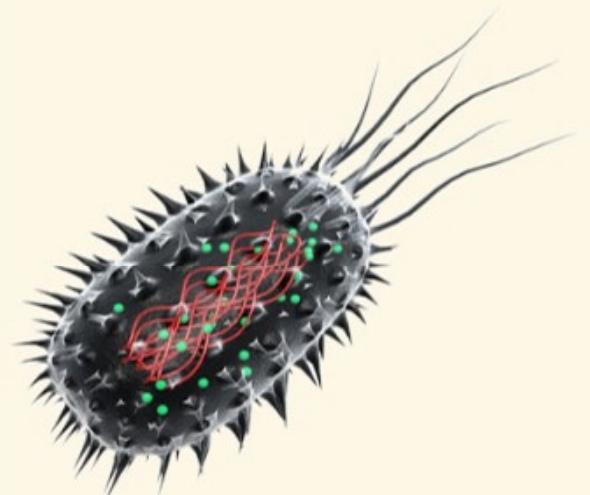


# (RE)PROGRAMMING BIOLOGY

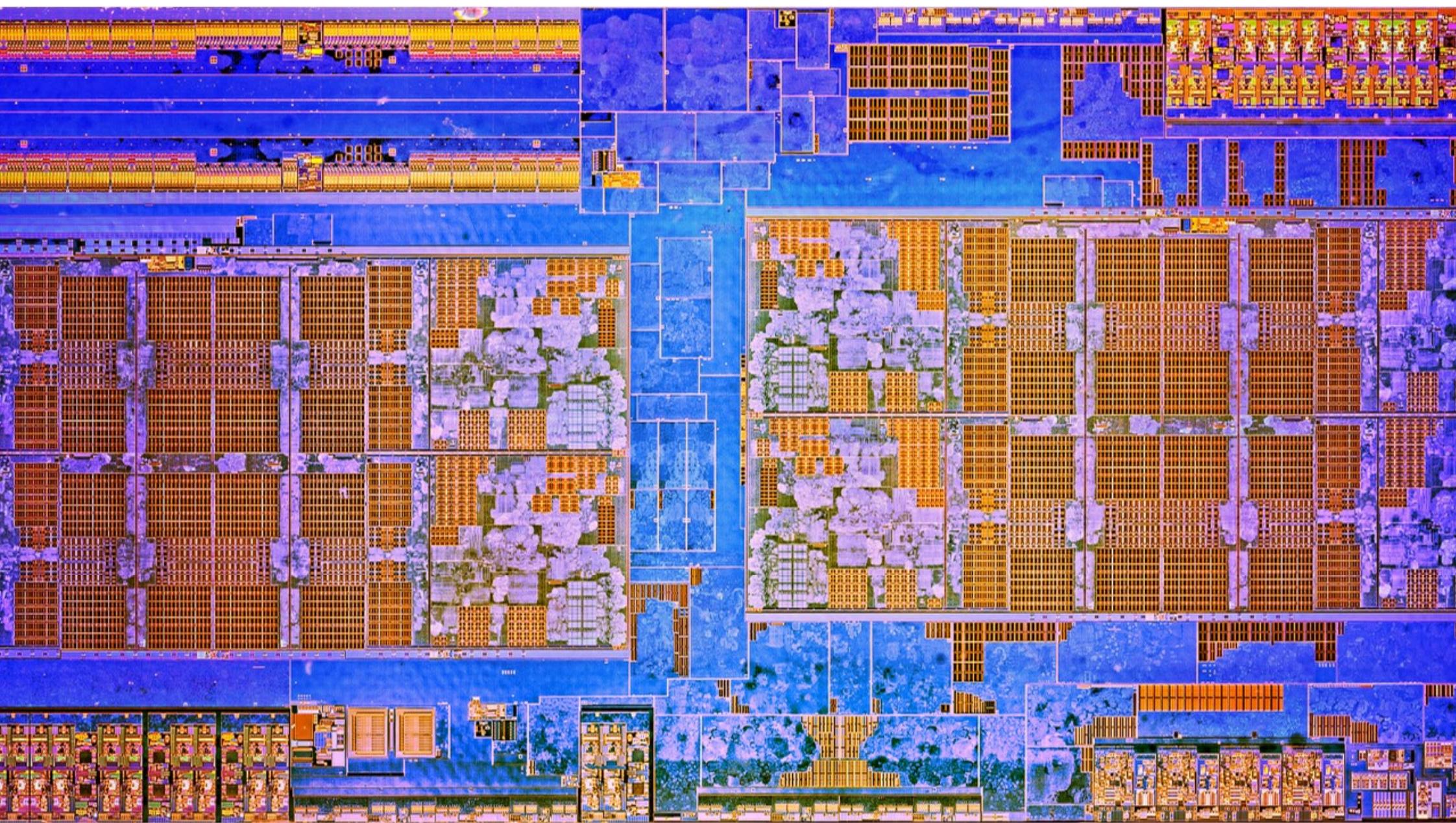
(BIOLOGICAL COMPUTING IN F#)

Colin Gravill  
Biological Computation Group  
Microsoft Research

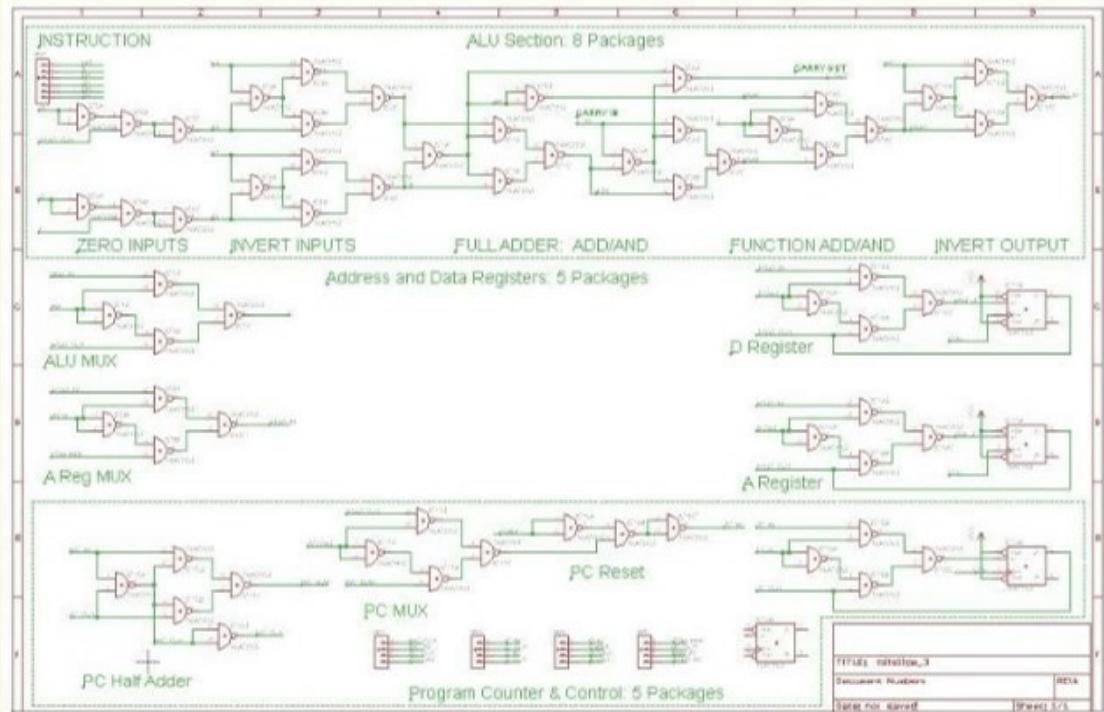
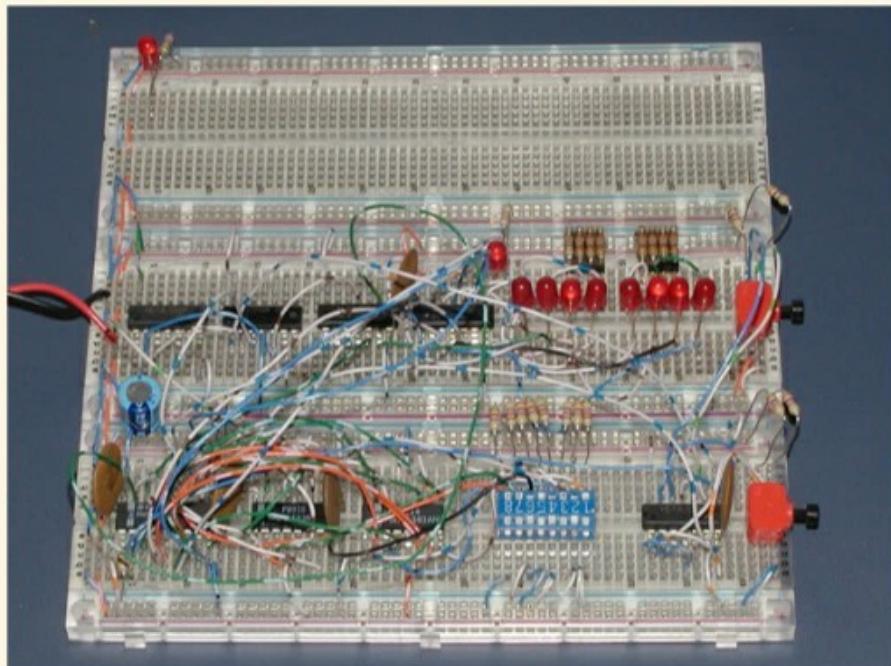


## PROGRAMMING SILICON (CHIPS)



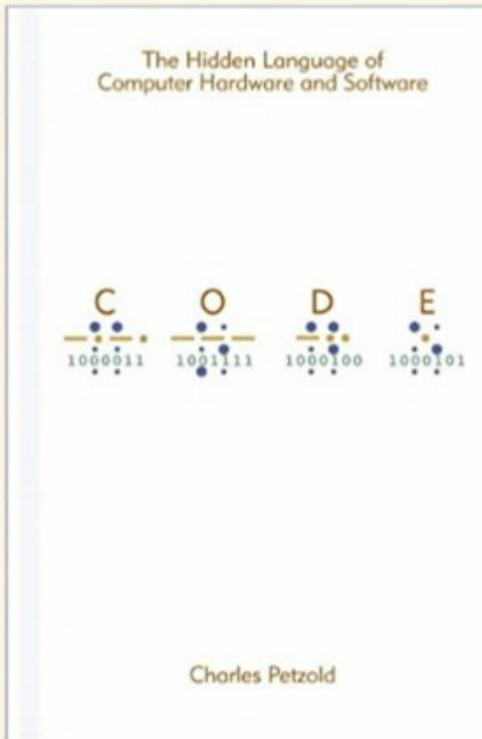
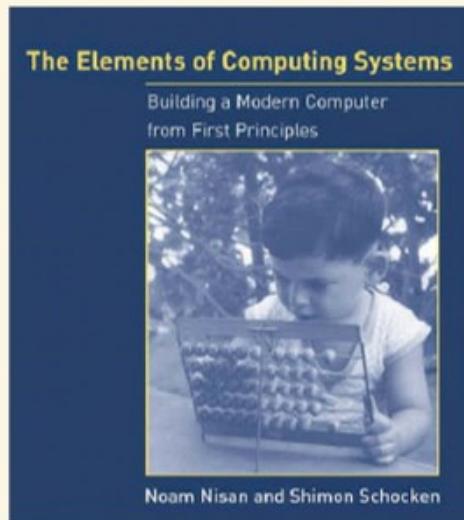


## PROGRAMMING SILICON (SMALLER)

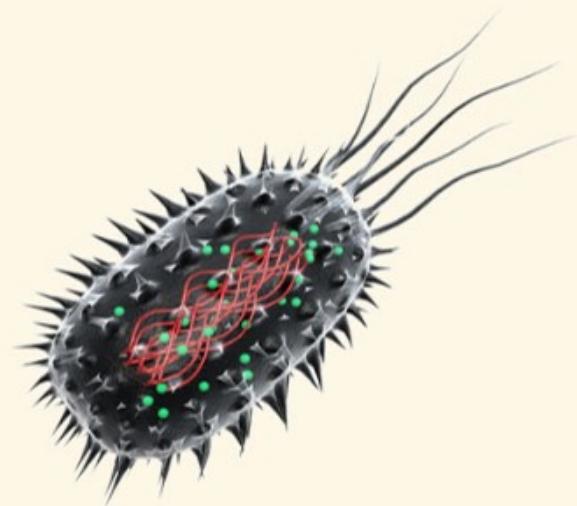


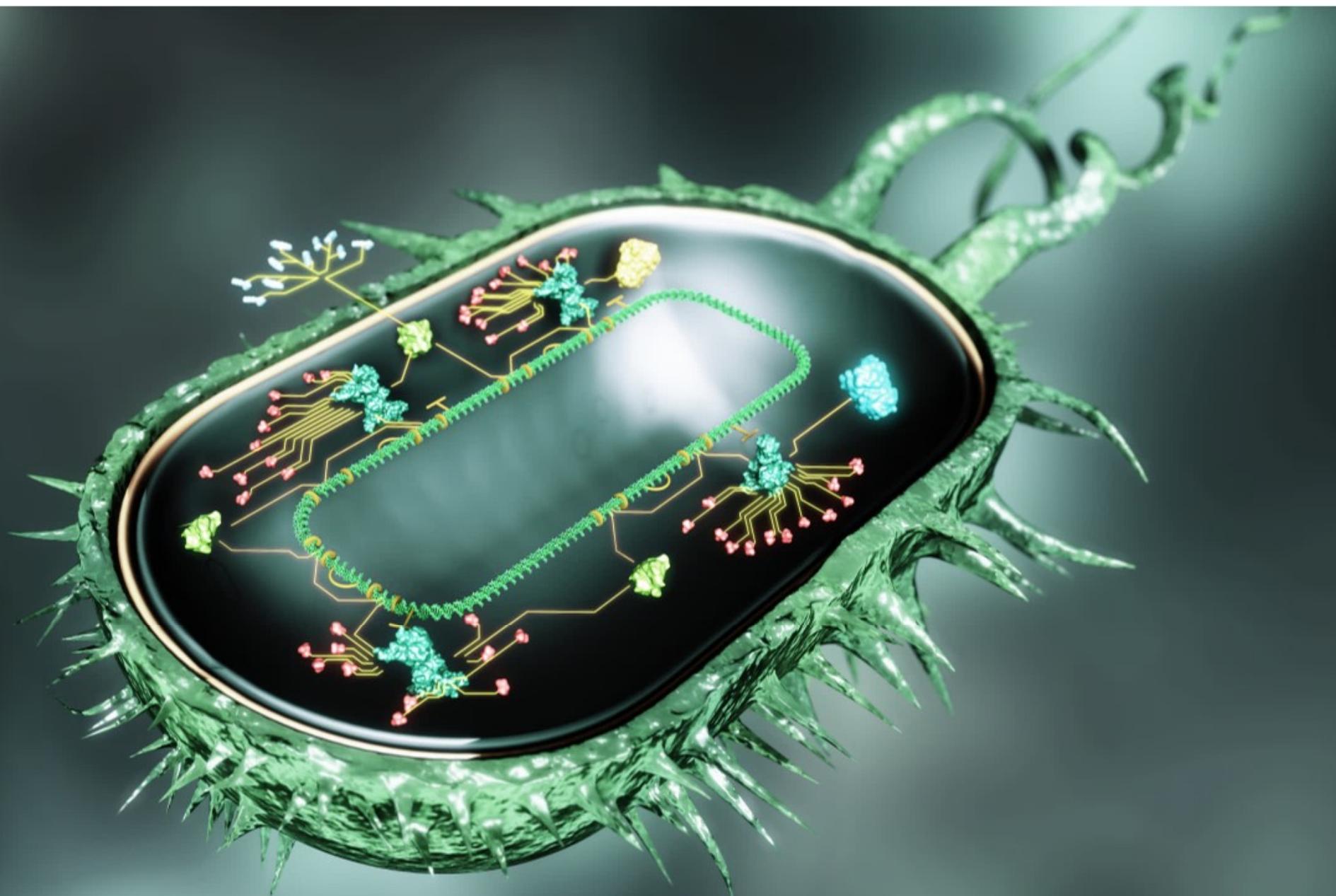
<http://nand2tetris-questions-and-answers-forum.32033.n3.nabble.com/Physical-implementation-of-NAND-and-DFF-primitives-td4028219.html>

# PROGRAMMING SILICON (SMALLER)

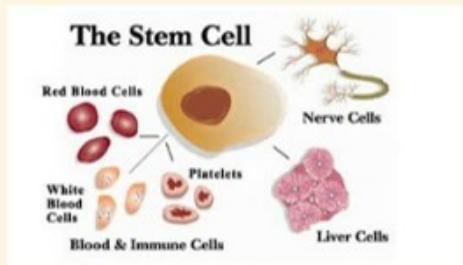


# NOW BIOLOGY





# BIOLOGICAL COMPUTATION



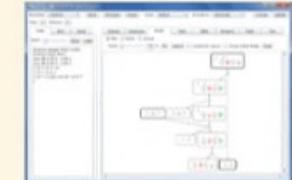
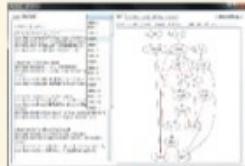
Development



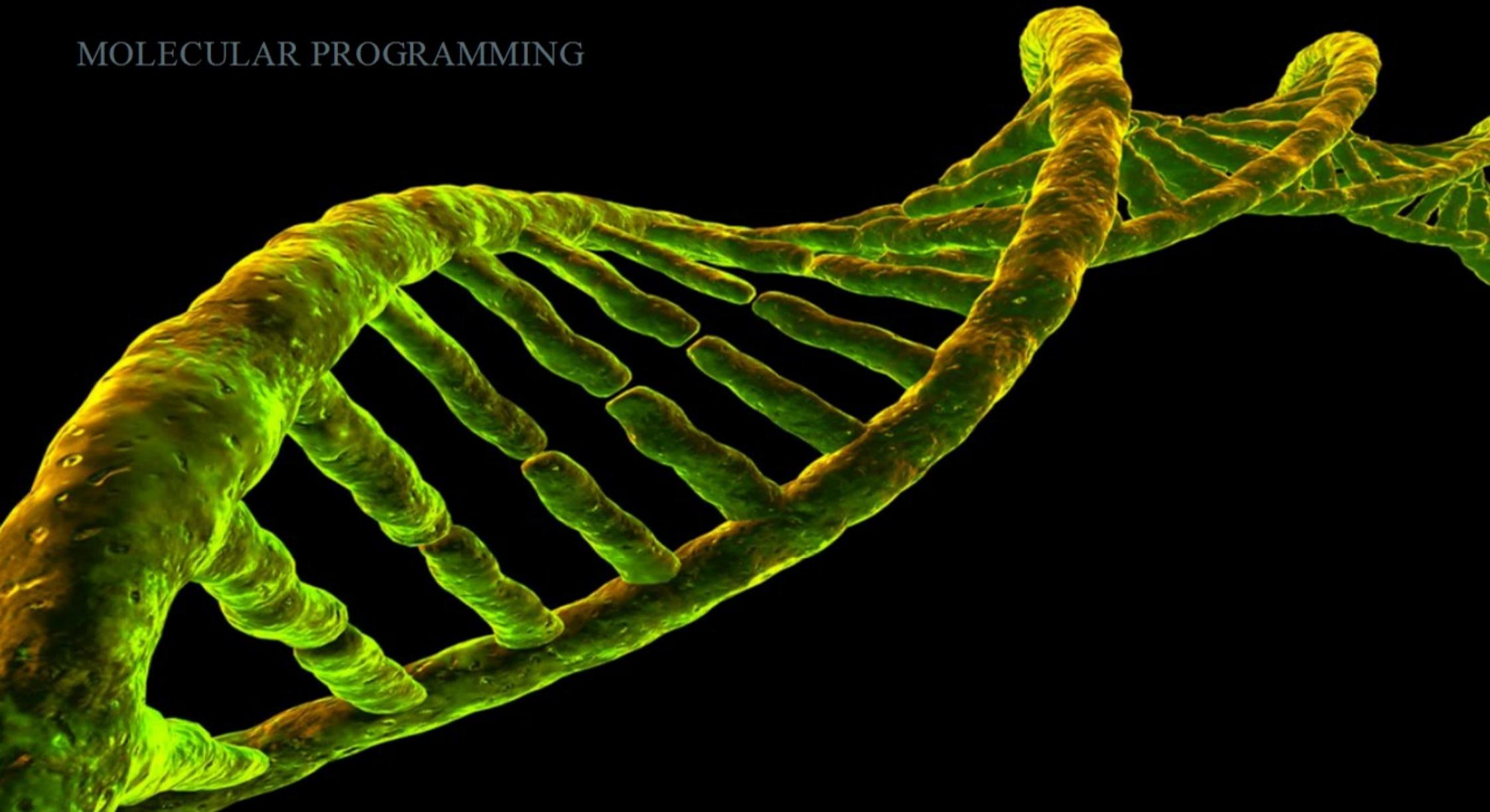
Molecular Programming



COMPUTER AIDED DESIGN TOOLS



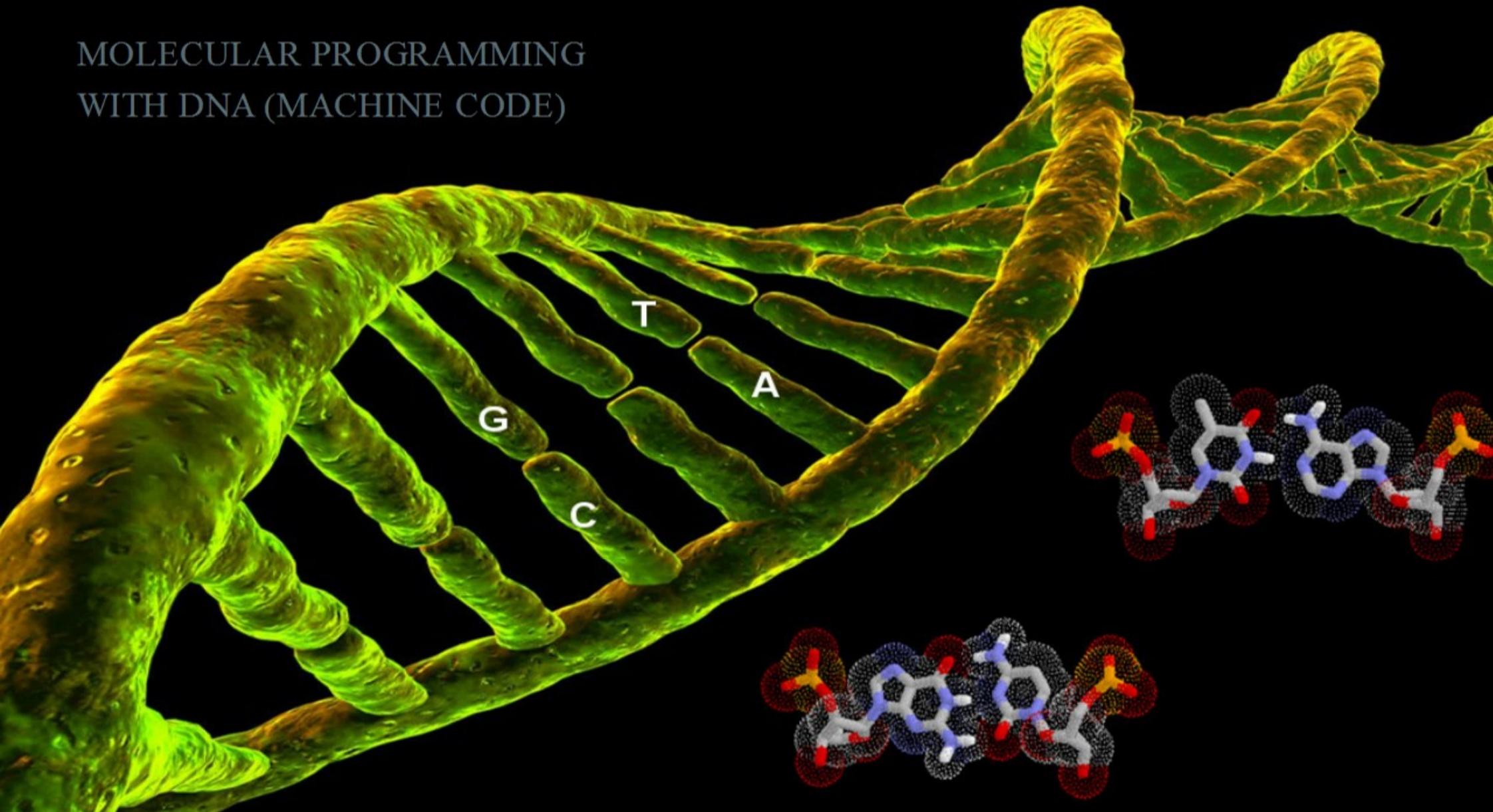
MOLECULAR PROGRAMMING



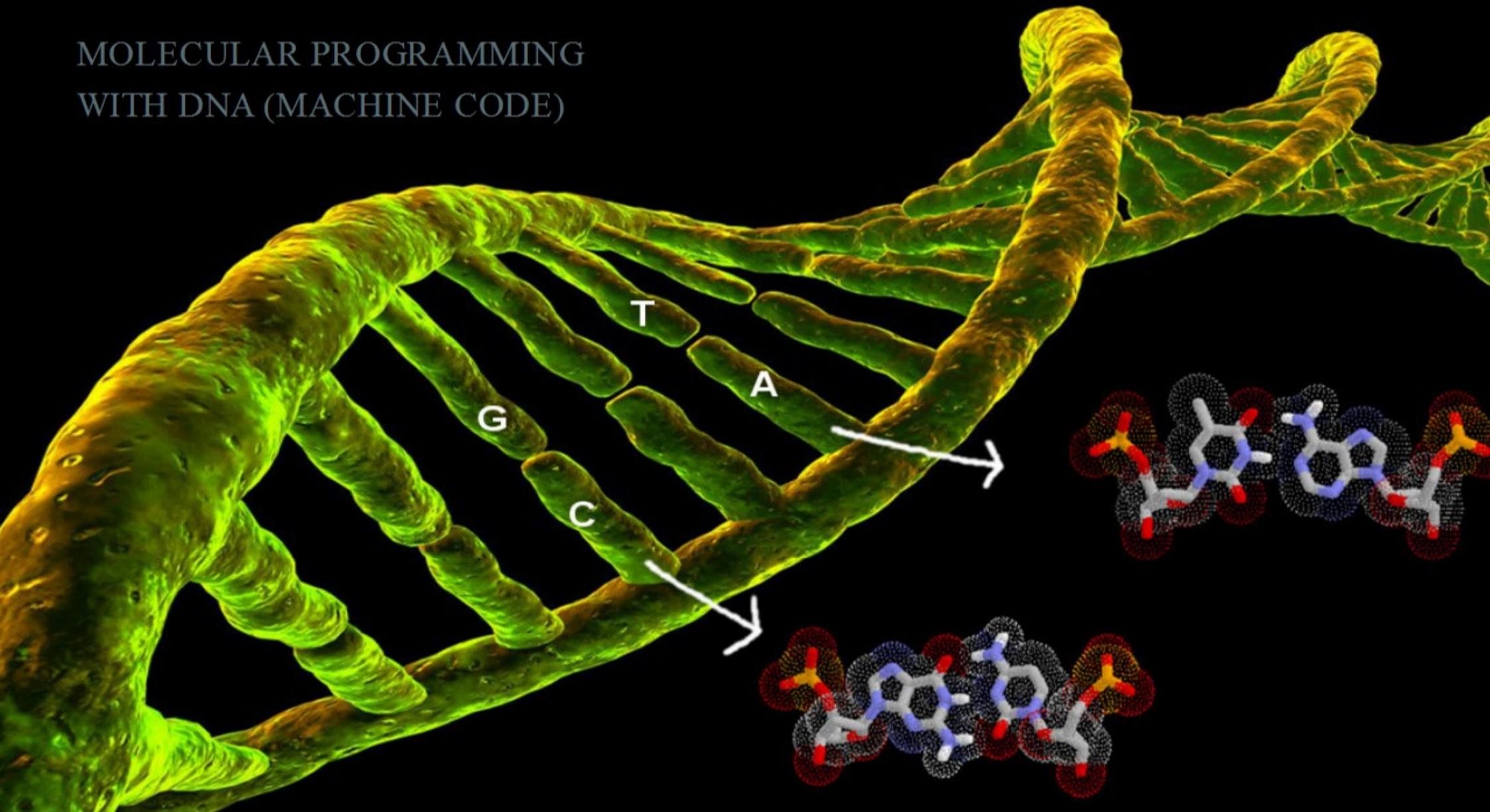
# MOLECULAR PROGRAMMING WITH DNA



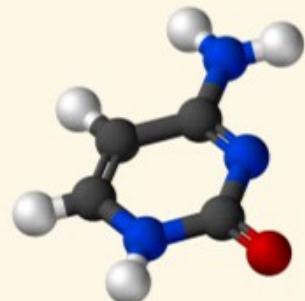
# MOLECULAR PROGRAMMING WITH DNA (MACHINE CODE)



# MOLECULAR PROGRAMMING WITH DNA (MACHINE CODE)



## REPURPOSING DNA



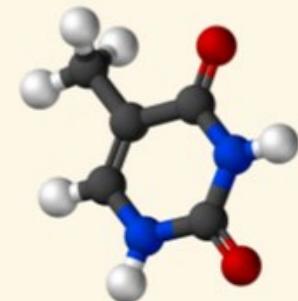
C - Cytosine



G - Guanine



A - Adenine



T - Thymine

APPEARS AS C-G, G-C, A-T, AND T-A, UNRAVELED:

GGCTTAAGTTTGAAATTGTT  
CCGAATTCAAAACTTAACCAA

# DNA STRAND AFFINITY

Short complementary segments bind *reversibly*



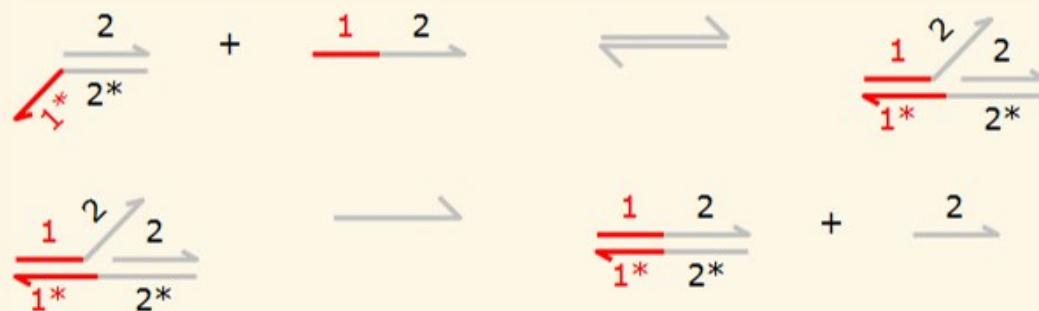
Long complementary segments bind *irreversibly*



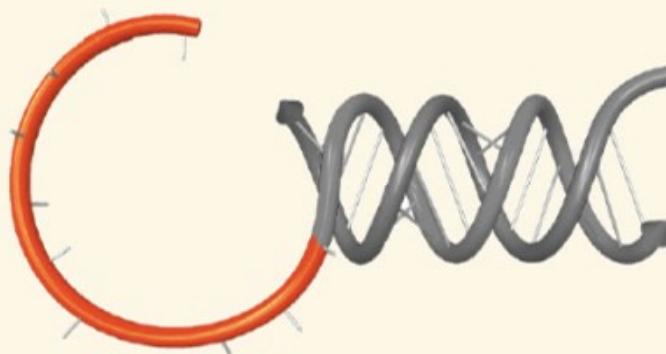
# MOLECULAR DISPLACEMENT

Video not supported

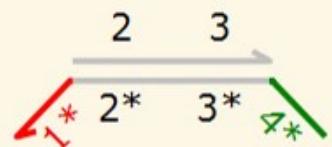
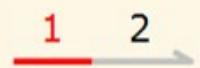
# REACTIONS



Describes strands like this interacting:



# AND CIRCUIT



# AND CIRCUIT

$$\begin{array}{c} 2 \quad 3 \\ \hline \longrightarrow \end{array}$$

$$\begin{array}{cccc} 1 & 2 & 3 & 4 \\ \overleftarrow{\text{---}} & \longrightarrow & \text{---} & \overrightarrow{\text{---}} \\ 1^* & 2^* & 3^* & 4^* \end{array}$$

## DOMAIN SPECIFIC LANGUAGE



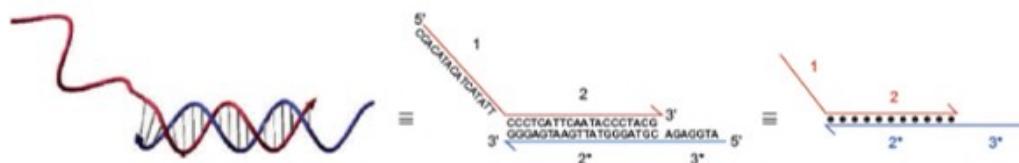
## DYNAMIC STRAND DISPLACEMENT (DSD) TOOL

<http://research.microsoft.com/dna>  
Search: Visual DSD

## DSD RELATED PUBLICATIONS

### Dynamic DNA nanotechnology using strand displacement reactions

David Yu Zhang<sup>1</sup> and Georg Seelig<sup>2</sup>



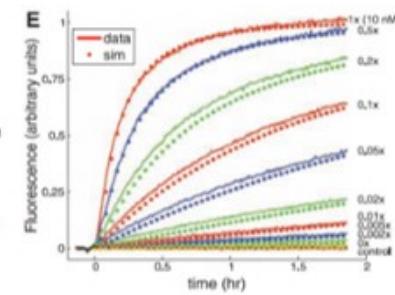
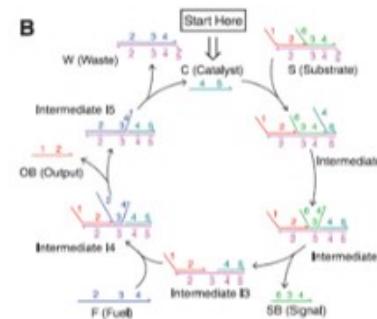
NATURE CHEMISTRY | VOL 3 | FEBRUARY 2011

### Scaling Up Digital Circuit Computation with DNA Strand Displacement Cascades

Lulu Qian<sup>1</sup> and Erik Winfree<sup>1,2,3\*</sup>

### Engineering Entropy-Driven Reactions and Networks Catalyzed by DNA

David Yu Zhang,<sup>1†</sup> Andrew J. Turberfield,<sup>2</sup> Bernard Yurke,<sup>3\*</sup> Erik Winfree<sup>1†</sup>

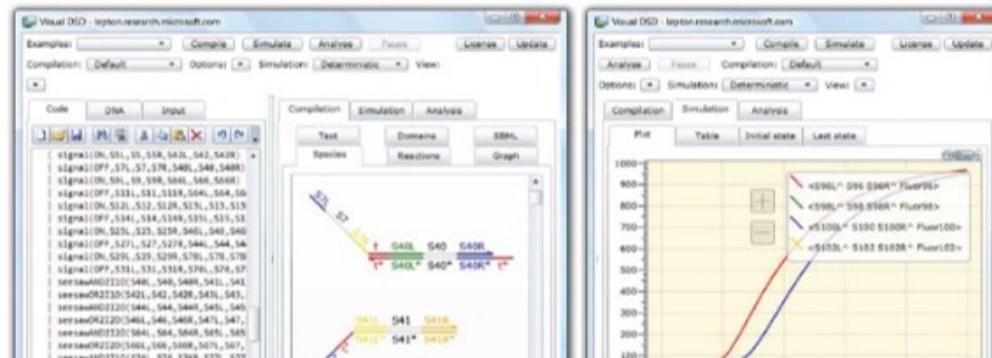
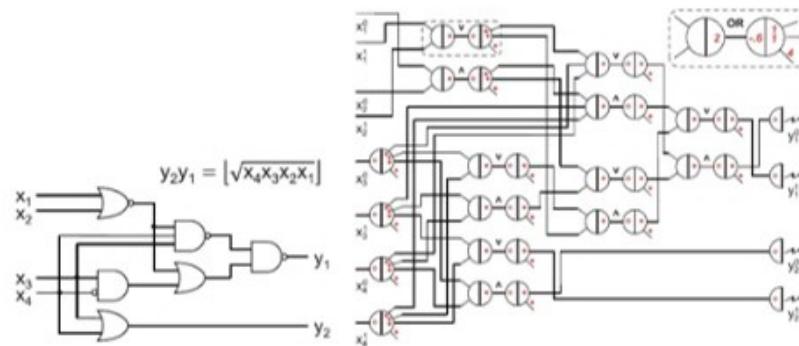


SCIENCE VOL 318 16 NOVEMBER 2007

# CIRCUITS DESIGNED WITH DSD

## Scaling Up Digital Circuit Computation with DNA Strand Displacement Cascades

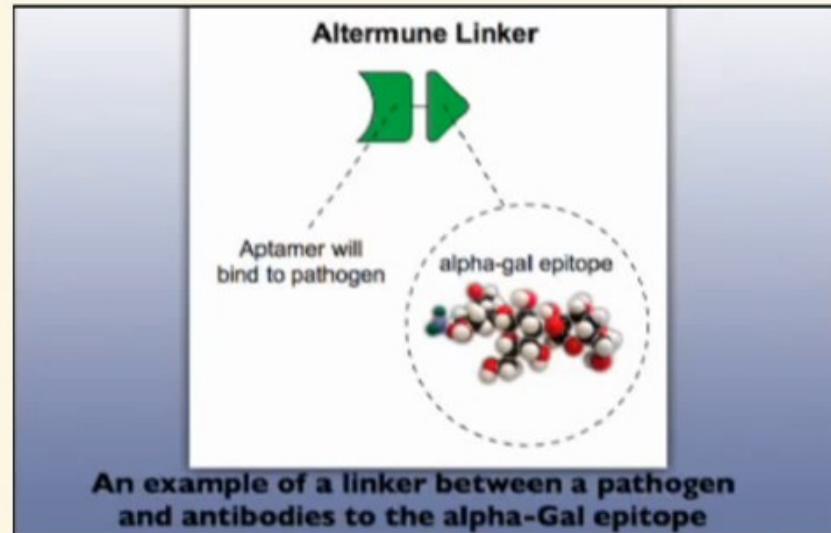
Lulu Qian<sup>1</sup> and Erik Winfree<sup>1,2,3\*</sup>



## DNA APTAMERS

DNA aptamer binds to:

- a pathogen (something bad)
- a molecule our immune system already recognizes and immediately removes (eats) along with anything attached to it



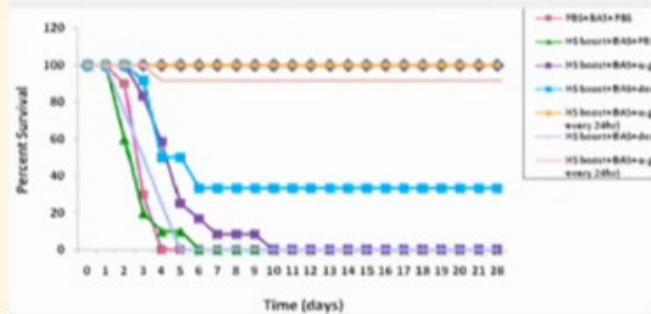
Patented (US20100285052) by Kary Mullis  
(incidentally, also Nobel prize for inventing the Polymerase Chain Reaction)

## DNA APTAMERS

Result: instant immunity

- Mice poisoned with Anthrax plus aptamer (100% survival)
- a molecule our immune system already recognizes and immediately removes (eats) along with anything attached to it

Survival Curve of A/J Mice Immunized with Human Serum, Challenged with BAS and Treated with  $\alpha$ -gal PAA-12 Aptamer and Doxycycline

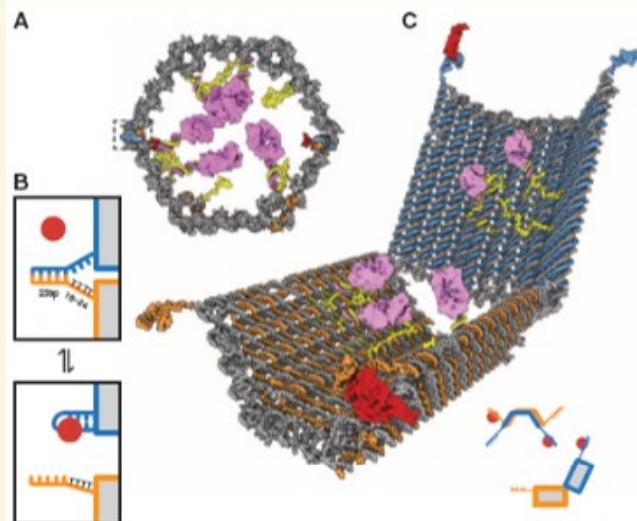


Patented (US20100285052) by Kary Mullis  
(incidentally, also Nobel prize for inventing the Polymerase Chain Reaction)

## DNA ORIGAMI BOX (DELIVERY)

### A Logic-Gated Nanorobot for Targeted Transport of Molecular Payloads

Shawn M. Douglas,\* Ido Bachelet,\* George M. Church†



# CORRECTNESS

At least two levels:

- The systems we describe
- The simulation of those systems

## FSCHECK

- F# port of QuickCheck from Haskell
- Allows property based testing
- Example: List.rev is idempotent
  - $\forall l. \text{rev}(\text{rev } l) = l$
- Testing:
  - Generate a large number of lists
  - Compute both sides
  - Compare

## FSCHECK (GENERATORS)

To generate a large number of list of pairs:

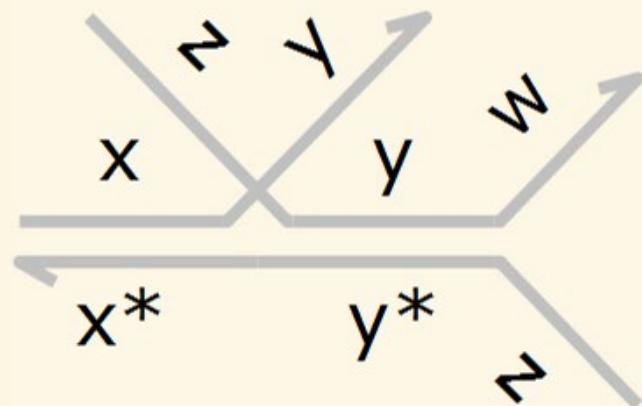
```
let gen_int = Arb.generate<int>

let gen_pair =
    Gen.map2 (fun a b -> (a,b)) gen_int gen_int

let gen_list = gen_int |> Gen.listOf
```

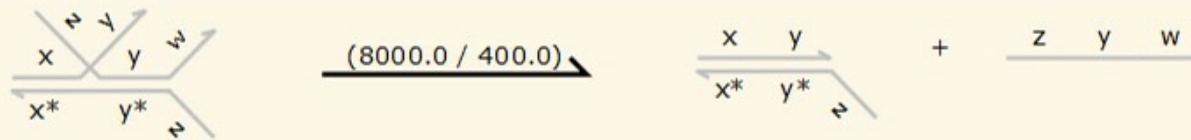
## FSCHECK (MELTING)

Obtain the constituent strands of a DSD molecule



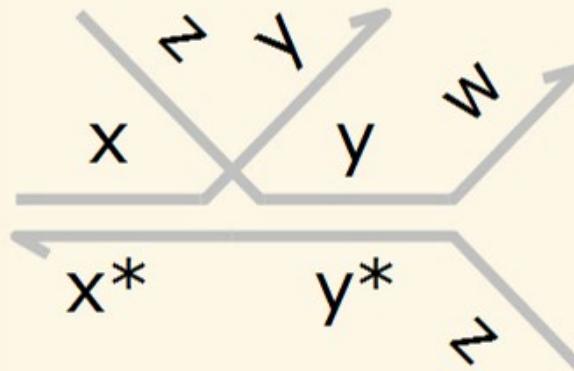
## FSCHECK (MELTING PROPERTY)

- Reactions preserve strands and thus melting
  - $\forall a \rightarrow b. \text{melt}(a) = \text{melt}(b)$
- Testing:
  - Generate a large number of reactions
  - Melt both sides
  - Compare

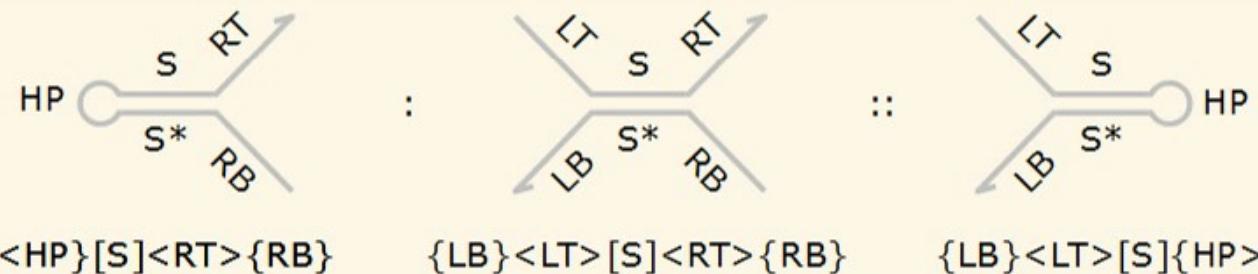


## FSCHECK (DATA STRUCTURES)

We have a textual representation of species



$[x]<y>:<z>[y]<w>\{z\}$



This representation mirrors the data structures

## FSCHECK (DATA STRUCTURES)

### From segment.ml

```
type side = Left | Right
type t =
  | Double of (domain list * domain list * domain list * domain list * domain list)
  | Hairpin of (domain list * domain list * domain list * domain list * side * bool)
```

### From gate.ml

```
type t = segment list list
```

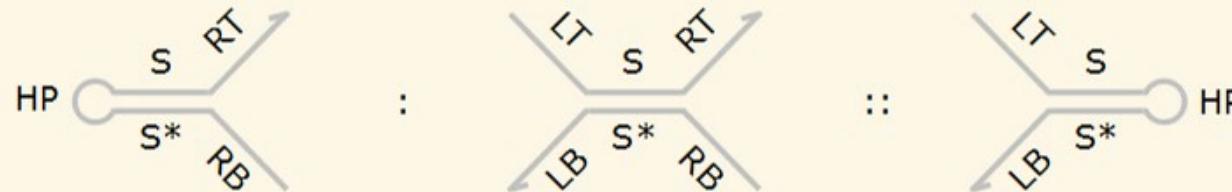
## FSCHECK (DATA STRUCTURES)

### From segment.ml

```
type side = Left | Right  
type t =  
| Double of (domain list * domain list * domain list * domain list * domain list)  
| Hairpin of (domain list * domain list * domain list * domain list * side * bool)
```

### From gate.ml

```
type t = segment list list
```



Hairpin(RB,RT,S,HP,Left,false)

Double(LB,LT,S,RT,RB)

Hairpin(LB,LT,S,HP,Right,true)

## FSCHECK (GENERATORS)

### Generating segments:

```
let dsd_segment_middle s =
    let ds = dsd_domain_list (s/5)
    Gen.map5 (fun lb lt s rt rb -> Segment.Double (lb, lt, s, rt, rb)) ds ds ds ds ds

let dsd_hairpin_left s =
    let ds = dsd_domain_list (s/4)
    Gen.map4 (fun ob ot s hp -> Segment.Hairpin (ob, ot, s, hp, Segment.Left, false)) ds ds ds ds

let dsd_hairpin_right s =
    let ds = dsd_domain_list (s/4)
    Gen.map4 (fun ob ot s hp -> Segment.Hairpin (ob, ot, s, hp, Segment.Right, true)) ds ds ds ds

let dsd_segment_left s =
    Gen.oneof [ dsd_segment_middle s
                dsd_hairpin_left s ]

let dsd_segment_right s =
    Gen.oneof [ dsd_segment_middle s
                dsd_hairpin_right s ]
```

## FSCHECK (GENERATORS)

### Generating segments:

```
let dsd_segments_middle s =
  let s = s|>float|>sqrt|>int
  Gen.nonEmptyListOf (dsd_segment_middle s) |> Gen.resize s

let dsd_segments_left s =
  let x = Gen.eval s (Random.newSeed ()) (dsd_segment_left s)
  let s = s|>float|>sqrt|>int
  let xs = Gen.eval s (Random.newSeed ()) (dsd_segment_middle s |> Gen.listOf)
  gen { return x::xs }

let dsd_segments_right s =
  let x = Gen.eval s (Random.newSeed ()) (dsd_segment_right s)
  let s = s|>float|>sqrt|>int
  let xs = Gen.eval s (Random.newSeed ()) (dsd_segment_middle s |> Gen.listOf)
  gen { return xs@[x] }
```

## FSCHECK (GENERATORS)

### Generating segments:

```
let dsd_gate_left s =
  let x = Gen.eval s (Random.newSeed ()) (dsd_segments_left s)
  let s = s|>float|>sqrt|>int
  let xs = Gen.eval s (Random.newSeed ()) (dsd_segments_middle s |> Gen.listOf)
  gen { return x::xs }

let dsd_gate_right s =
  let x = Gen.eval s (Random.newSeed ()) (dsd_segments_right s)
  let s = s|>float|>sqrt|>int
  let xs = Gen.eval s (Random.newSeed ()) (dsd_segments_middle s |> Gen.listOf)
  gen { return xs@[x] }

let dsd_gate s =
  Gen.oneof [ dsd_gate_left s
              dsd_gate_right s ]
```

# CORRECTNESS

At least two levels:

- The systems we describe
- The simulation of those systems

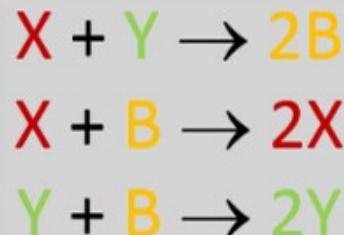
# A DNA CONSENSUS ALGORITHM



Y (Minority)



X (Majority)



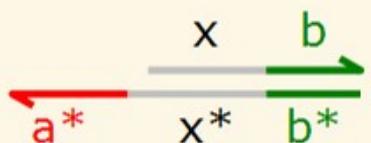
X (Majority)

# A DNA CONSENSUS ALGORITHM

Video not supported

## MOLECULAR COMPONENTS

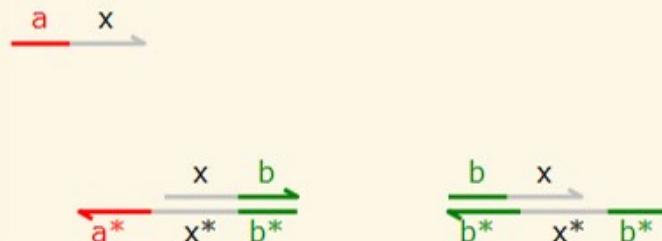
Possible to encode arbitrary reactions  
A useful motif: (called seesaw)



This implements  $a \leftrightarrow b'$

## MOLECULAR COMPONENTS

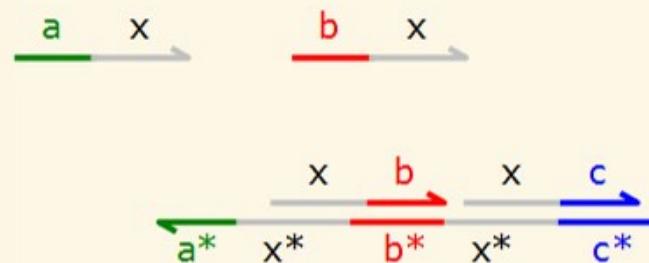
Possible to encode arbitrary reactions  
A useful motif: (called seesaw)



This implements  $a \leftrightarrow b$

## MOLECULAR COMPONENTS

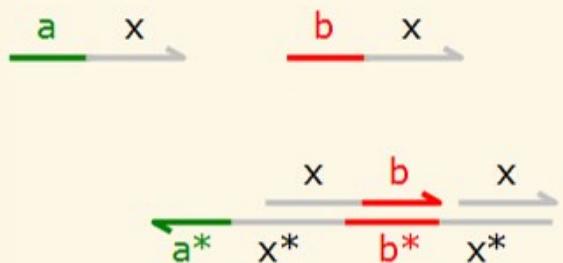
Possible to encode arbitrary reactions  
Seesaws can be chained



This implements  $a + b \leftrightarrow b' + c'$

## MOLECULAR COMPONENTS

Possible to encode arbitrary reactions  
Seesaws can be made irreversible

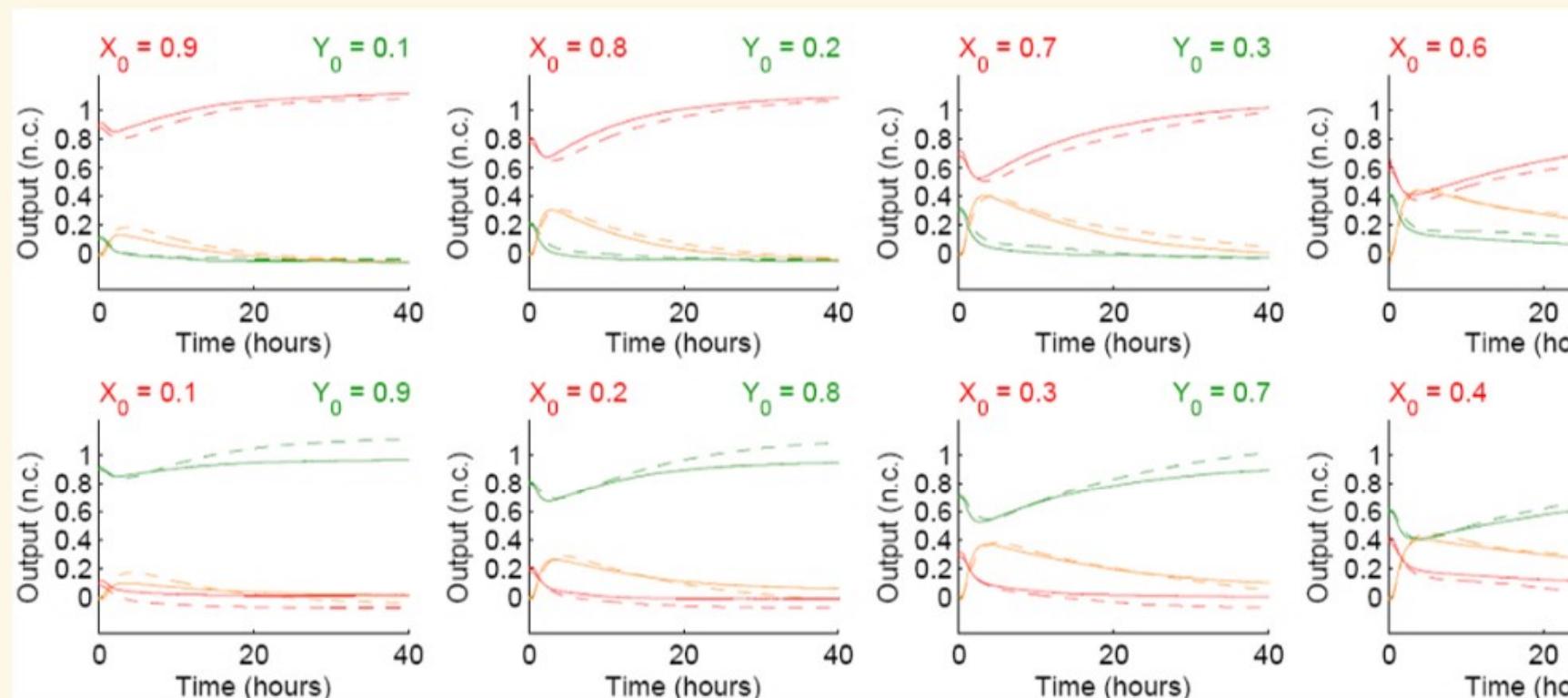
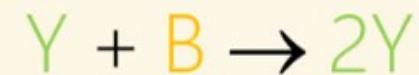
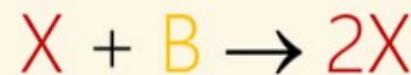
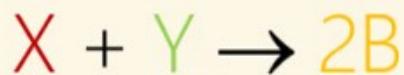


This implements  $a + b \rightarrow b' + w$

## MOLECULAR COMPONENTS

- $X + Y \rightarrow 2B$
- $X + B \rightarrow 2X$
- $Y + B \rightarrow 2Y$

## PREDICTING DYNAMICS OF THE FULL CIRCUIT



— Experimental Data  
 - - - Model prediction

# ANALYSING FUNCTION: Z3 SMT SOLVER

## Satisfiability Modulo Theories

## FAQ (TO THE SMT SOLVER)

- Is there a trace of this program that leads to buffer overflow?
- Is there an execution of this protocol that reveals the secrets?
- Is there a command line argument that will crash this program?
- Is there a program implementing this function?
- Is there a program with this behaviour?
- Is there a program solving this problem?

## FAQ (TO THE SMT SOLVER)

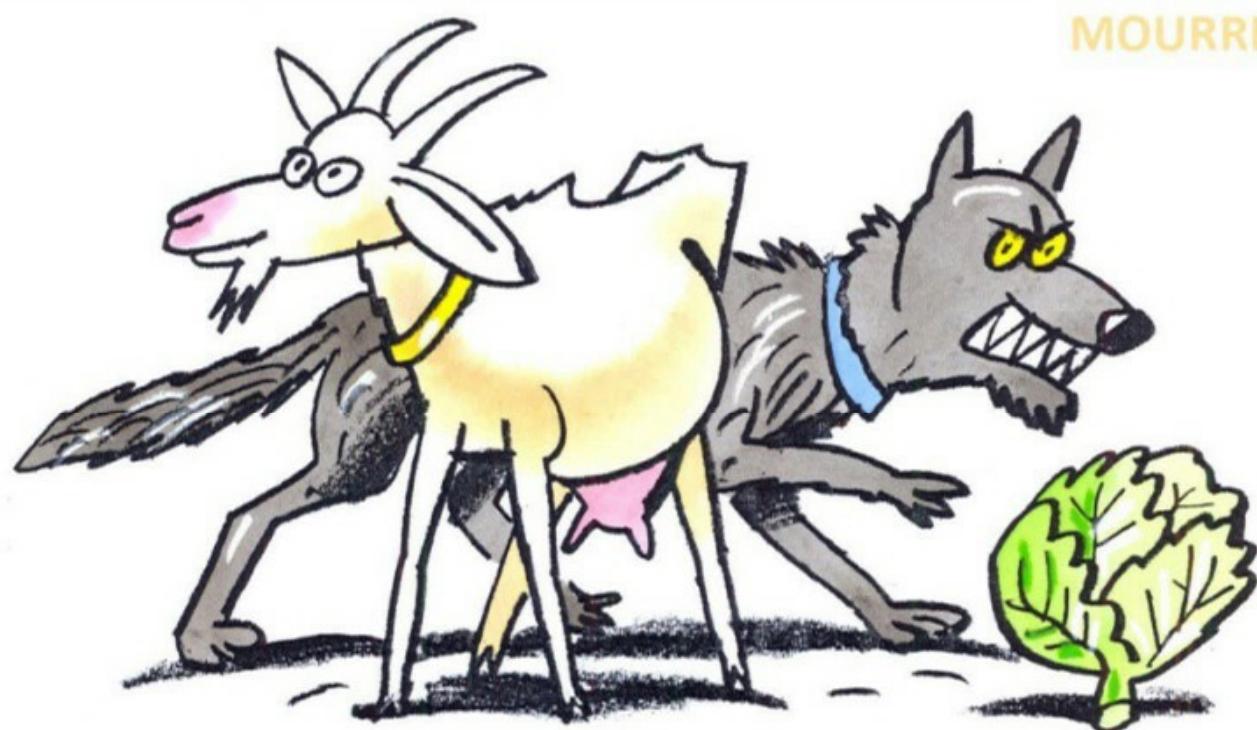
- Is there a trace of this program that leads to buffer overflow?
  - $\exists t. t \in \text{Traces}(P) \wedge \text{overflow}(t)$
- Need a theory rich enough to express Traces and overflow
- A negative answer is a proof of absence of buffer overflows

Execution trace  $\leftrightarrow$  series of states of biological system

## A CLASSICAL PUZZLE

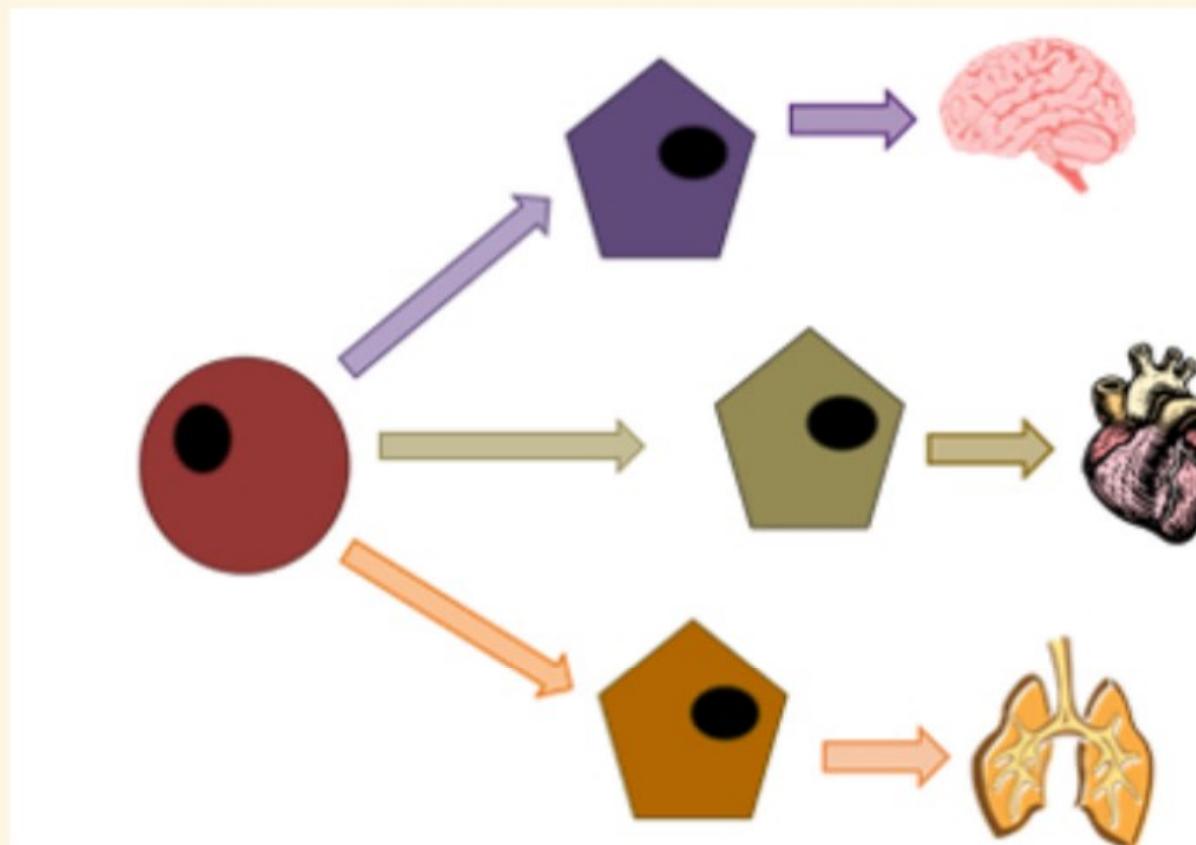
A man wish to cross a river with his Cabbage, his Goat and his Wolf

- If left alone, goat eats cabbage
- If left alone, wolf eats goat
- Boat can only carry man plus 1 item



# DEMO SMT/Z3

# STEM CELLS



Stem cells can become any adult cell type. How they decide their fate is currently unknown.

## GENETIC PROGRAMS

- Human DNA contain about 20000-25000 genes



- Genes act by being *transcribed* into a protein.
- Some of these proteins are transcription factors which perform the transcriptions.

# GENE TRANSCRIPTION

Video not supported <http://www.wehi.edu.au/education/wehitv>

## GENE NETWORK

Genes:



Genes affect the transcription rate of other genes.

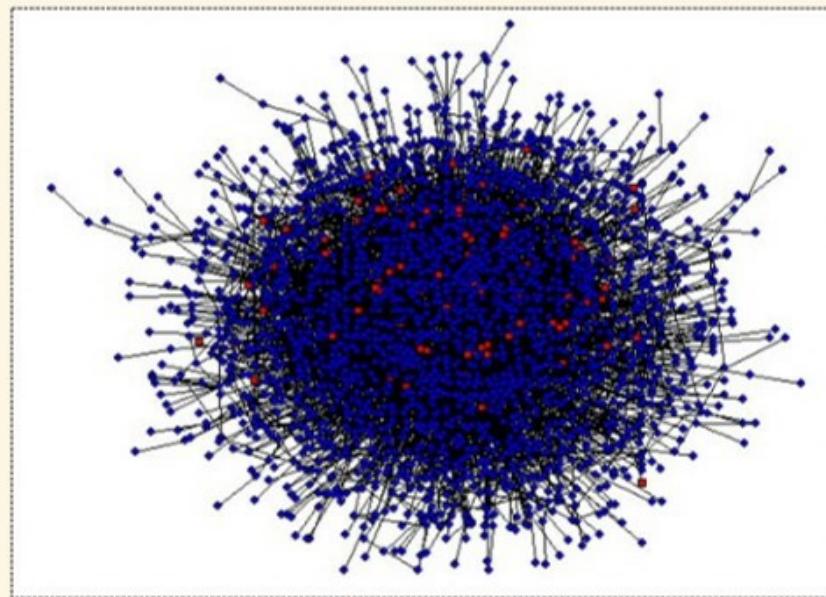
Upregulation (positive interaction):

→ **black arrow**

Downregulation (negative interaction):

¬ **red tack**

## FULL NETWORK (MOUSE)



## INTERACTIONS

The interactions are from experimental results of gene expression levels.

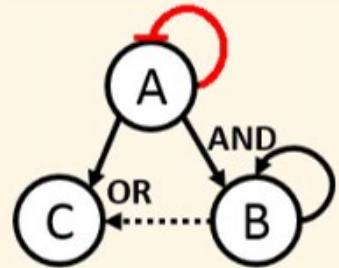
Positive interaction:

→ **black arrow**

Possible positive interaction:

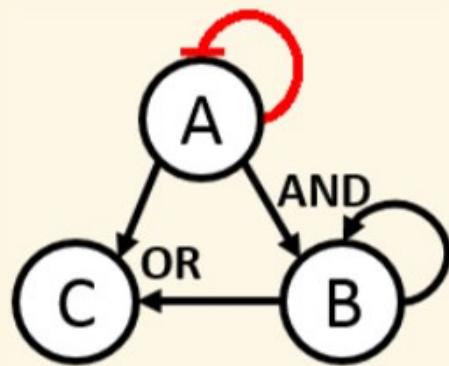
-→ **dotted arrow**

## TEXTUAL ENCODING

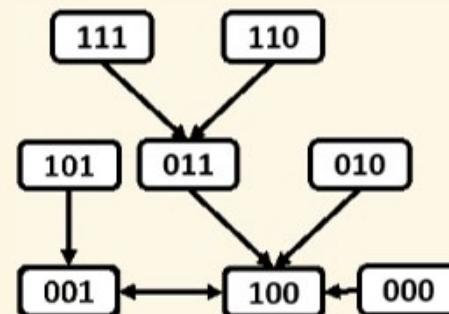
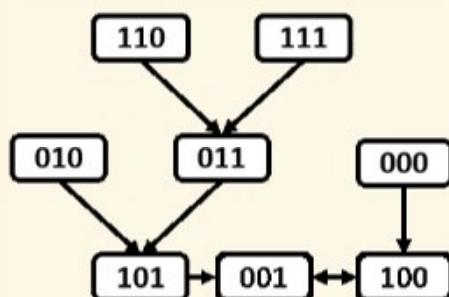
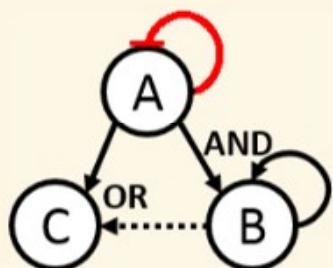
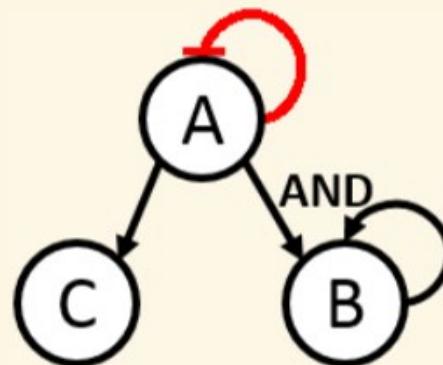

$$\begin{aligned}\forall b, b'. T(b, b') \leftrightarrow [b'(1) = \neg b(1)] \wedge \\ [b'(2) = b(1) \wedge b(2)] \wedge \\ [b'(3) = \text{if } c(1) \text{ then} \\ \quad b(1) \vee (2) \\ \text{else} \\ \quad b(1)]\end{aligned}$$

## SMT ENCODING

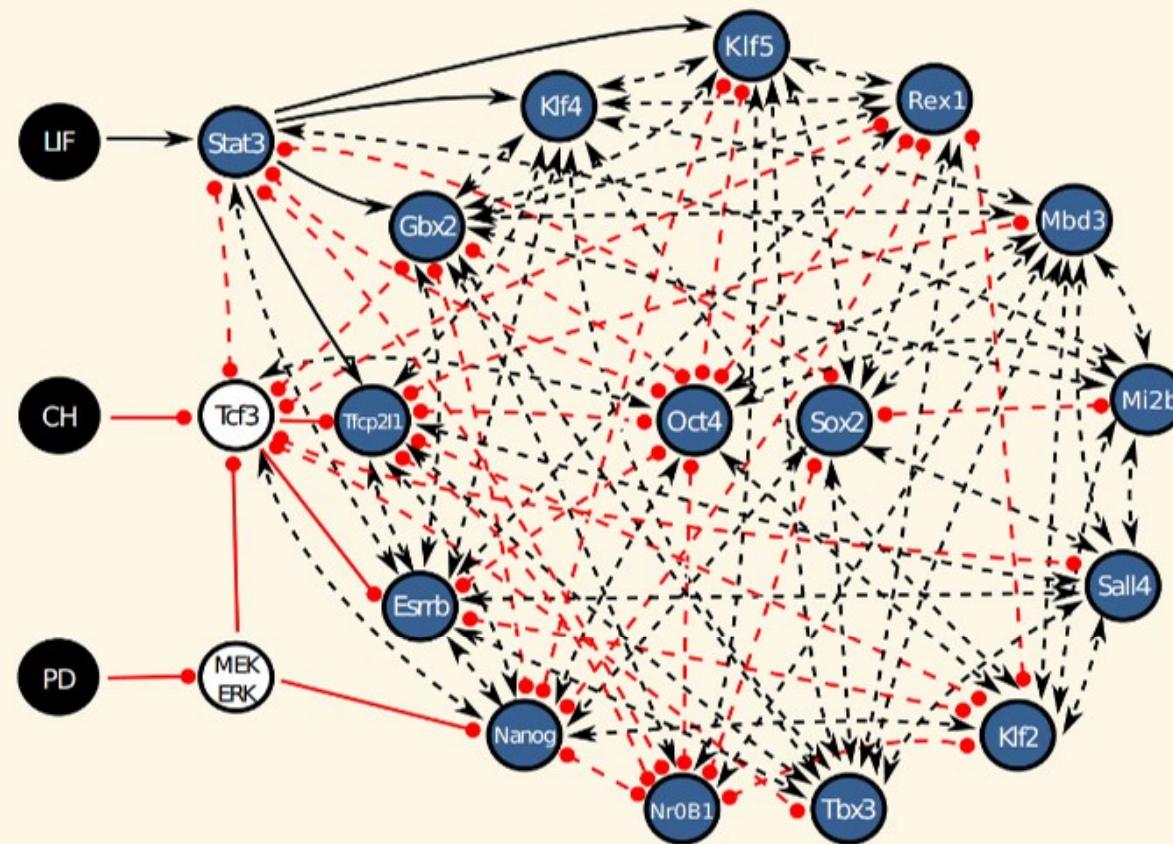
Try the optional B->C interaction



and with B-C missing

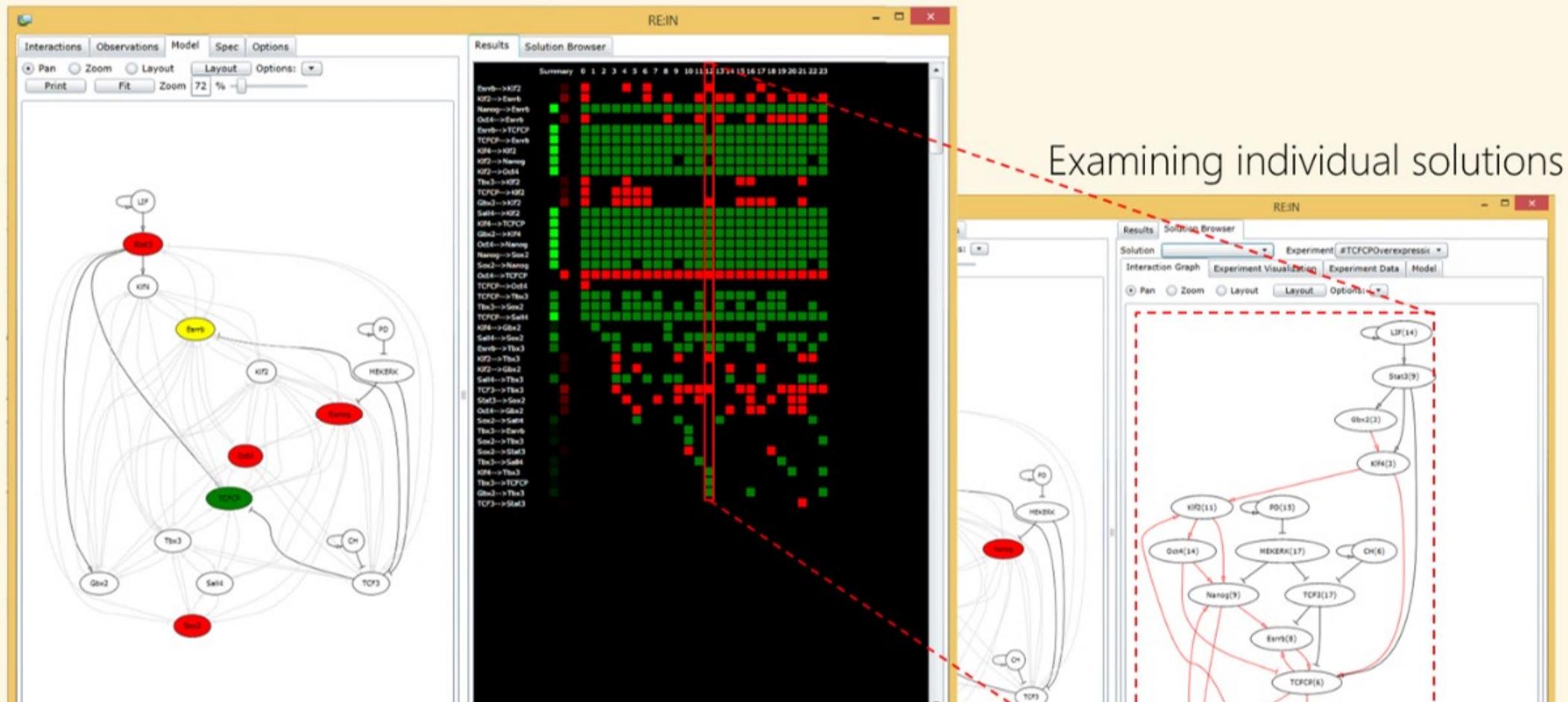


## STEM CELL NETWORK



# MODEL SYNTHESIS

Enumerating and comparing solutions



## REASONING ENGINE FOR INTERACTION NETWORKS (REIN) TOOL

<http://research.microsoft.com/rein>

Search:

## COMPUTE RESOURCES

Despite the sophisticated methods each model and specification has substantial compute requirements

- 20 minutes compute on one core per model and spec
- One researcher easily saturates 100s cpu HPC cluster for days

Loads are extremely bursty

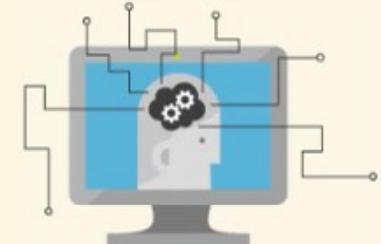
- For the public version we use Azure
- Fairly reasonable process to share compute code
- Then stick an HTTP socket on with a web UI

Azure cloud computing



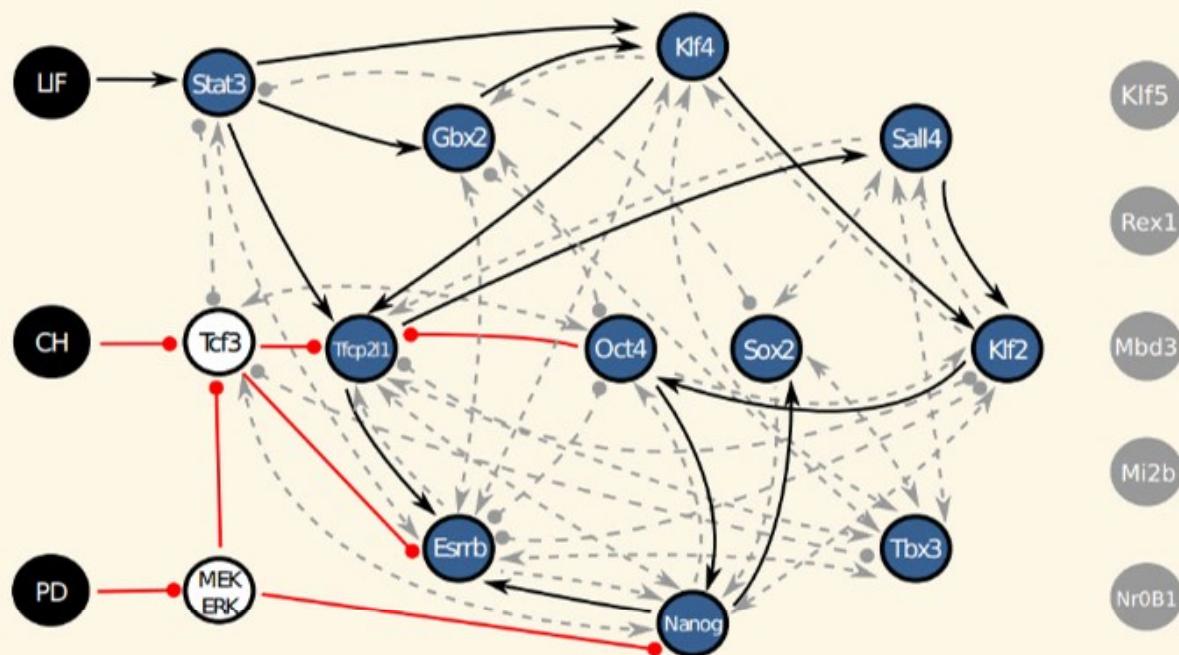
[azure.microsoft.com/services/functions/](https://azure.microsoft.com/services/functions/)

Azure machine learning



[azure.microsoft.com/services/machine-learning/](https://azure.microsoft.com/services/machine-learning/)

# MINIMAL GENE NETWORK



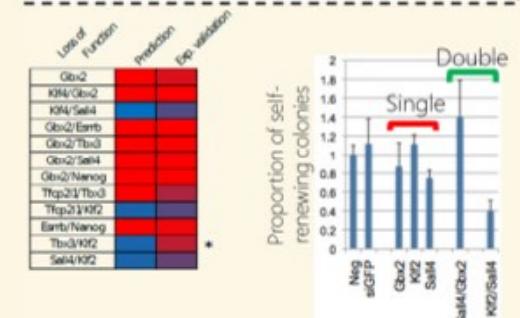
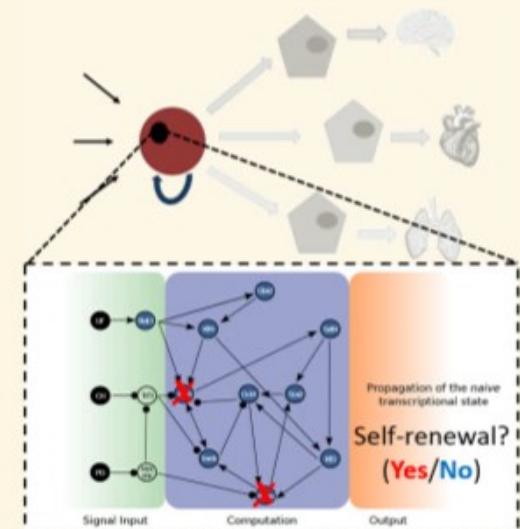
## A MINIMAL SELF-RENEWAL PROGRAM

Identified a simple minimal network capable of reproducing the experimentally observed self-renewal behaviour

Reasoned about the effects of compound gene perturbations (double gene knockdowns) on self-renewal

Generated a number of predictions capturing complex compound effects

Validated predictions experimentally with high success rate



Defining an essential transcription factor program for naïve pluripotency  
S-J. Dunn, G. Martello, B. Yordanov, S. Emmott, A. G. Smith (2014)

## STEM CELLS IN THE CLINIC

Type 1 diabetes => embryonic stem cell derived pancreatic precursor cells



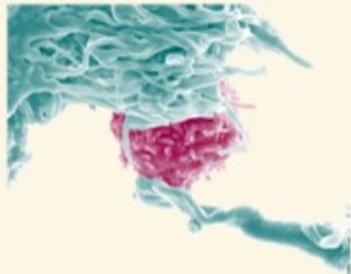
Severe myopia => transplantation of human retinal pigmented epithelium



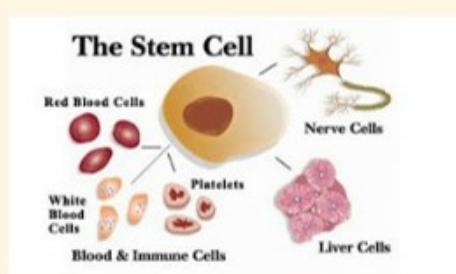
Macular degeneration => transplation of iPS grown retinal (September, 2014)



# BIOLOGICAL COMPUTATION



Immunology



Development



Synthetic Biology



Molecular Programming



## BIOLOGY DESIGN TOOLS

Simulation (Stochastic, ODE, PDE);  
Analysis (probabilistic model-checking, symbolic verification with Z3);  
Parameter estimation (Filzbach); Visualisation (DDD, MSAGL);  
Unbounded computation  
Interoperability (SBML, C#, PRISM, Matlab, Chaste, CellModeller)

## COMPUTATIONAL SCIENCE GROUP & COLLABORATORS



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