

Module 43

Partha Pratim Das

Objectives 8
Outline

B+-Tree Index Files

Simple B⁺ Tre

Index Files

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Observation

Observation

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Non-Unique Ke
Relocation and
Secondary Indic

B-Tree Inde

Comparison

Module Summar

Database Management Systems

Module 43: Indexing and Hashing/3: Indexing/3

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Module Recap

Module 43

Objectives & Outline

- Recapitulated the notions of Balanced Binary Search Trees as options for optimal in-memory search data structures
- Understood the issues relating to external data structures for persistent data
- Explored 2-3-4 Tree in depth as a precursor to B/B+-Tree for an efficient external data structure for database and index tables

Module Objectives

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Objectives & Outline

• To understand the design of B⁺ Tree Index Files as a generalization of 2-3-4 Tree

• To understand the fundamentals of B-Tree Index Files

Module Outline

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Objectives & Outline

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B-Tree Index Files

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- B⁺ Tree Index Files
- B-Tree Index Files

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B-Tree Inde Files

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B⁺ Tree Index Files

Database Management Systems



B⁺ Tree

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Nodes Observations Query

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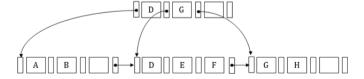
Insertion

Deletion

File Organization Non-Unique Keys Relocation and Secondary Indices Strings

B-Tree Index Files Comparison The B⁺ Tree

- Is a balanced binary search tree
 - o Follows a *multi-level index* format like 2-3-4 Tree
- Has the leaf nodes denoting actual data pointers
- Ensures that all *leaf nodes remain at the same height* (like 2-3-4 Tree)
- Has the leaf nodes are linked using a link list
 - o Can support random access as well as sequential access
- Example:

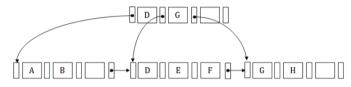




B⁺ Tree (2)

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Simple B+ Tree



- Internal node contains
 - At least $\frac{n}{2}$ child pointers, except the root node
 - At most *n* pointers
- Leaf node contains
 - At least $\frac{n}{2}$ record pointers and $\frac{n}{2}$ key values
 - \circ At most \overline{n} record pointer and \overline{n} key values
 - One block pointer P to point to next leaf node

Note: These are approximate values, we will discuss more precise values later in this lecture.



B⁺ Tree (3): Search

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Objectives Outline

B+-Tree Inde

Simple B⁺ Tree

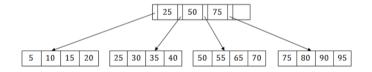
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B-Tree Index Files Comparison

- Suppose we have to search 55 in the B⁺ tree below
 - First, we will fetch for the intermediary node which will direct to the leaf node that can contain a record for 55
- So, in the intermediary node, we will find a branch between 50 and 75 nodes
 - o Then at the end, we will be redirected to the third leaf node
 - \circ Here DBMS will perform a sequential search to find 55





B⁺ Tree (3): Insert

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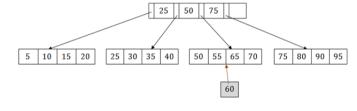
Query

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B-Tree Index Files Comparison



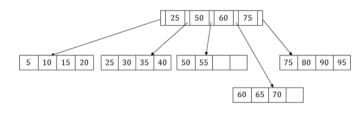
- Suppose we want to insert a record 60 that goes to 3rd leaf node after 55
- The leaf node of this tree is already full, so we cannot insert 60 there
- So we have to split the leaf node, so that it can be inserted into tree without affecting the fill factor, balance and order
- The 3rd leaf node has the values (50, 55, 60, 65, 70) and its current root node is 50
- We will split the leaf node of the tree in the middle so that its balance is not altered



B⁺ Tree (4): Insert

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Simple B⁺ Tree



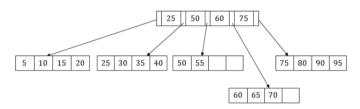
- So we can group (50, 55) and (60, 65, 70) into 2 leaf nodes
- If these two has to be leaf nodes, the intermediate node cannot branch from 50
- It should have 60 added to it, and then we can have pointers to a new leaf node
- This is how we can insert an entry when there is overflow. In a normal scenario, it is very easy to find the node where it fits and then place it in that leaf node



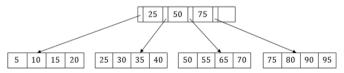
B⁺ Tree (5): Delete

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Simple B+ Tree



- To delete 60, we have to remove 60 from intermediate node as well as 4th leaf node
- If we remove it from the intermediate node, then the tree will not remain a B+ tree
- So with deleting 60 we re-arranging the nodes:





B⁺ Tree Index Files

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B+-Tree Inde Files Simple B⁺ Tree Index Files Nodes Observations

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3-Tree Index

3-Tree Index Files Comparison

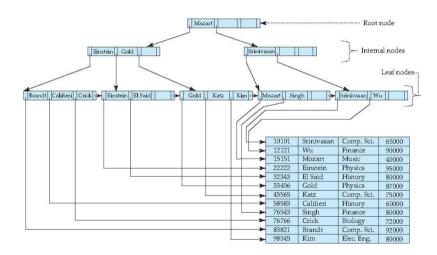
- B⁺ tree indices are an alternative to indexed-sequential files
- Disadvantage of ISAM files
 - o Performance degrades as file grows, since many overflow blocks get created
 - Periodic reorganization of entire file is required
- Advantage of B⁺ tree index files:
 - Automatically reorganizes itself with small, local, changes, in the face of insertions and deletions
 - o Reorganization of entire file is not required to maintain performance
- (Minor) disadvantage of B⁺ trees:
 - o Extra insertion and deletion overhead, space overhead
- Advantages of B⁺ trees outweigh disadvantages
 - B⁺ trees are used extensively



B⁺ Tree Index Files (2): Example

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Index Files



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B⁺ Tree Index Files (3): Structure

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B-Tree Inde Files Comparison A B⁺ tree is a rooted tree satisfying the following properties:

- All paths from root to leaf are of the same length
- Each node that is not a root or a leaf has between $\lceil \frac{n}{2} \rceil$ and n children
- ullet A leaf node has between an $\lceil \frac{n-1}{2} \rceil$ and n-1 values
- Special cases:
 - o If the root is not a leaf, it has at least 2 children.
 - o If the root is a leaf (that is, there are no other nodes in the tree), it can have between 0 and (n-1) values.



B⁺ Tree Index Files (4): Node Structure

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B-Tree Inde Files Comparison Typical node

P_1	K_1	P_2		P_{n-1}	K_{n-1}	P_n
-------	-------	-------	--	-----------	-----------	-------

- \circ K_i are the search-key values
- \circ P_i are pointers to children (for non-leaf nodes) or pointers to records or buckets of records (for leaf nodes).
- The search-keys in a node are ordered

$$K_1 < K_2 < K_3 < \cdots < K_{n-1}$$

(Initially assume no duplicate keys, address duplicates later)



B⁺ Tree Index Files (5): Leaf Nodes

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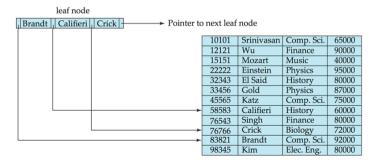
Updates
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B-Tree Inde Files Comparison

Properties of a leaf node

- For $i = 1, 2, \dots, n-1$, pointer P_i points to a file record with search-key value K_i ,
- If L_i, L_j are leaf nodes and i < j, L_i 's search-key values are less than or equal to L_j 's search-key values
- \bullet P_n points to next leaf node in search-key order





B⁺ Tree Index Files (6): Non-Leaf Nodes

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Nodes

- Non leaf nodes form a multi-level sparse index on the leaf nodes. For a non-leaf node with *m* pointers:
 - \circ All the search-keys in the subtree to which P_1 points are less than K_1
 - \circ For 2 < i < n-1, all the search-keys in the subtree to which Pi points have values greater than or equal to K_{i-1} and less than K_i
 - All the search-keys in the subtree to which Pn points have values greater than or equal to K_{n-1}

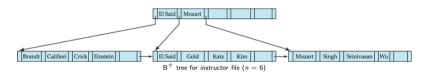
P_1 K_1 P_2		P_{n-1}	K_{n-1}	P_n
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B⁺ Tree Index Files (7): Example

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Nodes



- Leaf nodes must have between 3 and 5 values: $\lceil \frac{n-1}{2} \rceil$ and n-1, with n=6
- Non-leaf nodes other than root must have between 3 and 6 children: $\lceil \frac{n}{2} \rceil$ and n with n = 6
- Root must have at least 2 children



B⁺ Tree Index Files: Observations

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B-Tree Index Files Comparison

- Since the inter-node connections are done by pointers, *logically* close blocks need not be *physically* close
- The non-leaf levels of the B⁺ tree form a hierarchy of sparse indices
- The B⁺ tree contains a relatively small number of levels
 - Level below root has at least $2 * \left\lceil \frac{n}{2} \right\rceil$ values
 - Next level has at least $2 * \lceil \frac{n}{2} \rceil * \lceil \frac{n}{2} \rceil$ values
 - o ... etc.
 - o If there are K search-key values in the file, the tree height is no more than $\lceil log_{\lceil n/2 \rceil}(K) \rceil$
 - o thus searches can be conducted efficiently
- Insertions and deletions to the main file can be handled efficiently, as the index can be restructured in logarithmic time

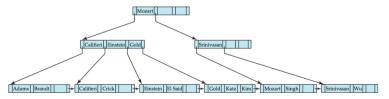


B⁺ Tree Index Files: Queries

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• Find record with search-key value V

- a) C = root
- b) While C is not a leaf node
 - i) Let i be least value such that $V < K_i$
 - ii) If no such exists, set C = last non-null pointer in C
 - iii) Else { if $(V = K_i)$ Set $C = P_{i+1}$ else set $C = P_i$ }
- c) Let i be least value s.t. $K_i = V$
- d) If there is such a value i, follow pointer Pi to the desired record
- e) Else no record with search-key value k exists





B⁺ Trees Index Files: Queries (2)

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B-Tree Inde Files Comparison

- If there are K search-key values in the file, the height of the tree is no more than $\left\lceil log_{\left\lceil \frac{n}{2} \right\rceil}(K) \right\rceil$
- A node is generally the same size as a disk block, typically 4 kilobytes
 - o and n is typically around 100 (40 bytes per index entry)
- With 1 million search key values and n = 100
 - \circ at most $log_{50}(1,000,000) = 4$ nodes are accessed in a lookup
- Contrast this with a balanced binary tree with 1 million search key values around 20 nodes are accessed in a lookup
 - above difference is significant since every node access may need a disk I/O, costing around 20 milliseconds



B⁺ Tree Index Files: Handling Duplicates

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B-Tree Inde Files With duplicate search keys

- o In both leaf and internal nodes,
 - \triangleright we cannot guarantee that $K_1 < K_2 < K_3 < \cdots < K_{n-1}$
 - \triangleright but can guarantee $K_1 \leq K_2 \leq K_3 \leq \cdots \leq K_{n-1}$
- Search-keys in the subtree to which P_i points
 - \triangleright are $\le K_i$, but not necessarily $< K_i$,
 - \triangleright To see why, suppose same search key value V is present in two leaf node L_i and L_{i+1} . Then in parent node K_i must be equal to V



B⁺ Tree Index Files: Handling Duplicates (2)

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B-Tree Inde Files Comparison • We modify find procedure as follows

- \circ traverse P_i even if $V = K_i$
- \circ As soon as we reach a leaf node C check if C has only search key values less than V
 - \triangleright if so set C= right sibling of C before checking whether C contains V
- Procedure printAll
 - \circ uses modified find procedure to find first occurrence of V
 - \circ Traverse through consecutive leaves to find all occurrences of V



Updates on B⁺ Trees: Insertion

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B-Tree Inde Files Comparison

- Find the leaf node in which the search-key value would appear
- If the search-key value is already present in the leaf node
 - Add record to the file
 - o If necessary add a pointer to the bucket
- If the search-key value is not present, then
 - Add the record to the main file (and create a bucket if necessary)
 - $\circ\,$ If there is room in the leaf node, insert (key-value, pointer) pair in the leaf node
 - Otherwise, split the node (along with the new (key-value, pointer) entry) as discussed in the next slide



Updates on B⁺ Trees: Insertion (2)

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Objectives Outline

B+-Tree Inde Files Simple B⁺ Tree Index Files

Query Duplicates

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B-Tree Index Files Comparison • Splitting a leaf node:

- o take the *n* (search-key value, pointer) pairs (including the one being inserted) in sorted order. Place the first $\lceil \frac{n}{2} \rceil$ in the original node, and the rest in a new node
- o let the new node be p, and let k be the least key value in p. Insert (k, p) in the parent of the node being split
- o If the parent is full, split it and **propagate** the split further up
- Splitting of nodes proceeds upwards till a node that is not full is found
 - $\circ\,$ In the worst case the root node may be split increasing the height of the tree by 1



esult of splitting node containing Brandt, Califieri and Crick on inserting Ada Next step: insert entry with (Califieri,pointer-to-new-node) into parent

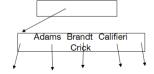


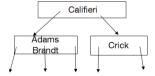
Updates on B^+ Trees: Insertion (3)

Module 43

Insertion

- Splitting a non-leaf node: when inserting (k, p) into an already full internal node N
 - \circ Copy N to an in-memory area M with space for n+1 pointers and n keys
 - o Insert (k, p) into M
 - \circ Copy $P_1, K_1, \cdots, K_{\lceil \frac{n}{2} \rceil 1}, P_{\lceil \frac{n}{2} \rceil}$ from M back into node N
 - \circ Copy $P_{\lceil \frac{n}{2} \rceil+1}, K_{\lceil \frac{n}{2} \rceil+1}, \cdots, K_n, P_{n+1}$ from M into newly allocated node N'
 - ∘ Insert $(K_{\lceil \frac{n}{2} \rceil}, N')$ into parent N
- Read pseudocode in book!







Updates on B⁺ Trees: Insertion Example

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Objectives & Outline

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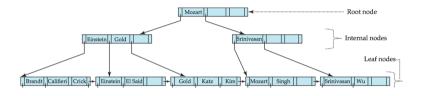
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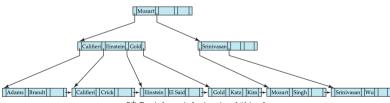
Non-Unique Key
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Comparison





 B^+ Tree before and after insertion of "Adams"



Updates on B^+ Trees: Insertion Example (2)

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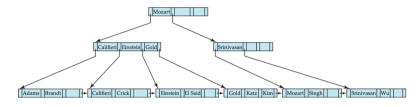
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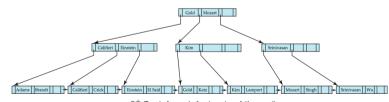
File Organizatio

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B-Tree Inde Files

Module Summary





 B^+ Tree before and after insertion of "Lamport"



Updates on B⁺ Trees: Deletion

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B-Tree Inde Files Comparison

- Find the record to be deleted, and remove it from the main file and from the bucket (if present)
- Remove (search-key value, pointer) from the leaf node if there is no bucket or if the bucket has become empty
- If the node has too few entries due to the removal, and the entries in the node and a sibling fit into a single node, then *merge siblings*:
 - Insert all the search-key values in the two nodes into a single node (the one on the left), and delete the other node.
 - Delete the pair (K_{i-1}, P_i) , where P_i is the pointer to the deleted node, from its parent, recursively using the above procedure.



Updates on B⁺ Trees: Deletion (2)

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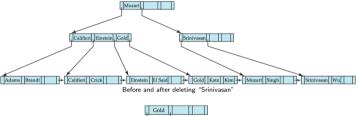
• Otherwise, if the node has too few entries due to the removal, but the entries in the node and a sibling do not fit into a single node, then redistribute pointers:

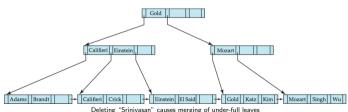
- Redistribute the pointers between the node and a sibling such that both have more than the minimum number of entries
- o Update the corresponding search-key value in the parent of the node
- The node deletions may cascade upwards till a node which has $\lceil \frac{n}{2} \rceil$ or more pointers is found
- If the root node has only one pointer after deletion, it is deleted and the sole child becomes the root



Updates on B⁺ Trees: Deletion Example

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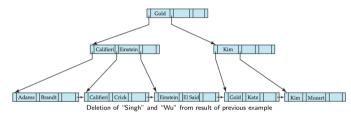




Updates on B⁺ Trees: Deletion Example (2)

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Deletion



- Leaf containing Singh and Wu became underfull, and borrowed a value Kim from its left sibling
- Search-key value in the parent changes as a result



Updates on B⁺ Trees: Deletion Example (3)

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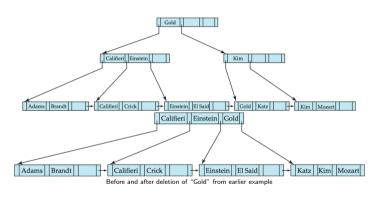
Insertio

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Non-Unique Keys Relocation and Secondary Indice Strings

B-Tree Index Files

Module Summar



- Node with "Gold" and "Katz" became underfull, and was merged with its sibling
- Parent node becomes underfull, and is merged with its sibling
 - Value separating two nodes (at the parent) is pulled down when merging
- Root node then has only one child, and is delete Partha Pratim Das



B⁺ Tree File Organization

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B-Tree Inde Files Comparison

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- Index file degradation problem is solved by using B⁺ Tree indices
- Data file degradation problem is solved by using B⁺ Tree File Organization
- The leaf nodes in a B⁺ tree file organization store records, instead of pointers
- Leaf nodes are still required to be half full
 - Since records are larger than pointers, the maximum number of records that can be stored in a leaf node is less than the number of pointers in a non-leaf node
- Insertion and deletion are handled in the same way as insertion and deletion of entries in a B⁺ tree index



B⁺ Tree File Organization: Example

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Simple B⁺ Tre Index Files Nodes

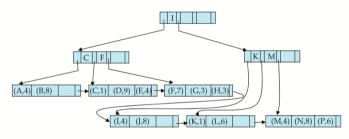
Observation

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B-Tree Index Files Comparison



Example of B⁺ tree File Organization

- Good space utilization important since records use more space than pointers.
- To improve space utilization, involve more sibling nodes in redistribution during splits and merges
 - Involving 2 siblings in redistribution (to avoid split / merge where possible) results in each node having at least $\lceil \frac{2n}{3} \rceil$ entries



Non-Unique Search Keys

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B-Tree Inde Files Comparison Alternatives to scheme described earlier

- o Buckets on separate block (bad idea)
- o List of tuple pointers with each key

 - ▷ Deletion of a tuple can be expensive if there are many duplicates on search key (why?)
- Make search key unique by adding a record-identifier

 - ▷ Simpler code for insertion/deletion
 - Widely used



Record Relocation and Secondary Indices

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Secondary Indices

If a record moves, all secondary indices that store record pointers have to be updated

- Node splits in B⁺ tree file organizations become very expensive
- Solution: Use primary-index search key instead of record pointer in secondary index
 - Extra traversal of primary index to locate record
 - Higher cost for queries, but node splits are cheap
 - Add record-id if primary-index search key is non-unique



Indexing Strings

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B-Tree Inde Files Comparison • Variable length strings as keys

- Variable fanout
- Use space utilization as criterion for splitting, not number of pointers
- Prefix compression
 - Key values at internal nodes can be prefixes of full key
 - Keep enough characters to distinguish entries in the subtrees separated by the key value
 - For example, "Silas" and "Silberschatz" can be separated by "Silb"
 - $\circ\,$ Keys in leaf node can be compressed by sharing common prefixes

B-Tree Index Files

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B-Tree Index Files



B-Tree Index Files

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Partha Pratim Das

Objectives Outline

B+-Tree Inde Files Simple B⁺ Tre

Simple B⁺ Tree Index Files Nodes Observations Query Duplicates

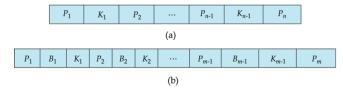
Updates
Insertion
Deletion

File Organization Non-Unique Keys Relocation and Secondary Indices Strings

B-Tree Index Files • Similar to B⁺ tree, but B-tree allows search-key values to appear only once; eliminates redundant storage of search keys

 Search keys in non-leaf nodes appear nowhere else in the B-tree; an additional pointer field for each search key in a non-leaf node must be included

Generalized B-tree leaf node



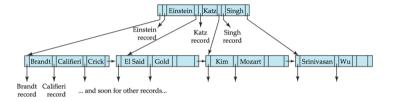
• Non-leaf node - pointers Bi are the bucket or file record pointers



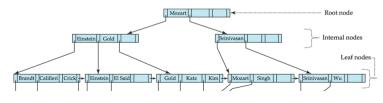
B-Tree Index File (2): Example

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B-Tree Index Files



B-tree (above) and B⁺ tree (below) on same data





Comparison of B-Tree and B⁺ Tree Index Files

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Nodes
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B-Tree Inde Files

- Advantages of B-Tree indices:
 - May use less tree nodes than a corresponding B⁺ Tree
 - o Sometimes possible to find search-key value before reaching leaf node
- Disadvantages of B-Tree indices:
 - o Only small fraction of all search-key values are found early
 - \circ Non-leaf nodes are larger, so fan-out is reduced. Thus, B-Trees typically have greater depth than corresponding B⁺ Tree
 - Insertion and deletion more complicated than in B⁺ Trees
 - \circ Implementation is harder than B⁺ Trees
- Typically, advantages of B-Trees do not outweigh disadvantages



Module Summary

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Module Summary

• Understood the design of B⁺ Tree Index Files in depth for database persistent store

Familiarized with B-Tree Index Files

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