

**Math 456/556: Networks and Combinatorics**  
**HW #7, due Wednesday, 3/2**

The following problems from the textbook are **not** to be turned in:

Chapter 12: 5, 11, 14, 16, 18, 21, 26.

The following problems are to be turned in:

**7.1** Compute the chromatic number, the chromatic polynomial, and the number of 3-colorings of the complete bipartite graph  $K_{2,3}$ .

**7.2** Let  $p(k) = k(k-1)(k-2)(k-3)(k-4)(k-5)^2$  and  $q(k) = k(k-1)(k-2)(k-3)(k-4)(k-6)^2$ .

a) Is  $p(k)$  the chromatic polynomial of any graph? If so, then find such a graph, and determine its chromatic number. If not, why not?

b) Same for  $q(k)$ .

c) Answer parts (a) and (b) with “graph” replaced by “planar graph”.