

LambdaConf 2018 – 6/05/2018

Metaphorisms: Deriving Divide-and-Conquer Recursive Programs from Relational Specifications

Presenter: William Harvey, PhD

Principal Engineer, OCLC



José N. Oliveira, PhD

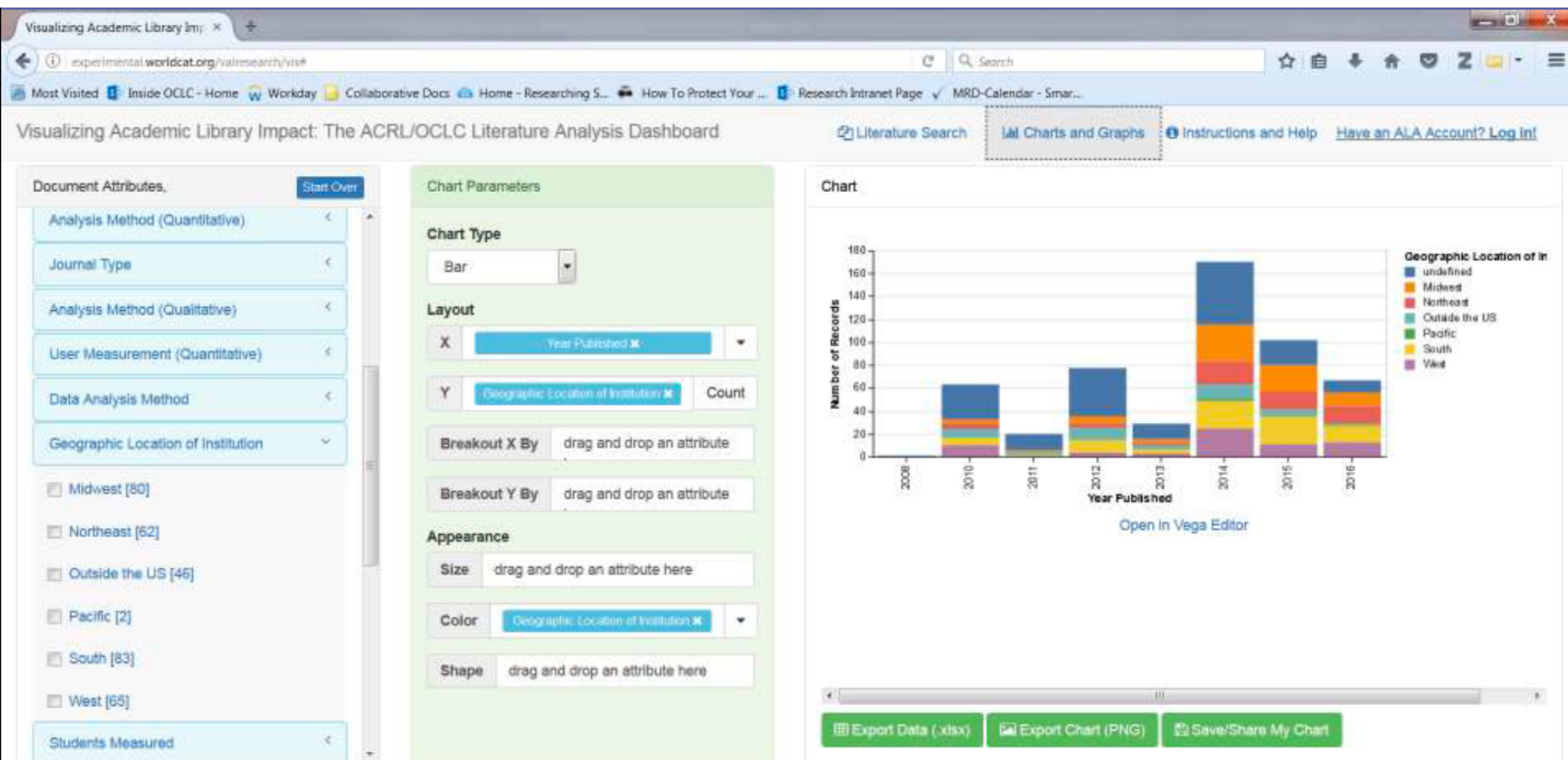
Professor, University of Minho, Portugal

Talk Overview

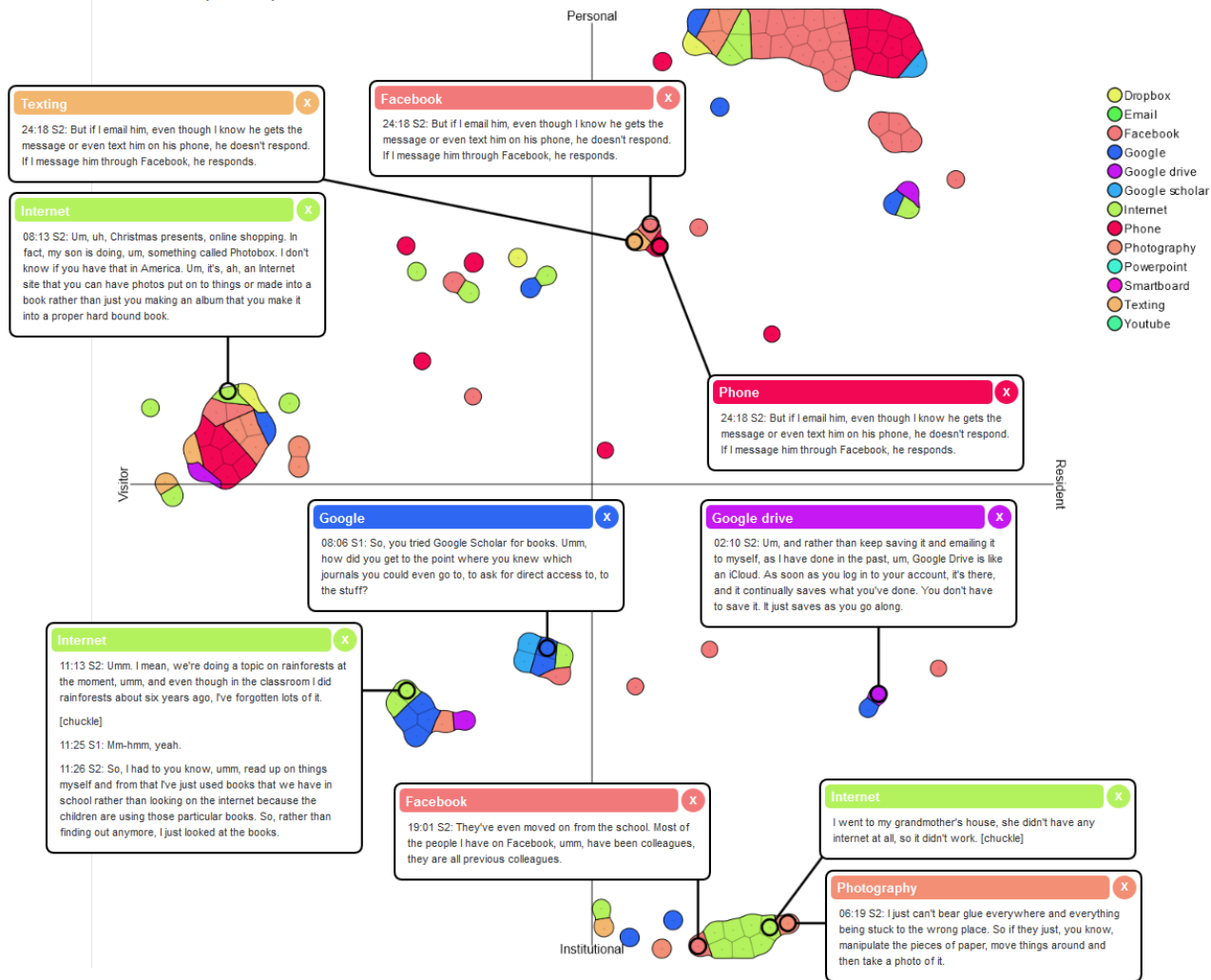
- FP and category theory at OCLC
- Our research problem
- Introduction to **metaphorisms**
- Examples

About OCLC

- We help libraries
- We're a nonprofit global library cooperative
- Thousands of library members in more than 100 countries
- WorldCat: Largest online public access catalog in the world
- We maintain the Dewey Decimal System



UKU7 (After)



Exciting Work

- Big data modeling: Homotopical patch theory, groupoids, torsors, etc.
- DSLs for data cleaning
- Information geometry
- Just starting the FP journey
- Let's talk!

METAPHORISMS: THE MOTIVATION

Our Research Project

**Use WorldCat Discovery to find more
than two billion library resources**

**More ways to explore the
resources of your library ...
and the world's libraries**



Our Research Project

- Behavioral (Clickstream) Analytics
 - What are users doing?
 - How can we assist?
- Terabytes of log data
- Reduced to ~100GB for our study
- **~5GB gzipped**

Succinct

Enabling Queries on Compressed Data



Rachit Agarwal, PhD



Anurag Khandelwal



Ion Stoica, PhD

Succinct

- A compression format for unstructured text
- Query unstructured, compressed text files directly
 - No data scans
 - No secondary indexes
 - No data decompression
- <http://succinct.cs.berkeley.edu/>

Succinct Operations

- `s.substring(offset: Nat, length: Nat): String`
- `s.count(str: String): Nat`
- `s.indicesOf(str: String): [Nat]`
- `s.findAllInRange(str1: String, str2: String): [Nat]`
- ...etc...

Unfortunately...

- Not implemented for our language
- Can't call OSS version through FFI
- OSS version maxes out at 4GB (Int32)

Reinventing the Wheel

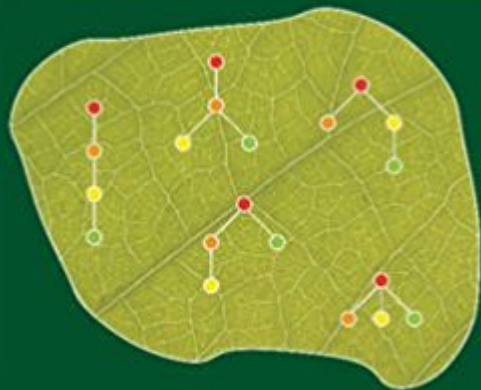
- Implement *de novo*
- Port to language X
- Copy/tweak

Build You A Succinct

- Two ingredients:
 - Compressed permutation data structure
 - Suffix array construction algorithm

COMPACT DATA STRUCTURES

A PRACTICAL APPROACH



GONZALO
NAVARRO

On Compressing Permutations and Adaptive Sorting *

Jérémy Barbay Gonzalo Navarro

Dept. of Computer Science, University of Chile

Suffix Array Construction

- DC3 / Skew algorithm
 - Clever algorithm!
 - Divide and conquer

There Should Be A Better Way

- Program Synthesis
 - Write a spec for program's desired behavior
 - (Semi-)mechanically synthesize a program satisfying that spec

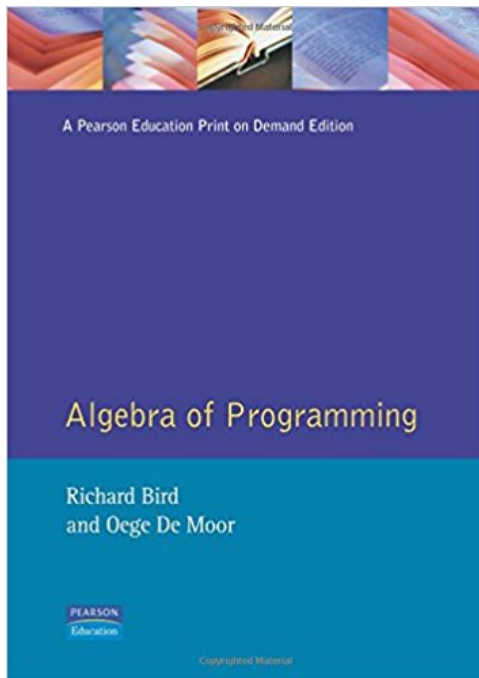
Bird-Meertens Formalism

- A categorical calculus of relations
- Category theory makes it language-agnostic
- Relations are more flexible than functions
- Calculus makes it formulaic
- Prove things!

Bird-Meertens Formalism

- Input: A **relational** spec of your algorithm
- Middle: Step-by-step derivation via algebraic rules
 - Exposes the degrees of freedom of implementation
- Output: A **functional** program

Bird-Meertens Formalism



- Dynamic programming
- Greedy algorithms
- Exhaustive search
- Divide and conquer
- And more!

Use of the Bird Meertens Formalism

Ankur Taly
(03005017)

Aditya Parameswaran
(03005015)

Ankit Jain
(03005021)

Abstract

In this report, we deal with the paradigm of Constructive Algorithmics or the science of program transformation. We examine the basic ideas of Bird Meertens Formalism and its application to segment problems. We first give the direct application of Bird Meertens Formalism to the Maximum Segment Sum Problem, and also indicate the underlying concepts involved. We then proceed to give an intuitive proof for the Sliding Tails theorem, and demonstrate how it can be applied to a problem.


Metaphorisms

- BMF-style relational program specifications...

...defined over inductive types...

...that mimic formal metaphors!

Metaphors

- “Time is money.”
- “All the world’s a stage.”
- “A monad is a burrito.”
- “Monads are trees with grafting.”
-  “Some say love...it is a razor...”

Metaphors in Software

- Tree
- Pipe
- Stack
- Heap
- Queue
- Spaghetti code





METAPHORS
WE LIVE BY

GEORGE LAKOFF
AND MARK JOHNSON

WITH A NEW AFTERWORD

Formal Metaphors

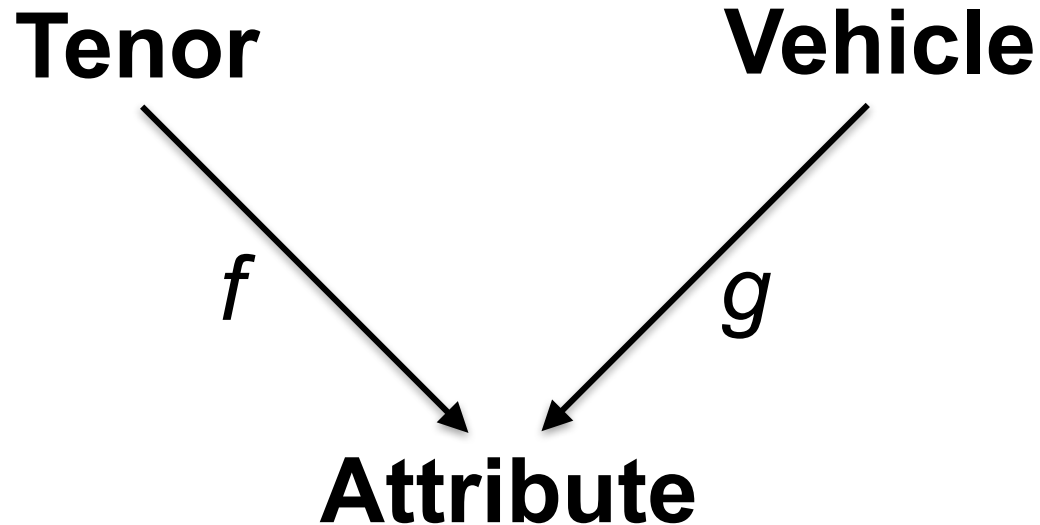
- Three components:
 1. A **tenor** (“Love”)
 2. A **vehicle** (“A Razor”)
 3. A **shared attribute** (“Ouch!”)

“Love is, that you are the knife which I plunge into myself.”

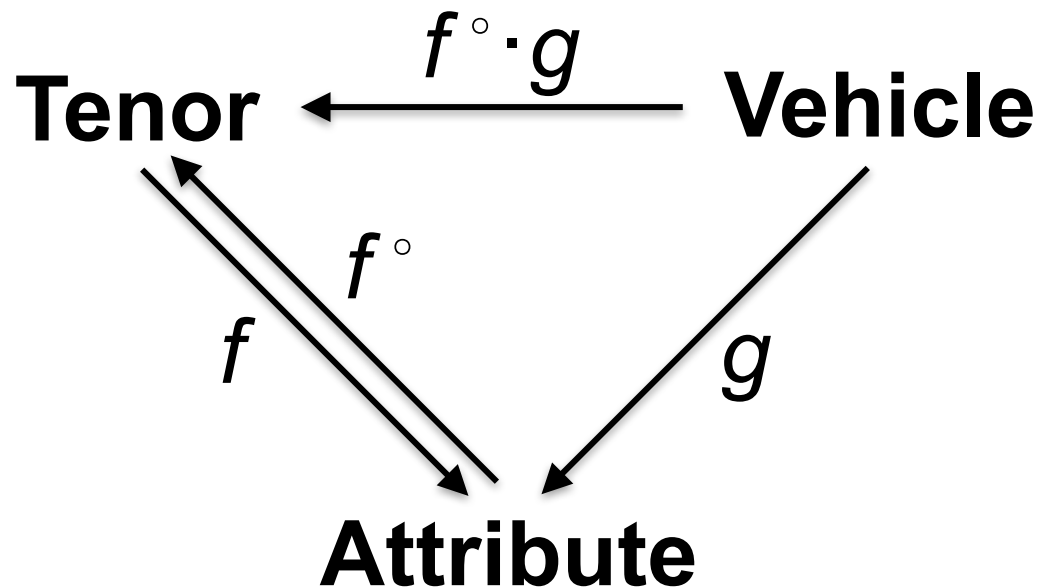
-Franz “Streaming” Kafka



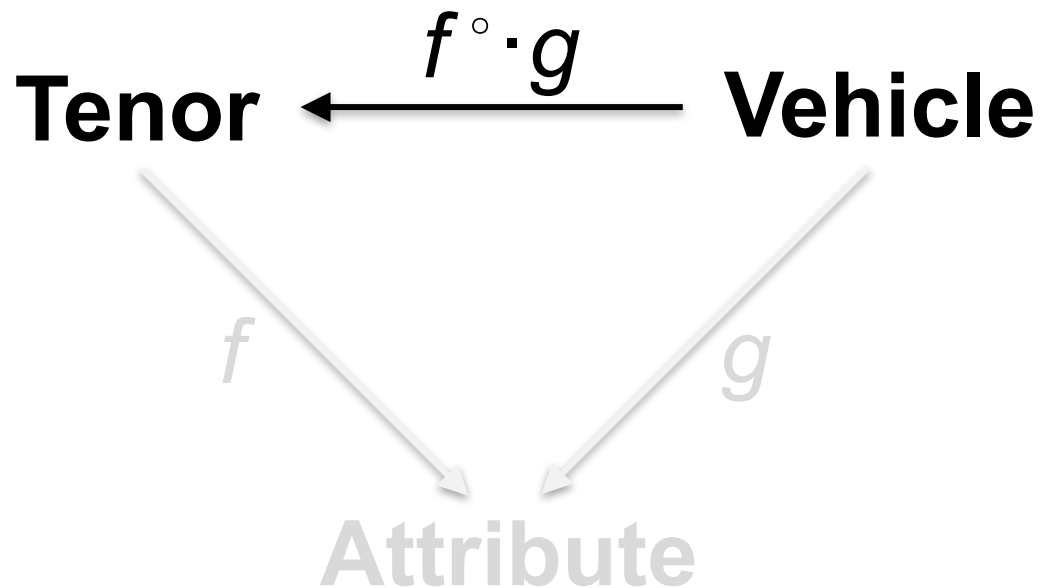
Metaphors, Categorically

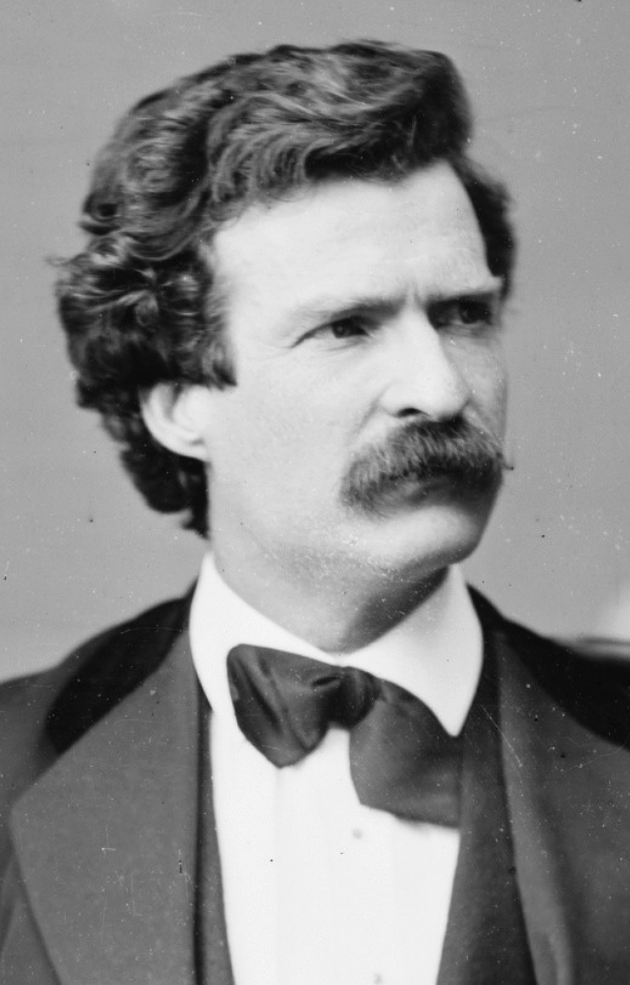


Metaphors, Categorically



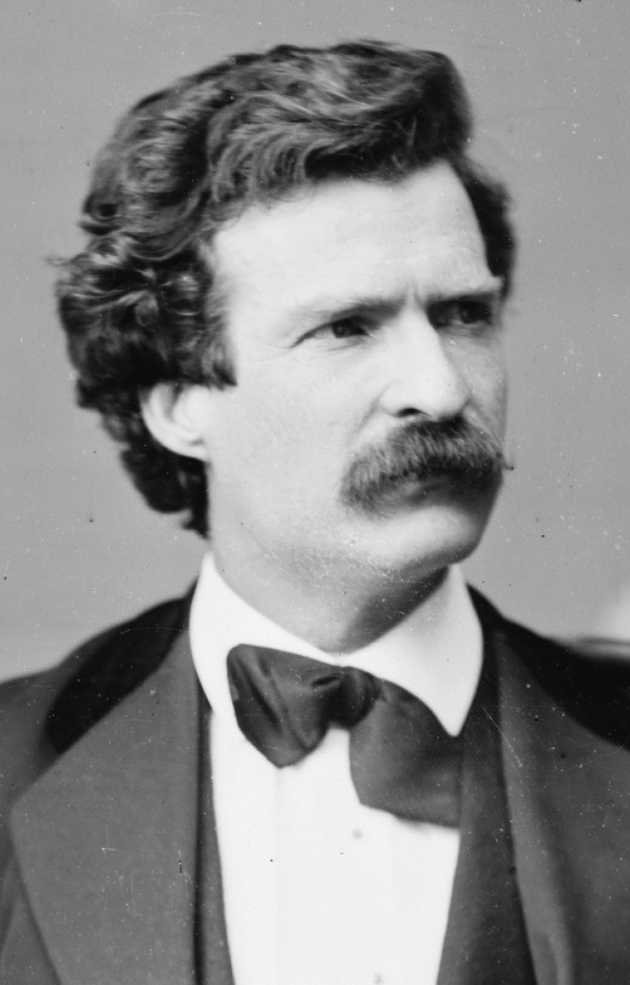
Metaphors, Categorically





**“Politicians and diapers
must be changed often,
and for the same reason.”**

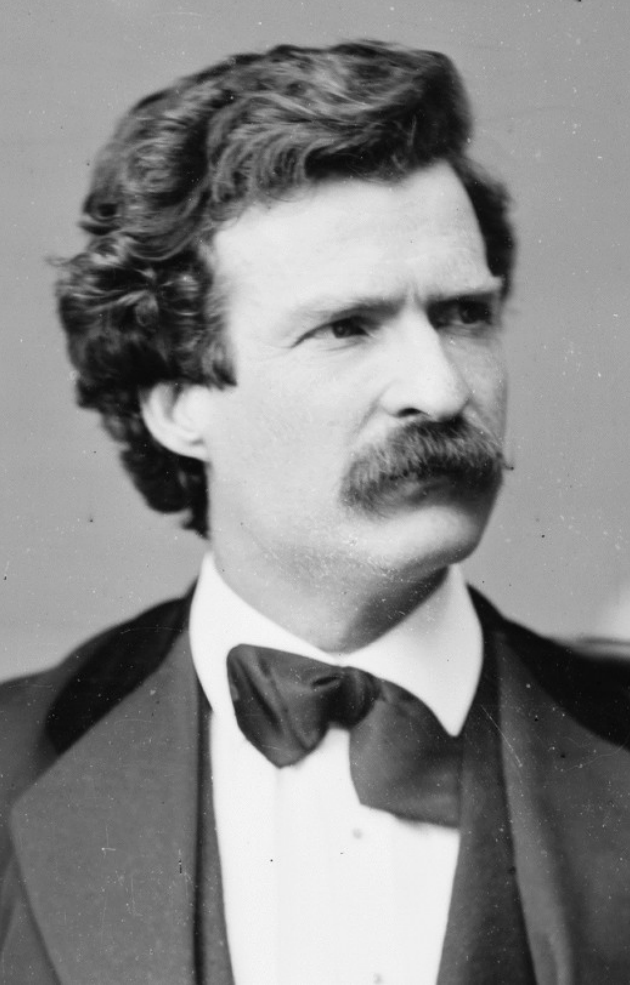
-Mark Twain



Tenor

**‘Politicians and diapers
must be changed often,
and for the same reason.’**

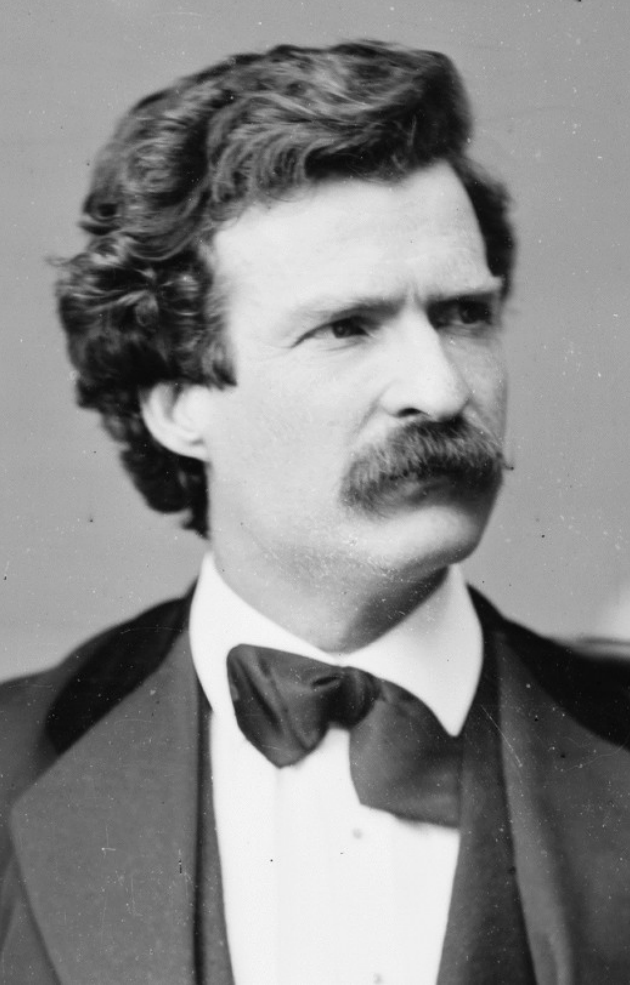
-Mark Twain



Vehicle

“Politicians and diapers must be changed often, and for the same reason.”

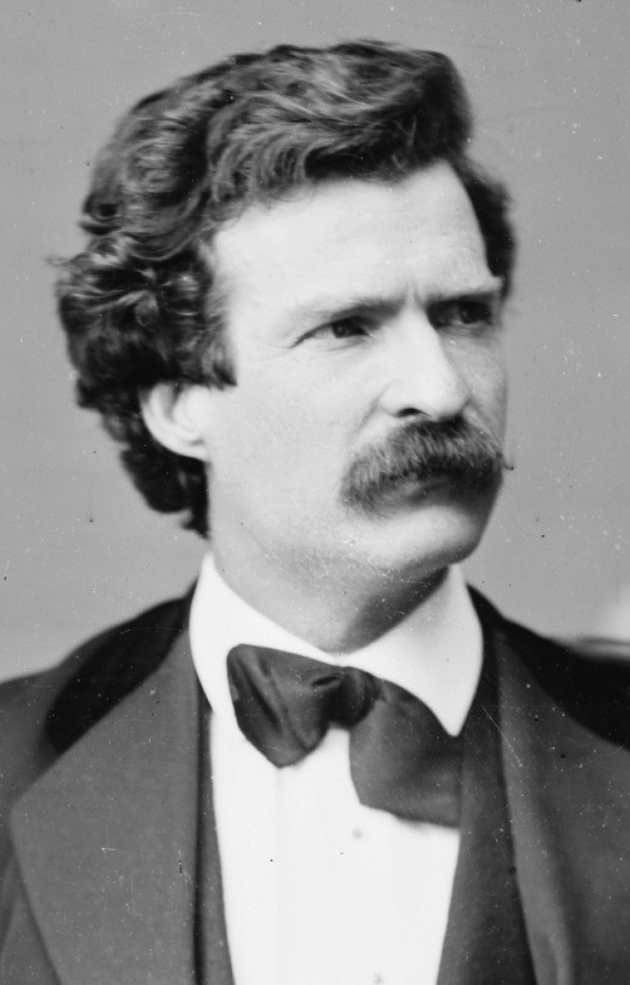
-Mark Twain



**“Politicians and diapers
must be changed often,
and for the same reason.”**

Shared attribute hint

-Mark Twain

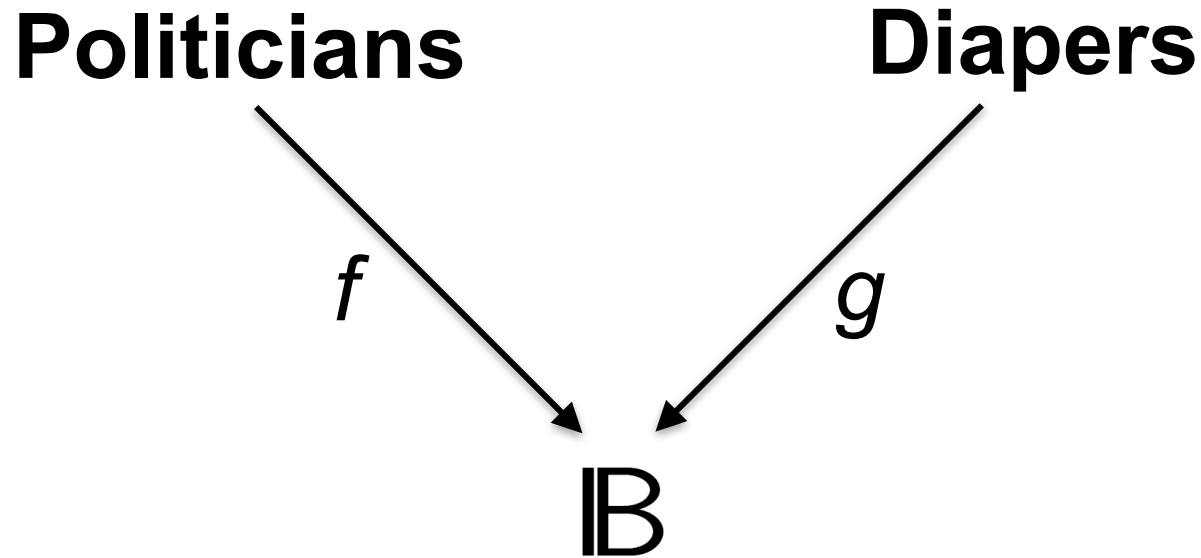


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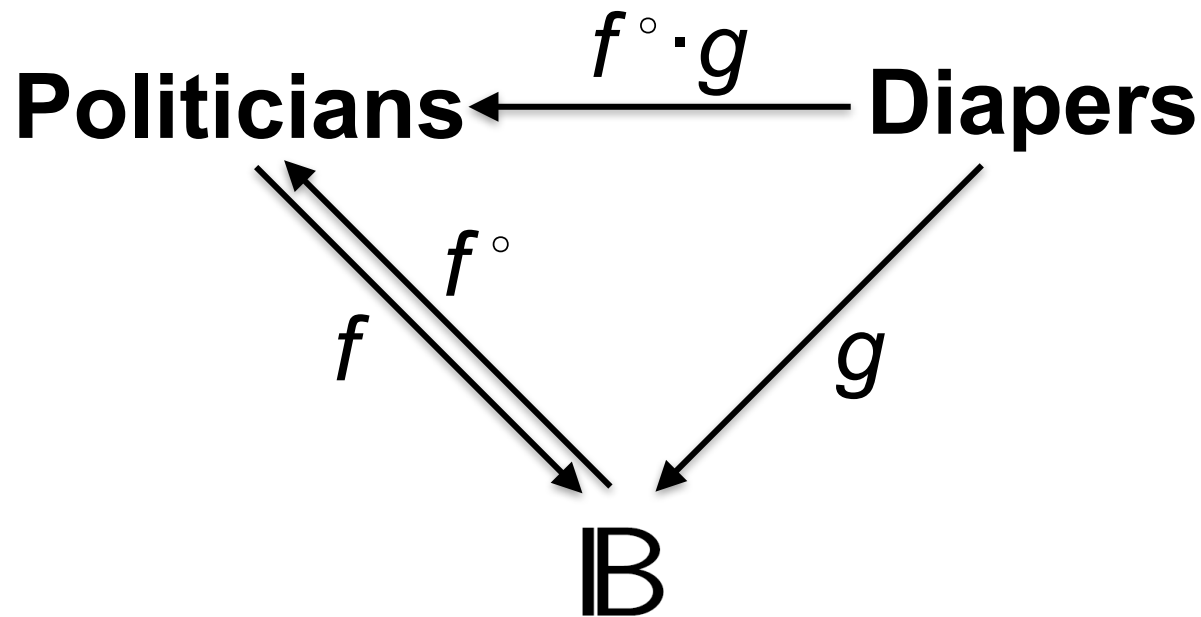
Shared attribute hint

-Mark Twain

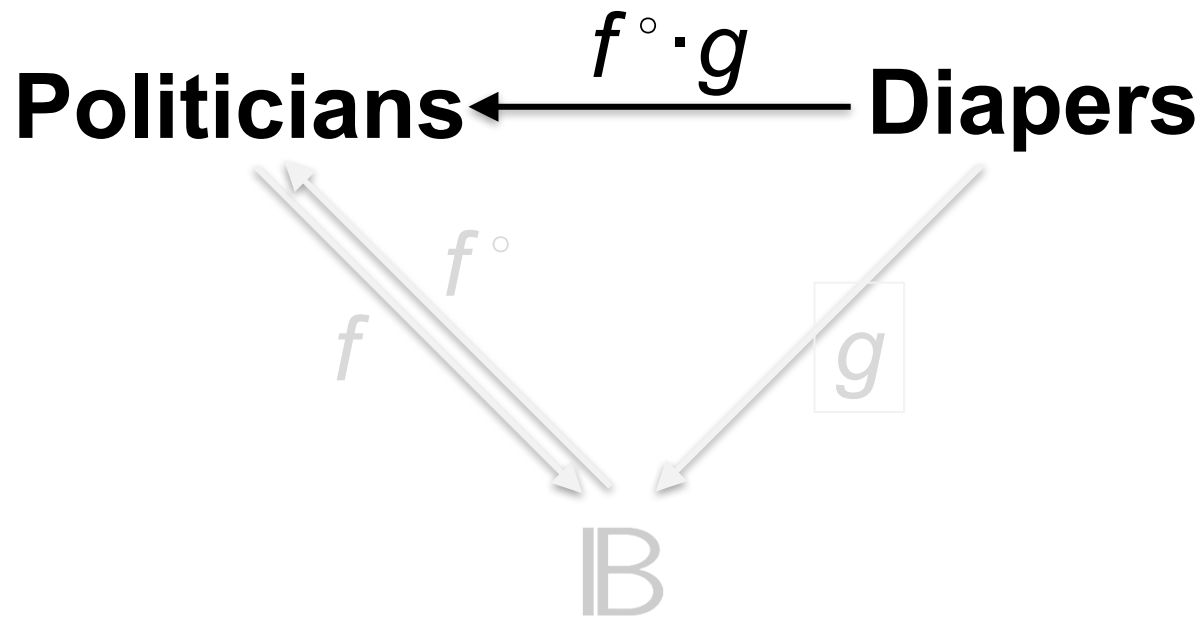
Metaphors, Categorically



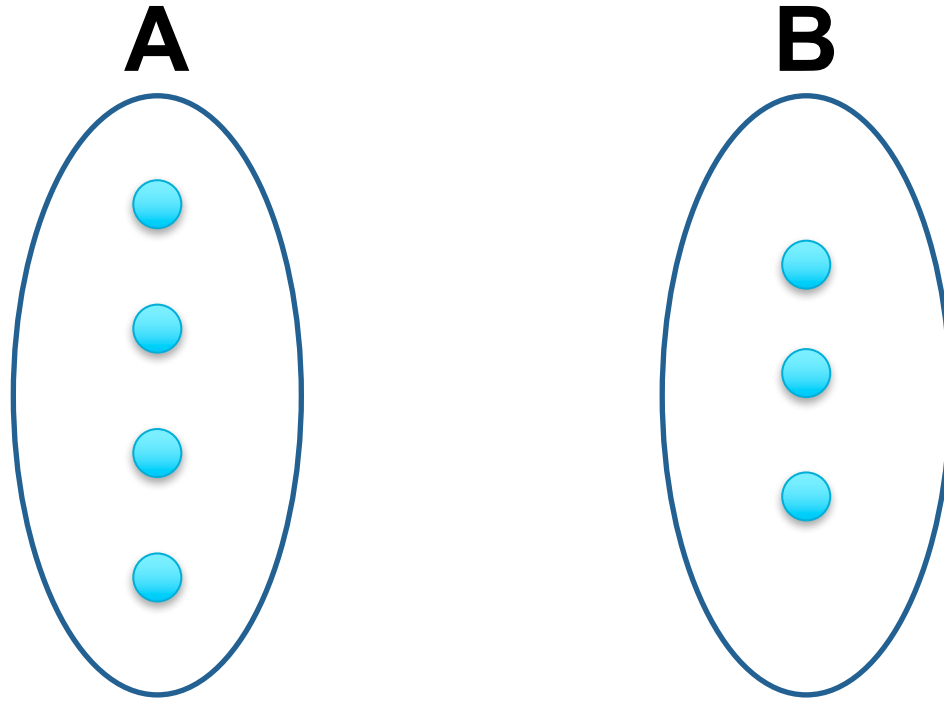
Metaphors, Categorically



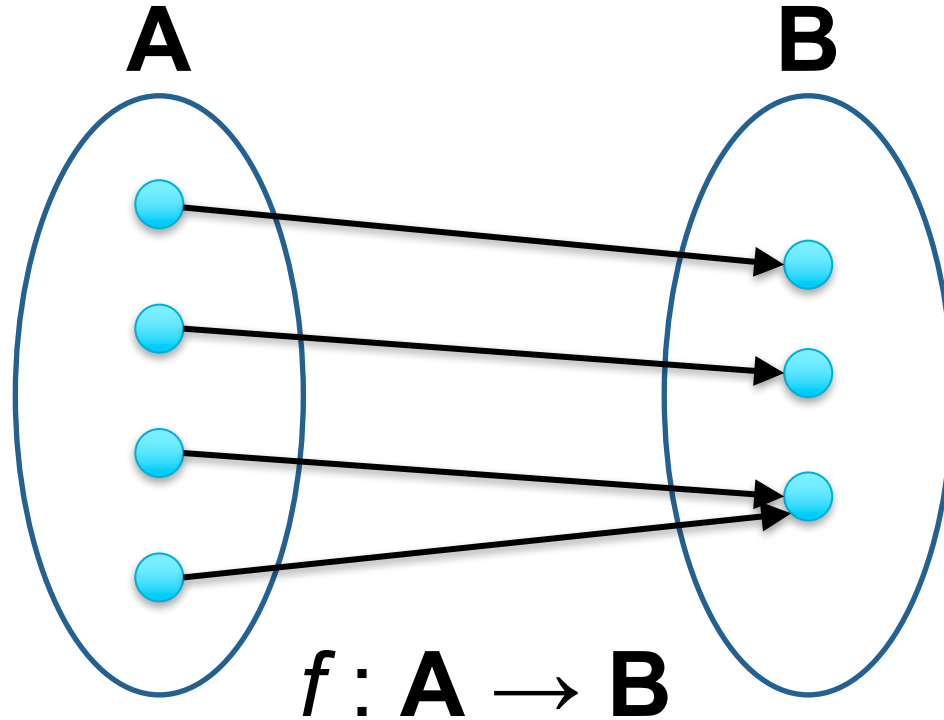
Metaphors, Categorically



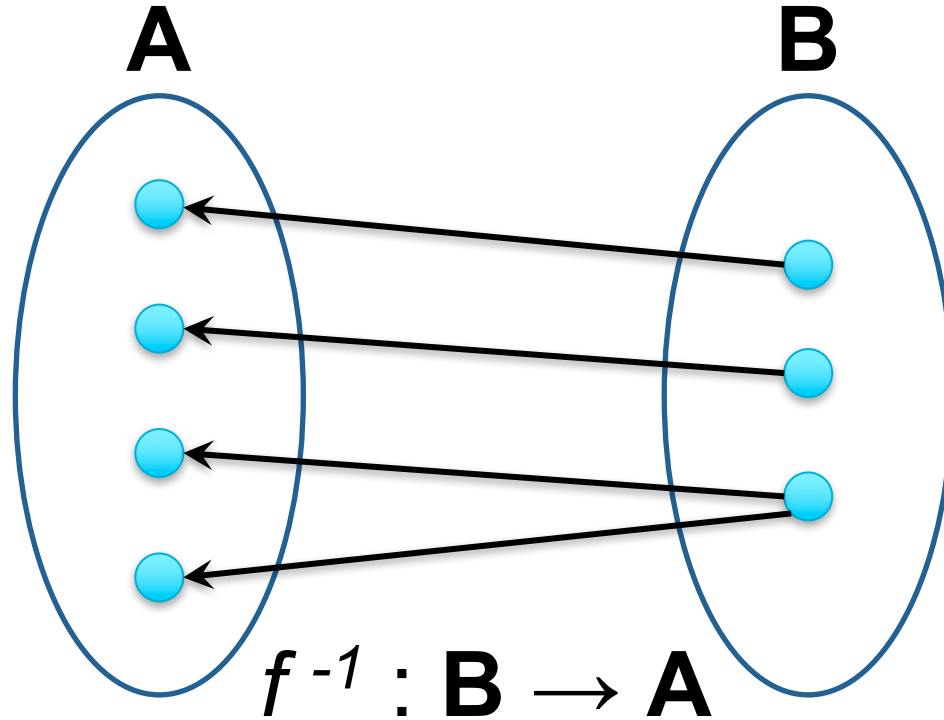
Interlude: Function Converse



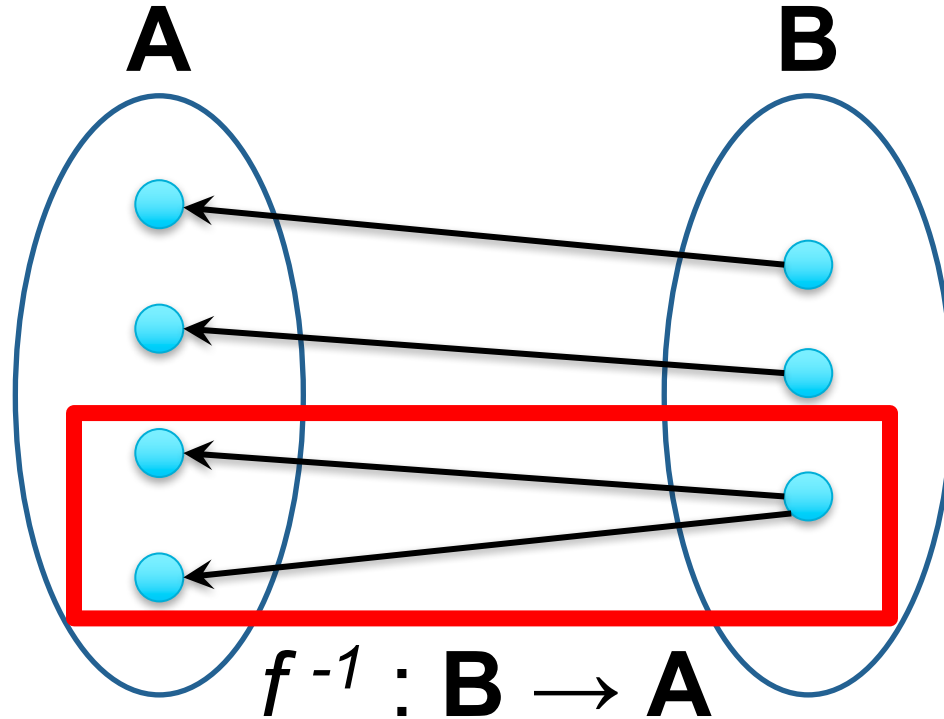
Interlude: Function Converse



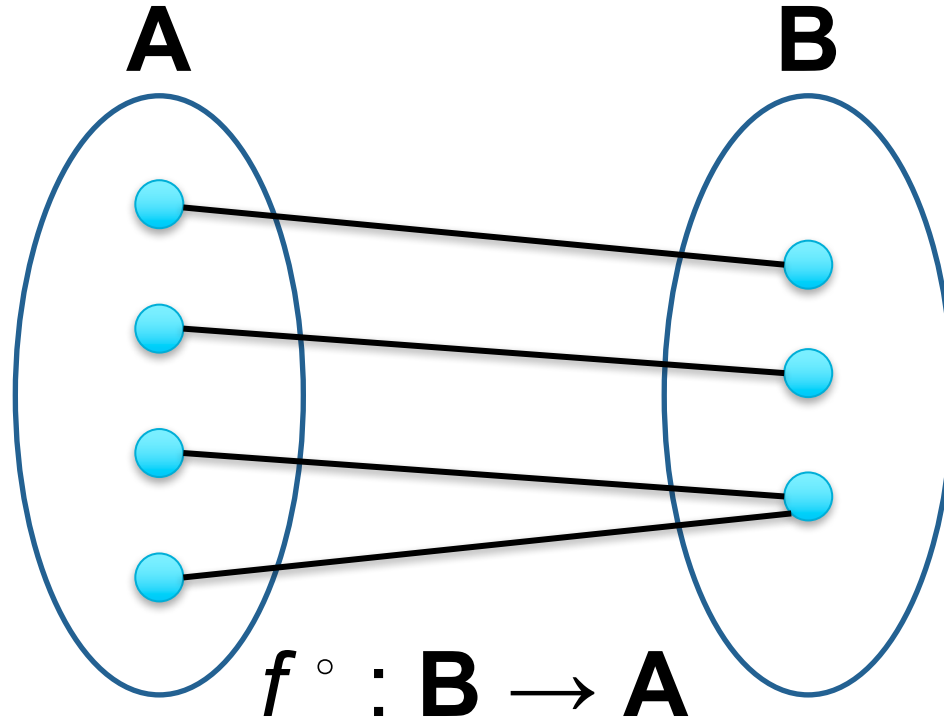
Interlude: Function Converse



Interlude: Function Converse




Interlude: Function Converse




SQL “sequel”


abbreviation for

(Computer Science) structured query language: a computer programming language used for database management

“CITE”  Collins English Dictionary – Complete and Unabridged, 12th Edition 2014 © HarperCollins Publishers 1991, 1994, 1998, 2000, 2003, 2006, 2007, 2009, 2011, 2014

sequela  (sē-kwē'lă) *plural*. **sequelae** [L., sequel]

A condition following and resulting from a disease.

“CITE”  Medical Dictionary, © 2009 Farlex and Partners

Example: Text Formatting

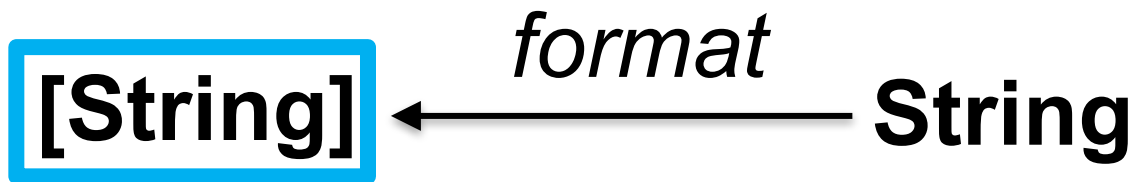
[String] $\xleftarrow{\textit{format}}$ **String**

(e.g., word wrap, scalariform, gofmt, etc.)

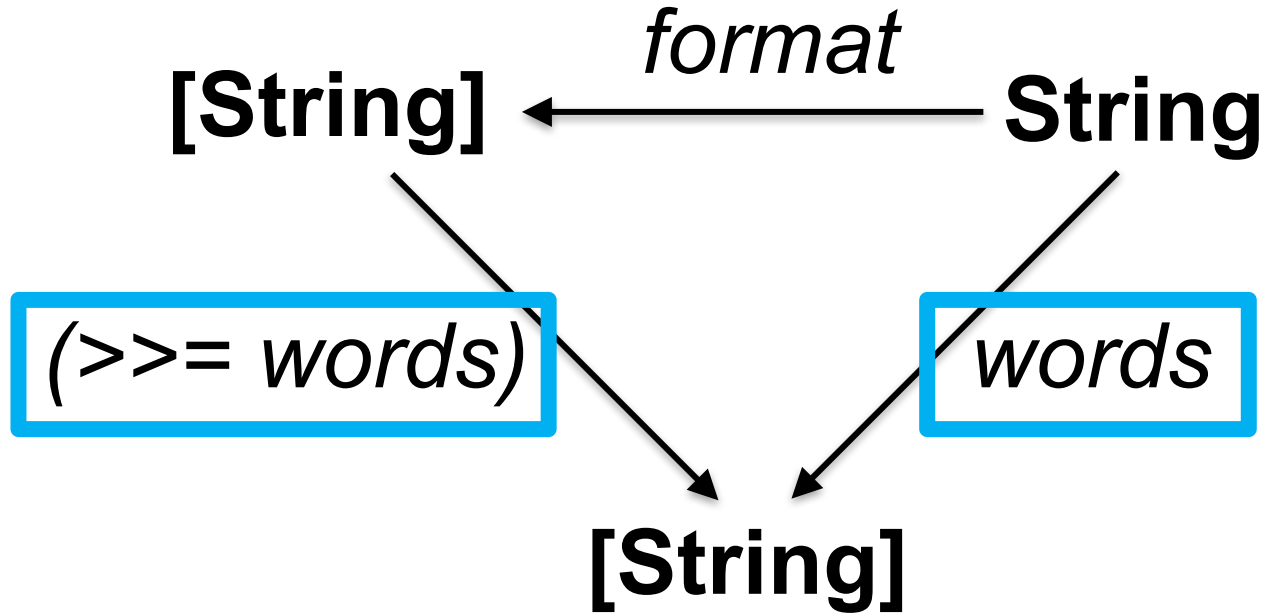
Example: Text Formatting

[String] ← *format* **String**

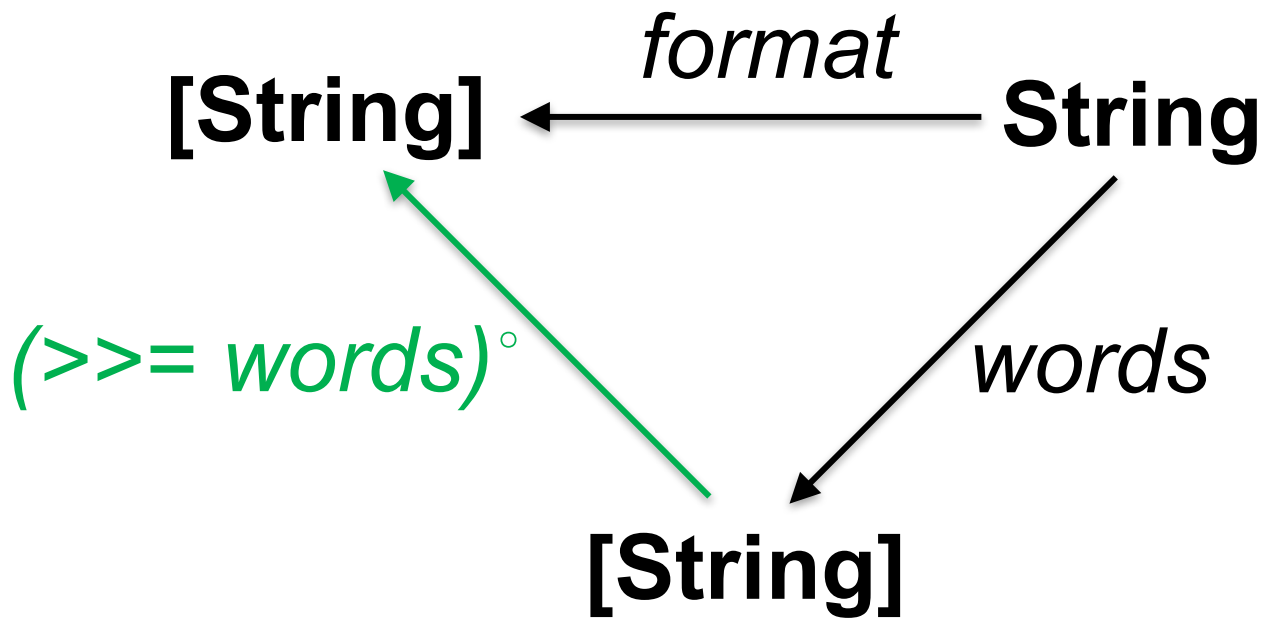
Example: Text Formatting



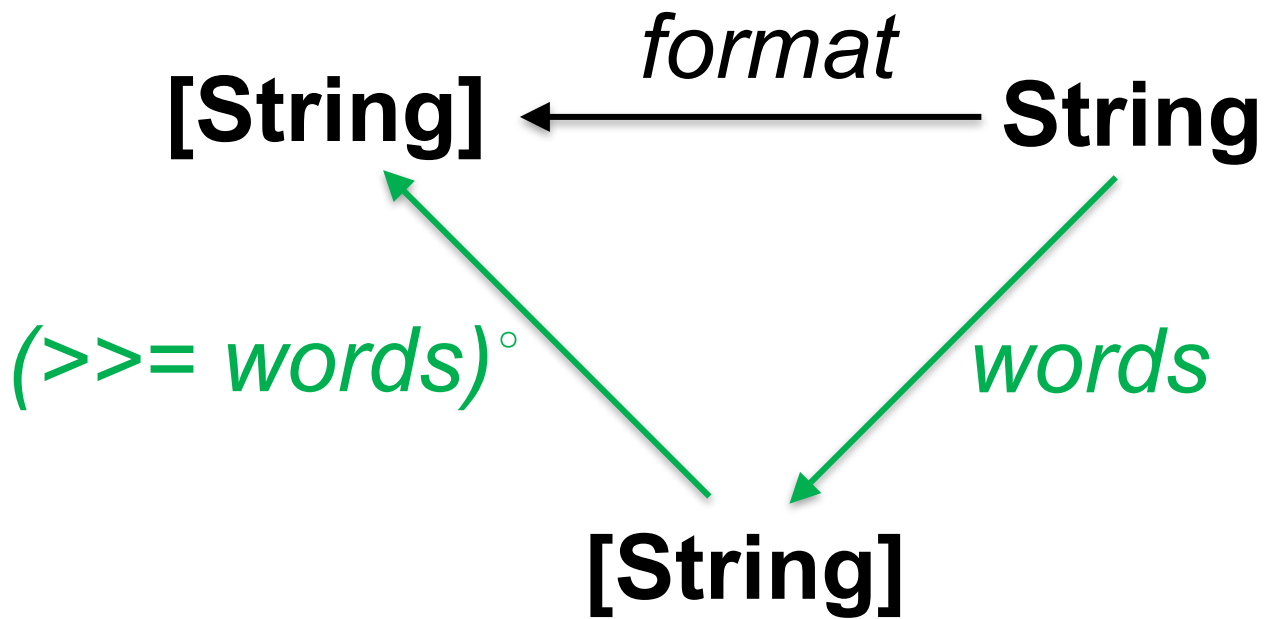
Example: Text Formatting



Example: Text Formatting



Example: Text Formatting



Example: Text Formatting

[“foo”, “bar”, “baz”] ← *words* “foo bar baz”

Example: Text Formatting

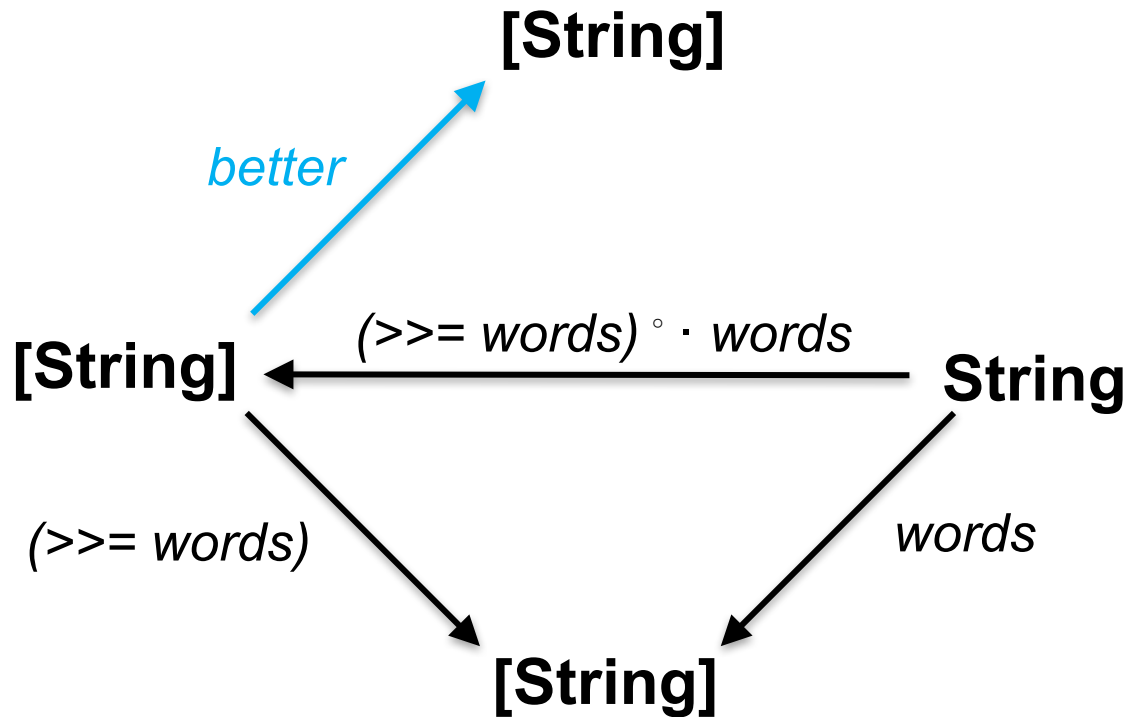
["foo", "bar", "baz"],
["foo bar", "baz"],
["foo", "bar baz"],
[" foo bar baz"]
[" foo", " bar", " baz"]
...
...etc.

$(\gg = \text{words})^\circ \cdot \text{words}$

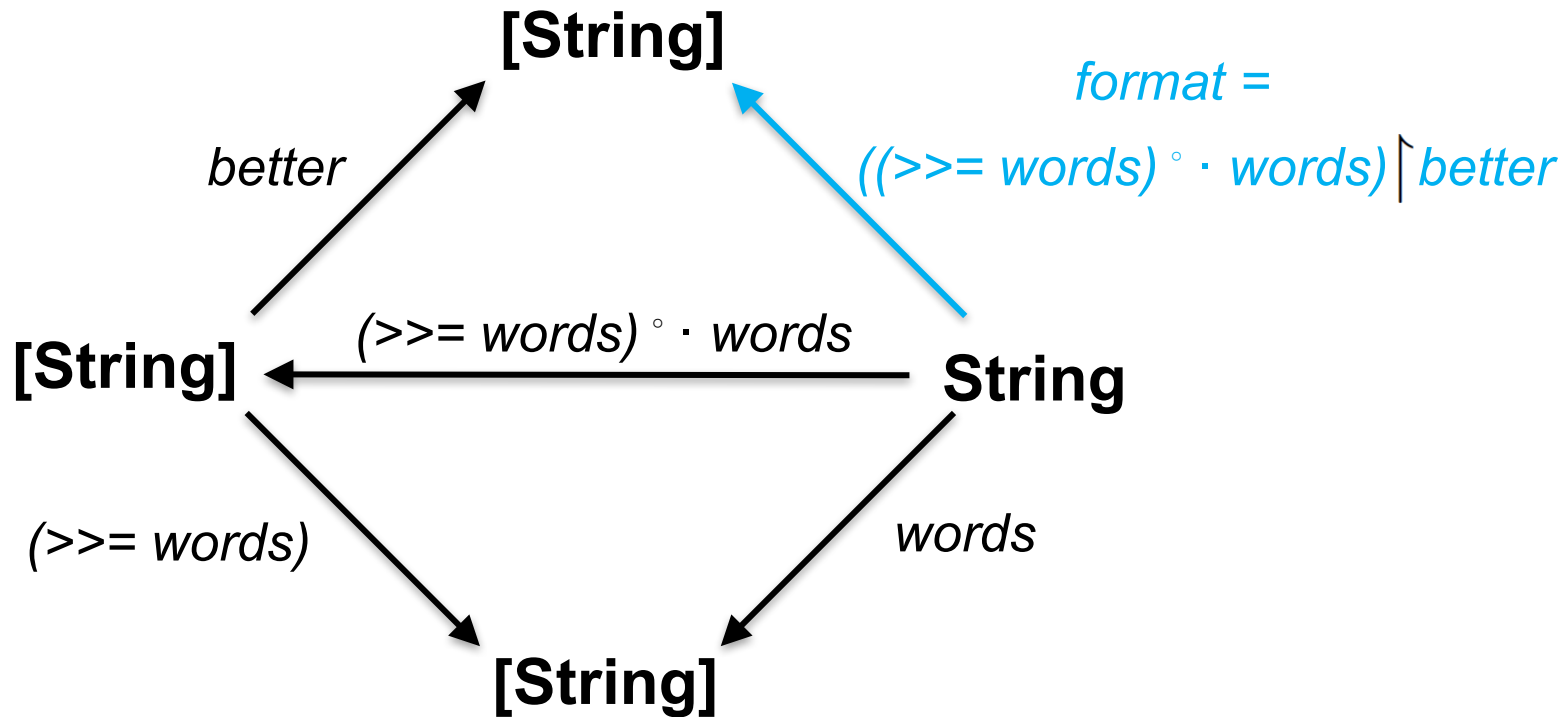


"foo bar baz"

Example: Text Formatting



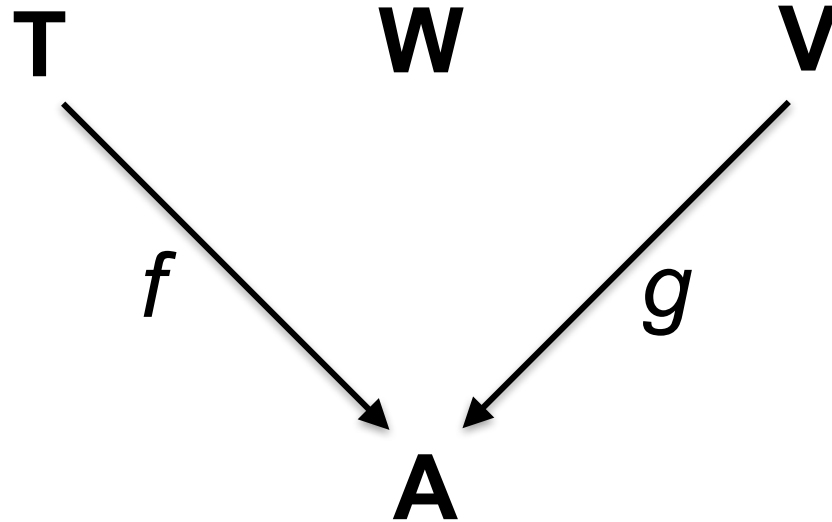
Example: Text Formatting



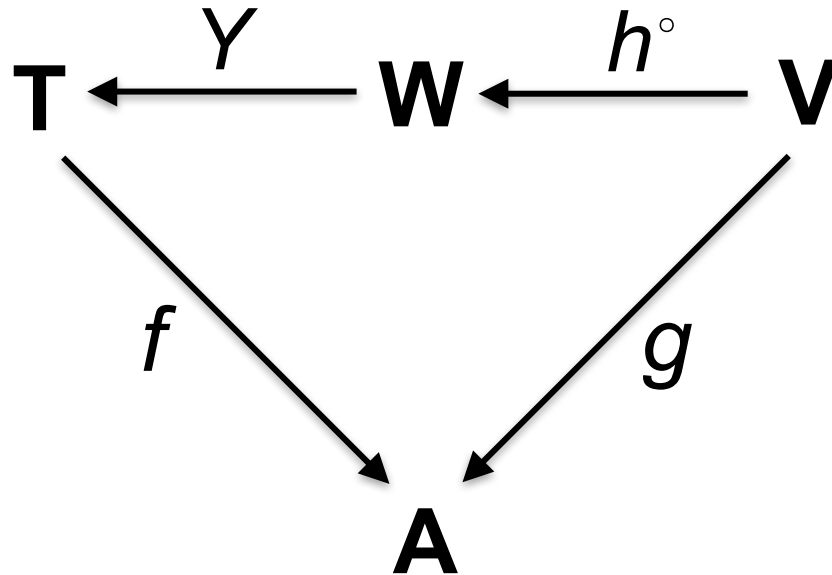
Divide and Conquer Algorithms

- Objects: Inductive types
- Arrows: Ana- and catamorphisms
- How?
 1. Introduce an intermediate inductive type
 2. Plug in a hylomorphism

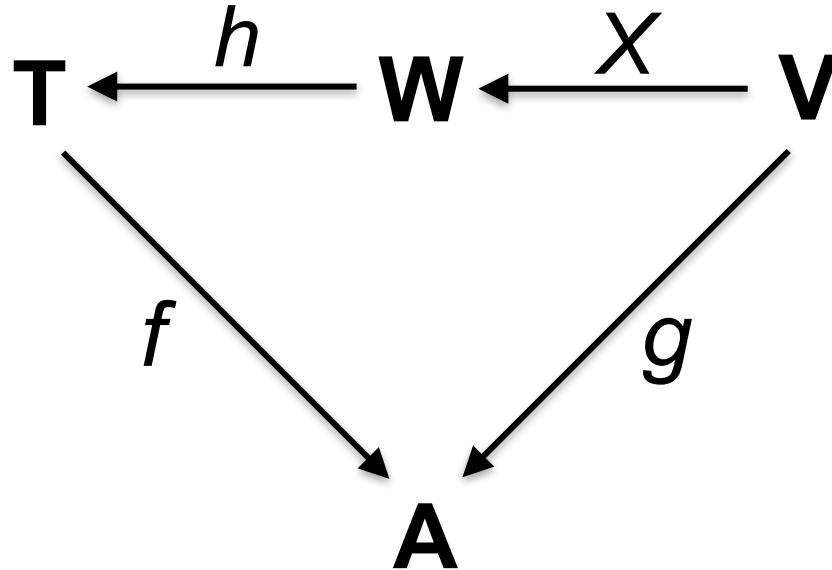
Divide and Conquer Algorithms



“Easy Divide, Hard Conquer”



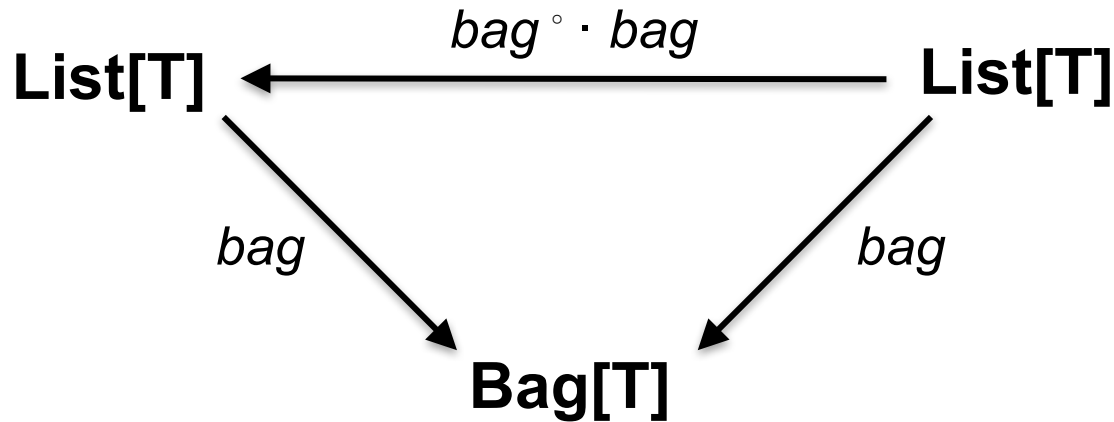
“Hard Divide, Easy Conquer”



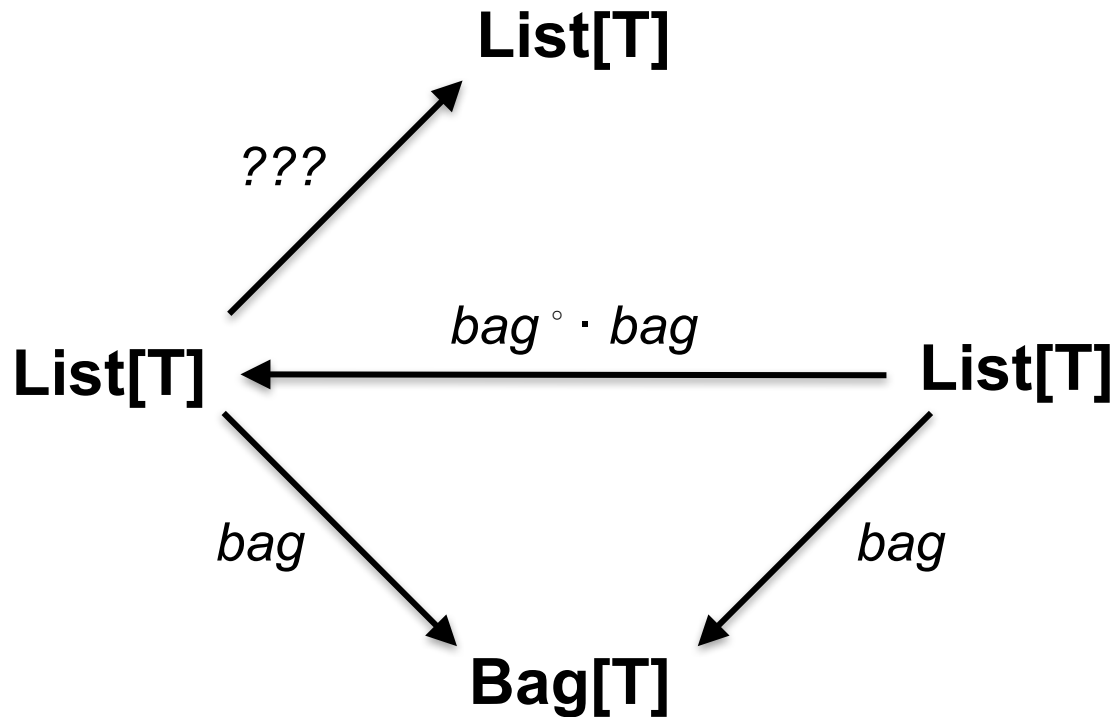
Example: Sorting a List



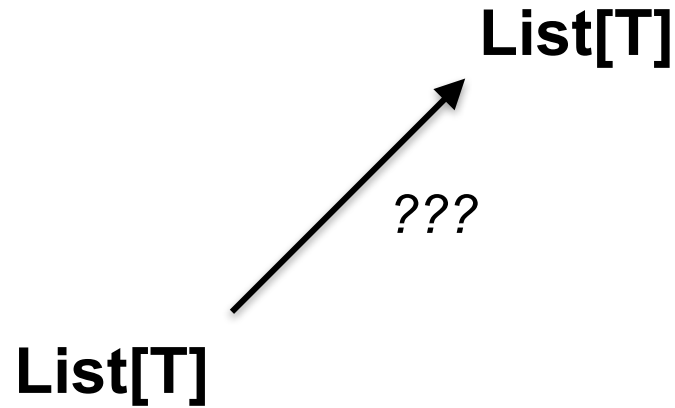
Example: Sorting a List



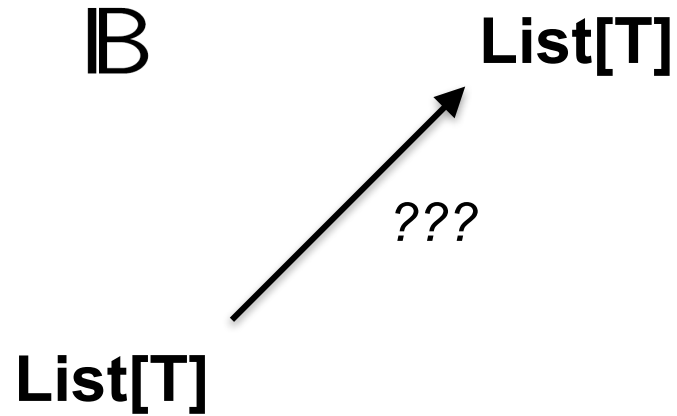
Example: Sorting a List



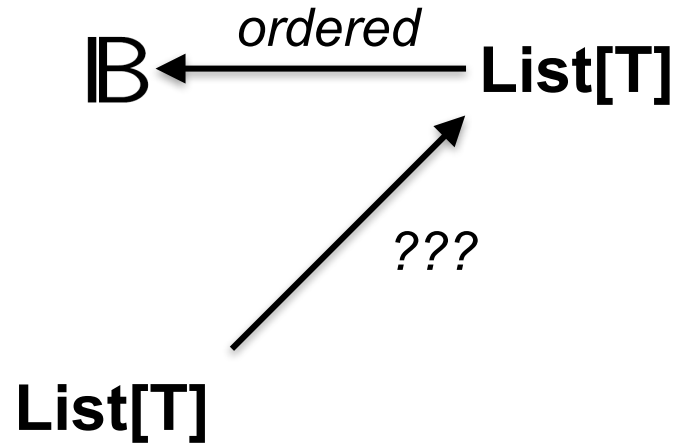
Example: Sorting a List



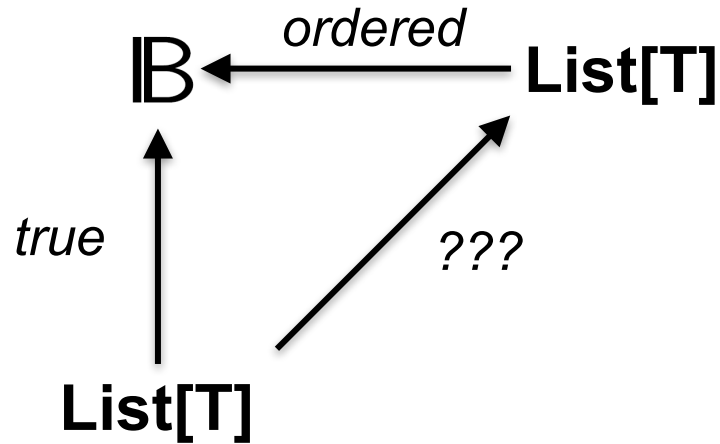
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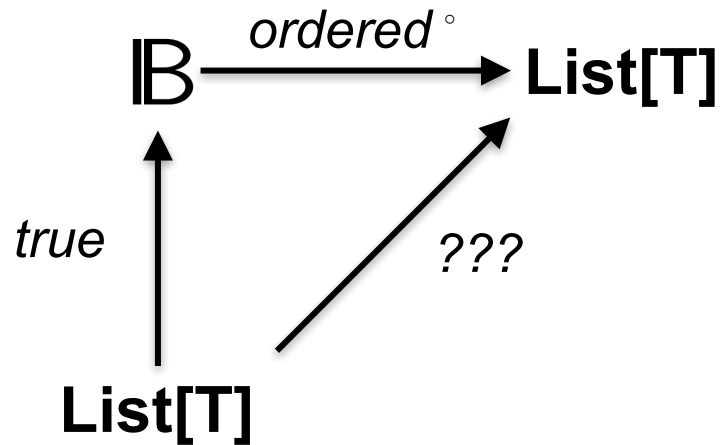
Example: Sorting a List



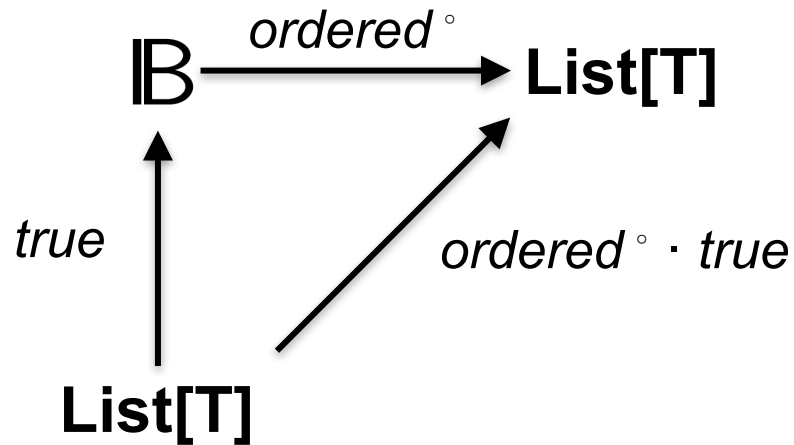
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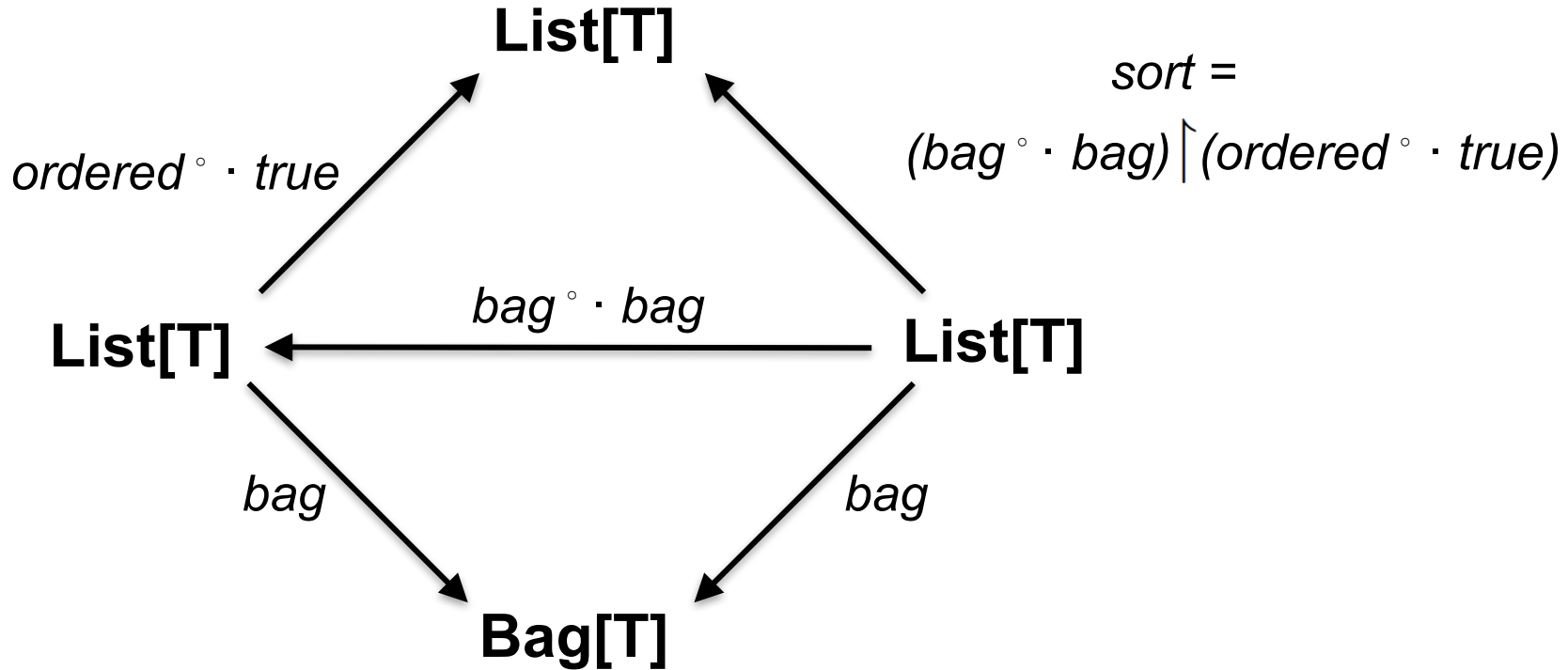
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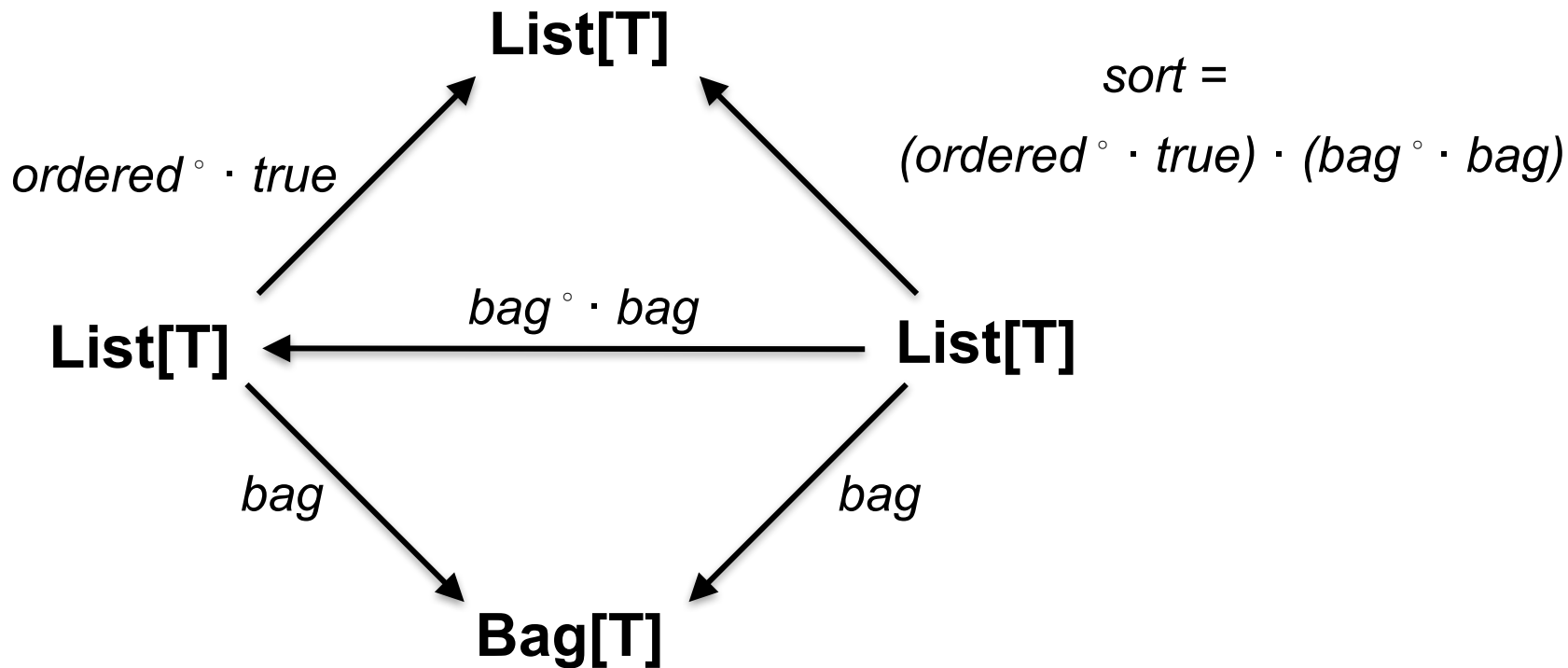
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Example: Sorting a List



Example: Sorting a List

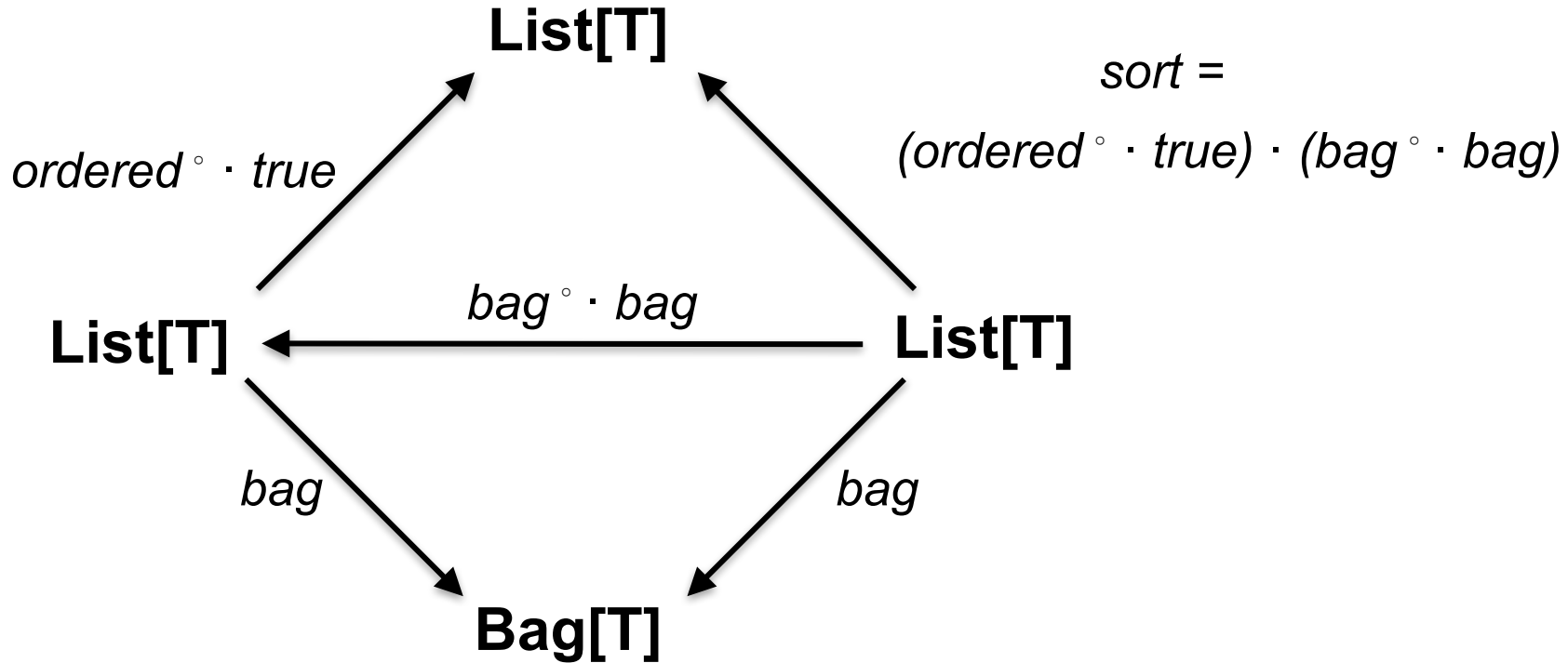


PROGRAM SYNTHESIS

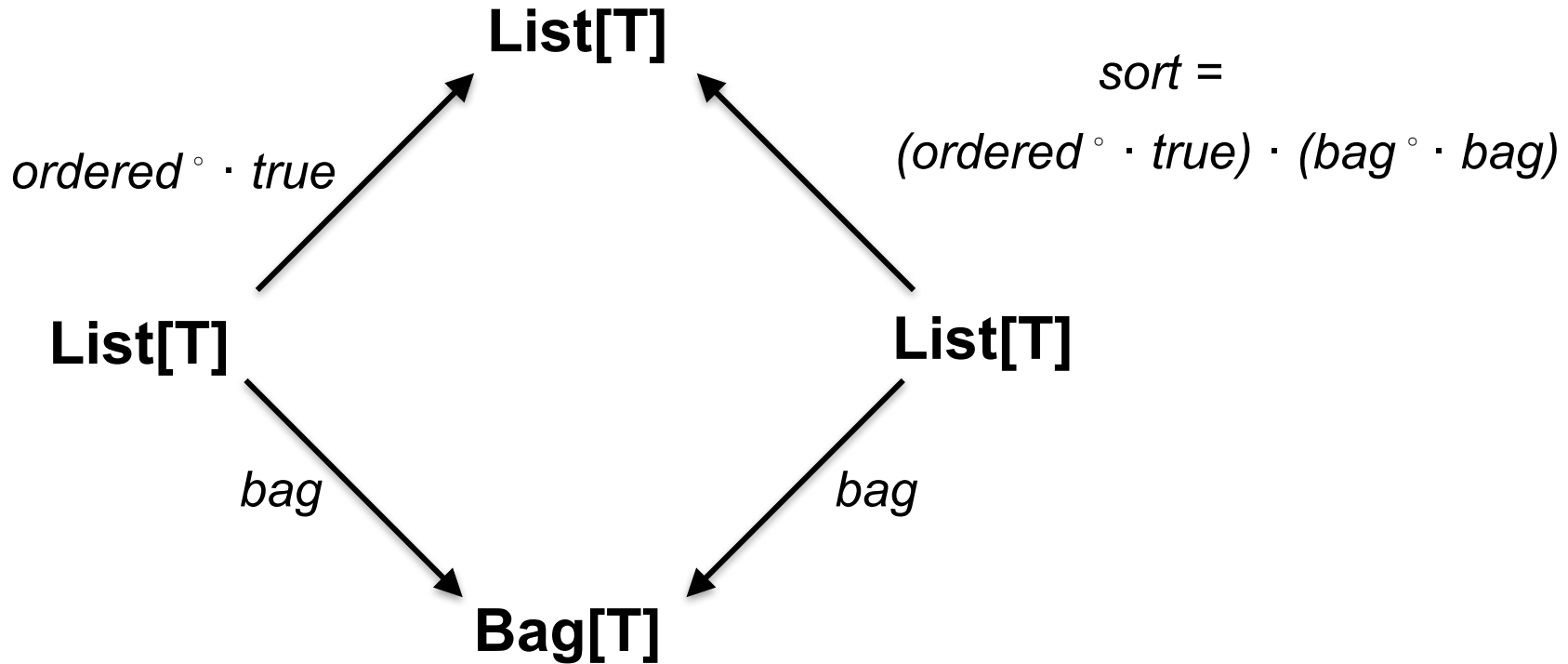
Example: “Mystery Sort”

- Start with a “Divide and Conquer” template
- Plug in bits/pieces of our spec for *sort*
- Turn the crank!

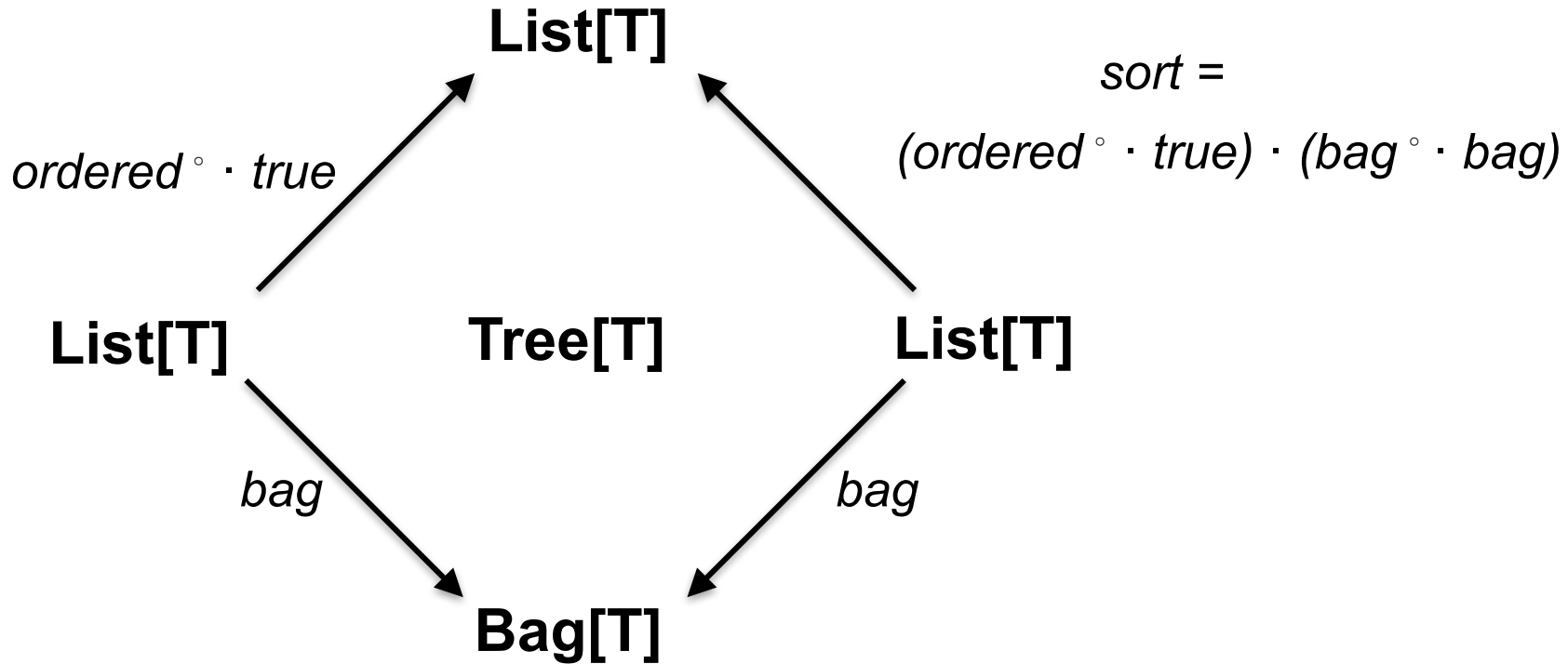
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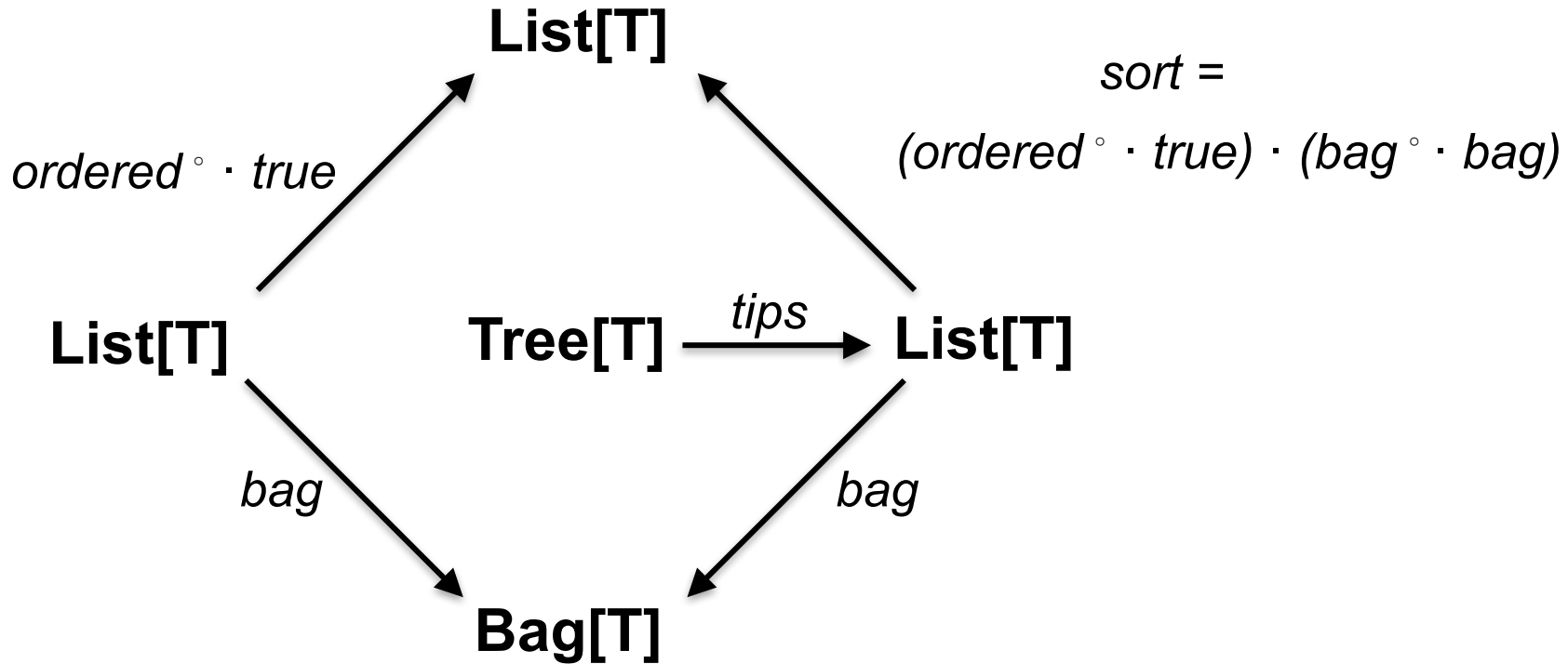
Example: “Mystery Sort”



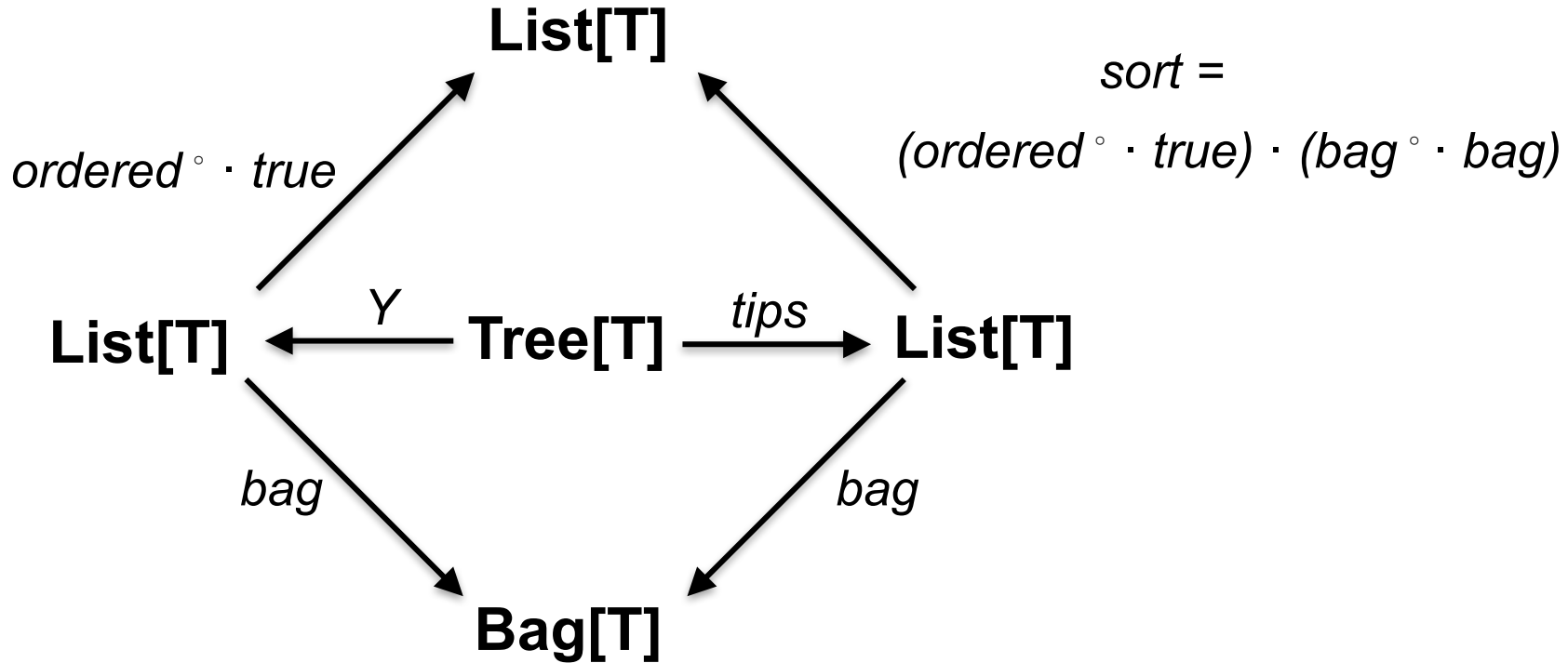
Example: “Mystery Sort”



Example: “Mystery Sort”



Example: “Mystery Sort”



Example: “Mystery Sort”

- Lemma (trust me...):

$$\begin{aligned} & \text{sort} \\ &= (\text{ordered}^\circ \cdot \text{true}) \cdot (\text{bag}^\circ \cdot \text{bag}) \\ &= (\text{ordered}^\circ \cdot \text{true}) \cdot \underbrace{\text{bag}^\circ \cdot \text{bag} \cdot \text{tips} \cdot \text{tips}^\circ}_Y \end{aligned}$$

Example: “Mystery Sort”

- Punchline: A function satisfying Y is the “list merge” seen in merge sort.
- We have derived **Merge Sort!**
- Different choices lead to different sorting algorithms

CONCLUSION

Conclusion

- Metaphors are everywhere
- We can use them in programming
- The Bird-Meertens Formalism is cool
- Functions to relations
- Keep climbing the ladder of abstraction

Meta-metaphors?

Burning the candle at both ends
Might seem super-neat,
But I'll guarantee it's not the way
To make our two ends meet!

-Ruth M. Walsh

ACKNOWLEDGEMENTS



William Harvey, PhD

Principal Engineer, OCLC



Lynn Silipigni Connaway, PhD

Senior Research Scientist & Director of User Research, OCLC



Erin M. Hood

Research Support Specialist, OCLC



Brittany Brannon

Research Assistant, OCLC

Thank You!

William Harvey, PhD

Principal Engineer

harveyw@oclc.org

**Because
what is
known must
be shared.SM**