

**Math 456/556: Networks and Combinatorics**  
**HW #3, due Monday, 1/25**

The following problems from the textbook are **not** to be turned in:

Chapter 5: 6, 9, 11, 15, 16, 18, 19, 48, 50.

The following problems are to be turned in:

**3.1** Evaluate the following two expressions:

a) 
$$\sum_{k=0}^{100} (-2)^k \binom{100}{k}$$

b) 
$$\sum_{k=0}^{100} \frac{(-2)^{k+1}}{k+1} \binom{100}{k}$$

**3.2** Let  $X$  be the poset consisting of the elements  $\{1, \dots, 100\}$ , ordered by divisibility. Show that  $X$  does not contain an antichain of size 51.

**3.3** What is the coefficient of  $x^3y^{10}$  in  $(y - 2x)^{13}$ ?