

FSVPDsee: A Forward Secure Publicly Verifiable Dynamic SSE Scheme

Laltu Sardar¹ Sushmita Ruj^{1,2}

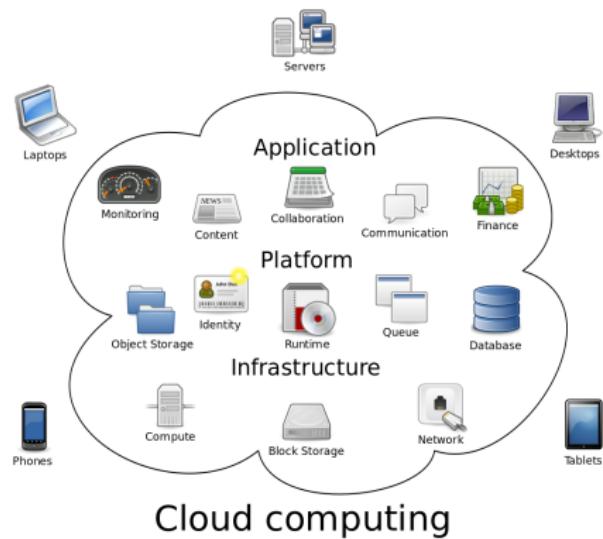
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ProvSec 2019, Cairns, Australia

Dependency on Cloud Computing and Storage Services



Google Cloud



Can we TRUST Cloud Service Providers?

TRUST?

Can we TRUST Cloud Service Providers?

TRUST?

Read Data



Sell Data



Hacked



Manipulation

**PRIVACY
BREACH**

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How to be SAFE?

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Encrypt data



Send Encrypted Data



Store in cloud



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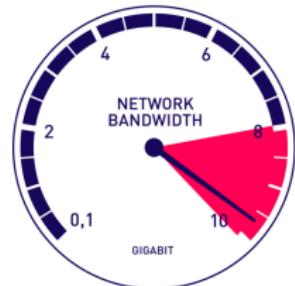
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Cloud can't Search!

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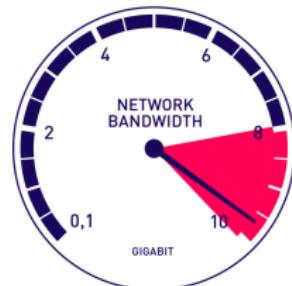
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Solution: **Searchable Encryption**

Searchable Encryption Idea

Initially

Build Search Index



1. Encrypt data and Index

2. Send



Encrypted Data & Search Index

3. Store data and index



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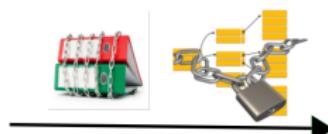
Initially

Build Search Index



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For Search:

1. Client Sends



Search Token

2. Cloud Search



over Encrypted Index

3. Client received



Result

Presence of Malicious adversary

Previous works

- Plenty of works on static SSE and dynamic SSE
- Dynamic SSE– Supports updates on database, popular
- Assumes– **Honest-but-curious** Server which Follows the protocol but wants to Learn data

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What happen if the server is malicious?

- Computation over data requires cost
- Can not provide free service as it can not sell data
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!!! Verification Needed !!!

Can Public also verify?

Private verifiability

- Only the owner/querier can verify
- Verifier has to do most of the computation

Public verifiability

- Any of the owner, querier or third party **Auditor** can verify.
- Most of the Computation for verifiability can be Outsourced
- Result not revealed

Forward Privacy & Client storage

Forward Privacy

- adding a keyword-document pair does not reveal any information about the previous search result with that keyword.

Attacks– when no Forward Privacy

- File-injection attack [ZKP16]: Cloud Can inject files
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Need of Owner Storage Reduction

- Owner should able to search and verify from lightweight devices
- Should require storage and computation as less as possible

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Challenge— Enabling Public verifiability without extra client storage !

Our Contribution

Verifiable SSE

- Described problem with existing static SSE schemes
- Proposed a generic efficient solution
- Solution that no needs of any extra storage at owner side

Forward Secure Verifiable DSSE

- Proposed a **GENERIC** publicly verifiable dynamic SSE scheme (Ψ_f)
- very efficient and easy to integrate

Extra Benefits

- **The owner does not use any extra storage than the embedded schemes.**
- very effective and efficient for a resource constrained client.

Verifiable SSE and DSSE schemes

Table: Different verifiable SSE and DSSE schemes

Data Type	static				dynamic			
Query Type	single		complex		single		complex	
Verification	private	public	private	public	private	public	private	public
Schemes	[CG12], [CYG ⁺ 15], [OK17], [LLL ⁺ 18], [SK19]		[WCS ⁺ 18], [LZQ ⁺ 18], [ZXZ18]	[SK19]	[YK17], [BFP16]	[MWWM19], Ψ_f	[ZLW16]	[JZGL15]
Forward Private	not applicable				[YK17], Ψ_f			

- Our scheme is Publicly verifiable single keyword search scheme.
- The only forward private scheme [YK17] is privately verifiable

Used Cryptographic tools

Bilinear Map

Let $\mathbb{G} = \langle g \rangle$ and \mathbb{G}_T be two **cyclic** groups of prime order q .

$\hat{e} : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$ is an *admissible non-degenerate bilinear map* if–

- $\hat{e}(u^a, v^b) = \hat{e}(u, v)^{ab}$, $\forall u, v \in \mathbb{G}$ and $\forall a, b \in \mathbb{Z}$ (bilinearity)
- $\hat{e}(g, g) \neq 1$ (non-degeneracy)
- \hat{e} can be computed efficiently.

Used Cryptographic tools

Bilinear signature

Let $\hat{e} : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$ be a bilinear map where $|\mathbb{G}| = |\mathbb{G}_T| = q$, a prime and $\mathbb{G} = \langle g \rangle$. A bilinear signature (BLS) scheme $\mathcal{S} = (\mathbf{Gen}, \mathbf{Sign}, \mathbf{Verify})$ is a tuple of three algorithms as follows.

- $(sk, pk) \leftarrow \mathbf{Gen}$: It selects $\alpha \xleftarrow{\$} [0, q - 1]$. It keeps the private key $sk = \alpha$, publishes the public key $pk = g^\alpha$.
- $\sigma \leftarrow \mathbf{Sign}(sk, m)$: Given $sk = \alpha$, and some message m , it outputs the signature $\sigma = (\mathcal{H}(m))^\alpha = (g^m)^\alpha$ where $\mathcal{H} : \{0, 1\}^* \rightarrow \mathbb{G}$ is a bilinear hash defined by $\mathcal{H}(m) = g^m$.
- $\{0/1\} \leftarrow \mathbf{Verify}(pk, m, \sigma)$: Return whether $\hat{e}(\sigma, g) = \hat{e}(\mathcal{H}(m), g^\alpha)$

Verifiability on Static SSE Schemes

Traditional Verifiable Schemes with client storage

- Target– Given w , verify $R_w = \{D_1^w, D_2^w, \dots, D_n^w\}$
- For each w , stores
$$\text{digest}(w) \leftarrow H(D_1^w || D_2^w || \dots || D_n^w)$$
- Drawback–Increases Client storage

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Our Solution for Static Verifiable SSE without extra client storage

- Bind w with the digest as $\boxed{\text{digest}(w) \leftarrow H(w || D_1^w || D_2^w || \dots || D_n^w)}$
- Upload $\boxed{\{\text{digest}(w), D_1^w, D_2^w, \dots, D_n^w\}}$ for all w
- Benefits: 1. Verification very efficient 2. only a hash computation
- Public verifiability not needed

System Model

1. Init Phase



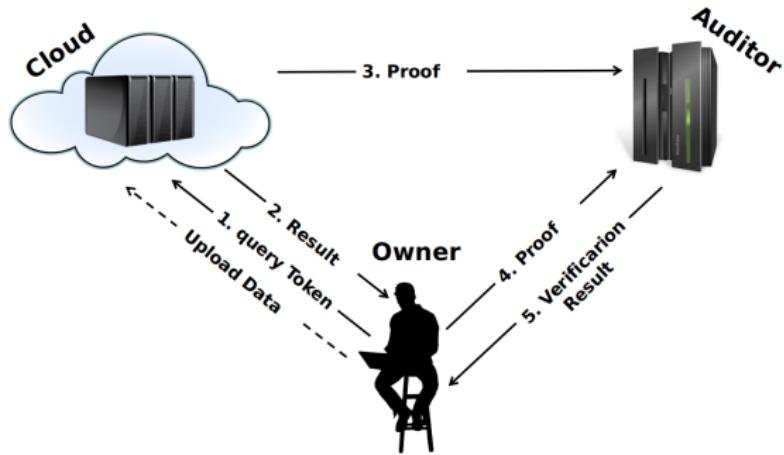
2. Search Phase



3. Update Phase



System Model



Black-box forward secure DSSE scheme Σ_f

- We take a forward secure DSSE scheme Σ_f as blackbox
- Σ_f has three phases
- We don't change anything in Σ_f

Black-box forward secure DSSE scheme Σ_f

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- Σ_f has three phases
- We don't change anything in Σ_f
- We add an independent extra (Table) data structure T for verification



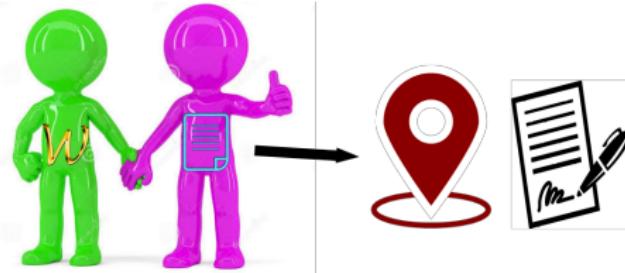
Data Structure Type



With ability to search efficiently

Our Generic Scheme

Key-value pair generation

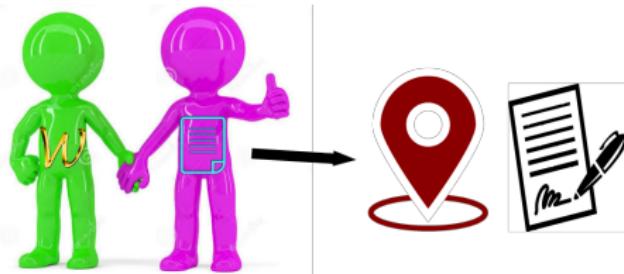


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Bindings



denoted as σ_i^w

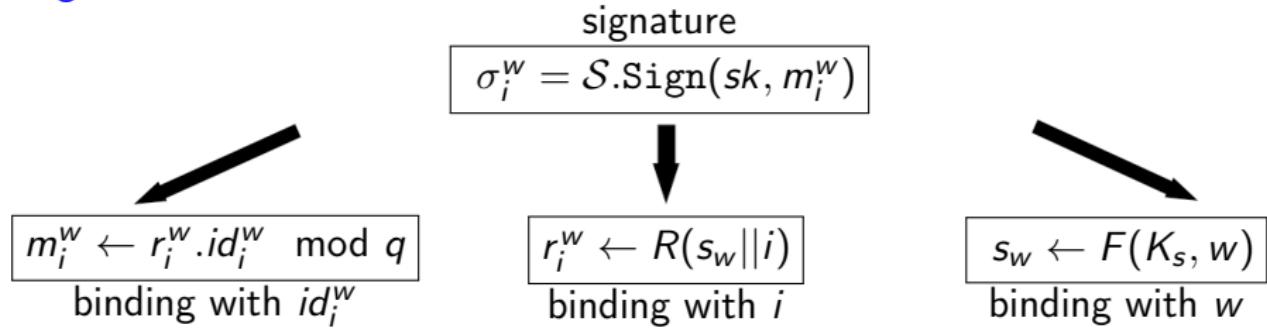
keyword w
document Identifier id_i^w
position i



denoted as pos_i^w

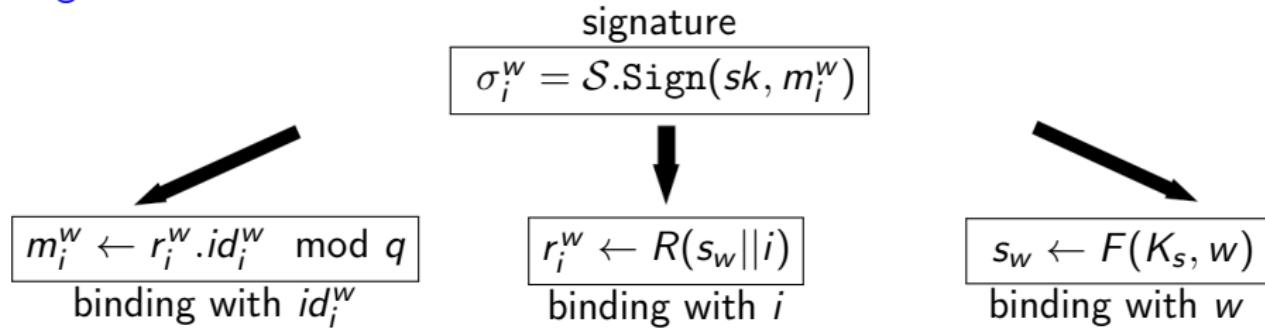
Binding in Signature and positions

Signature Generation

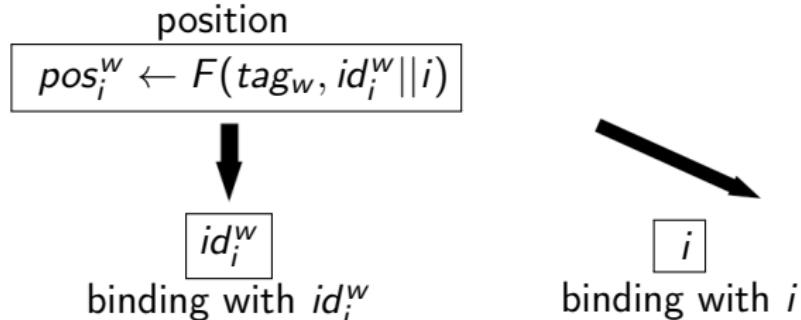


Binding in Signature and positions

Signature Generation



Position Generation



Search

During search

- ① Cloud first gets $R_w = \{id_1^w, id_2^w, \dots, id_n^w\}$ using Σ_f
- ② Then calculates positions $\{pos_1^w, pos_2^w, \dots, pos_n^w\}$ where
 $pos_i^w \leftarrow F(tag_w, id_i^w || i)$
- ③ tag_w is provided to cloud with search token
- ④ Retrieve signatures as
 $\{\sigma_1^w = T[pos_1^w], \sigma_2^w = T[pos_2^w], \dots, \sigma_n^w = T[pos_n^w]\}$

Observation

- $\prod_1^n \sigma_i^w = \prod_1^n \mathcal{S}.\text{Sign}(sk, m_i^w) = \prod_1^n (g^{sk})^{m_i^w} = (g^{sk})^{\sum_1^n m_i^w}$

Verification

- We observe $\prod_1^n \sigma_i^w = (g^{sk})^{\sum_1^n m_i^w}$
- Cloud computes $\sigma_w = \prod_1^n \sigma_i^w$, Aggregate Signature
- Client computes $m = \sum_1^n m_i^w = \sum_1^n r_i^w \cdot id_i^w$ Aggregate of IDs
- Possible as client can regenerate r_i^w and gets id_i^w 's from cloud

Verification

- $\mathcal{S}.\text{Verify}(pk, m, \sigma_w)$

Correctness

- $\hat{e}(\mathcal{H}(m), pk) = \hat{e}(g^m, g^{sk}) = \hat{e}(g^{sk \sum m_i}, g) = \hat{e}(\prod g^{sk \cdot m_i}, g) = \hat{e}(\prod \sigma_i, g) = \hat{e}(\sigma, g)$

Update and Forward Privacy

Assumption

- Any Σ_f stores keyword frequency list C

Update

- Owner can compute position-signature pairs for each word-doc pair
- Possible because C gives frequency
- C is also gets updated

Forward Privacy

- Cloud don't know which id can be added next
- \Rightarrow Cant calculate positions
- \Rightarrow from position, cant link with keyword

Security

Simulation

- Takes the simulator of the black-box scheme
- Additionally Simulates T_{sig}
- Simulates Query tokens.
- Simulates Update tokens.

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Indistinguishability for Query and Update token

- Relies on Random oracle model
- The MAC function F is generated simulated with a random oracle.

Our Stands in the Literature

Table 2: Comparison of verifiable dynamic SSE schemes

Scheme Name	Forward privacy	Publicly verifiable?	Extra Storage		Extra Computation		Extra Communication owner
			owner	cloud	owner	cloud	
Yoneyama and Kimura [YK17]	✓	✗	$O(\mathcal{W})$	$O(\mathcal{W} \log \mathcal{DB})$	$O(R_w)$	$O(R_w)$	$O(1)$
Bost and Fouque [BFP16]	✗	✗	$O(\mathcal{W})$	$O(\mathcal{W})$	$O(R_w)$	$O(1)$	$O(1)$
Miao et al. [MWWM19]	✗	✓	$O(\mathcal{W})$	$O(N + \mathcal{W})$	$O(R_w)$	$O(R_w)$	$O(1)$
Zhu et al. [ZLW16]	✗	✗	$O(1)$	$O(1)$	$O(R_w)$	$O(R_w + N)$	$O(R_w)$
Jiang et al. [JZGL15]	✗	✓	$O(1)$	$O(\mathcal{W})$	$O(\log \mathcal{W})$	$O(R_w + N)$	$O(1)$
Ψ_f	✓	✓	$O(1)$	$O(N)$	$O(R_w)$	$O(R_w)$	$O(1)$

Where N is the #keyword-doc pairs.

Results

- Ψ_f is very efficient with respect to low resource owner.
- To verify the search, owner needs only $|R_w|$ multiplication which very less from the others.
- The owner also does not require any extra storage

Possible future works

Increasing Efficiency

- Storage reduction
- Communication cost reduction
- Computation cost reduction

Verifiability on Complex Queries

- Conjunctive or Boolean Queries
- Ranked search
- Range searched

Verifiability with more secure schemes

- Backward secure schemes
- Type-I, Type-II and Type-III backward Secrecy



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In *2016 IEEE Trustcom/BigDataSE/ISPA, Tianjin, China, August 23-26, 2016*, pages 845–851, 2016.

Questions?



Thank You!

Leakage Function

- $\mathcal{L}_{bld}^{\Psi_f}(\mathcal{DB}) = \{\mathcal{L}_{bld}^{\Sigma_f}(\mathcal{DB}), |T_{sig}|\}$
- $\mathcal{L}_{srch}^{\Psi_f}(w) = \{\mathcal{L}_{srch}^{\Sigma_f}(w), \{(id_i^w, pos_i^w, \sigma_i^w) : i = 1, 2, \dots, c_w\}\}$
- $\mathcal{L}_{updt}^{\Psi_f}(f) = \{id, \{(\mathcal{L}_{updt}^{\Sigma_f}(w_i, id), pos^{w_i}, \sigma^{w_i}) : i = 1, 2, \dots, n_id\}\}$

Related Works

Type 1 Works

- Should be added

Type 2 Works

- Should be added

Type 3 Works

- Should be added