

# **SEDI**

Version 1.0

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A sediment transport model for large-scale  
basins in cold regions.

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# Contents

# 1 Introduction

- Solutes are transported across the catchment via surface runoff and groundwater flow.
- Nitrogen (N) and phosphorus are abundant nutrient especially in agricultural areas.
- Nutrients can cause eutrophication and water quality deterioration. Pollutants can also deteriorate the water quality.
- Sediments can be considered as proxies of solutes.

## 1.1 Sediment transport processes

- Overland and in-stream erosion and deposition.
- Soil leaching of sediments.
- Atmospheric deposition
- In cold region:
  - Soil freeze-thaw cycles enhance rock weathering and soil leaching
  - Frozen soil-enhance runoff and erosion in surface layer

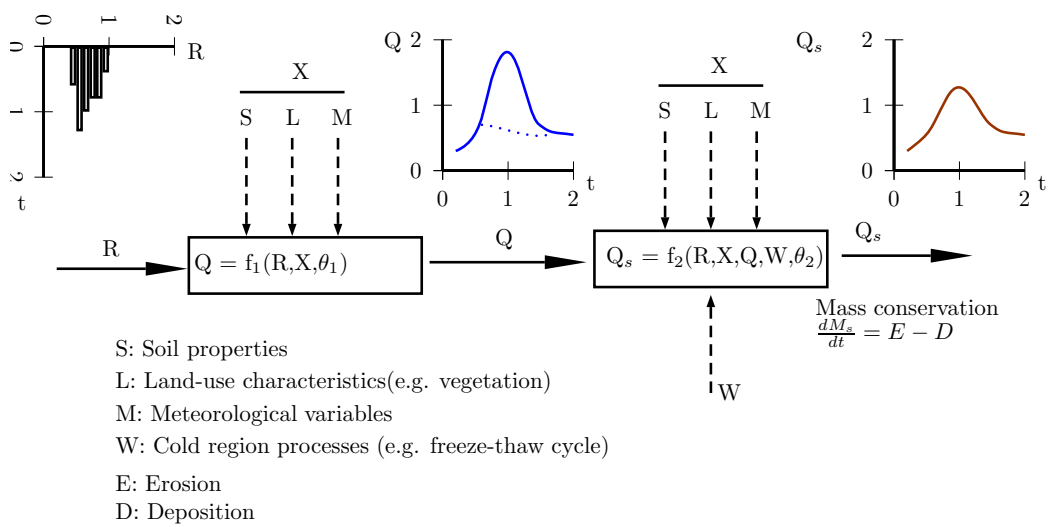
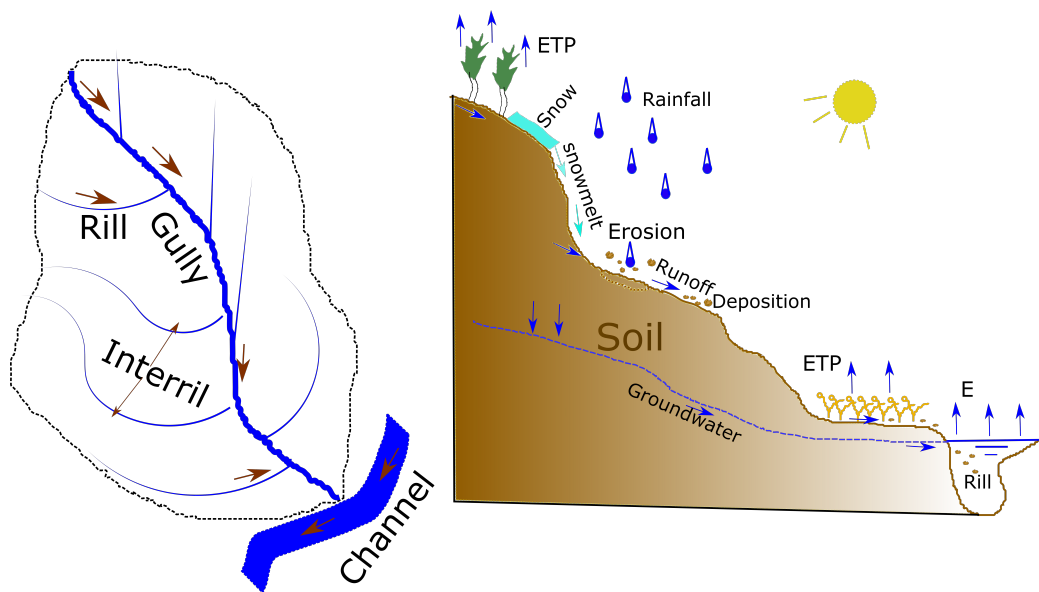
# 2 Controls and boundary conditions

Controls in overland and groundwater transport.

- Slope, land type, soil type (diameter, resistance, specific weight, etc)
- Rainfall, air temperature, soil water content, soil conductivity

Controls in in-stream transport:

- Channel slope and section geometry
- Bank and bottom material properties (diameter, resistance, specific weight), discharge, shear stress (function of slope and discharge) and



## 2.1 System representation of solute transport

# 3 Model structure

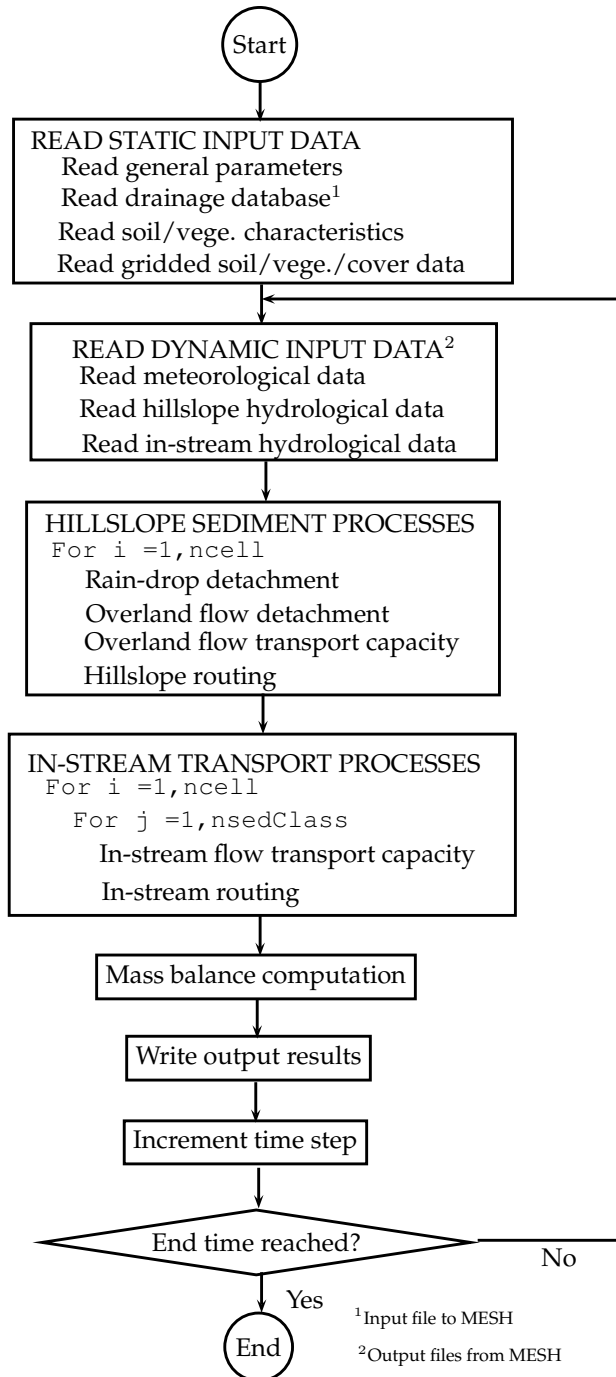
Some **MESH-SED** features:

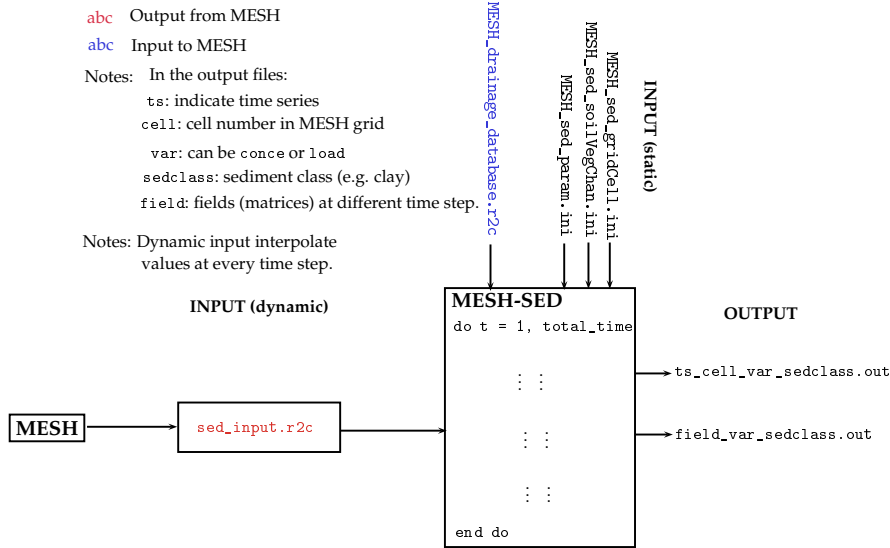
- loosely coupled with MESH [1].
- physically-based watershed sediment transport model.
- developed based on SHETRAN [2] and SHESED [3].
- semi-distributed model that work on a orthogonal grid (MESH grid).
- suitable for large-scale catchment to run on a continuous basis.
- include different sediment classes.
- future work: sedimentation in reservoirs, code parallelization.

## 3.1 Source code structure

Program `mesh_sed.f90`: Before main loop

```
[commandchars=\\{\}]  
  \verb{Read the study case name}  
  call mesh_sed_case  
  !> Read 'MESH_sed_param.ini'  
  call read_sed_param  
  !> Read 'MESH_drainage_database.r2c'  
  call read_MESH_drainage_database  
  !> Allocate memory space of important variables  
  call sed_allocate_var  
  !> Get (i,j) position of RANK cells and neighbor cells.  
  call sed_config_init  
  !> Read 'MESH_sed_gridCell.ini'  
  call read_sed_gridCell  
  !> Read 'MESH_sed_soilVegChan.ini'  
  call read_sed_soilVegChan  
  !> Read 'MESH_sed_reservoir.ini'  
  call read_sed_reservoir
```





## 4 Input data

### 4.1 MESH-SED input/output structure

### 4.2 Static input data

#### 4.2.1 MESH drainage database data

The information regarding catchment topology, cells connectivity, and model 'skeleton' is contained in `MESH_drainage_database.r2c`. This file is an input file for MESH and it is usually produced by Green Kenue.

In **MESH-SED**, `MESH_drainage_database.r2c` is read at the beginning of the model.

#### 4.2.2 Sediment transport model data

The following input files are read at the beginning of the program.

- `MESH_sed_param.ini`: Contains general information require to run de model.
- `MESH_sed_soilVegChan.ini`: Contains the soil and vegetation type characteristics.

- MESH\_sed\_gridCell.ini: Soil, vegetation and cover information for every cell of the grid.

### 4.2.3 MESH\_sed\_param.ini

```

Line 1  Comment
Line 2  MESH study case directory path
Line 3  Comment
Line 4  Hillslope.time.weighting_factor in-stream.time.weighting_factor in-stream.space.weighting_factor
Line 5  Comment
Line 6  Hillslope transport capacity method: 1[Yalin, 1963][4] 2[Engelund-Hansen, 1967][5]
Line 7  Comment
Line 8  In-stream transport capacity method: 1[Engelund-Hansen, 1967][5], 2[Ackers and White, 1973][6], 3[Day, 1980][]
Line 9  Comment
Line 10  Simulation time step (sec). It must be a multiple or factor of 60s but  $\leq 3600s = 1h$ .
Line 11  Comment
Line 12  Comment
Line 13  Start time: year julian_day hour minutes seconds
Line 14  End time: year julian_day hour minutes seconds
Line 15  Comment
Line 16  Upper limit of volumetric suspended sediment concentration
Line 17  Comment
Line 18  Output directory
Line 19  Comment
Line 20  Number of output grid points (ngr)
Line 21  Comment
Line 22  Comment
      cell_number1  variable1  particle_class1
Line 23  :           :           :
      cell_numberngr  variablengr  particle_classngr
      where cell_number is equal to rank in MESH_drainage_database.r2c, variable can be conce (concentration) or load
      and particle_class is listed in Table 1.

```

### 4.2.4 MESH\_sed\_param.ini

```

Line 1  Comment
Line 2  Number of output fields (gridded data)
Line 3  Comment
      variable1  particle_class1
Line 4  Comment :           :
      variablengr  particle_classngr

```



Table 1: Sediment/soil particles classes and diameters [7]

		particle_class	$\phi$ range (mm)
Mud	1	clay	$0.00006 \leq \phi < 0.0039$
	2	veryFineSilt	$0.0039 \leq \phi < 0.0078$
Silt	3	fineSilt	$0.0078 \leq \phi < 0.0156$
	4	mediumSilt	$0.0156 \leq \phi < 0.0313$
	5	coarseSilt	$0.0313 \leq \phi < 0.0625$
Sand	6	veryFineSand	$0.0625 \leq \phi < 0.125$
	7	fineSand	$0.125 \leq \phi < 0.25$
	8	mediumSand	$0.25 \leq \phi < 0.5$
	9	coarseSand	$0.5 \leq \phi < 1.0$
	10	veryCoarseSand	$1.0 \leq \phi < 2.0$
Gravel	11	granule	$2.0 \leq \phi < 4.0$
	12	pebble	$4.0 \leq \phi < 64.0$
	13	cobble	$64.0 \leq \phi < 256.0$
	14	boulder	$256.0 \leq \phi < 4096.0$

Example

```

! MESH study case directory path
'/media/Data3/MESH/Graham_River_WFDEI_Luis/07FA005_Graham_Riv/'
! Hillslope time weigh. factor      in-stream time weigh. factor      in-stream space weigh. factor
0.65      0.50      0.50
! Flag for overland sediment transport capacity
2      ! Choose transport capacity method: 1[Yalin, 1963] 2[Engelund-Hansen, 1967]
! Flag for instream sediment transport capacity
3      ! Choose transport capacity method: 1[Engelund-Hansen, 1967], 2[Ackers and White, 1973], 3[Day, 1980]
! Simulation time step sec
3600
! Simulation Run Times
-----#-----#-----#-----#
2002 365 23 0 0      ! Start year, jday, hour, minutes, seconds      5I4
2003 360 1 0 0      ! Stop year, jday, hour, minutes, seconds      5I4
! Upper limit of volumetric suspended sediment concentration
0.9
! TS output Directory
'/media/Data3/MESH/MESH_SED/test/output_ts/'
! Number of output grid points
5
! Grid numbersranks      variable_name      sed_class_name
1234567890123456789012345678901234567890123456789012345678901234567890
1      load      clay
2      conce      veryCoarseSand
4      conce      cobble
10     conce      boulder
15     load      clay
! Field output Directory
'/media/Data3/MESH/MESH_SED/test/output_field/'
! Number of output fields gridded
0
! variable_name      sed_class_name
123456789012345678901234567890123456789012345678901234567890
load      clay
conce      fineSand

```

## 4.2.5 MESH\_sed\_soilVegChan.ini

Line 1 Comment

Line 2 Number of soil types (ns)

```

          frac11 ... fracj1 ... frac141
          ρs1 λ1 kR1 kF1 kb1
          ⋮ ⋮ ⋮
          frac1i ... fracji ... frac14i
Line 3 For each soil type i ρsi λi kRi kFi kbi
          ⋮ ⋮ ⋮
          frac1ns ... fracjns ... frac14ns
          ρsns λns kRns kFns kbns

```

Line 4 Comment

Line 5 Number of vegetation classes (nv)

```

          vege1 ... vegej ... vegenv
          X1 ... Xj ... Xnv
Line 6 For each vegetation type j d1 ... dj ... dnv
          DRIP1 ... DRIPj ... DRIPnv

```

Line 7 Comment

Line 8 β δ<sub>max</sub> α

frac = Fraction occupied for each particle class.

ρ<sub>s</sub> = Soil density (kg m<sup>-3</sup>).

λ = Soil surface porosity (0. ≤ λ ≤ 1.).

k<sub>R</sub> = Soil detachability (J<sup>-1</sup>).

k<sub>F</sub> = Overland flow detachment (mg m<sup>-2</sup> s<sup>-1</sup>).

k<sub>b</sub> = Channel bank flow detachment (mg m<sup>-2</sup> s<sup>-1</sup>).

vege = Vegetation class.

X = Fall height (m).

d = Leaf drip diameter (mm).

DRIP = % drainage as leaf drip.

β = Threshold sediment concentration in channels for infiltration and overbank sediment flow.

δ<sub>max</sub> = Maximun thickness (m) of top (active) bed sediment layer in channel. δ<sub>max</sub> = 1 or 2 D<sub>9</sub> for gravel-bed channels and δ<sub>max</sub> = 10 mm for sand-bed channels.

α = Ratio of critical shear stresses for deposition and initiation of motion (α < 1). Likely range 0.25-0.75.

! Soil type characterization												! Number of soil types			
5												0.			! Fra
0.	.05	.10	.30	.30	.25	0.	0.	0.	0.	0.	0.	0.	0.		
2650.	0.2	25.	2.	2.											! Density kg/m3, Surface porosi
0.	.05	.20	.25	.30	.20	0.	0.	0.	0.	0.	0.	0.	0.		
2650.	0.2	25.	2.	2.											
0.	0.	.10	.35	.25	.30	0.	0.	0.	0.	0.	0.	0.	0.		
2650.	0.2	25.	2.	2.											
0.05	0.05	0.05	0.20	0.30	0.15	0.10	0.10	0.	0.	0.	0.	0.	0.	0.	
2650	0.2	25.	2.	2.											
0.05	0.05	0.05	0.20	0.30	0.15	0.10	0.10	0.	0.	0.	0.	0.	0.	0.	

```

2650.      0.2      25.      2.      2.
! Canopy vegetation parameters
8
maize  bsprout subeet  potato  tforest  soybean  spruce  sycamore  ! # of vegetation type
0.5    1.1    0.5    1.1      6.      0.87   18.      20.      ! Vegetation type
4.5    6.3    4.6    5.9      6.      5.      7.      3.      ! Fall height m
35     23     18     2        3        4       10     5      ! Drip diameter mm
! In-stream sediment transport parameters
5.0      0.01     0.4

```

---

## 4.2.6 MESH\_sed\_gridCell.ini

```

Line 1  Comment
Line 2  Initial depth of loose soil
         $\delta_{11}$   $\delta_{12}$  ...  $\delta_{1n}$ 
         $\delta_{21}$   $\delta_{22}$  ...  $\delta_{2n}$ 
        .
        .
        .
         $\delta_{m1}$   $\delta_{m2}$  ...  $\delta_{mn}$ 
Line 3  Comment
Line 4  Ground cover
         $G_{11}$   $G_{12}$  ...  $G_{1n}$ 
         $G_{21}$   $G_{22}$  ...  $G_{2n}$ 
        .
        .
        .
         $G_{m1}$   $G_{m2}$  ...  $G_{mn}$ 
Line 5  Comment
Line 6  Hillslope soil type
         $hst_{11}$   $hst_{12}$  ...  $hst_{1n}$ 
         $hst_{21}$   $hst_{22}$  ...  $hst_{2n}$ 
        .
        .
        .
         $hst_{m1}$   $hst_{m2}$  ...  $hst_{mn}$ 
Line 7  Comment
Line 8  Steady-state sediment flux boundary conditions
         $bc_{11}$   $bc_{12}$  ...  $bc_{1n}$ 
         $st_{21}$   $bc_{22}$  ...  $bc_{2n}$ 
        .
        .
        .
         $bc_{m1}$   $bc_{m2}$  ...  $bc_{mn}$ 
Line 9  Comment

```

$m$  = Number of rows (latitudes coordinates) of the MESH grid.

$n$  = Number of columns (longitudes coordinates) of the MESH grid.

$\delta$  = Initial depth of hillslope loose soil (m) at each cell.

$G$  = Proportion [ $0 \leq G \leq 1$ ] of impervious area in the cell.

$hst$  = Index ( $hst = 1..ns$ ) of the predominant hillslope soil type at each cell.

Steady-state sediment flux boundary conditions at each cell .

Note: **MESH-SED** can be modified to introduce dynamically time-dependant  $G$  and  $bc$  fields.

#### 4.2.7 MESH\_sed\_gridCell.ini

```

Line 10  Predominant vegetation type
         vt11 vt12 ... vt1n
         vt21 vt22 ... vt2n
         .
         .
         .
         vtm1 vtm2 ... vtmn

Line 11  Comment

Line 12  Canopy cover
         C11 C12 ... C1n
         C21 C22 ... C2n
         .
         .
         .
         Cm1 Cm2 ... Cmn

Line 13  Comment

Line 14  Channel soil type
         cst11 cst12 ... cst1n
         cst21 cst22 ... cst2n
         .
         .
         .
         cstm1 cstm2 ... cstmn

Line 15  Comment

```

$vt$  = Predominant vegetation class at each cell (see *vege*)

$C$  = Proportion [ $0 \leq C \leq 1$ ] of the cell area covered by vegetation (canopy) at each cell.

$cst$  = Index ( $hst = 1...ns$ ) of the predominant channel bed soil type at each cell.

Note: **MESH-SED** can be modified to introduce dynamically time-dependent  $vt$  and  $C$  fields

#### 4.2.8 MESH\_sed\_gridCell.ini

```

Line 10  Channel bank soil type
         cbst11 cbst12 ... cbst1n
         cbst21 cbst22 ... cbst2n
         .
         .
         .
         cbstm1 cbstm2 ... cbstmn

Line 11  Comment

Line 12  Initial thickness of channel bed material
         δc11 δc12 ... δc1n
         δc21 δc22 ... δc2n
         .
         .
         .
         δcm1 δcm2 ... δcmn

```

- $cbst$  = Index ( $hst = 1...ns$ ) of the predominant channel-bank soil type at each cell.
- $\delta c$  = Initial thickness of channel bed material (m). Usually  $0.5m \leq \delta c \leq 5m$  for small to medium size streams,  $\delta c \geq 5m$  for large rivers.

Example									
! Initial depth of loose soil m									
1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03
1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03
1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03
1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03	1.0E-03
! Ground cover: %[0. -> 1.] of cell area covered by snowe.g. glaciers, rock or impervious									
0.1	0.	0.2	0.6	0.3	0.5	0.9	0.8	0.1	0.2
0.1	0.	0.2	0.6	0.3	0.5	0.9	0.8	0.1	0.2

```

0.1 0. 0.2 0.6 0.3 0.5 0.9 0.8 0.1 0.2 0.8 0.9 0.1
0.1 0. 0.2 0.6 0.3 0.5 0.9 0.8 0.1 0.2 0.8 0.9 0.1
! Soil type
1 2 3 4 5 1 2 3 4 5 1 2 3
1 2 3 4 5 1 2 3 4 5 1 2 3
1 2 3 4 5 1 2 3 4 5 1 2 3
1 2 3 4 5 1 2 3 4 5 1 2 3
! Sediment flux boundary conditions
0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
! Predominant vegetation type in each cell
maize bsprout subeet potato tforest soybean spruce sycamore maize spruce tforest subeet potato
maize bsprout subeet potato tforest soybean spruce sycamore maize spruce tforest subeet potato
maize bsprout subeet potato tforest soybean spruce sycamore maize spruce tforest subeet potato
maize bsprout subeet potato tforest soybean spruce sycamore maize spruce tforest subeet potato
! Canopy cover: %[0. -> 1.] of cell area covered by canopy see the canopy types above
0.9 1.0 0.8 0.4 0.7 0.5 0.1 0.2 0.9 0.8 0.2 0.1 0.9
0.9 1.0 0.8 0.4 0.7 0.5 0.1 0.2 0.9 0.8 0.2 0.1 0.9
0.9 1.0 0.8 0.4 0.7 0.5 0.1 0.2 0.9 0.8 0.2 0.1 0.9
0.9 1.0 0.8 0.4 0.7 0.5 0.1 0.2 0.9 0.8 0.2 0.1 0.9
! Channel-bed soil type
1 2 3 1 2 3 1 2 3 1 2 3 1
1 2 3 1 2 3 1 2 3 1 2 3 1
1 2 3 1 2 3 1 2 3 1 2 3 1
1 2 3 1 2 3 1 2 3 1 2 3 1
! Type of soil on banks of channel = Soil type
1 2 3 4 5 1 2 3 4 5 1 2 3
1 2 3 4 5 1 2 3 4 5 1 2 3
1 2 3 4 5 1 2 3 4 5 1 2 3
1 2 3 4 5 1 2 3 4 5 1 2 3
! Initial thickness of channel bed material m [0.5 - 5m, >5big rivers]
0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50
0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50
0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50
0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50 0.50

```

## 4.3 Dynamic input data

### 4.3.1 sed\_input.r2c

All the dynamic input data required by **MESH-SED** is saved into `sed_input.r2c` file. This file is produced by MESH (see r1295 version and newer) in `rte_module.f90` (see starting at line 923) and contains gridded information in r2c format at 1h time step. Variables are written into the file in the following order:

1. Average flow (discharge) ( $\text{m}^3 \text{s}^{-1}$ ). Note: Averaged over the time-step.
2. Channel depth (m).
3. Channel width (m).
4. Channel length (m).
5. Channel slope ( $\text{m m}^{-1}$ ).  $\text{slope} = \sqrt{\text{SLOPE\_CHNL}}$
6. Stream velocity ( $\text{m s}^{-1}$ ). Take stream speed to be average flow ( $\text{m}^3 \text{s}^{-1}$ ) divided by channel x-sec area ( $\text{m}^2$ ) (from `rte_sub.f`).
7. Precipitation ( $\text{mm h}^{-1}$ ). Note: Accumulated over the time-step.
8. Evapotranspiration ( $\text{mm h}^{-1}$ ). Note: Of evapotranspiration accumulated over the time-step.

9. Overland water depth (mm). Note: Accumulated over the time-step.
10. Surface slope ( $\text{m m}^{-1}$ ). SLOPE\_INT isn't used in CLASS, so average slope from tiles in cell?
11. Cell width (m).

## 5 Output data

### 5.1 Output data

**MESH-SED** estimates sediment concentration and loads at every cell of the computational grid and for every sediment class at every time step. **MESH-SED** also estimates changes of the land surface due to accumulation or erosion of sediments. The format of the output information is specified in `MESH_sed_param.ini`. The typical output files are:

`ts.cell.var.sedclass.out`  
(e.g. `ts_10_load.veryFineSand.out`)

$time_1$	$var_1$
$time_2$	$var_2$
$\vdots$	$\vdots$
$time_n$	$var_n$

- `ts`: indicate time series.
- `cell`: cell number in MESH grid (`rank`).
- `var`: it can be `conce` or `load`.
- `sedclass`: sediment class (see Table 1)
- `field`: field (matrices) at different time steps.

`field.var.sedclass.out`  
(e.g. `field.conce.coarseSilt.out`)

$time\_1$			
$var_{11}$	$var_{12}$	$\cdots$	$var_{1n}$
$var_{21}$	$var_{22}$	$\cdots$	$var_{2n}$
$\vdots$	$\vdots$	$\ddots$	$\vdots$
$var_{m1}$	$var_{m2}$	$\cdots$	$var_{mn}$
$\vdots$	$\vdots$		$\vdots$
$\vdots$	$\vdots$		$\vdots$
$time\_n$			
$var_{11}$	$var_{12}$	$\cdots$	$var_{1n}$
$var_{21}$	$var_{22}$	$\cdots$	$var_{2n}$
$\vdots$	$\vdots$	$\ddots$	$\vdots$
$var_{m1}$	$var_{m2}$	$\cdots$	$var_{mn}$

## 6 Download, compile and execute

### 6.1 Download

**MESH-SED** can be download from <https://github.com/lmoralesma/MESH-SED> Github Repository or from command line as: `git clone https://github.com/lmoralesma/M`

### 6.2 Compile

Compile **MESH-SED** by typing `make`; produce `sa_mesh_sed`. Use `make clean` for removing `*.o` and `*.mod` files.

### 6.3 execute

To run **MESH-SED** , `./sa_mesh_sed projname` (e.g. `./sa_mesh_sed test`).

## 7 References

### References

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