate on educational policies, see for instance, [Stiglitz \(1975\)](#) in an imperfect information context, and [Becker \(1962\)](#) in a perfect information context.

6. Policies and conclusions

In this paper, we have considered a model of intergenerational social mobility and economic growth, in which innate ability of workers, and the type of their education and jobs determine the rate of technological progress and social mobility. More talented individuals with higher education and working in the growth enhancing sectors can lead to higher rate of technical progress and wage growth. Moreover, higher is the rate of mobilization of these talented individuals to higher education and growth sectors, the higher is the rate of social mobility. The incentive structure in the labor market that matches workers to jobs, together with the talent level and cost of education of individuals of various social backgrounds, determine the incentives for various types of education for individuals. Important features of our model are that the innate ability of an individual is a private knowledge, i.e., (possibly) known only to the individual and that education not only increases productivity of the individual, more so for an higher ability individual, it also acts, at least at the time of initial hiring, as a signaling for individual's innate productive ability for the purpose of job matching in the labor market.

In economies with one-time non-renegotiable wage contracts¹⁰, it is shown that the asymmetric information regarding innate ability (hence productivity level) of workers leads to existence of multiple signaling equilibria arising from multiplicities of unprejudiced employers' self-fulfilling beliefs regarding the relationship between schooling and productivity. These equilibria vary in the degree of social mobility and economic growth, and all of them could be inefficient in the sense of being far from generating the maximum possible rate of social mobility and economic growth. Furthermore, there are no natural *refinements* based on economic grounds that can lead to selection of an equilibrium.

The paper considered various labor market practices¹¹ such as implicit contracts involving quits, layoffs, promotions and demotion of workers based on the employer's or worker's assessments of realized productivity on the job, and explicit wage contracts contingent upon the outcome of some publicly observed indicator of one's actual productivity. It is shown that these labor market practices can lead to removal of some of the above inefficiencies and thus to a higher rate of economic growth and social mobility. The remaining impediments to economic growth and social mobility can only be removed by intervening in the educational system.

The paper considered briefly various school systems — purely public systems such as in South Korea, and dual systems with both private and public education such as in India and the US. It is argued that, within the dual private-public system, subsidies or school vouchers for higher education to children from poorer family backgrounds can lead to self-selection of the more talented ones with the poorer backgrounds into higher education and growth enhancing jobs, and hence to higher social mobility and economic growth in a cost effective way. It also follows from our analysis that increasing average education level of the population may not be the most effective way of raising the growth rate.

In most countries, especially in less developed countries, higher education is highly subsidized by the government. If the source of lower social mobility is due to higher cost of education faced by children of poorer family background, subsidizing higher education uniformly for children of all family backgrounds is not necessarily going to be effective in inducing the talented children from poorer family background to opt for higher education.

The paper has the following implication for the proposed educational policy allowing children to borrow for college education. This will be effective only to the students on the margin who have

¹⁰By this we mean an employment contract in which wage is a function of schooling level only, which is offered during hiring, and not renegotiated later during the tenure of the employment upon receiving further information about the worker's innate ability.)

¹¹These institutions themselves might be the result of asymmetric information.

enough preschool investment so that the rate of return from college is higher than the interest rate on the loan. For those with poorer family background, they would need loans at lower interest rates, or their parents should be given targeted subsidies for the purpose of prenatal and preschool investment to reduce their children's cost of higher education.

The practical relevance of the above types of policies hinges on important empirical questions: How to estimate the schooling cost as a function of schooling level, schooling type, school quality, family background and innate ability? How much more scope remains in an economy to reduce inefficiency by developing appropriate labor market practices? Another important empirical issue in this connection is to examine if observed educational attainment and job assignments of individuals in a society are according to their innate ability, or according to their family backgrounds. The existence of multiple equilibria arising from unprejudiced employer's self-fulfilling expectations also raises important empirical questions: How to verify whether an economy is stuck with a low level equilibrium where growth rate, and social mobility are low, and how to design policies that will allow the economy to move from a low level equilibrium to an equilibrium with higher growth and social mobility?

The framework proposed here could be calibrated using real data and be used to carry out various policy analyses regarding the cost of schooling subsidies, or school vouchers, and benefits that will accrue to the society in terms higher mobility, faster economic growth, and more egalitarian income distribution. In our future work, we plan to pursue some of these issues using the NLSY (National Longitudinal Surveys of Youths) data for the US.

Bibliography

- [1] Adams, J. D. Fundamental Stocks of Knowledge and Productivity Growth. English, *Journal of Political Economy*, **98**, no. 4 (1990), pp. 673–702. DOI: [10.1086/261702](https://doi.org/10.1086/261702) (cit. on p. 2).
- [2] Becker, G. S. Investment in Human Capital: A Theoretical Analysis, *Journal of Political Economy*, **70**, no. 5, Part 2 (1962), 9–49. DOI: [10.1086/258724](https://doi.org/10.1086/258724) (cit. on pp. 3, 20).
- [3] Becker, G. S. and Tomes, N. An Equilibrium Theory of the Distribution of Income and Intergenerational Mobility, *Journal of Political Economy*, **87**, no. 6 (Dec. 1979), 1153–1189. DOI: [10.1086/260831](https://doi.org/10.1086/260831) (cit. on p. 3).
- [4] Becker, G. S. and Tomes, N. Human Capital and the Rise and Fall of Families, *J. Lab. Econ.* (1986) (cit. on p. 3).
- [5] Ben-Porath, Y. The Production of Human Capital and the Life Cycle of Earnings, *Journal of Political Economy*, **75**, no. 4, Part 1 (1967), 352–365. DOI: [10.1086/259291](https://doi.org/10.1086/259291) (cit. on p. 3).
- [6] Coe, D. and Helpman, E. Internal R&D Spillovers, *European Economic Review*, **39** (1995), 859–887 (cit. on p. 2).
- [7] Conlisk, J. Monotone mobility matrices, *The Journal of Mathematical Sociology*, **15**, no. 3–4 (Jan. 1990), 173–191. DOI: [10.1080/0022250x.1990.9990068](https://doi.org/10.1080/0022250x.1990.9990068) (cit. on p. 11).
- [8] Daniel, K. et al. College quality and the wages of young men, (1997) (cit. on p. 4).
- [9] Gottfredson, L. S. Why g matters: The complexity of everyday life, *Intelligence*, **24**, no. 1 (1997), 79–132. DOI: [https://doi.org/10.1016/S0160-2896\(97\)90014-3](https://doi.org/10.1016/S0160-2896(97)90014-3) (cit. on p. 4).
- [10] Griliches, Z. and Mason, W. M. Education, Income, and Ability, *Journal of Political Economy*, **80**, no. 3, Part 2 (May 1972), S74–S103. DOI: [10.1086/259988](https://doi.org/10.1086/259988) (cit. on p. 5).
- [11] Heckman, J. et al. *Does Measured School Quality Really Matter? An Examination of the Earnings-Quality Relationship*. Tech. rep. Sept. 1995. DOI: [10.3386/w5274](https://doi.org/10.3386/w5274) (cit. on p. 4).
- [12] Heckman, J. J. Lessons from the Bell Curve, *Journal of Political Economy*, **103**, no. 5 (1995), 1091–1120. DOI: [10.1086/262014](https://doi.org/10.1086/262014) (cit. on p. 4).
- [13] Herrnstein, R. and Murray, C. *The Bell Curve: Intelligence and Class Structure in American Life*. 1st Free Press pbk. ed. Free Press, 1994 (cit. on p. 4).
- [14] Jaffe, A. Technological Opportunity and Spillovers of R&D: Evidence from Firms’ Patents, Profits and Market Value, (Jan. 1986). DOI: [10.3386/w1815](https://doi.org/10.3386/w1815) (cit. on p. 2).
- [15] Jovanovic, B. Job Matching and the Theory of Turnover, *Journal of Political Economics* (1979) (cit. on pp. 3, 17).
- [16] Jovanovic, B. and Moffitt, R. An Estimate of a Sectoral Model of Labor Mobility, *Journal of Political Economy*, **98**, no. 4 (Aug. 1990), 827–852. DOI: [10.1086/261708](https://doi.org/10.1086/261708) (cit. on p. 11).
- [17] Kreps, D. M. *A course in microeconomic theory*. Harvester Wheatsheaf New York, 1990 (cit. on pp. 6, 7).
- [18] Loury, G. Intergenerational Transfers and the Distribution of Earnings, *Econometrica* (1981) (cit. on p. 3).
- [19] Loury, G. Is Equal Opportunity Enough?, *American Economic Review* (1981) (cit. on p. 3).
- [20] Lucas, R. E. On the mechanics of economic development, *Journal of Monetary Economics*, **22**, no. 1 (1988), 3–42. DOI: [10.1016/0304-3932\(88\)90168-7](https://doi.org/10.1016/0304-3932(88)90168-7) (cit. on p. 2).

- [21] Mincer, J. Investment in Human Capital and Personal Income Distribution, *Journal of Political Economics* (1958) (cit. on pp. 3, 5).
- [22] Raut, L. K. Capital accumulation, income distribution and endogenous fertility in an overlapping generations general equilibrium model, *Journal of Development Economics*, **34**, no. 1-2 (Nov. 1990), 123–150. DOI: [10.1016/0304-3878\(90\)90079-q](https://doi.org/10.1016/0304-3878(90)90079-q) (cit. on p. 7).
- [23] Raut, L. K. R & D spillover and productivity growth: Evidence from Indian private firms, *Journal of Development Economics*, **48**, no. 1 (Oct. 1995), 1–23. DOI: [10.1016/0304-3878\(95\)00028-3](https://doi.org/10.1016/0304-3878(95)00028-3) (cit. on p. 2).
- [24] Rosen, S. Human capital: relations between education and earnings, *Frontiers of quantitative economics*, **3** (1977), 731–53 (cit. on p. 3).
- [25] Rothschild, M. and Stiglitz, J. E. Increasing risk: I. A definition, *Journal of Economic Theory*, **2**, no. 3 (1970), 225–243. DOI: [10.1016/0022-0531\(70\)90038-4](https://doi.org/10.1016/0022-0531(70)90038-4) (cit. on p. 6).
- [26] Roy, A. D. Some Thoughts on the Distribution of Earnings, *Oxford Economic Papers*, **3**, no. 2 (1951), 135–146 (cit. on p. 4).
- [27] Sicherman, N. and Galor, O. A Theory of Career Mobility, *Journal of Political Economy*, **98**, no. 1 (Feb. 1990), 169–192. DOI: [10.1086/261674](https://doi.org/10.1086/261674) (cit. on p. 11).
- [28] Spence, M. Job Market Signaling, *The Quarterly Journal of Economics*, **87**, no. 3 (1973), 355–374 (cit. on pp. 3, 7).
- [29] Stiglitz, J. E. The Theory of "Screening," Education, and the Distribution of Income, *The American Economic Review*, **65**, no. 3 (1975), 283–300 (cit. on p. 20).
- [30] Willis, R. J. "Chapter 10 Wage determinants: A survey and reinterpretation of human capital earnings functions", vol. 1. Handbook of Labor Economics. Elsevier, 1986, 525–602. DOI: [10.1016/S1573-4463\(86\)01013-1](https://doi.org/10.1016/S1573-4463(86)01013-1) (cit. on pp. 3, 5).