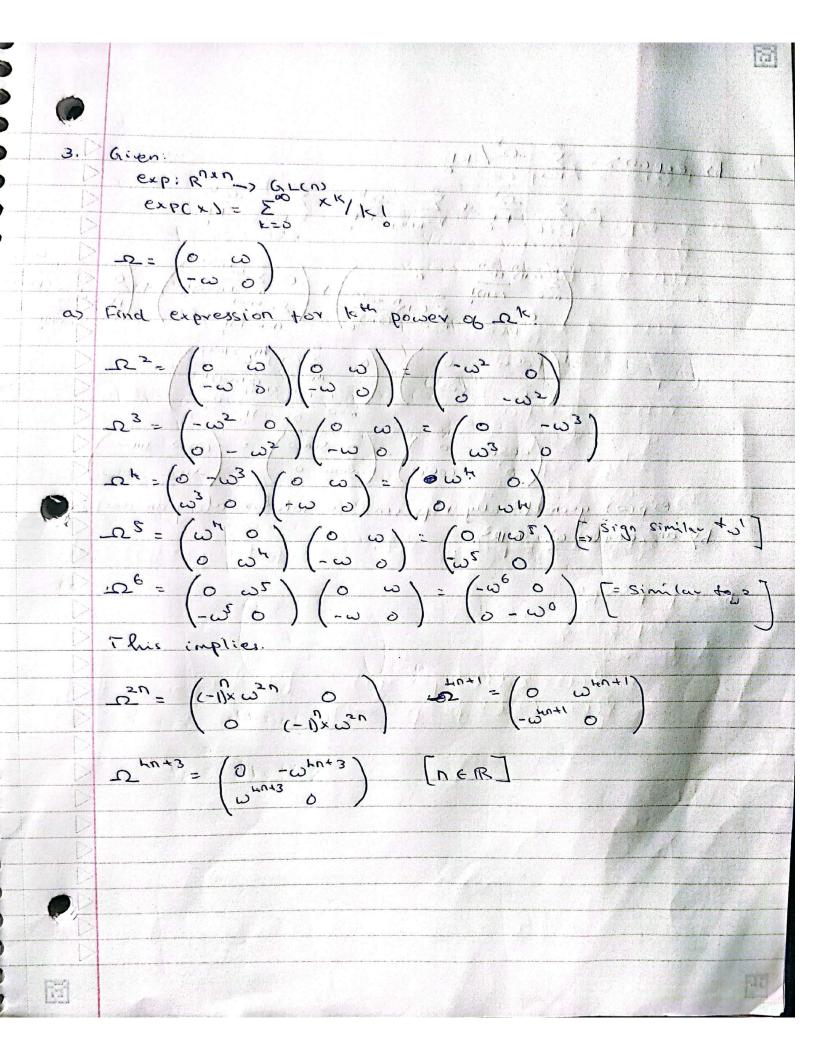
LAB-1. 1. OBJECT POSE ESTIMATION Given $OP_1 = \begin{pmatrix} 2 \\ 3 \\ -3 \end{pmatrix}, OP_2 = \begin{pmatrix} 0 \\ 0 \\ -3 \end{pmatrix}, OP_3 = \begin{pmatrix} -1 \\ -2 \\ 2 \end{pmatrix}, OP_1 = \begin{pmatrix} 0 \\ -2 \\ 2 \end{pmatrix}$ $SP_1 = \begin{pmatrix} -1.3840 \\ 4.5620 \\ -0.1280 \end{pmatrix}$, $SP_2 = \begin{pmatrix} -0.9608 \\ 1.3110 \\ -1.6280 \end{pmatrix}$, $SP_3 = \begin{pmatrix} 1.3250 \\ -2.3890 \\ 1.7020 \end{pmatrix}$ Total: Pose TSOE SE(3) of O wort s. WKI SP = TSO DP => TSO = SPIDE 188.17 1.325 -1.311 -1.38 H -0. abo8 H.562 1.311 -2.389 0.251 -0.762 1-0-1280 -1.628 1.702 10000 20-1-110000 Op = 20-1-1 30-200100 0 0 1 -3 3 -2 00 001 0 -6 1 -7 3020 0001 00010001 0001 3 R1 - 2 R2 3 R. 12 RZ 20-1-11000 20-1-11000 NO-60-8 6.920 -7 3 0 90 0 0 1 -3 3 -2 00 10000 10001 100001 100-22-100 OO 2 0 0 -4 h -2 ~ 0 1 0 2/3 = 1/3 0 0 9 20 00 0 1 -3 3 -200 3-200

$$0p^{-1} = \begin{bmatrix} 2 & -1 & 0 & 2 \\ -2 & -1 & 3 & -1 \\ 3 & -1 & 3 & -1 \\ 3 & -2 & 0 & 3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\frac{1}{180} = \begin{bmatrix} -1.384 & -0.9608 & 1.325 & -1.314 \\ 4.562 & 1.3110 & -2.389 & 0.250 \end{bmatrix} \begin{bmatrix} 2 & -1 & 0 & 2 \\ 0 & -1/3 & 1/3 & -2/3 \\ -0.128 & 1.628 & 1.702 & -0.762 \end{bmatrix} \begin{bmatrix} 3 & -2 & 0 & 3 \\ 3 & -2 & 0 & 3 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Given: Gr is a lie group with group operation * Lg: 6-74 Y: Tecas -> Lie cas.
Yews = Vw Lg cx> ≜ gxx Vwcxx & d(Lx)e(w) VER" The left translation Ly: 1R1-> 1R1 0 Lv(x) = VXX=V+X XER? [*-addition] if v= (v, v2 ... vn) d x= (x, x2, ... xn) LV(x) = (V1, V2, ... Va) + (x1, 12, ... xa). dLv(2)= Q your) d'Lvin 6) Drack) STACKS grack) Vw cxs = d(-x)e(w) => VE = dlv (x) &

A & GLOW La: GLCD -> GLCD. LACX) = AXX $\frac{dLA = dLA = d(A2)}{dx}$ Va = dla)I 2 40 = dAI of & Roxn



b)
$$\exp(\Omega) = \sum_{k=0}^{\infty} \frac{\Omega^{k}}{k!} + \sum_{k=hn+1}^{\infty} \frac{\Omega^{k}}{k!}$$

by an angle w. in 122.

4. Given: V(1) = x x exp(tw) as x = exp (log(x)) 1(0) = x where t=0 8(1) = 4 where 6=1 O t=0 P(1) = 2 * exp(0) x = x * exp (0) 3 6= 1 P(1) = n x exp(w) y = x * εφιω)
x-1 y = exp(ω) => w= log(x'y) Ster x * expelled 8(t) = x * exp(t log (x'y)) - (A) b) eap: 1Rn->1Rn exp(&)= &. A becomes 1(t) = x * (t log (x - 'y)) [x-Addition for 12]
=> 1(t) = x + t log(x - 'y) - B

C) C61, R) + C62, R2) = CR1 t2+t1, R(R2) - @ 11/1/11 66 July 11 18 31. 2 1831.0 (1) (0.4330 0.1768 0.8839), 0.2500 b. 9186 -0.3062 0.7500 -0.QHTH (70.5000 10.612h 10.612h O (can be written of 1921) 11's 1" to (R2 = (Petz, Pitz+ti)
= (Pitz+ti, PiR2). D more ?(1)= x * exp (log x 'y) [R, t] [Rz, tz 10d 0 (X/10 pol 10 pox 2Ct) = X 0 to exp (thoq to \$X1) (1882.) Sprang SE10.0 \ 3 (01)8 K-42 8(42) = x0 * exp (+ log xo x1) V 0002 0000 0000 00 VOV 3" 0. H 331 0.2500 -0.866 1,70.6831 0.1767 0.9185 0-3535 -1-0953 0.8838 -0.3062 0.3535 -0.5776 0.8661 -0.3536 + 0.35350 Fl. hlhq 0.3535 0.9329 -0.067 3.9926 0.3535 1-0.0670 0 9329 1.0257

```
expc/2/0g(x=x))= 0.9659 -0.183 -0.183 -0.4738
                       0.1829 0.9829 -0.017 2.0622
                        0.1829 -0.0170 0.9829 0.5787
        V(12) = x0 x Y
                 0.6122 0.0795
                                       0.7865 1-6709
                  0.3535 0.8623
                                       -0.362312.5986
                  -0.7071 D.5000
                                       0.50001 1.3 KH
                      0 0
                             · R3
    (t1) R() * (t2, R2) = (t1+t2, R1R2)
d)
     (D) mort
          P(1) = x * exp (slag x'y)
    x=x00; 4= exp(=10g (x6'x)) => from @

\frac{2(1/2)}{0.6122} = \begin{cases}
0.6122 & 0.0795 & 0.7865 \\
0.3535 & 0.8623 & -0.3623 \\
-0.707 & 0.5000 & 0.5000
\end{cases}

e) plot translation components of VSECTS & Vp over
       is te Eo, 1]
        ii) t & [0,30]
   during interval @ => plot shows that the robot is gradually
   in K,Y, z axis
   during interval (i) => plot reveals that the brajectory (av)
    translation of the robot tollows a screw or, helix motion,
     Both Vsecs & Pp are similar plots.
```

4. e

1. Plot of translational components of the curves $\gamma SE(3)$

https://drive.google.com/file/d/1flbrm8a00GY1dr2C6QoROwRtPdsh1ybx/view?usp=sharing

2. Plot of translational components of the curves γP

https://drive.google.com/file/d/1l8aP9yAl319_djsn0N0v7XQQD0itUScd/view?usp=sharing